



# From nuclei to quarks and gluons

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**6th Lisbon Mini-School on Particle and Astroparticle Physics  
July 15, 2021**

# Standard model

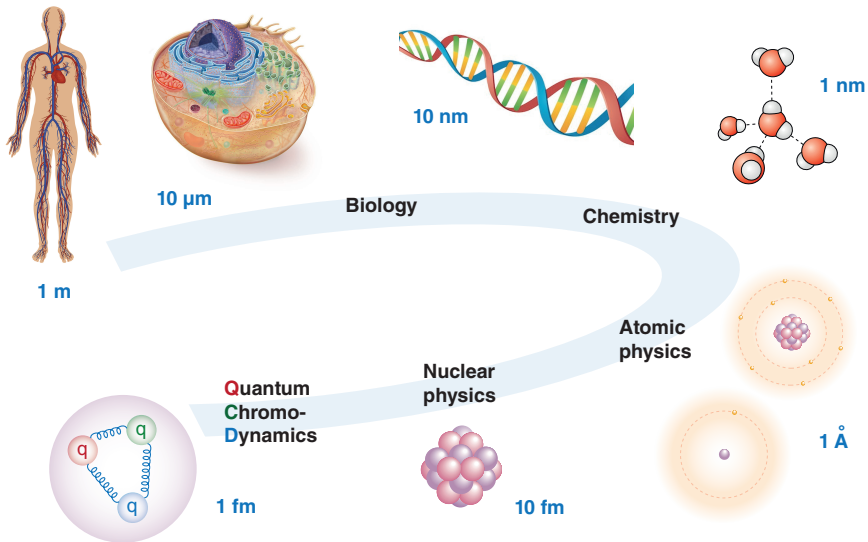
	Fermions			Bosons	
Quarks	$u$ up	$c$ charm	$t$ top	$\gamma$ photon	Force carriers
	$d$ down	$s$ strange	$b$ bottom	$Z$ Z boson	
Leptons	$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino	$W$ W boson	
	$e$ electron	$\mu$ muon	$\tau$ tau	$g$ gluon	
				Higgs boson	

Source: AAAS

## Quantum Chromodynamics (QCD):

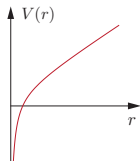
Particles with **color charge** interact by exchanging **gluons**

# QCD binds us together



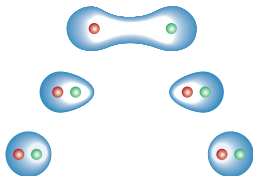
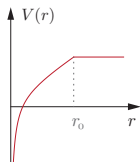
# Confinement

Quarks & gluons are confined in **colorless hadrons**,  
so we can never observe them in isolation!



Potential between quarks  
grows **linearly** with distance

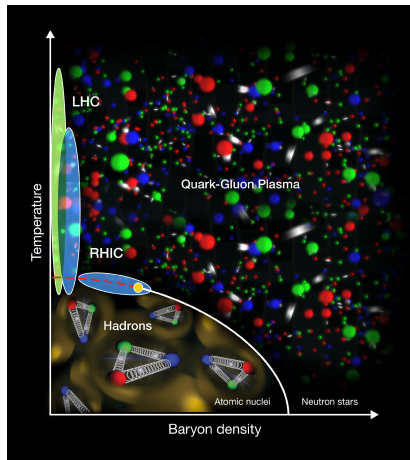
**Microscopic origin still  
unclear** – \$1M prize



Eventually:  
**string breaking**

→ Hands-on **Hadron Physics**

# QCD forms hadrons



Mesons



Baryons



# The hadron zoo

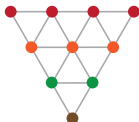
## Mesons

$0^{-+}$	$0^{++}$	$1^{-+}$	$1^{--}$	$1^{++}$	$1^{+-}$	$2^{-+}$	$2^{++}$	$3^{--}$
$\pi(140)$ $\pi(1300)$ $\pi(1800)$	$a_0(980)$ $a_0(1450)$ $a_0(1960)$	$\pi_1(1400)$ $\pi_1(1600)$	$\rho(770)$ $\rho(1450)$ $\rho(1870)$ $\rho(1700)$ $\rho(1800)$	$a_1(1260)$ $a_1(1420)$ $a_1(1640)$	$b_1(1235)$	$\pi_2(1670)$ $\pi_2(1880)$	$a_2(1320)$ $a_2(1700)$	$\rho_3(1690)$ $\rho_3(1990)$
$K(494)$ $K(1460)$ $K(1830)$	$K_0^*(800)$ $K_0^*(1430)$ $K_0^*(1950)$		$K^*(892)$ $K^*(1410)$ $K^*(1680)$	$K_1(1400)$ $K_1(1650)$	$K_1(1270)$	$K_2(1580)$ $K_2(1770)$ $K_2(1820)$	$K_2^*(1430)$ $K_2^*(1980)$	$K_3^*(1780)$
$\eta(548)$ $\eta'(958)$ $\eta(1296)$ $\eta(1405)$ $\eta(1475)$ $\eta(1780)$	$f_0(500)$ $f_0(980)$ $f_0(1370)$ $f_0(1500)$ $f_0(1710)$		$\omega(782)$ $\phi(1020)$ $\omega(1420)$ $\omega(1650)$ $\phi(1680)$	$f_1(1285)$ $f_1(1430)$ $f_1(1610)$	$h_1(1170)$ $h_1(1380)$ $h_1(1595)$	$\eta_2(1645)$ $\eta_2(1870)$	$f_2(1270)$ $f_2(1430)$ $f_2'(1525)$ $f_2(1555)$ $f_2(1640)$ $f_2(1810)$ $f_2(1910)$ $f_2(1980)$	$\omega_3(1670)$ $\phi_3(1850)$



## Baryons

$\frac{1}{2}^{+}$	$\frac{1}{2}^{-}$	$\frac{3}{2}^{+}$	$\frac{3}{2}^{-}$	$\frac{5}{2}^{+}$	$\frac{5}{2}^{-}$	$\frac{7}{2}^{+}$
$N(939)$ $N(1440)$ $N(1710)$ $N(1880)$	$N(1535)$ $N(1650)$ $N(1895)$	$N(1720)$ $N(1900)$	$N(1520)$ $N(1700)$ $N(1875)$	$N(1690)$ $N(1860)$ $N(2000)$	$N(1675)$	$N(1990)$
$\Delta(1910)$	$\Delta(1620)$ $\Delta(1900)$	$\Delta(1232)$ $\Delta(1600)$ $\Delta(1920)$	$\Delta(1700)$ $\Delta(1940)$	$\Delta(1905)$ $\Delta(2000)$	$\Delta(1930)$	$\Delta(1950)$
$\Lambda(1116)$ $\Lambda(1800)$ $\Lambda(1810)$	$\Lambda(1405)$ $\Lambda(1670)$ $\Lambda(1800)$	$\Lambda(1890)$	$\Lambda(1520)$ $\Lambda(1690)$	$\Lambda(1820)$	$\Lambda(1830)$	
$\Sigma(1189)$ $\Sigma(1680)$ $\Sigma(1880)$	$\Sigma(1750)$	$\Sigma(1385)$	$\Sigma(1670)$ $\Sigma(1940)$	$\Sigma(1915)$	$\Sigma(1775)$	
$\Xi(1315)$		$\Xi(1530)$	$\Xi(1820)$			
		$\Omega(1672)$				



<http://pdglive.lbl.gov>

# And it doesn't stop there ...

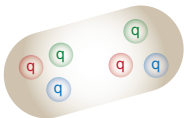
## Familiar states



Mesons



Baryons



Nuclei??

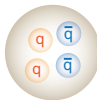
## Exotic states



Glueballs?



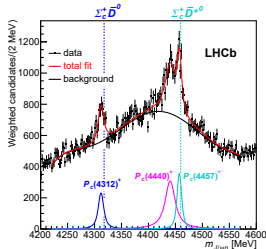
Hybrid mesons?



Tetraquarks?



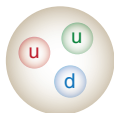
Pentaquarks?



Aaij et al., Phys. Rev. Lett. 112 (2019) 222001

To understand QCD, we must understand **spectrum and interactions of hadrons!**

# Mass generation



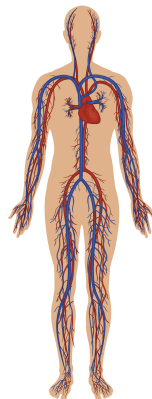
$2m_u + m_d \sim 10 \text{ MeV}$ ,  
but **proton**  $\sim 1 \text{ GeV}$  !?

**Higgs**  $\rightarrow$  Current-quark masses

**QCD**  $\rightarrow$  **Mass generation** due to spontaneous breaking of **chiral symmetry**:  
“constituent-quark masses”

u	d	s	c	b	t
3	5	100	1000	4000	175000
350	350	350	350	350	350

[MeV]

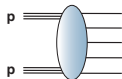




# Experiments?

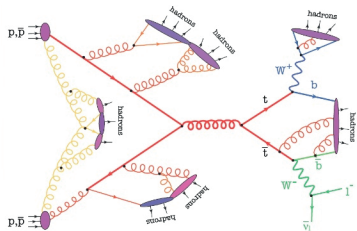
How can we **probe** quarks and gluons **experimentally** if we can never set them free?

- $pp, pA, AA \rightarrow X, \dots$



LHC (CERN)  
RHIC (BNL)  
GSI/FAIR (Germany)  
...

- **Hadronization & Jets**
- **QCD phase diagram**
- **Quark-gluon plasma**



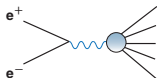
K. Hamilton

→ **Hands-on QCD Jets**

# Experiments?

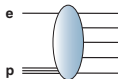
Use **electromagnetic probes**:

- $e^+e^- \rightarrow X$



BES III,  
Belle,  
BaBar,  
...

- $ep \rightarrow X$

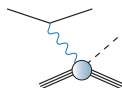


EIC (USA)  
COMPASS (CERN)  
Jefferson Lab (USA)  
MAMI & ELSA (Germany)  
...

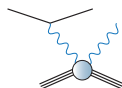
- Extract properties of **individual hadrons**
- Quark-gluon substructure, **“Hadron tomography”**



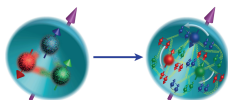
eN scattering



meson  
electro-  
production



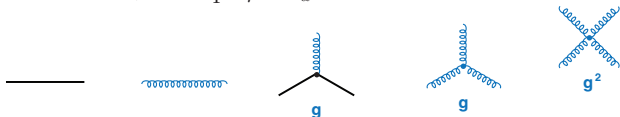
Compton  
scattering



- Extraction of **resonances**

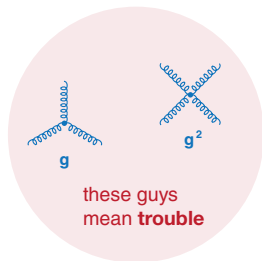
# QCD Lagrangian

$$\mathcal{L} = \bar{\psi} (\not{\partial} + i g \not{A} + m) \psi + \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}$$



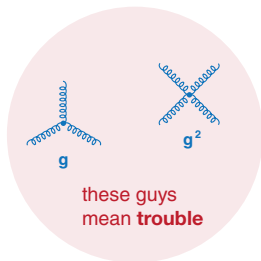
# QCD Lagrangian

$$\mathcal{L} = \bar{\psi} (\not{\partial} + i g \not{A} + m) \psi + \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}$$

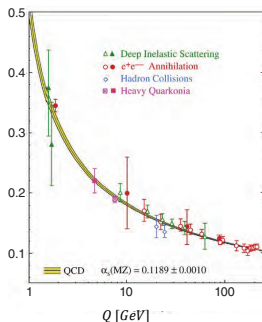


# QCD Lagrangian

$$\mathcal{L} = \bar{\psi} (\not{\partial} + i g \not{A} + m) \psi + \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu}$$



$$\alpha = \frac{g^2}{4\pi}$$



these guys mean trouble

At large momenta, quarks & gluons behave as quasi-free particles:  
**asymptotic freedom**

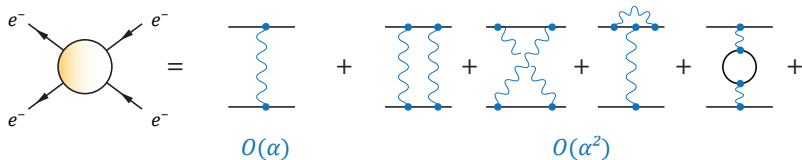


Gross, Politzer, Wilczek 1973

At small momenta, coupling becomes large → we need **nonperturbative methods!**

# Perturbative vs. nonperturbative

Interaction between **two electrons**:



“Quantum  
mechanics”

**Perturbative QFT:**  
Feynman diagrams & loops



J. S. Schwinger



S. Tomonaga



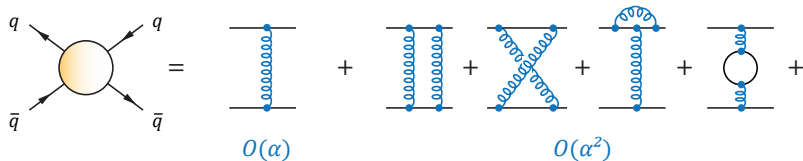
R. P. Feynman



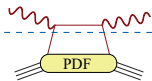
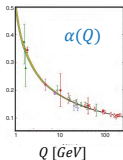
F. J. Dyson

# Perturbative vs. nonperturbative

Interaction between **quark and antiquark?**



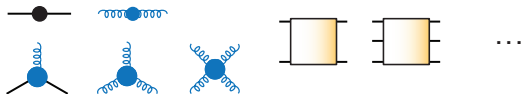
Answer still correct at large momenta:  
**high-energy scattering experiments**



What about low momenta, confinement, mass generation, hadron physics?  
→ need **nonperturbative methods!**

# Mass generation

A QFT is completely determined by its **correlation functions**:

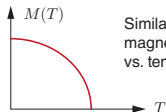


satisfy nonperturbative  
**Dyson-Schwinger** and  
**Bethe-Salpeter** equations

**Quark mass function**  $M(p^2) \neq 0$ , even for massless quarks: spontaneous breaking of chiral symmetry if  $\alpha > \alpha_{\text{crit}}$

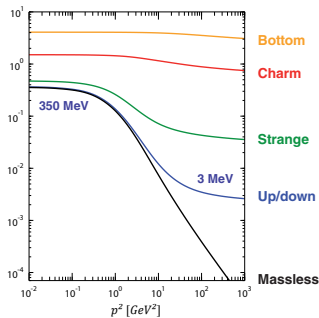
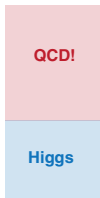


Cannot happen in perturbation theory!



Similar: magnet, magnetization vs. temperature

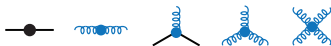
$M(p^2)$



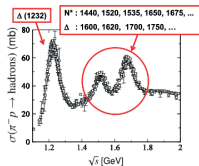


# Theory tools

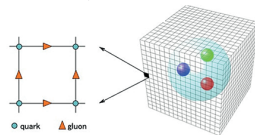
## Functional methods (DSEs & BSEs, FRG, ...)



## Amplitude analyses



## Lattice QCD



## Phenomenological models



## Effective theories (ChPT, ...)

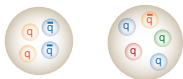


# Some hot topics in QCD

- **Confinement & mass generation**

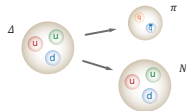
- **Hadron structure calculations:** form factors, PDFs, GPDs, ...

- **Exotic hadrons & multiquark states:** tetraquarks, pentaquarks, nuclei?

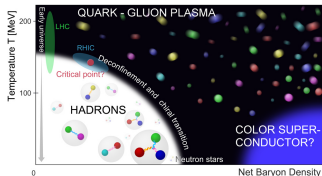


- **QCD contributions to BSM searches:** muon anomalous magnetic moment, flavor matrix elements, ...

- **Resonances:** most hadrons decay into other hadrons  $\leftrightarrow$  poles in complex plane



- **QCD under extreme conditions:** early universe, exotic phases, hadrons at large T and  $\mu$



# Toolbox

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## Physics:

- Particle physics
- Quantum field theory
- QCD & Hadron physics
- Nuclear physics
- Group theory
- ...

## Math:

- **Linear algebra:**  
dealing with large matrices
- **Complex analysis:**  
accessing the complex plane
- **Integral equations:**  
nonperturbative calculations

## Numerics:

- **Symbolic:**  
Mathematica, ...
- **Programming:**  
C++, Fortran, ...
- **Parallel computing:**  
MPI, OpenMP, CUDA, ...

# NPStrong at LIP



Alfred Stadler  
Lisboa  
Researcher



Ana Arriaga  
Lisboa  
Researcher



André Nunes  
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Trainee



André Torcato  
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