

MPI 2021

Lisbon, October 14th, 2021

# Accessing the proton UGD via exclusive polarized $\rho$ -meson leptoproduction at HERA and the EIC

Francesco Giovanni Celiberto

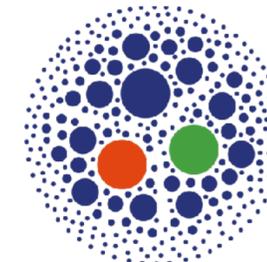
ECT\*/FBK Trento & INFN-TIFPA

ECT\*

EUROPEAN CENTRE FOR THEORETICAL STUDIES  
IN NUCLEAR PHYSICS AND RELATED AREAS



Trento Institute for  
Fundamental Physics  
and Applications



HAS QCD

HADRONIC STRUCTURE AND  
QUANTUM CHROMODYNAMICS

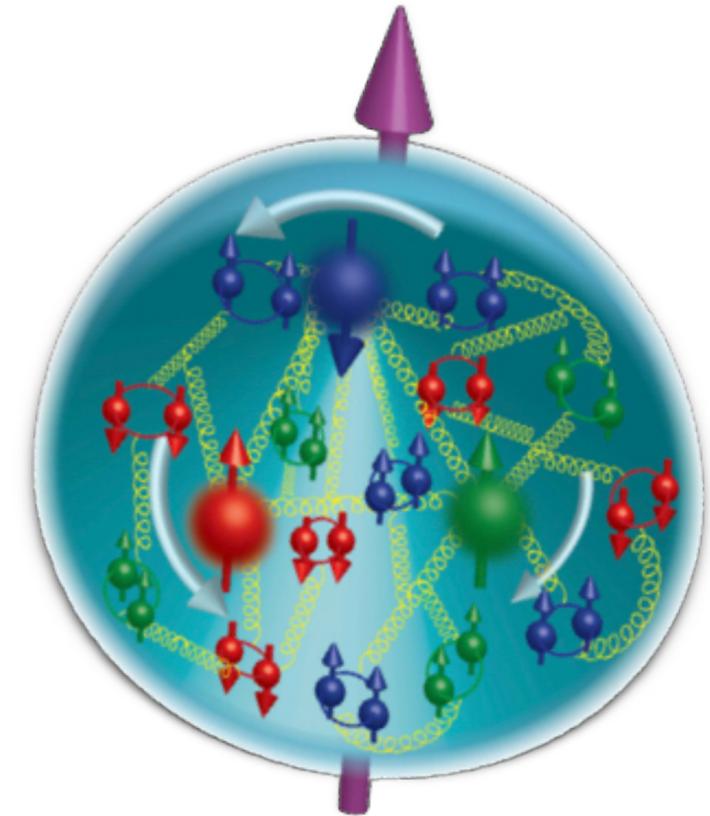
# Parton densities: hors d'œuvre



**Parton densities** → relevant for the search of **New Physics**...

→ ...crucial role in the understanding and exploration of **QCD**

- Describe the internal structure of the nucleon in terms of its elementary constituents (quarks and gluons)
- Nonperturbative** objects that enter the expression of cross sections
- Can be *extracted* from experiments via *global fits*



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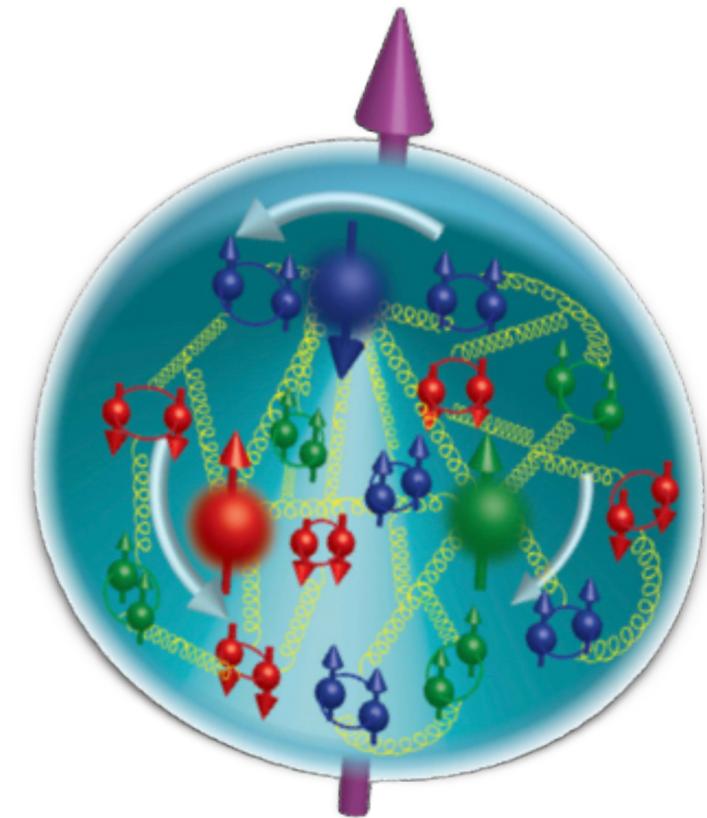
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Several types of distributions...

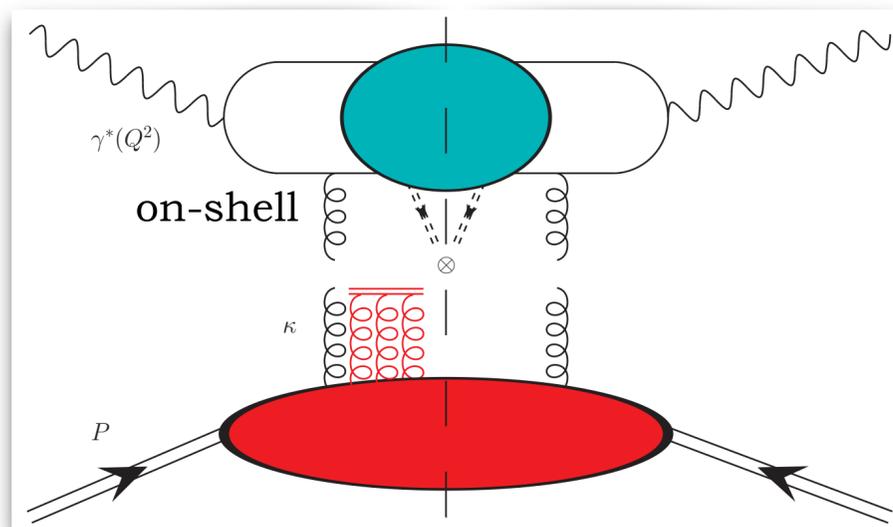
- Respect different **factorization theorems**
- Exhibit peculiar **universality properties**
- Obey distinct **evolution equations**



# TMD versus HEF



- \* Semi-inclusive processes
- \*  $\kappa_T \ll$  hardest scale
- \* Language of **parton correlators**
- \* Diagram: **SIDIS onium**

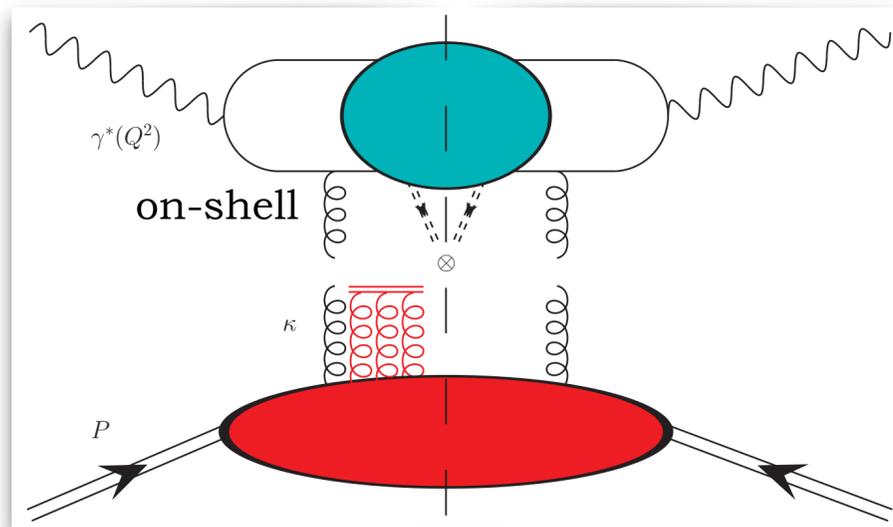


TMD  
PDF

# TMD versus HEF



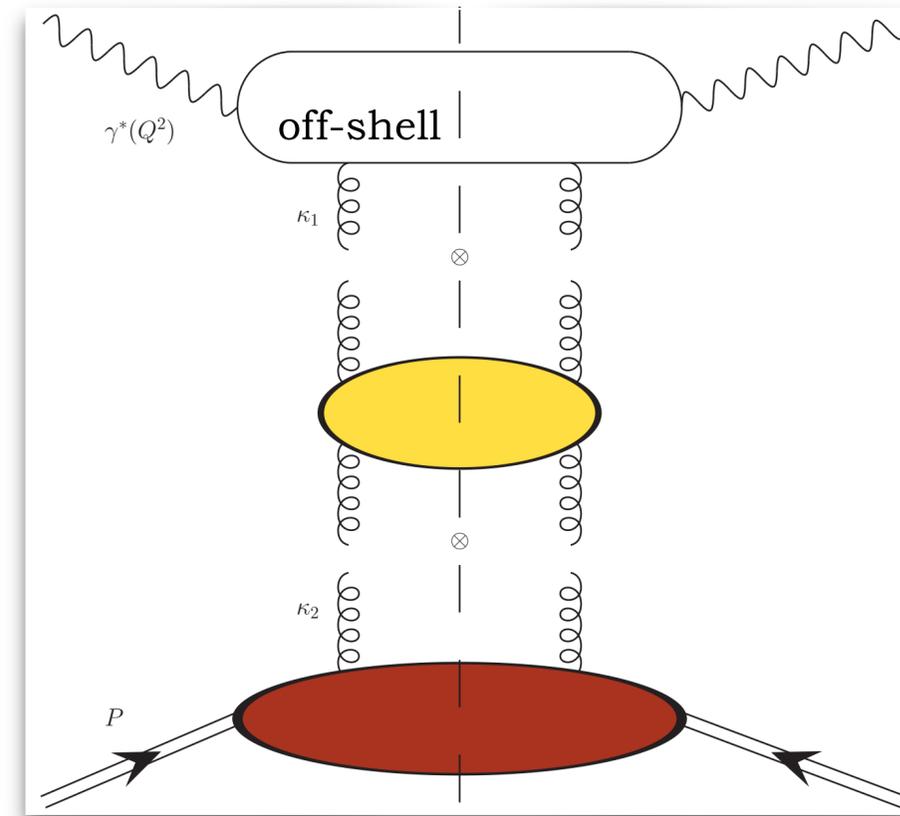
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TMD  
PDF



- \* Inclusive or exclusive processes (!)
- \* Small  $x$ , large  $\kappa_T$
- \* Language of **Reggeized gluons**
- \* Diagram: **DIS**



$\Phi^{\gamma^* \rightarrow \gamma^*}$



$\mathcal{G}_{\text{BFKL}}$

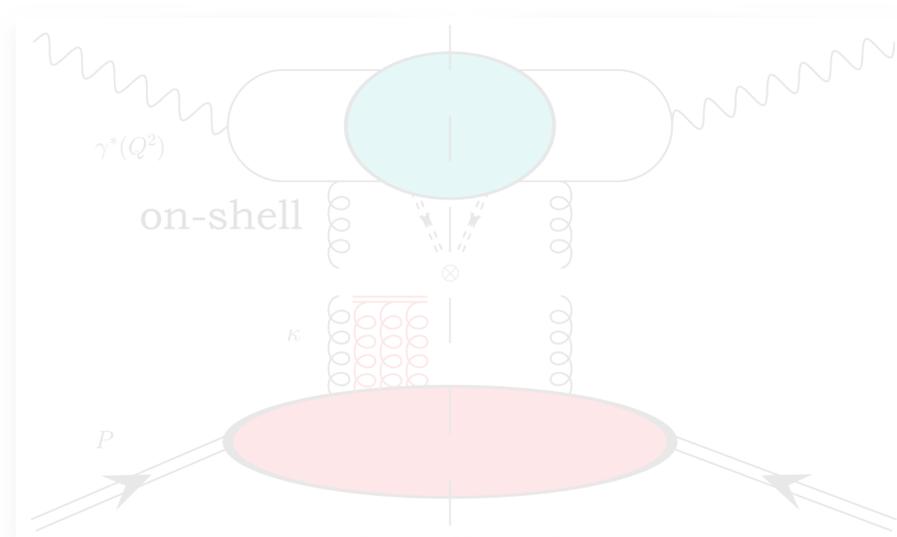


$\Phi^P_{[\text{NP}]}$

# TMD versus HEF

**IR-safe colorless**  $\{\Phi^{i \rightarrow 0}\}$   
 \* Semi-inclusive processes (Fadin-Martin theorem)  
 [V.S. Fadin, A.D. Martin (1999)]

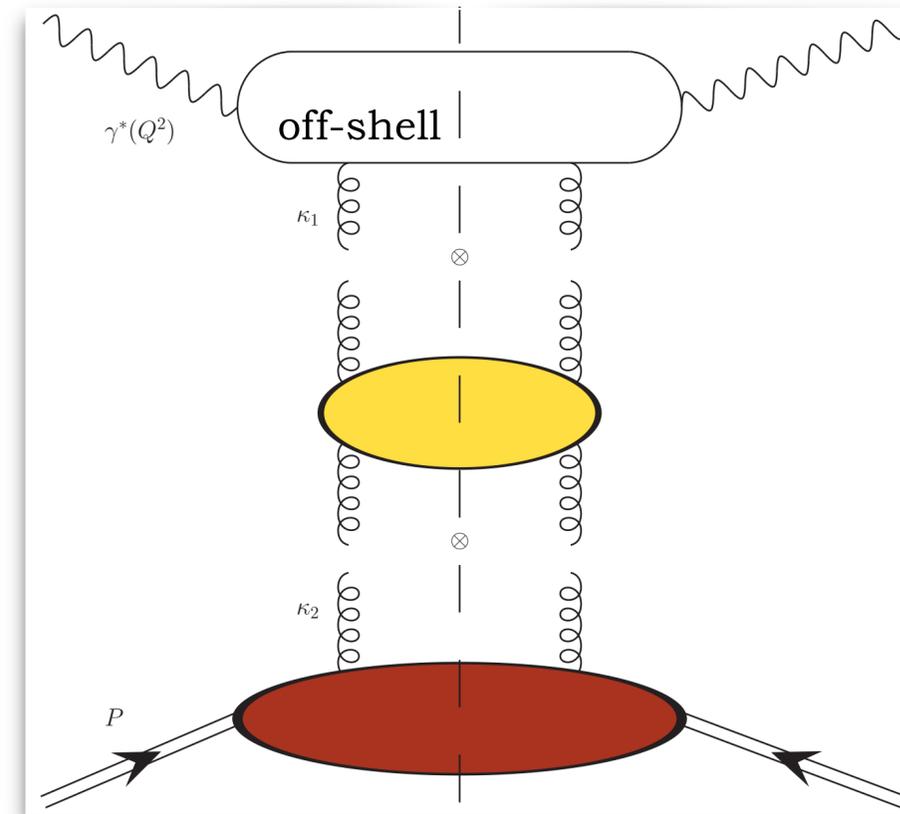
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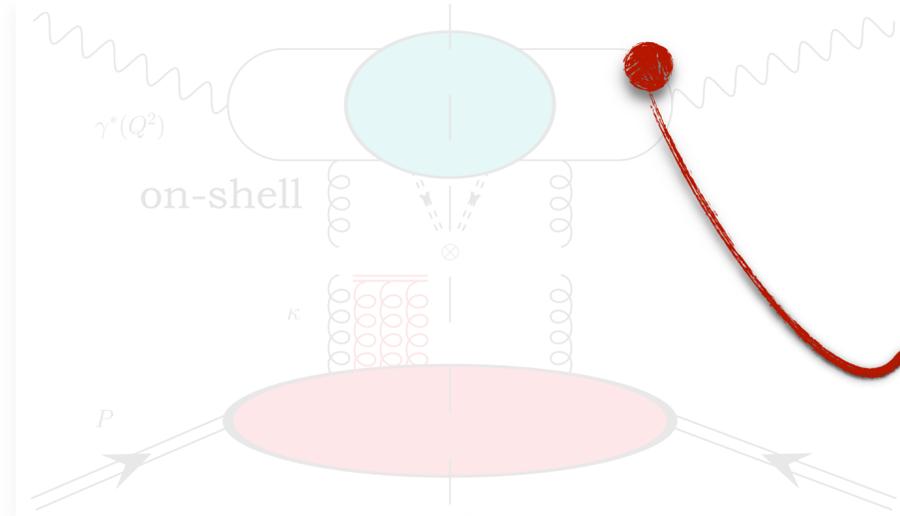
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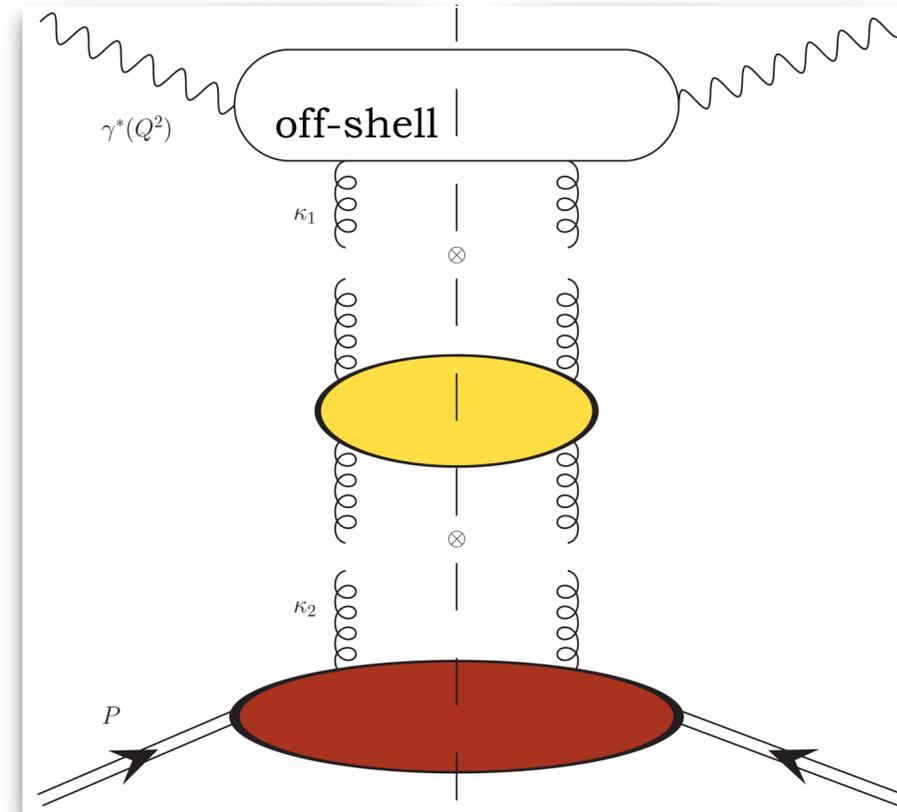
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**IR diffusion pattern**  
 (Bartels' cigar)  
 [J. Bartels, H. Lotter (1993)]



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$\Phi^{\gamma^* \rightarrow \gamma^*}$

$\otimes$

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$Q^2$



$Q_0^2$

# HEF at work: hybrid or pure factorization?

## Forward emissions

- \* *Asymmetric* config.  $\leftrightarrow$  fast parton + small- $x$  gluon

## Central emissions

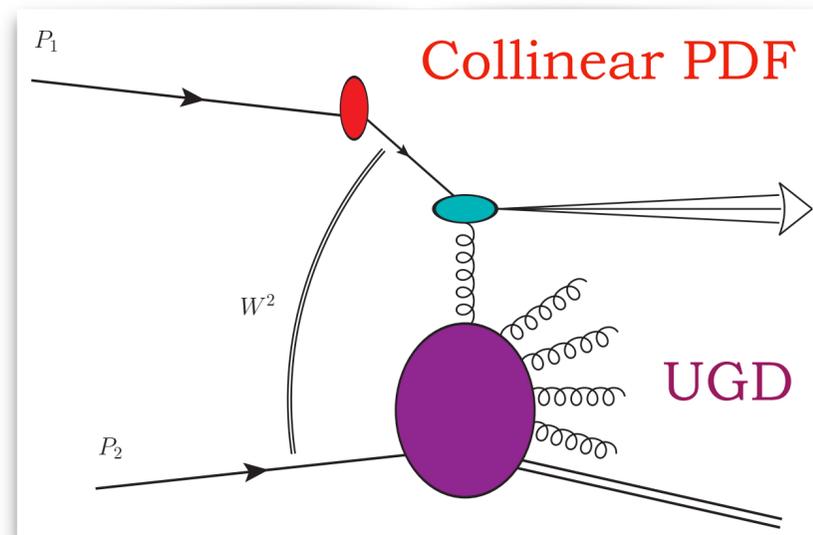
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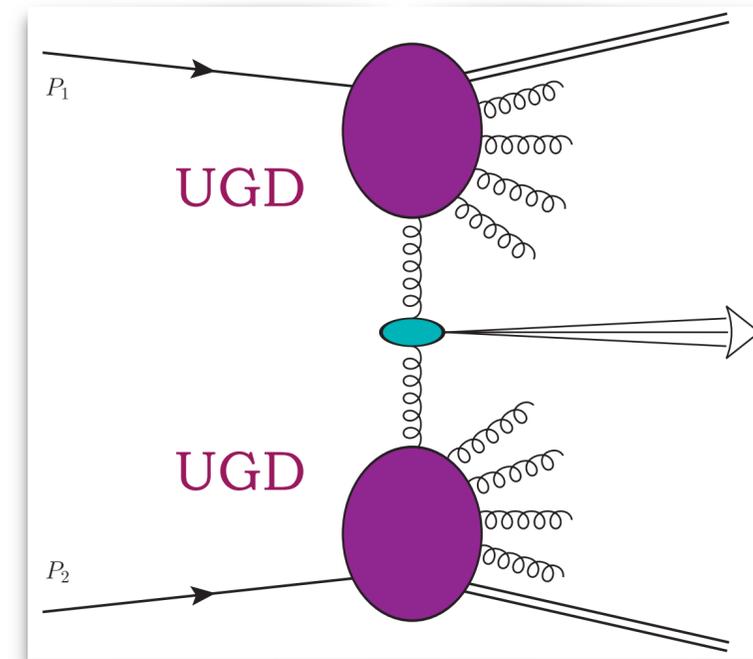
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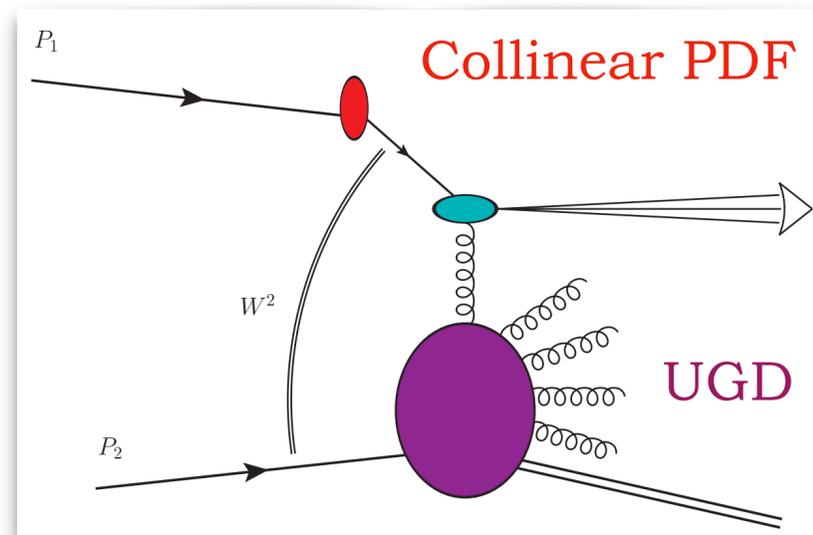
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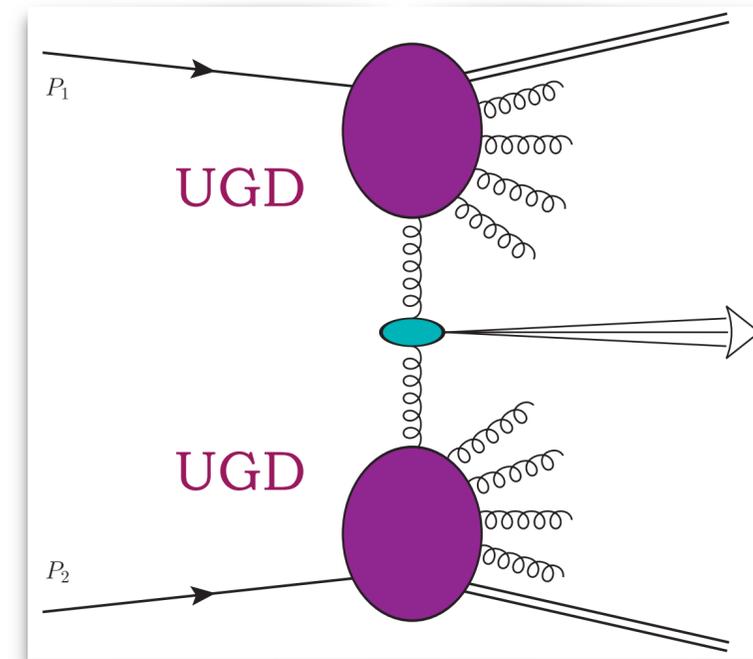
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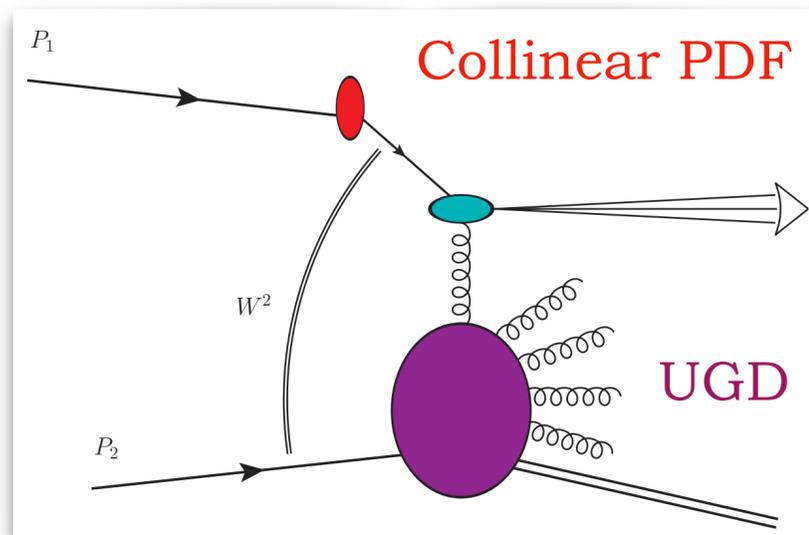


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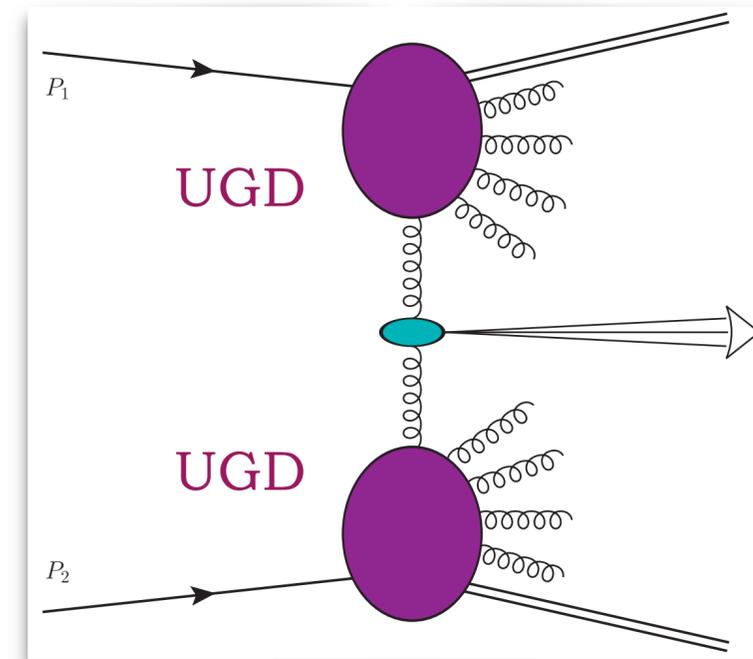
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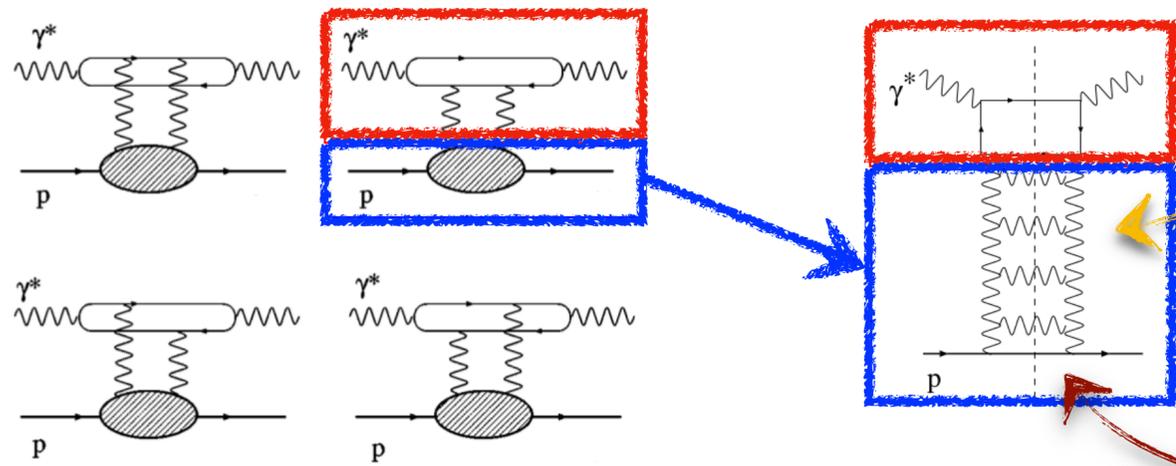
Table complemented by *exclusive* counterparts and *lepto-hadronic* channels

# High-energy factorization and the UGD

- example: **virtual photoabsorption** in **high-energy factorization**

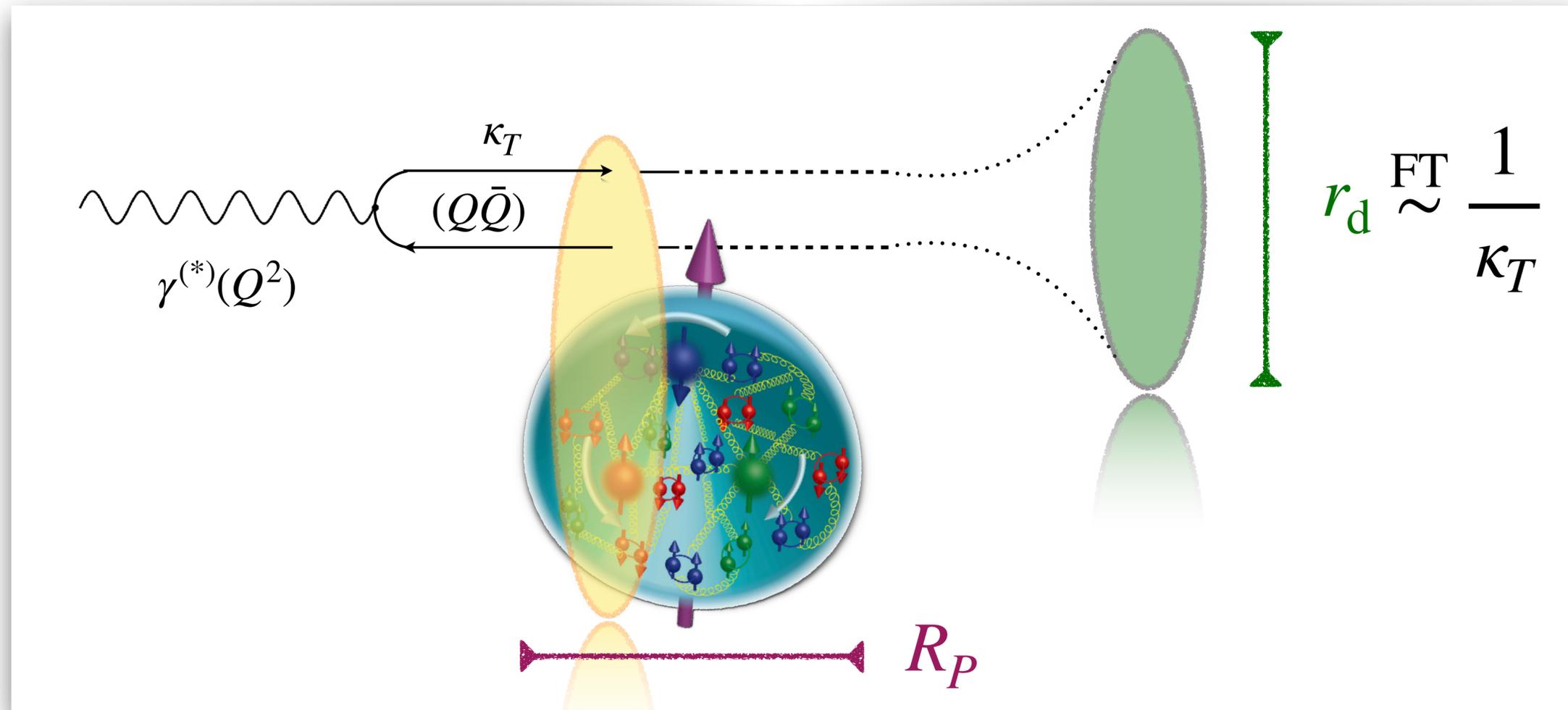
$$\sigma_{\text{tot}}(\gamma^* p \rightarrow X) \propto \text{Im}_s \{ \mathcal{A}(\gamma^* p \rightarrow \gamma^* p) \} \equiv \Phi_{\gamma^* \rightarrow \gamma^*} \circledast \mathcal{F}(x, \kappa^2)$$

- ◇  $\mathcal{F}(x, \kappa^2)$  is the **unintegrated gluon distribution (UGD)** in the proton



- ▶ Small- $x$  limit: **UGD** = [ **BFKL gluon ladder** ]  $\circledast$  [ **proton impact factor** ]
  - ◇ Takes into account the **resummation** of **high-energy logs**
  - ◇ Describes the **coupling** of the gluon Green's function to the **proton**
- ▶ Proton impact factor is non-perturbative  $\implies$  UGD needs to be modeled!

# Diffractive $\gamma^{(*)}P$ scattering and color dipoles

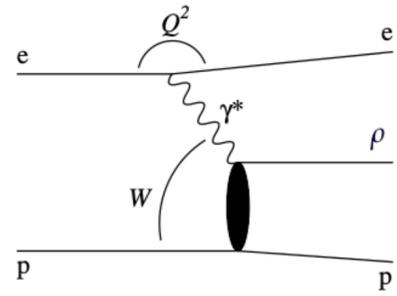


$$W_{\mu\nu} \propto \text{Im} \left\{ i \int d^4x e^{iq \cdot x} \langle P | T [J_\mu(x) J_\nu(0)] | P \rangle \right\}$$

- \* Small- $x \Rightarrow$  ***Ioffe time***  $\gg R_P$
- \* At least one  $J_\mu$  outside proton...
- \* **...color dipole picture!**

**Exclusive emissions  
of forward mesons**

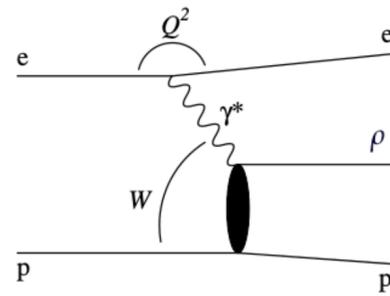
# Exclusive forward $\rho$ -meson leptonproduction



- High-energy regime:  
 $s \equiv W^2 \gg Q^2 \gg \Lambda_{\text{QCD}}^2 \implies \text{small } x = \frac{Q^2}{W^2}$
- photon virtuality  $Q$  is the **hard scale** of the process

► **Process solved in helicity**  $\implies$  so far **unexplored testfield** for UGD

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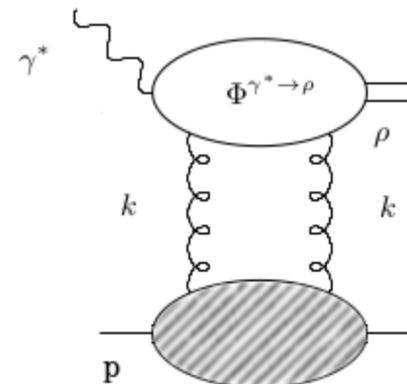
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Leading **helicity amplitudes** are known

## Assumption:

- $\mathcal{I}m_s \{ \mathcal{A}(\gamma^* p \rightarrow \rho p) \}$
- same  $W$ - and  $t$ -dependence for  $T_{11}$  and  $T_{00}$   $\implies$  high-energy factorization  
 $\rightarrow$  same physical mechanism, scattering of small transverse size of dipole on the proton target, at work  $\implies$  high-energy factorization

$$T_{\lambda_\rho \lambda_\gamma}(s; Q^2) = is \int \frac{d^2 \kappa}{(\kappa^2)^2} \Phi^{\gamma^*(\lambda_\gamma) \rightarrow \rho(\lambda_\rho)}(\kappa^2, Q^2) \mathcal{F}(x, \kappa^2), \quad x = \frac{Q^2}{s}$$



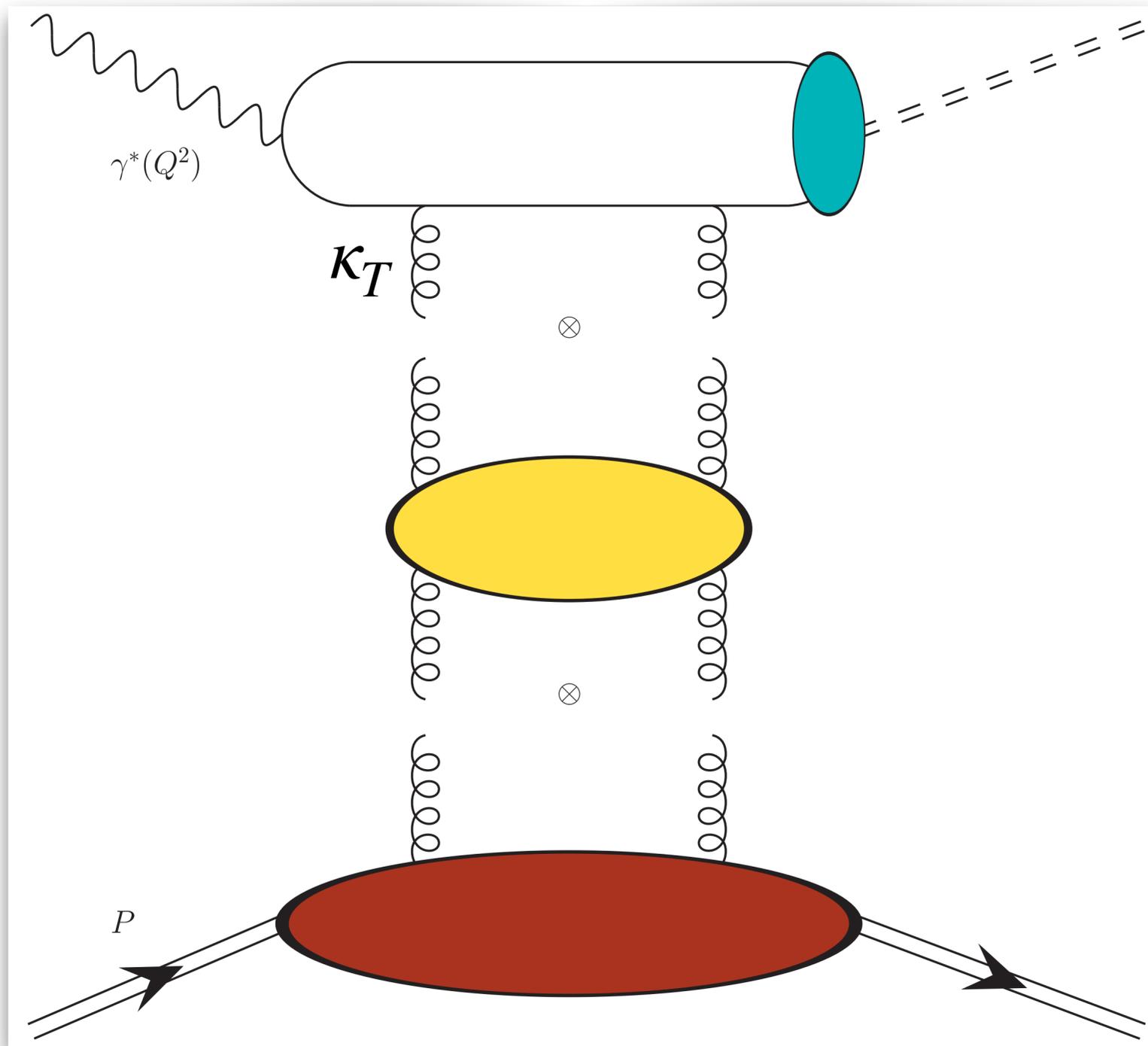
Interesting transitions:

- $\gamma_L^* \rightarrow \rho_L$   $\xrightarrow{\text{encoded by}}$   $\Phi^{\gamma_L^* \rightarrow \rho_L}$
- $\gamma_T^* \rightarrow \rho_T$   $\xrightarrow{\text{encoded by}}$   $\Phi^{\gamma_T^* \rightarrow \rho_T}$

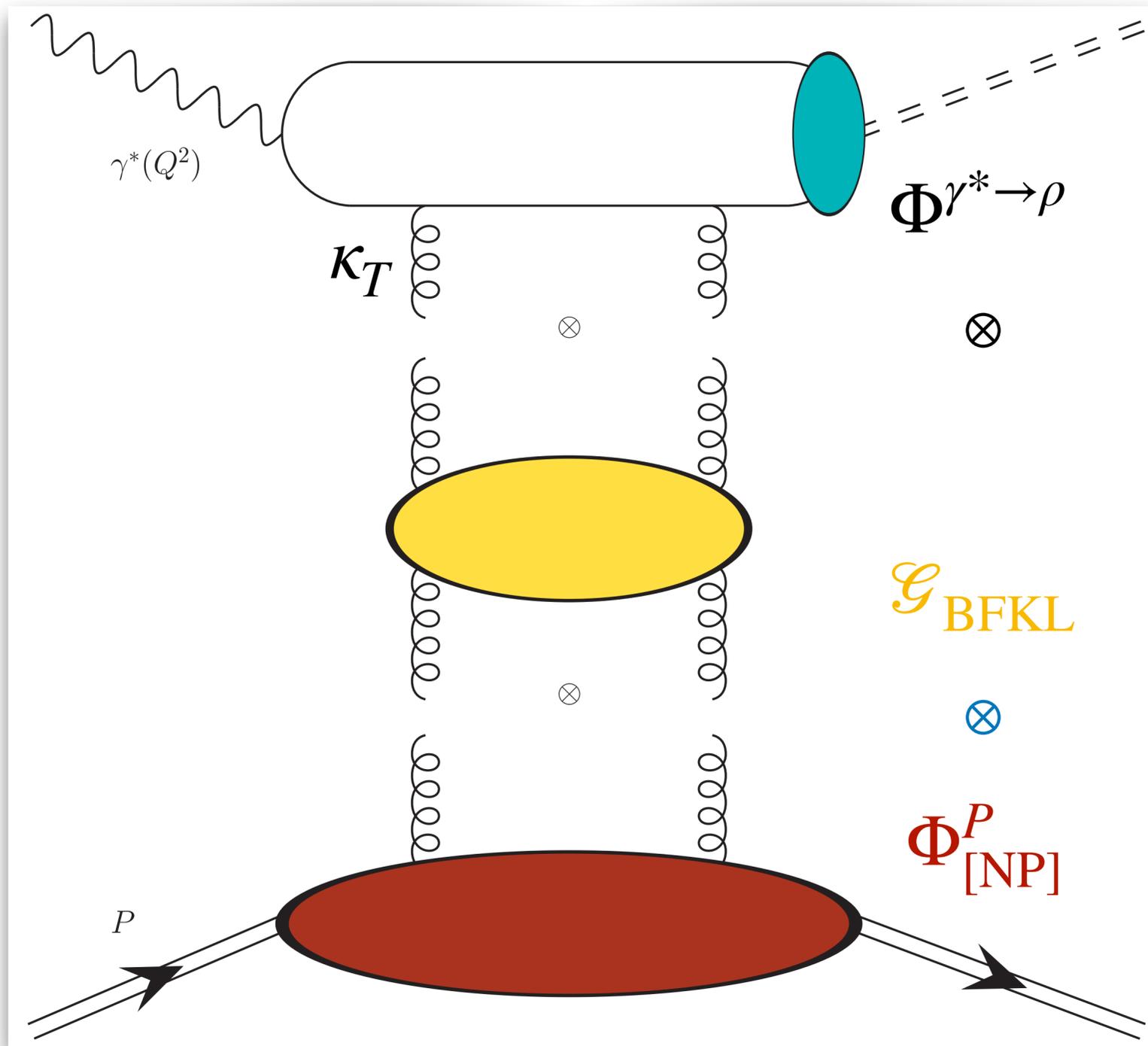
$\implies$  **DAs** enter in  $\Phi^{\gamma^* \rightarrow \rho}$



# A factorization...of factorizations

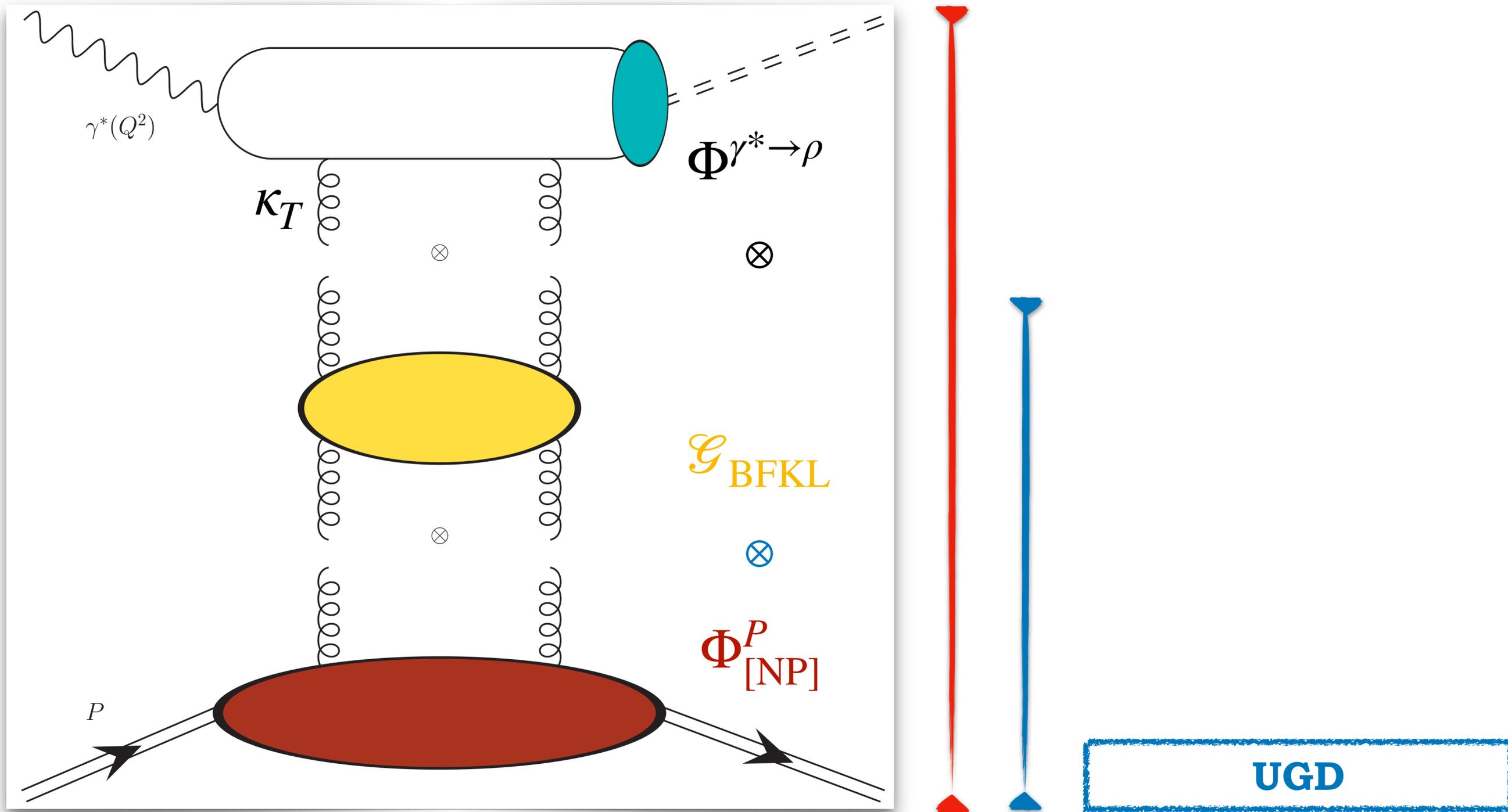


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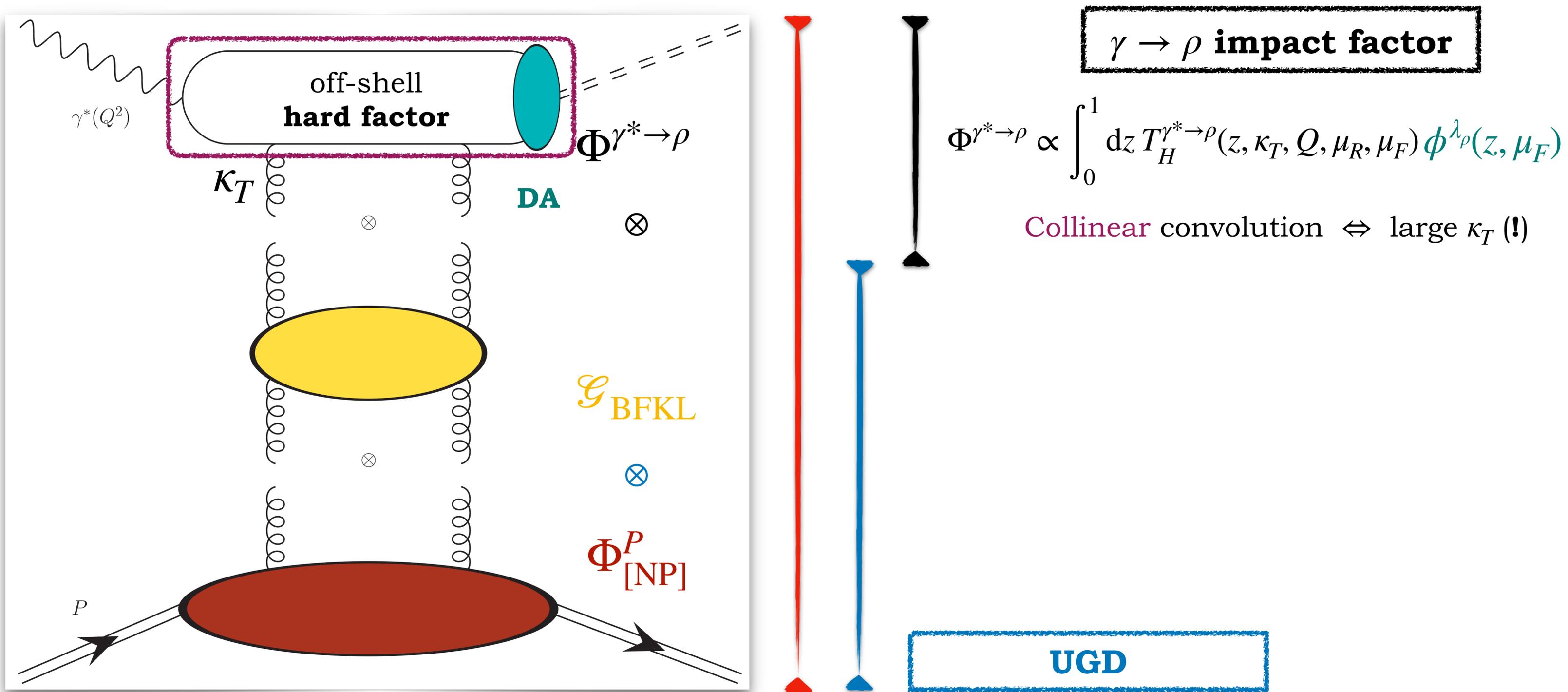
**BFKL factorization**

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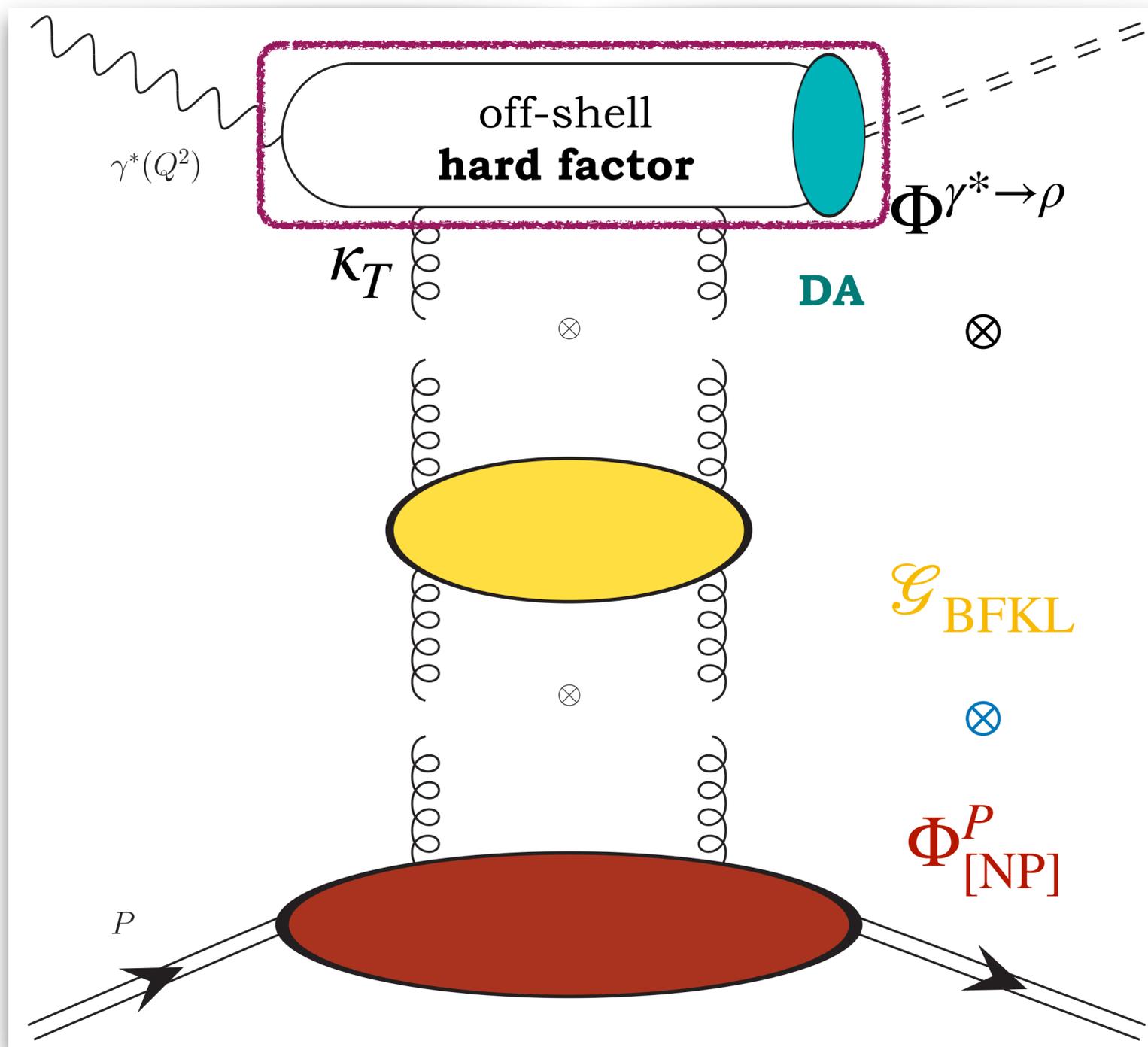
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**$\gamma \rightarrow \rho$  impact factor**

$$\Phi^{\gamma^* \rightarrow \rho} \propto \int_0^1 dz T_H^{\gamma^* \rightarrow \rho}(z, \kappa_T, Q, \mu_R, \mu_F) \phi^{\lambda_\rho}(z, \mu_F)$$

Collinear convolution  $\Leftrightarrow$  large  $\kappa_T$  (!)

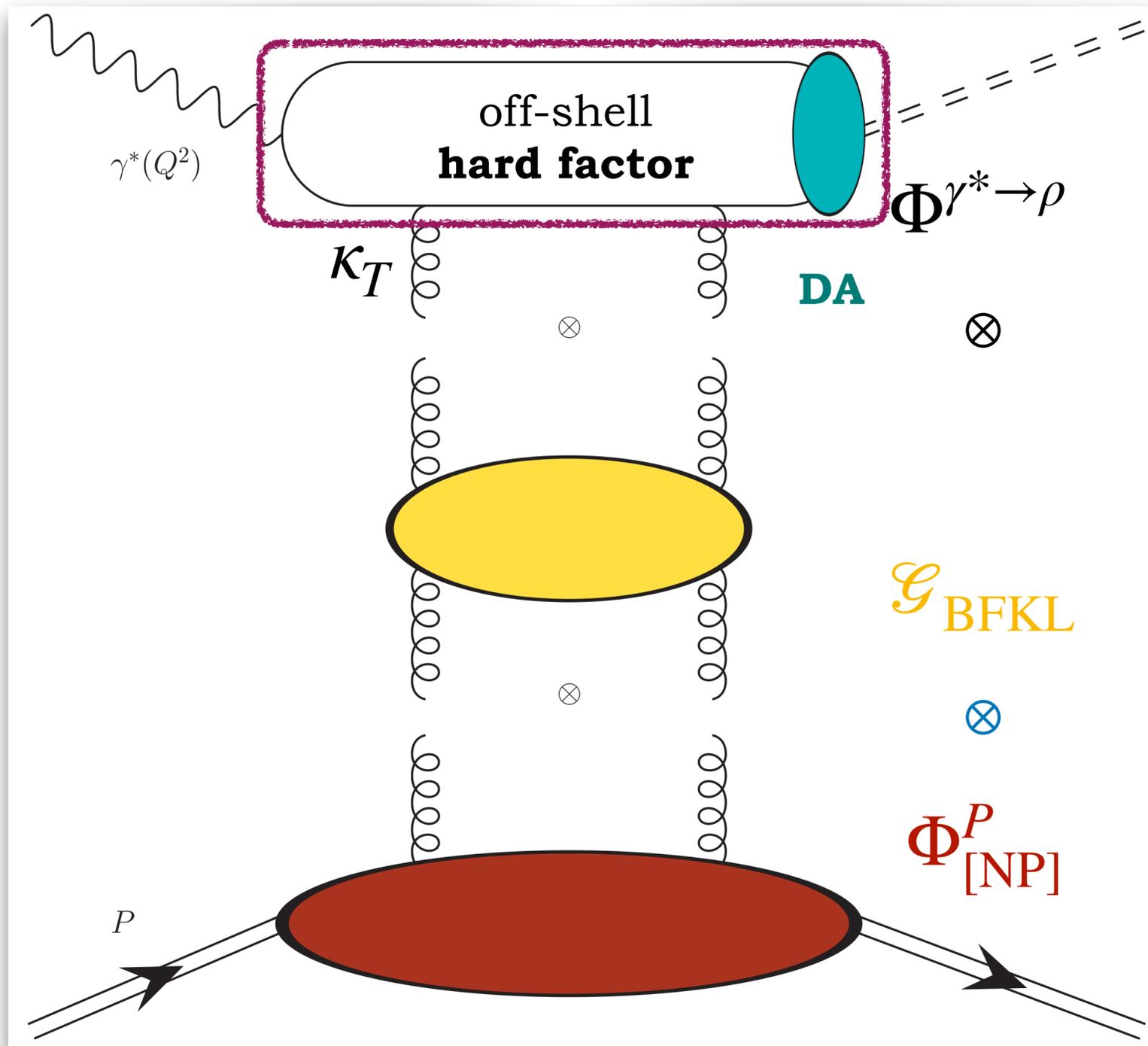
\*  $\gamma_L^* \rightarrow \rho_L$  transition:

$$\frac{1}{\kappa_T^2} \Phi^{\gamma_L^* \rightarrow \rho_L} \underset{\kappa_T \rightarrow 0^+}{\sim} \text{constant}$$

**UGD**

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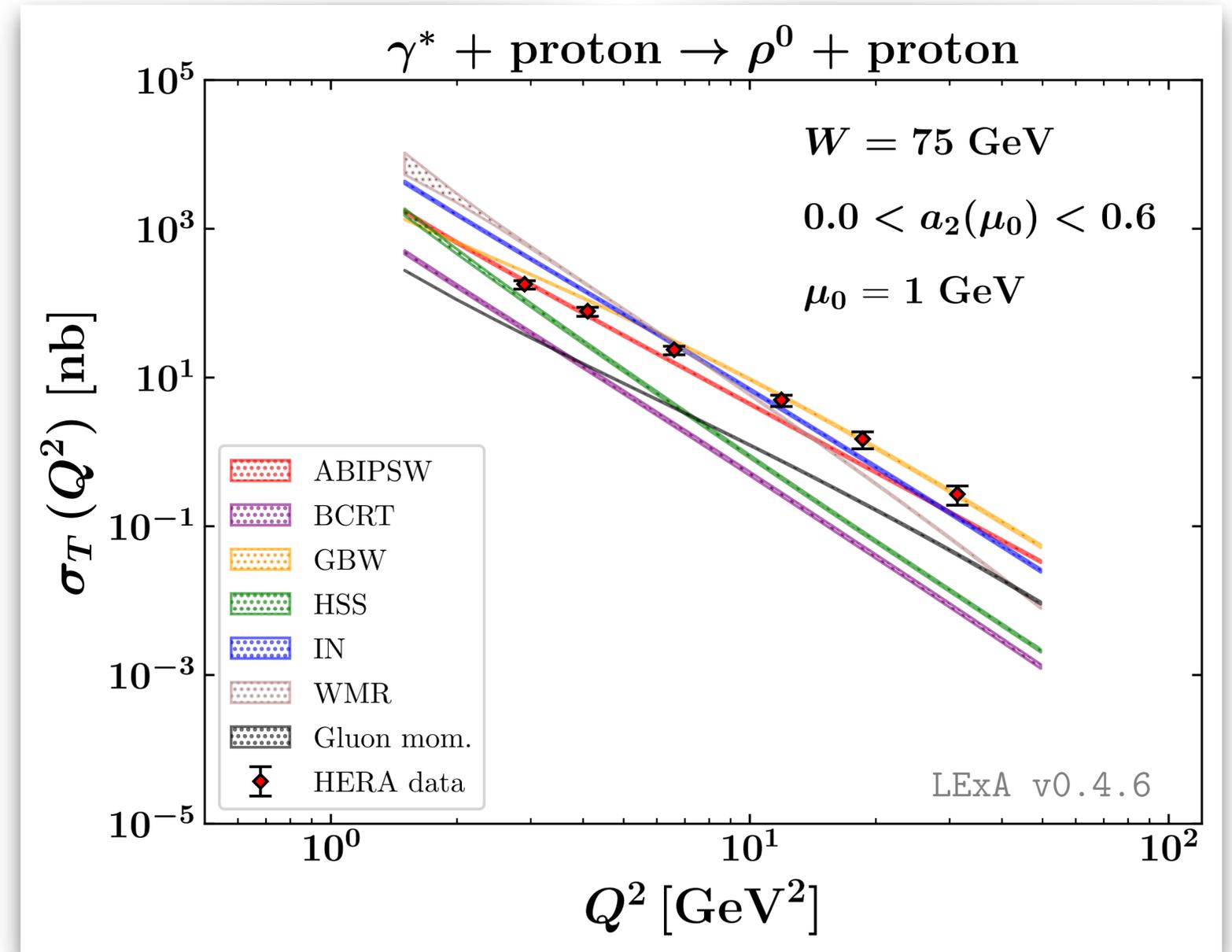
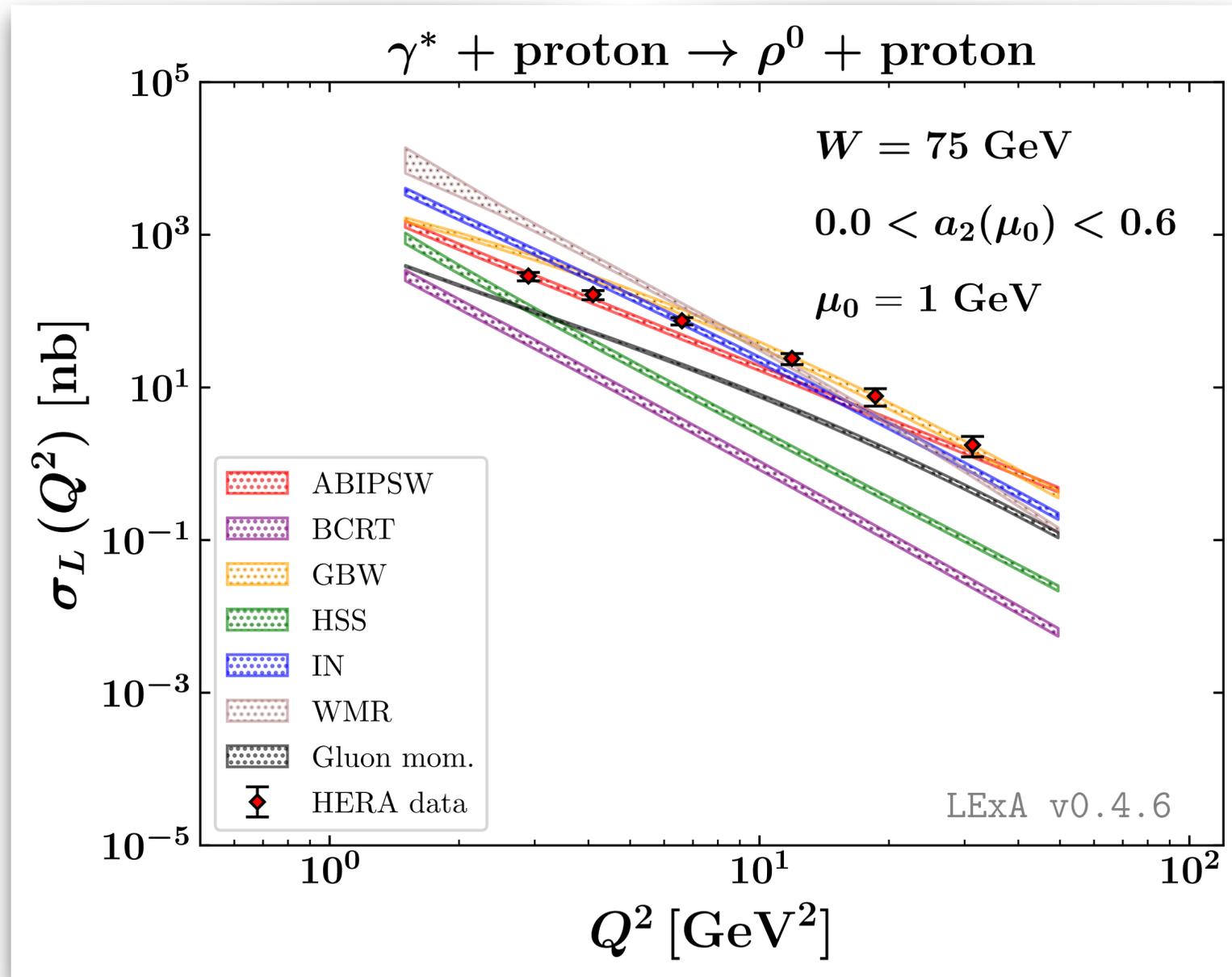
\*  $\gamma_T^* \rightarrow \rho_T$  transition:

$$\frac{1}{\kappa_T^2} \Phi^{\gamma_T^* \rightarrow \rho_T} \sim \ln \frac{\kappa_T^2}{Q^2}_{\kappa_T \rightarrow 0^+}$$

UGD

**BFKL factorization**

# Exclusive forward $\rho$ -meson production at HERA

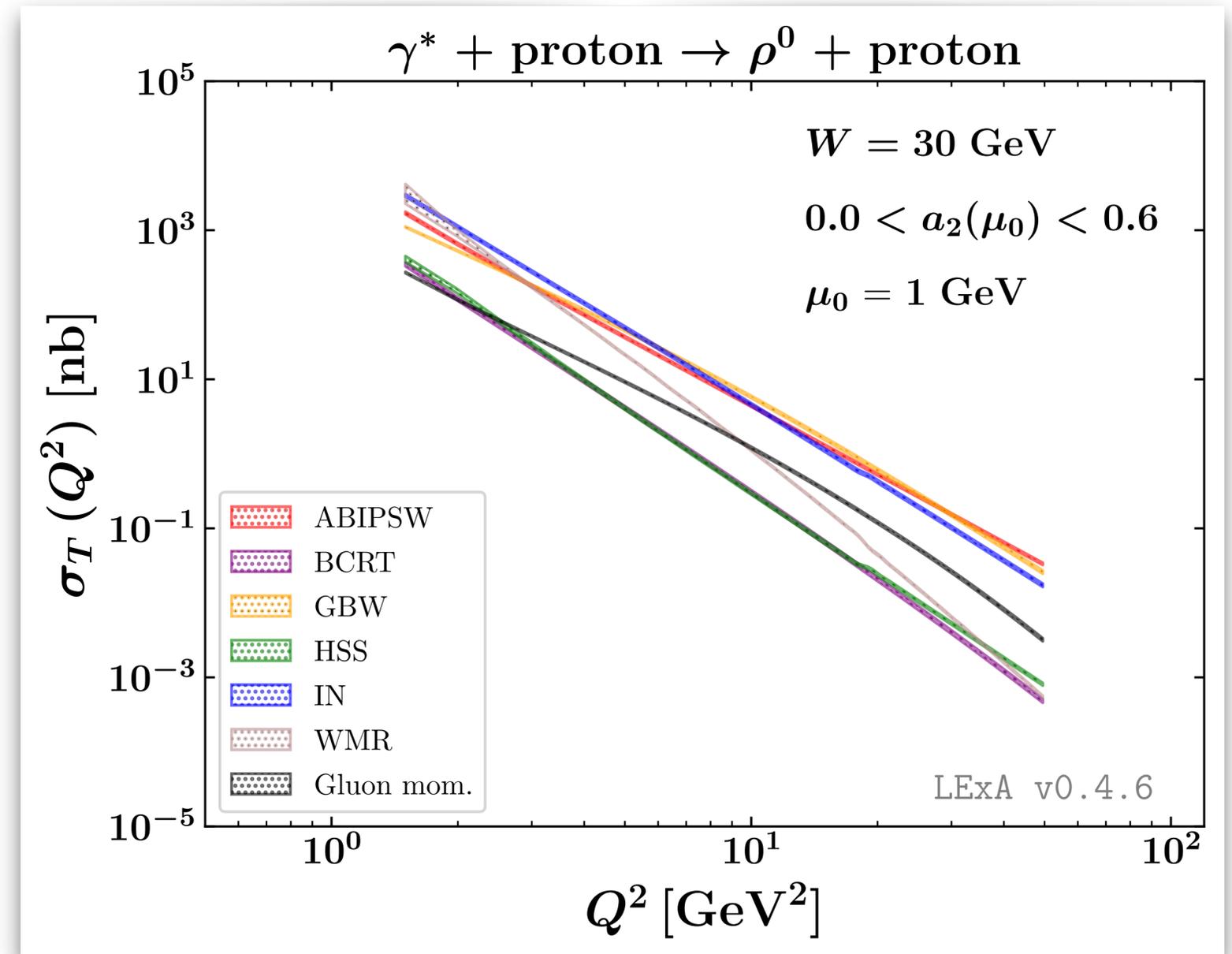
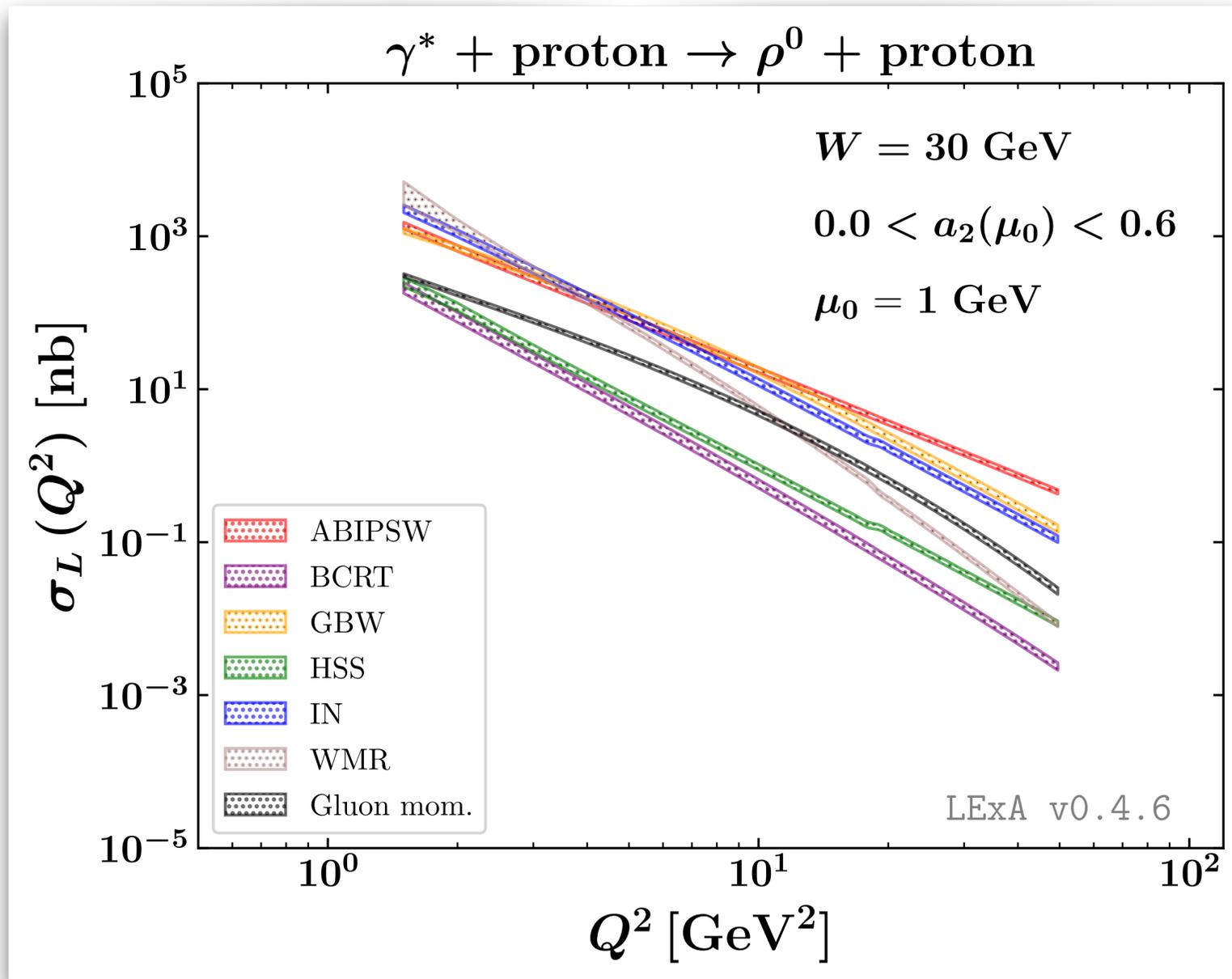


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# Single forward emissions

## Exclusive light VM: $\rho^0, \omega, \phi$

- \* *Small-size* dipoles  $\Rightarrow$  large  $\kappa_T$
  - \* **Collinear** description: twist-2/-3 LVM NP **DAs**
- $$\Phi^{\gamma^* \rightarrow \rho} \propto \int_0^1 dz T_H^{\gamma^* \rightarrow \rho}(z, \kappa_T, Q, \mu_R, \mu_F) \phi^{\lambda_\rho}(z, \mu_F)$$
- \* Significance of small  $\kappa_T$  under investigation...
  - \* HERA indication: no large- $r_d$  dynamics
  - \* Pheno outcome: sensitivity to **intermediate**  $\kappa_T$
  - \* **LVMs as tools**: discrimination among UGD models

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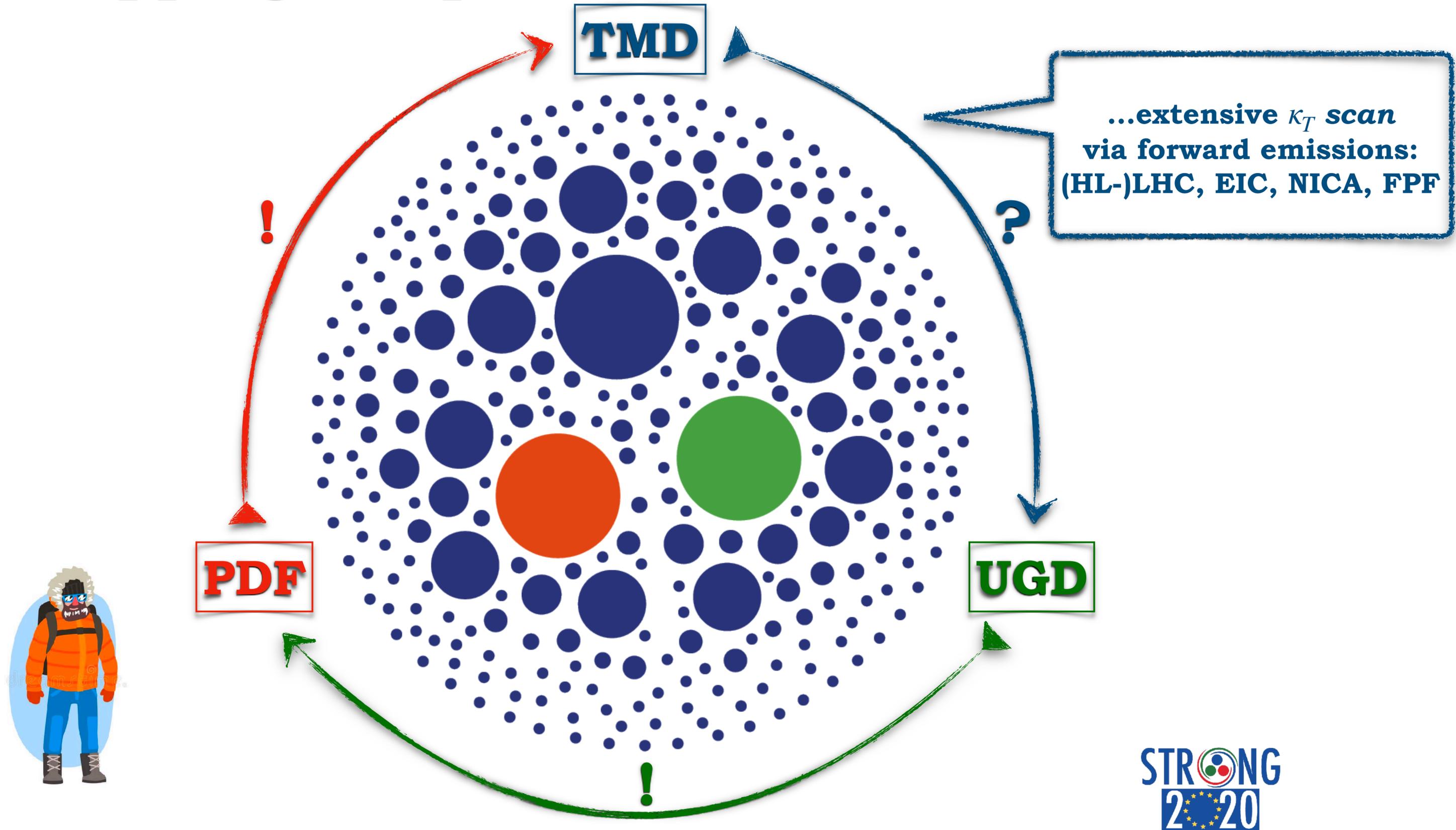
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## Quarkonia

- \* Size of dipoles  $\Rightarrow$  wide range of  $\kappa_T$
- \* Description: **NRQCD** (combined with LFWFs)
- $$\left[ \text{LFWF} \otimes \mathcal{A}_{\text{dip.}} \right] \xleftrightarrow{\text{dilute}} \left[ \Phi^{\gamma^* \rightarrow J/\Psi} \otimes \text{UGD} \right]$$
- \* Validity of *small-size* dipoles questionable...
- \* NRQCD: large- $r_d$  dynamics for  $\Psi(2s)$  ( $\Upsilon(2s)$  ?)
- 🔗 [K. Suzuki et al. (2000)]; 🔗 [J. Cepila et al. (2019)]; 🔗 [M. Hentschinski et al. (2020)]
- \* **Onia as tools**: scan of TMD/HEF intersection range

# Mapping the proton content at small- $x$



**Backup  
slides**

# Omnes viae small- $x$ ducunt

Incomplete list of small- $x$  formalisms  $\rightarrow$  *linear* (BFKL) or *saturation* (BK/JIMWLK) effects embodied



## Unintegrated parton densities

*A (hybrid) high-energy factorization established*

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- \* HEF, CCFM, PRA **uPDFs**: BFKL + collinear matching

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*DGLAP description improved via BFKL*

- \* **ABF approach**: PDFs + small- $x$  resummed splitting

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*Nonperturbative content via an enhanced spectator model*

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## Helicity and OAM at small- $x$

*Need for sub-eikonal corrections, neglected by BFKL*

- \* **BER**: DLA, flavor singlet and nonsinglet
- \* **KPS**: evolution via Wilson lines, saturation



## CGC/JIMWLK gluon TMDs

*Gluon-recombination effects encoded*

- \* **WW** vs **DP** gluon TMDs, **GTMDs**
- \* **iTMD**: interpolating between TMD and BFKL regimes

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[\[R.D. Ball, V. Bertone, M. Bonvini, S. Marzani, J. Rojo, L. Rottoli \(2018\)\]](#)



## Small- $x$ improved gluon TMDs

*Nonperturbative content via an enhanced spectator model*

- \* **Pavia model**: initial-scale  $f_1^g$  and  $g_{1L}^g$  matched to PDFs

[\[A. Bacchetta, F.G.C., M. Radici, P. Taelis \(2020\)\]](#)



## Helicity and OAM at small- $x$

*Need for sub-eikonal corrections, neglected by BFKL*

- \* **BER**: DLA, flavor singlet and nonsinglet
- \* **KPS**: evolution via Wilson lines, saturation



## CGC/JIMWLK gluon TMDs

*Gluon-recombination effects encoded*

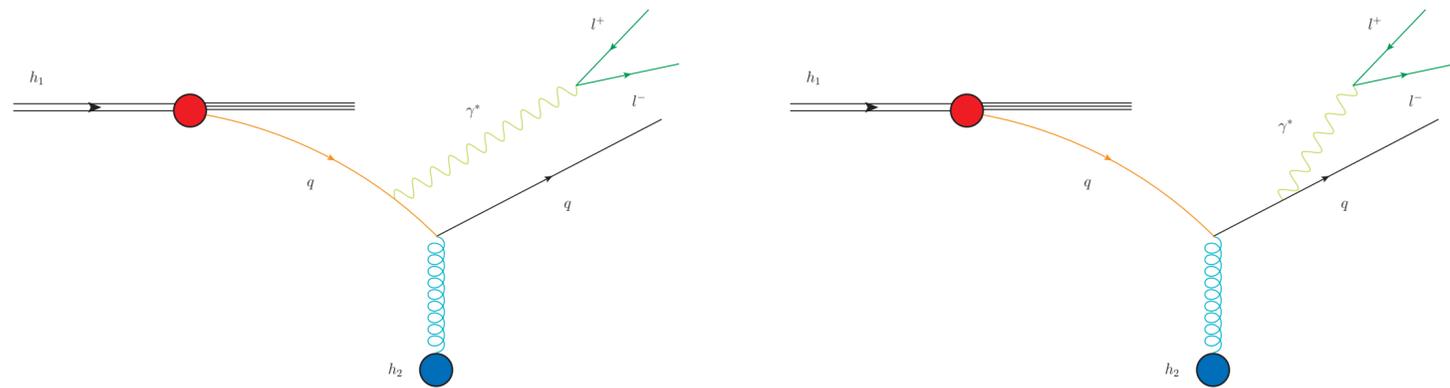
- \* **WW** vs **DP** gluon TMDs, **GTMDs**
- \* **iTMD**: interpolating between TMD and BFKL regimes

# Inclusive forward Drell-Yan dilepton production

- LHC, **forward region**  $\rightarrow (l^+ l^-)$  produced in the fragmentation region of  $h_2$ 
  - ◇ Asymmetric configuration:  $x_1 \gg x_2$ , down to  $x_2 \simeq 10^{-6}$
  - $\implies$  **possible small- $x$  resummation effects expected!**
- **small- $x$**   $\rightarrow$  evolution of sea  $q(\bar{q})$  inside  $h_2$  driven by gluon evolution
  - ◇ Dominance of sea  $q(\bar{q})$  emerging in the last splitting (suppression of quark propagator at large rapidity)
- **high-energy factorization**  $\rightarrow$  gluon exchange in the  $t$ -channel
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- Helicity structure functions in high-energy factorization:

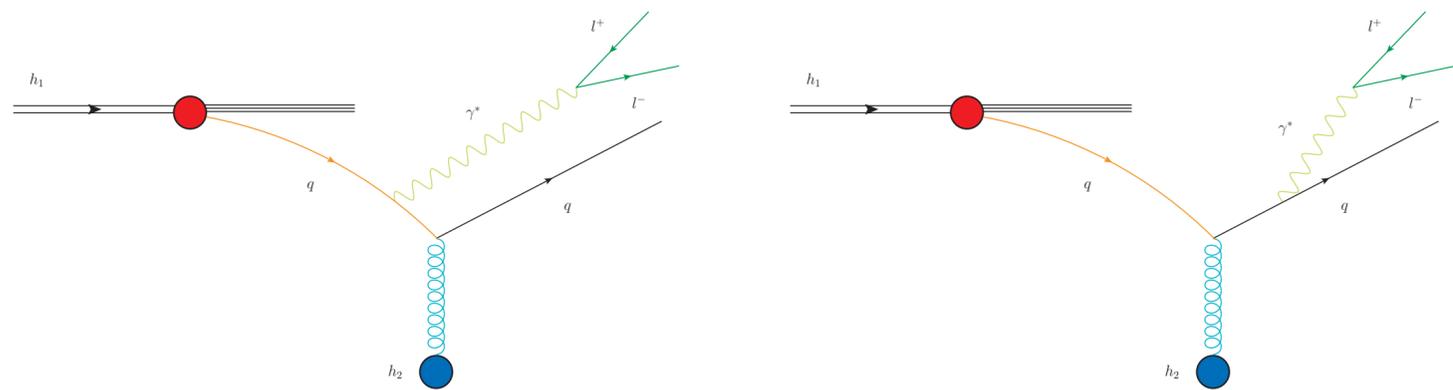
$$\mathcal{W}_{[\lambda]} = \frac{2\pi M^2}{3} \int_{x_F}^1 \frac{dz}{z^2} \sum_{r=q, \bar{q}} f_r\left(\frac{x_F}{z}, \mu_F\right) \int \frac{d\kappa_T d\Phi_{\kappa_T}}{(\kappa_T^2)^2} \alpha_s(\mu_R) \mathcal{F}(x_g, \kappa_T^2) \Phi_{[\lambda]}(q_T, \vec{\kappa}_T, z)$$

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[D. Brzemiński, L. Motyka, M. Sadzikowski, T. Stebel (2017)]

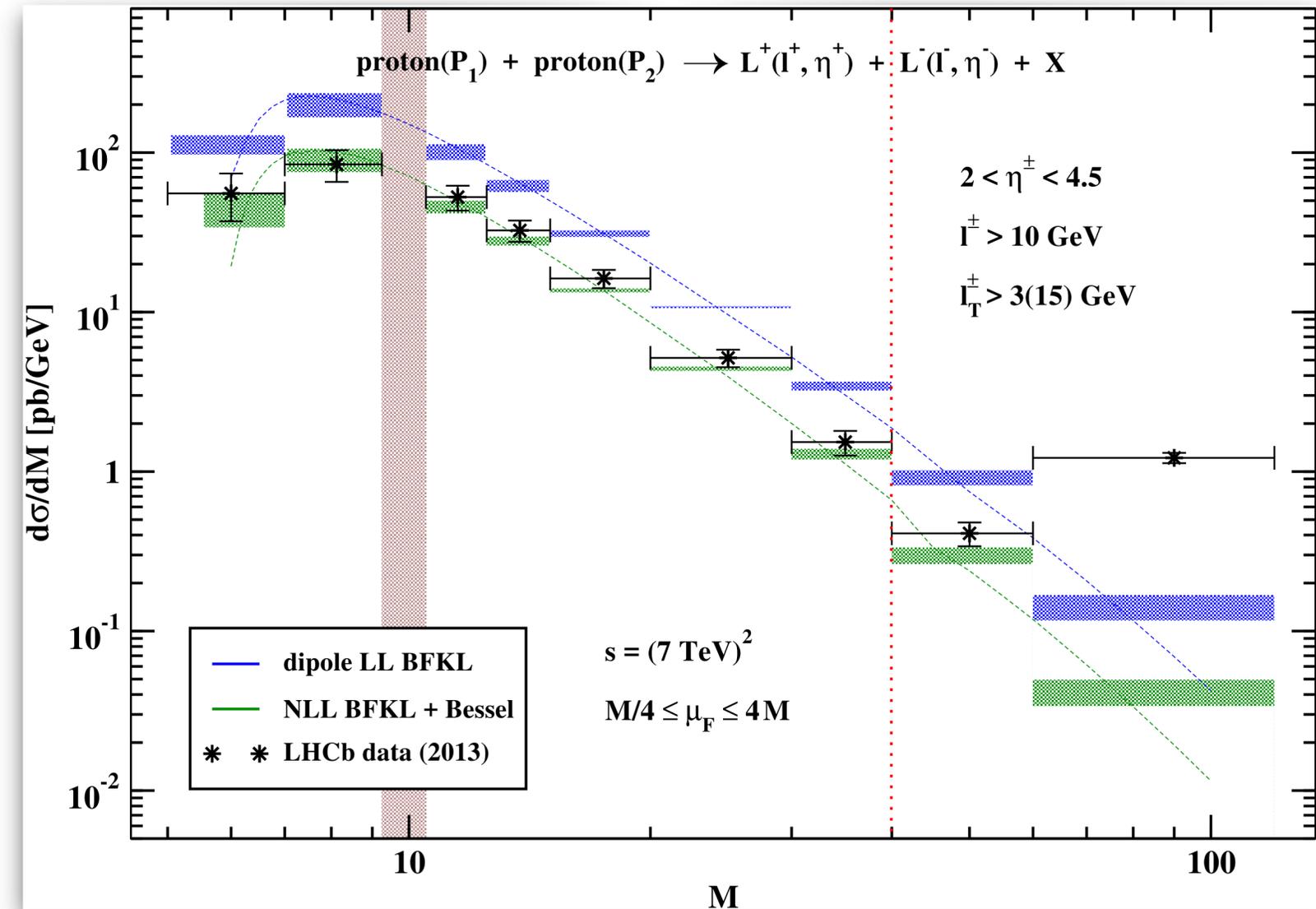
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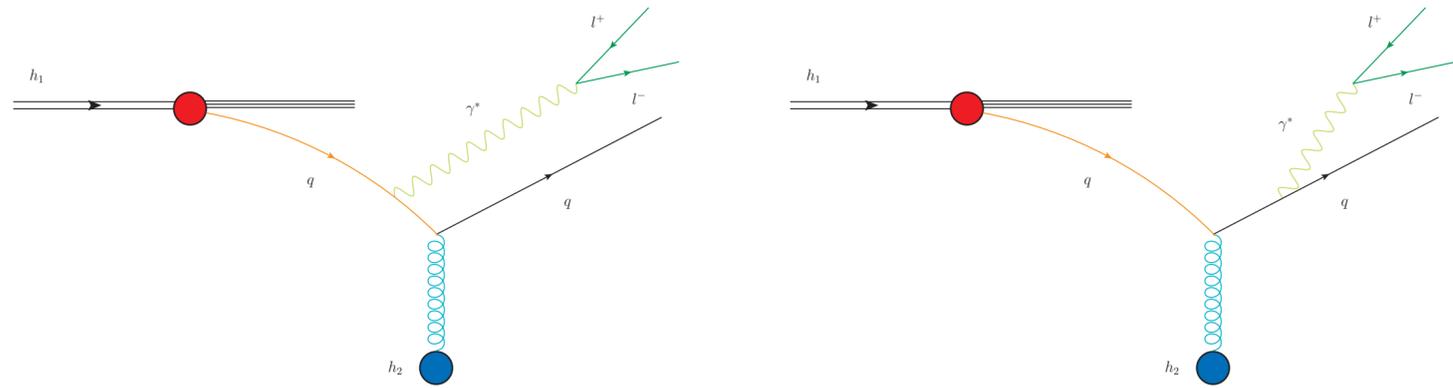


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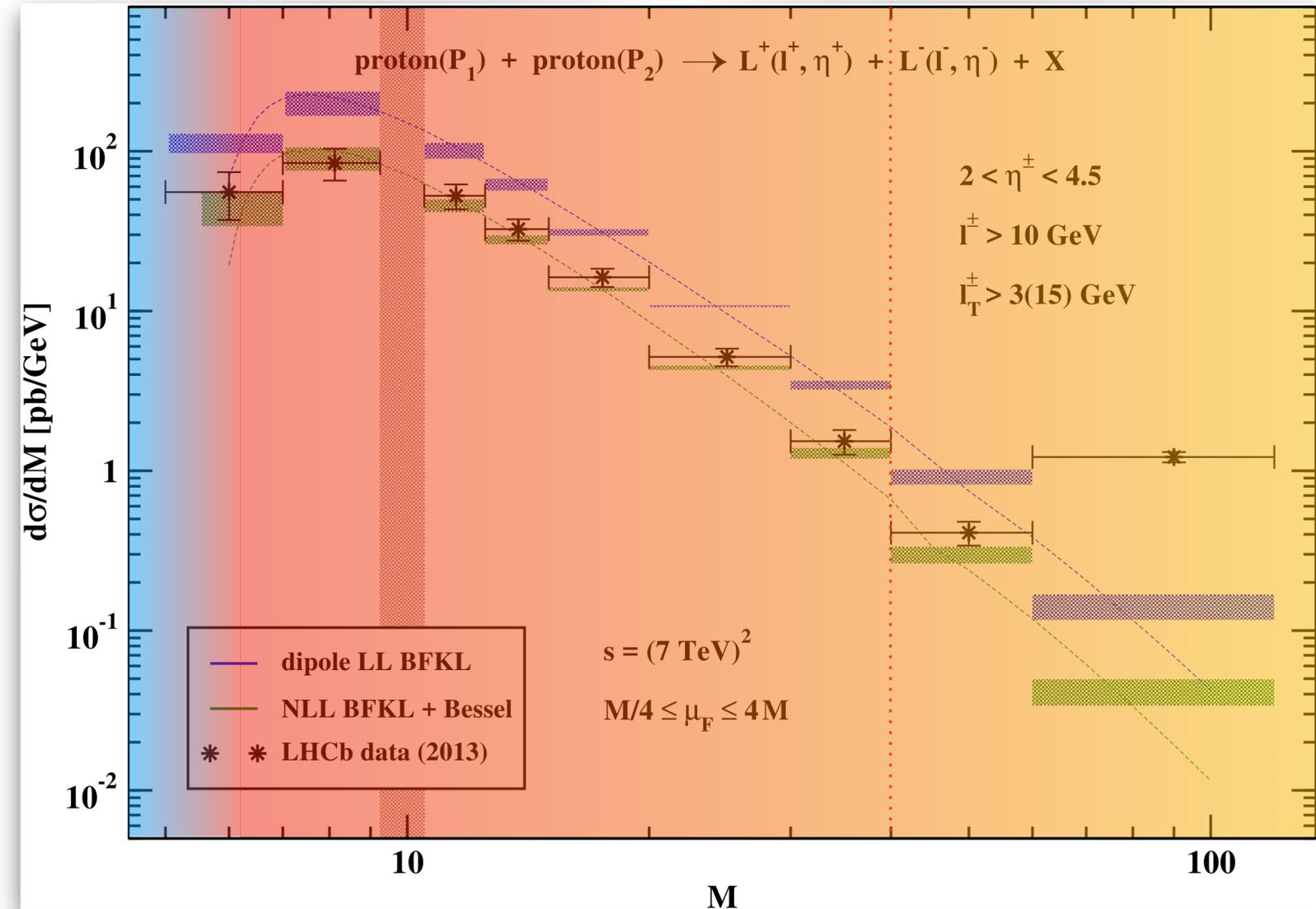
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approaching limits of semi-hard regime



$Z^0$  contribution becoming relevant

Backup

# Diffraction slope

Empirical parametrization → introduces *smaller* uncertainties than UGD ones

🔗 [J. Nemchik, N.N. Nikolaev, E. Predazzi, B.G. Zakharov, V. R. Zoller (1998)]

$$b(Q^2) = \beta_0 - \beta_1 \log \left[ \frac{Q^2 + m_\rho^2}{m_{J/\psi}^2} \right] + \frac{\beta_2}{Q^2 + m_\rho^2}$$

$$\sigma_L(\gamma^* p \rightarrow \rho p) = \frac{1}{16\pi b(Q^2)} \left| \frac{T_{00}(s, t=0)}{W^2} \right|^2$$

$$\sigma_T(\gamma^* p \rightarrow \rho p) = \frac{1}{16\pi b(Q^2)} \left| \frac{T_{11}(s, t=0)}{W^2} \right|^2$$

$$\beta_0 = 6.5 \text{ GeV}^{-2}, \beta_1 = 1.2 \text{ GeV}^{-2} \text{ and } \beta_2 = 1.6$$

