

Program update: now two talks, instead of only the WDM talk

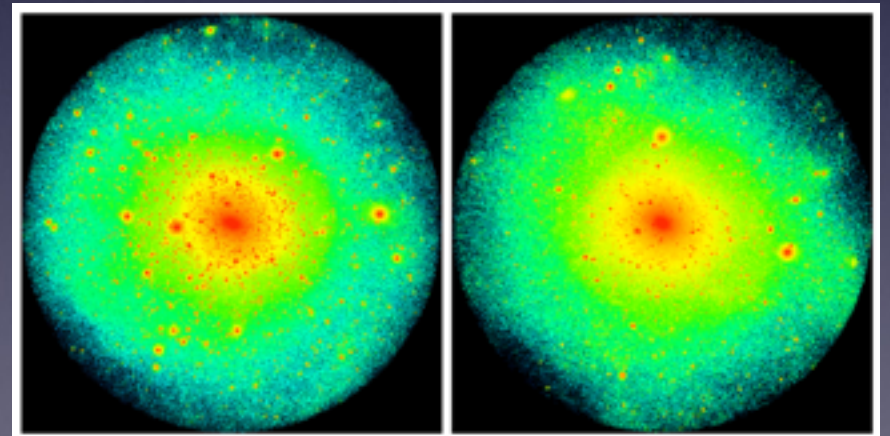
1. Review of LCDM and implications for indirect detection

~ 30 + 5 minutes



2. Warm Dark Matter and Mixed Dark Matter Models

~ 15 + 5 minutes



Review of LCDM and implications for indirect detection

0. introduction

1. density profiles

2. subhalos and
indirect detection

3. other substructure

4. microhalos revisited

for details see reviews:

Diemand & Moore, ASL, 2011

Kuhlen, Vogelsberger, Angulo, PDU, 2012

recent microhalo results:

Ishiyama+, ApJ 2010; Anderhalden & Diemand, JCAP 2014; Ishiyama, ApJ 2014

a very short history of dark matter

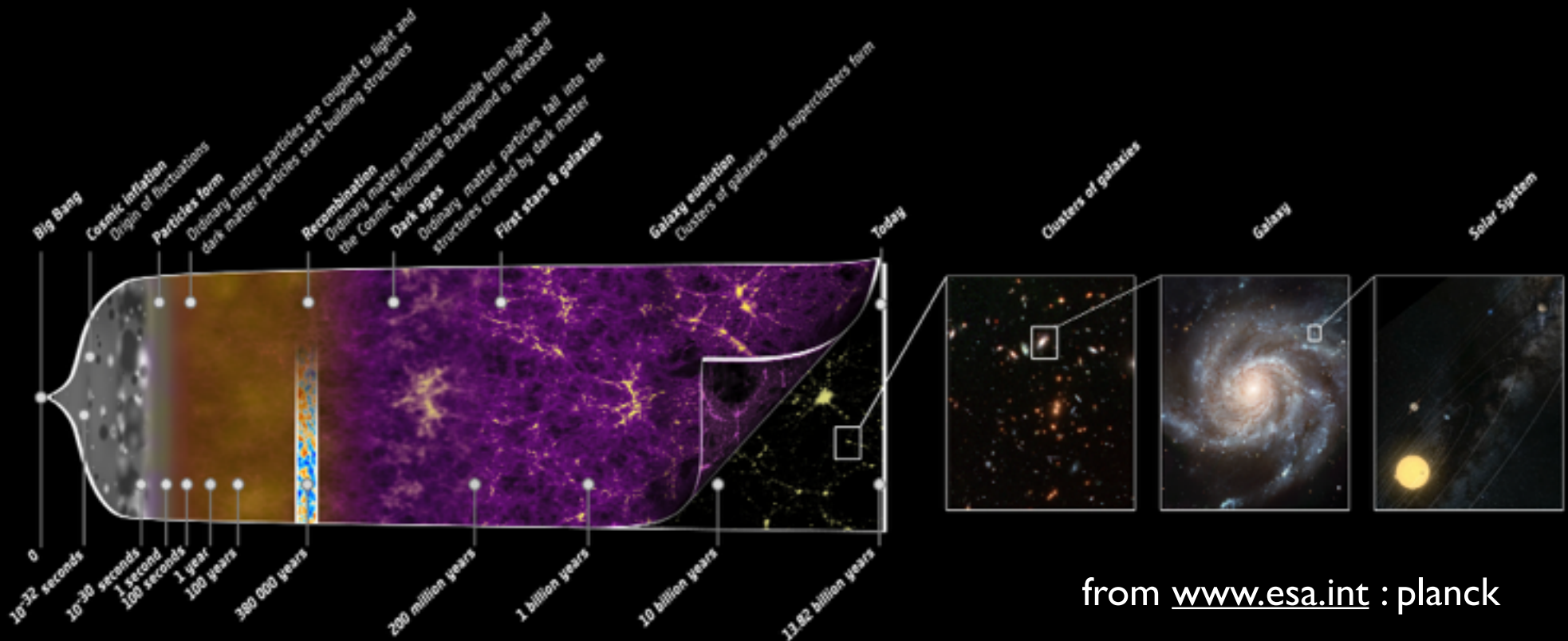
- high velocity dispersion of Coma cluster galaxies (Zwicky 1933)
- flat rotation curves in spiral galaxies (Rubin, Ford 1975)
- x-rays and lensing observations in galaxy clusters (e.g. bullet cluster)
- kinematics of galactic stellar halo and satellite galaxies
- mass-to-light ratios dwarf galaxies



Markevitch et al.; Clowe et al.

a very short history of dark matter

today we have wide range of different cosmological observations:
cosmic microwave background, supernovae Ia, large scale structure
all are consistent with the LCDM model !



from www.esa.int : planck

dark matter dominates structure formation

collision-less simulations

(pure N-body, dark matter only)
treat all matter like dark matter

no free parameters
high resolution, good scaling

good approximation for dwarf galaxy halos and for
smaller, dark halos and subhalos

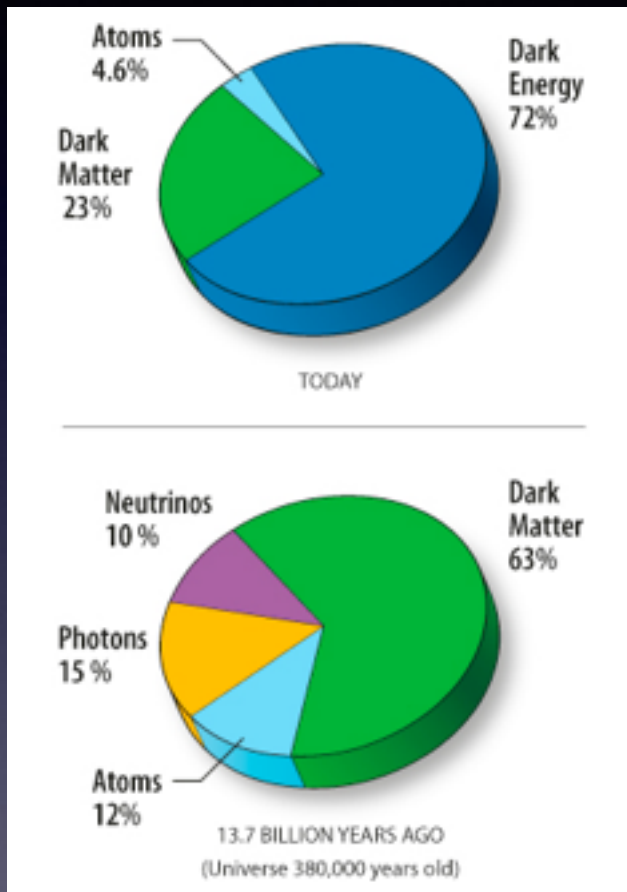
not accurate near centers of galaxies

accurate solution of idealized problem

one main motivation:

DM annihilation signal $\sim \text{density}^2$

i.e. structures on all scales increase the signal



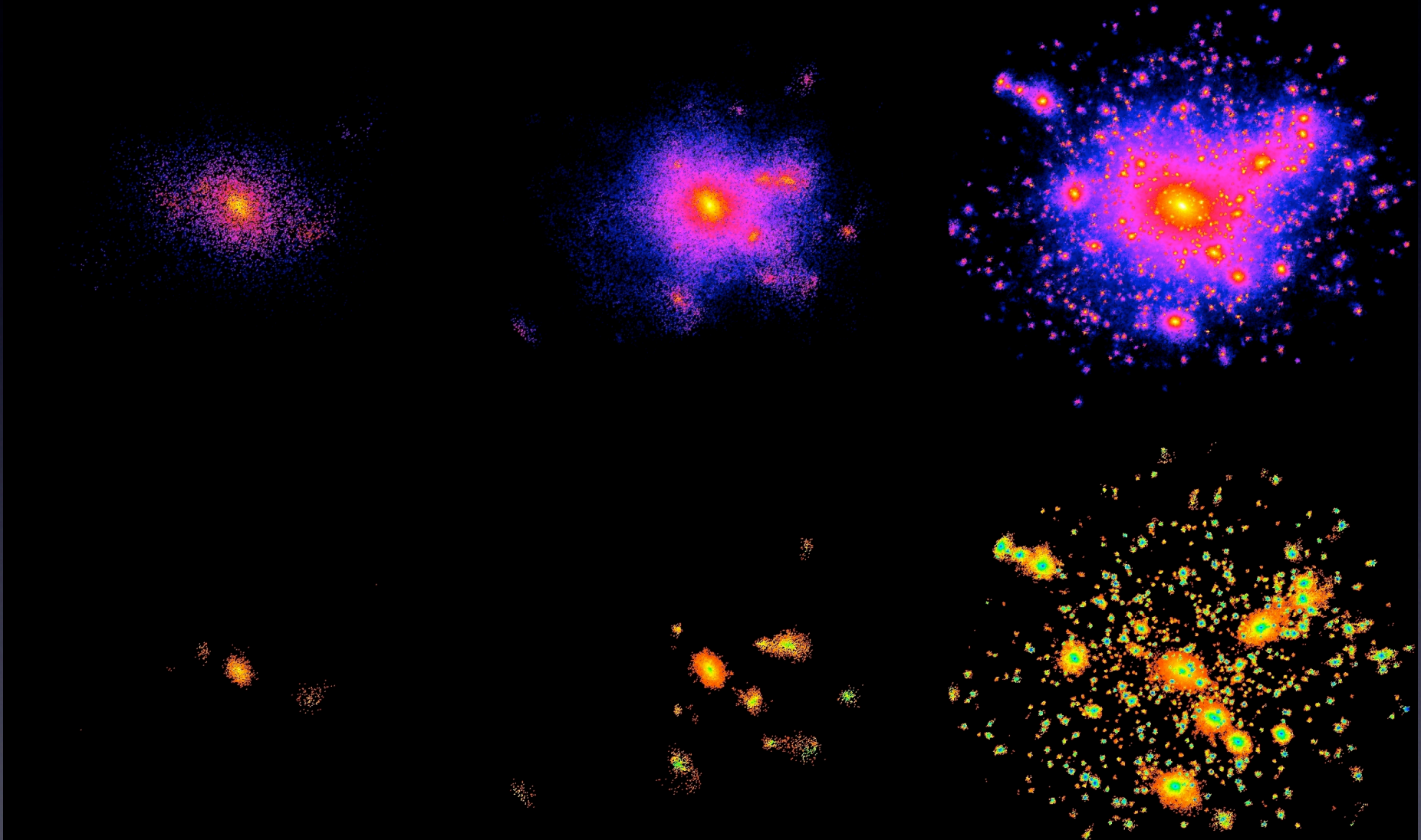
NASA / WMAP Science Team

Simulating structure formation

N-body models approximating CDM halos (about 1995 to 2000)

log density

N_halo from about 10k to a million



log phase space density

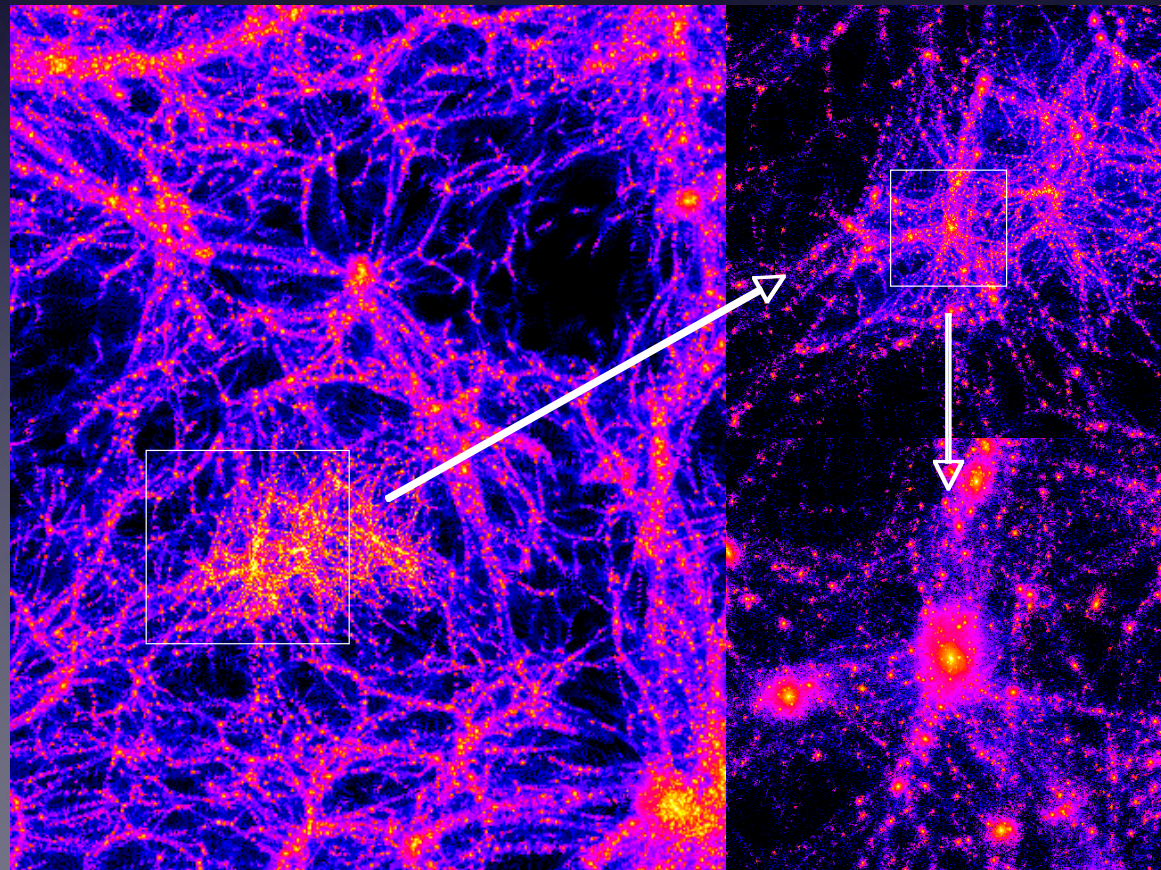
from Ben Moore : www.nbody.net

uniform resolution, periodic cubes

- good statistics, lower resolution
- large scale structure
- fair sample of halos and environments

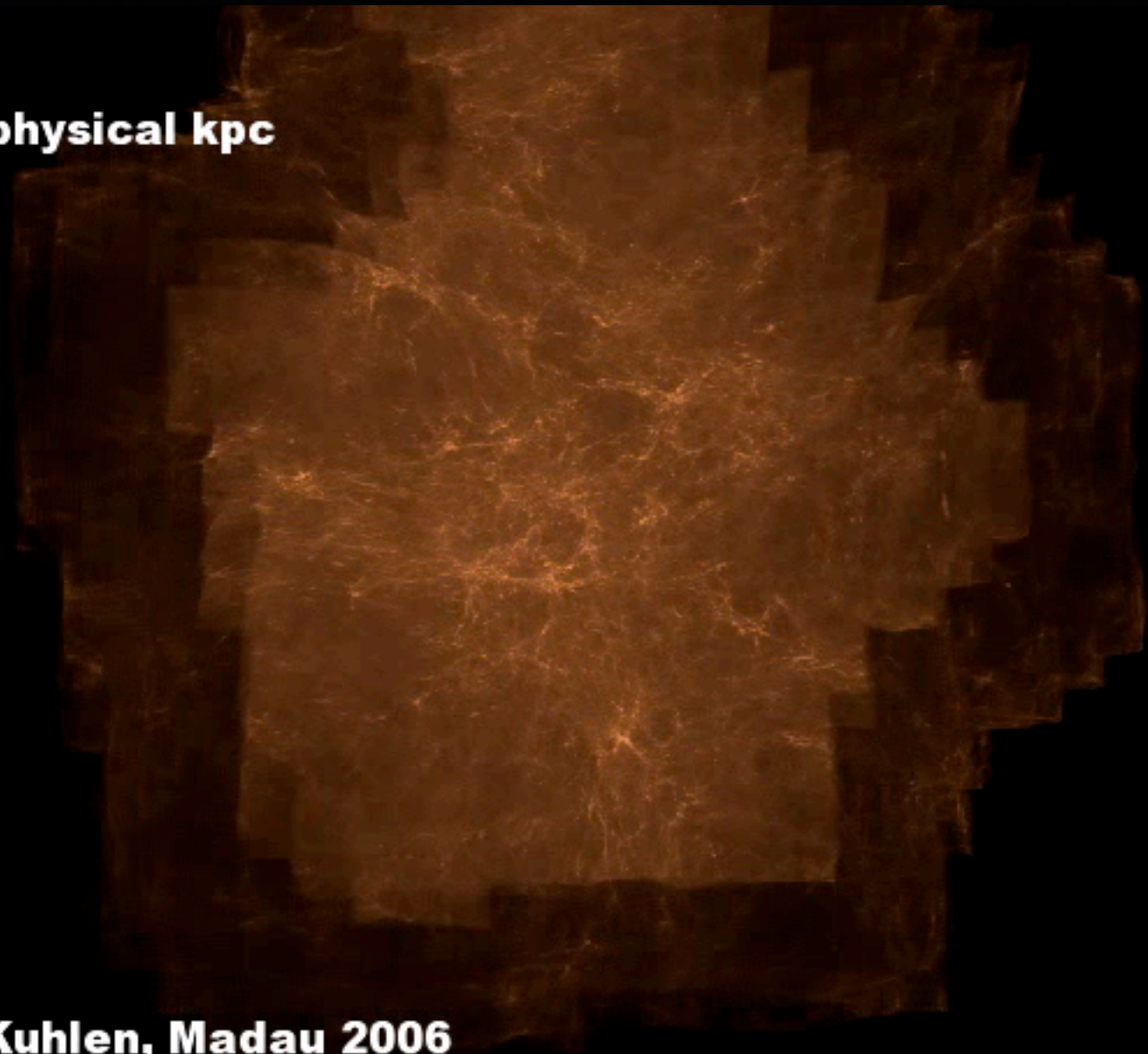
refined, re-simulations of individual halos

- low statistics, high resolution
- selection effects?
see e.g. Ishiyama et al 2008



$z=11.9$

800 x 600 physical kpc



Diemand, Kuhlen, Madau 2006

via lactea II at redshift zero



the via lactea project

high resolution Milky Way dark matter halos simulated on NASA's [Columbia](#) and ORNL's [Jaguar](#) supercomputers

[main](#)

[movies](#)

[images](#)

[publications](#)

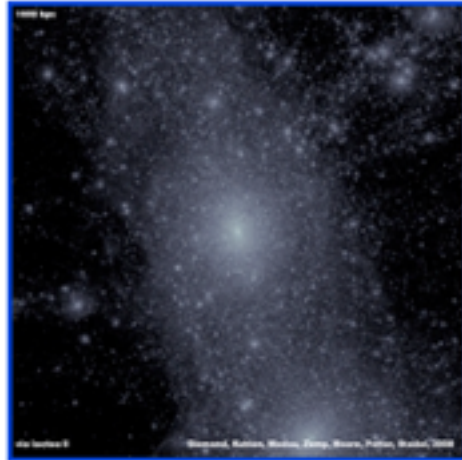
[data](#)

[screensavers](#)

[about](#)

VL-2 movies

This movie rotates and zooms into the via lactea-2 halo at $z=0$ (today). The colors show the local dark matter densities.



- slow rotation (larger files) : [high quality \(174 MB\)](#) [medium \(43 MB\)](#) [low \(18 MB\)](#)
- fast rotation (smaller files) : [high quality \(87 MB\)](#) [medium \(24 MB\)](#) [low \(12 MB\)](#)

VL-1 movies

These animations show the projected dark matter density-square maps of the simulated Milky Way-size halo via lactea-1. The logarithmic color scale covers the same 20 decades in projected density-square in physical units in each frame. All movies are encoded in MPEG format and some are available in different quality versions.

the formation of the via lactea halo



- entire formation history ($z=12$ to 0): [high quality \(218 MB\)](#)
smaller frames, quality: [high\(55 MB\)](#) [medium\(11 MB\)](#) [low\(4.7 MB\)](#)
- entire formation history, plus rotation and zoom at $z=0$:

What is a (sub)halo? Operational definitions

mass profiles around
peaks in (phase-space)
density

$$V_{\text{circ}}^2 = GM(<r)/r$$

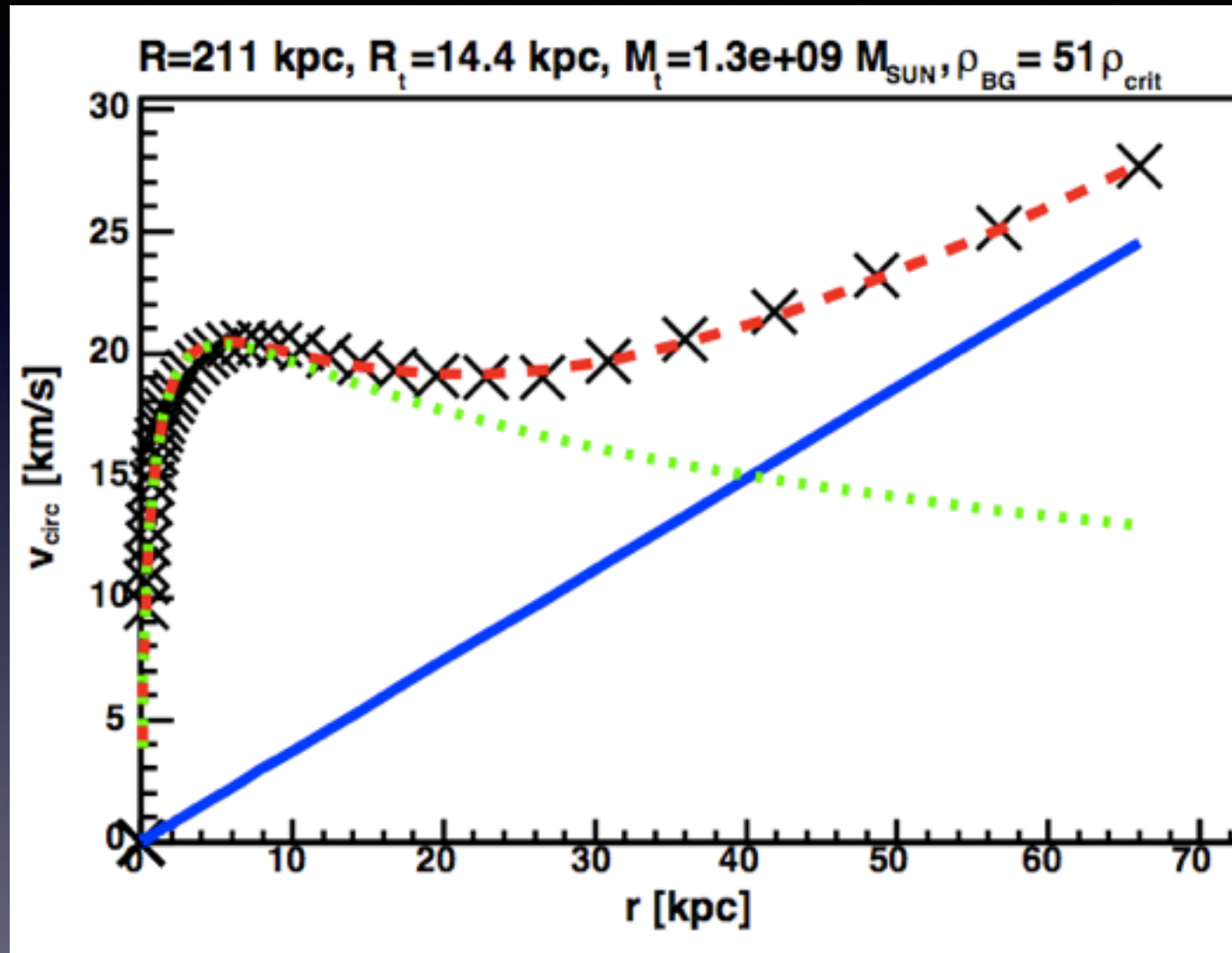
has a well defined peak:

$$V_{\text{max}} \text{ at } r_{V_{\text{max}}}$$

no clear outer boundary:
“virial” radius is a simple,
but arbitrary scale

Anderhalden&JD 2011

halos with the virial
radius of another are
called subhalos



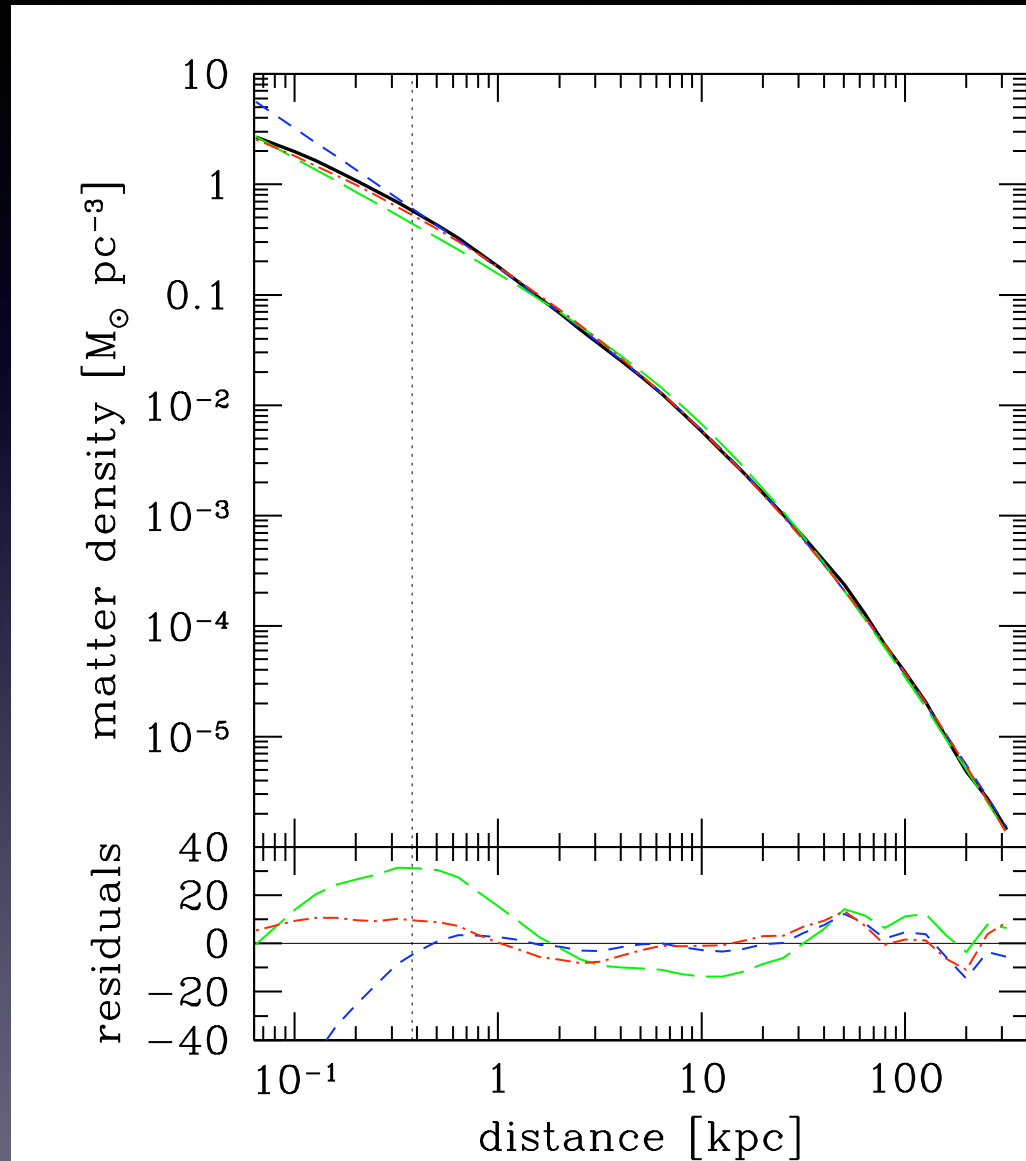
(sub)halo concentrations:

$$c_v = \rho(<r_{V_{\text{max}}}) / \rho_{\text{crit}, z=0}$$

$$\text{CNWF} = r_{\text{vir}} / r_s, \quad r_s = r_{V_{\text{max}}} / 2.16$$

I. density profiles

main halo density profile

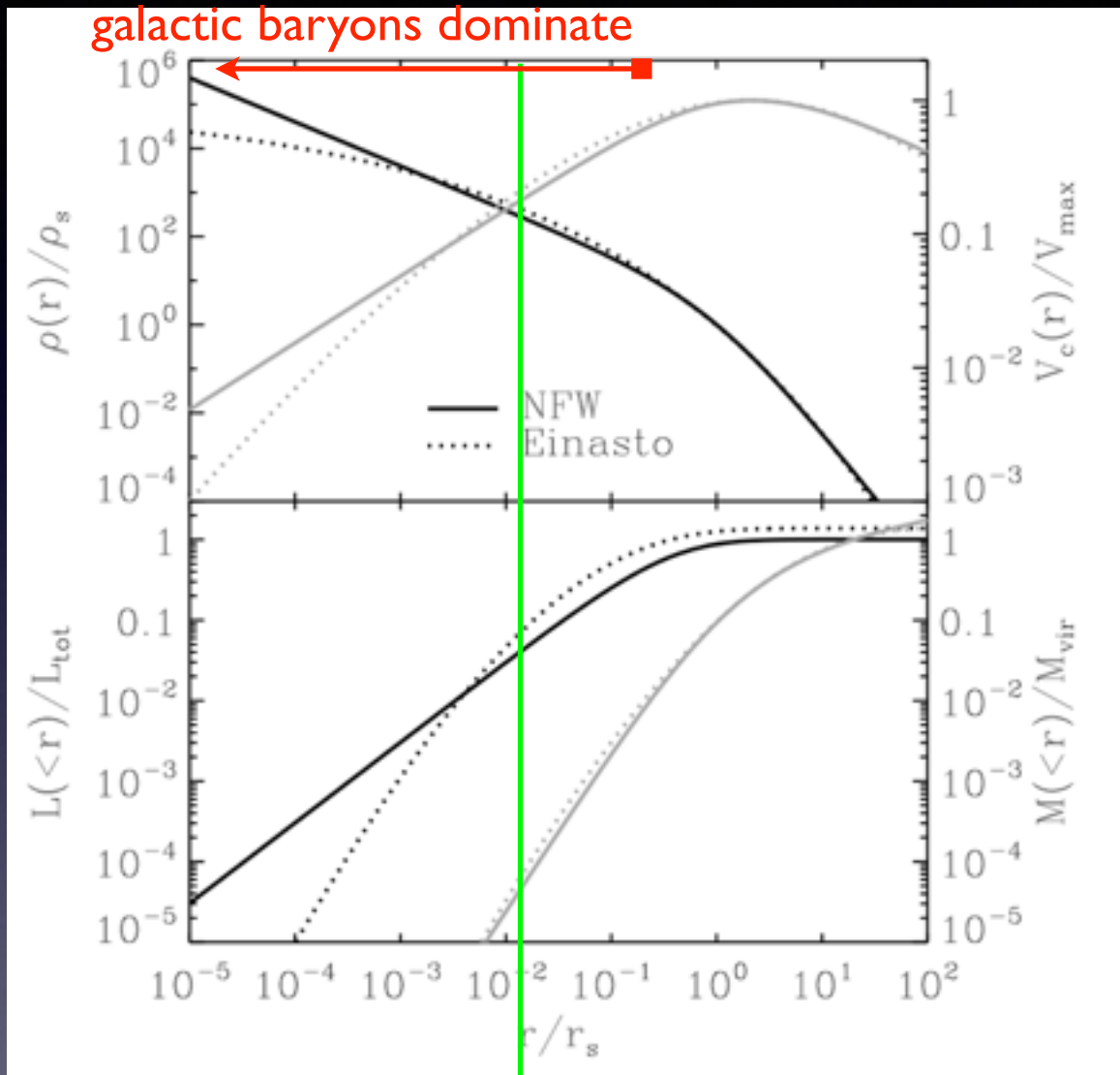


NFW
Einasto
 $r^{-1.24}$ inner profile

JD et al. Nature 2008

inner region is denser than NFW: Einasto and $r^{-1.24}$ fit well down to 400 pc.
probably shallower than $r^{-1.24}$ on very small scales (scatter / convergence?).

main halo density profile



comparison of NFW and Einasto ($\alpha=0.17$) profiles

normalized at V_{\max} and rV_{\max}

$$L_{\text{Einasto}} = 1.41 L_{\text{NFW}}$$

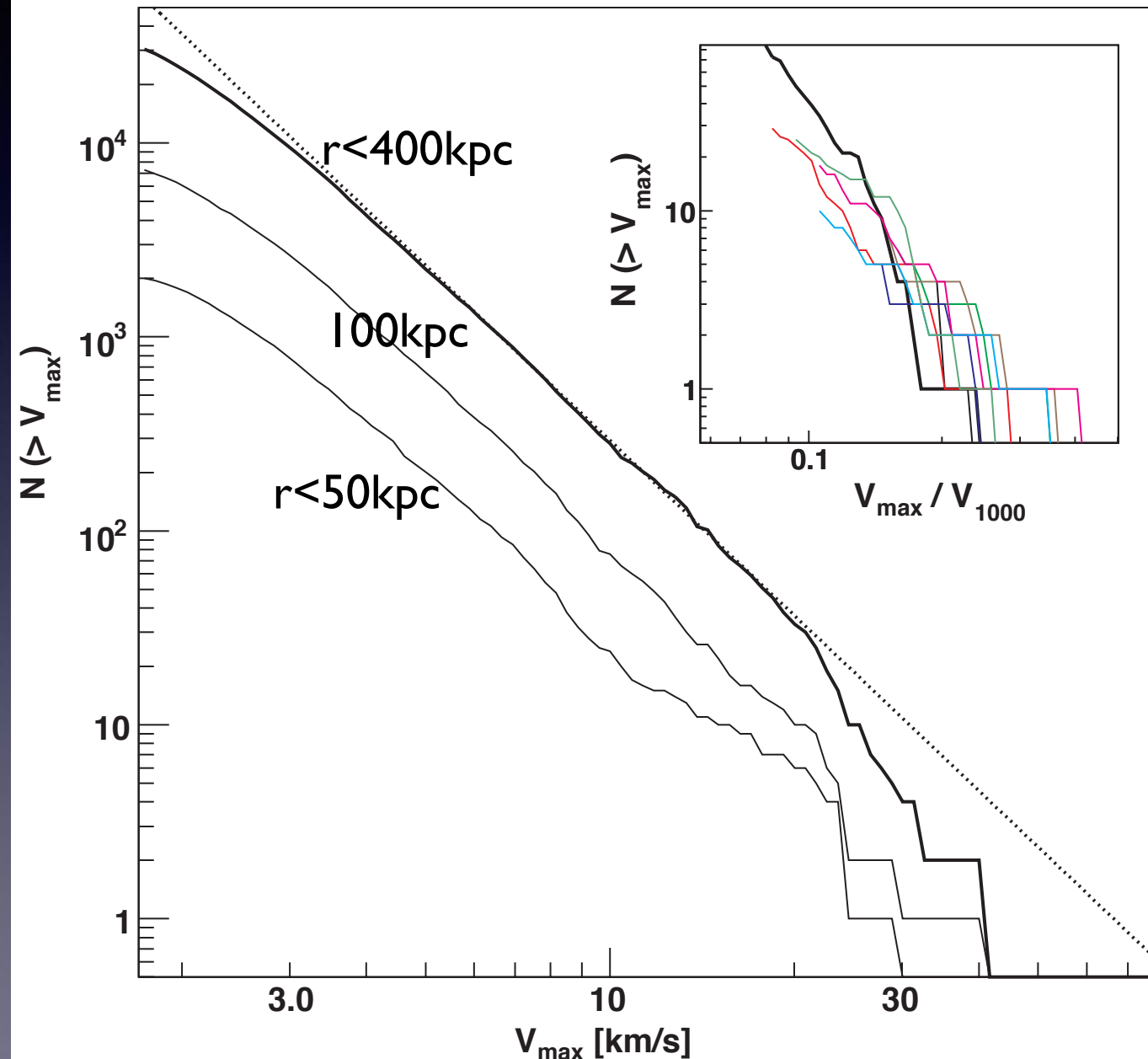
Kuhlen, AdAst 2010

well resolved region in pure dark matter simulations contains > 99 percent of the annihilation luminosity L (Einasto and $r^{-1.24}$ inner profile are very similar here)

2. subhalos and indirect detection

subhalo and sub-subhalo abundance

$$L \propto \rho_s^2 r_s^3 \propto V_{\max}^4 / r_{V_{\max}} \propto V_{\max}^3 \sqrt{c_V}$$



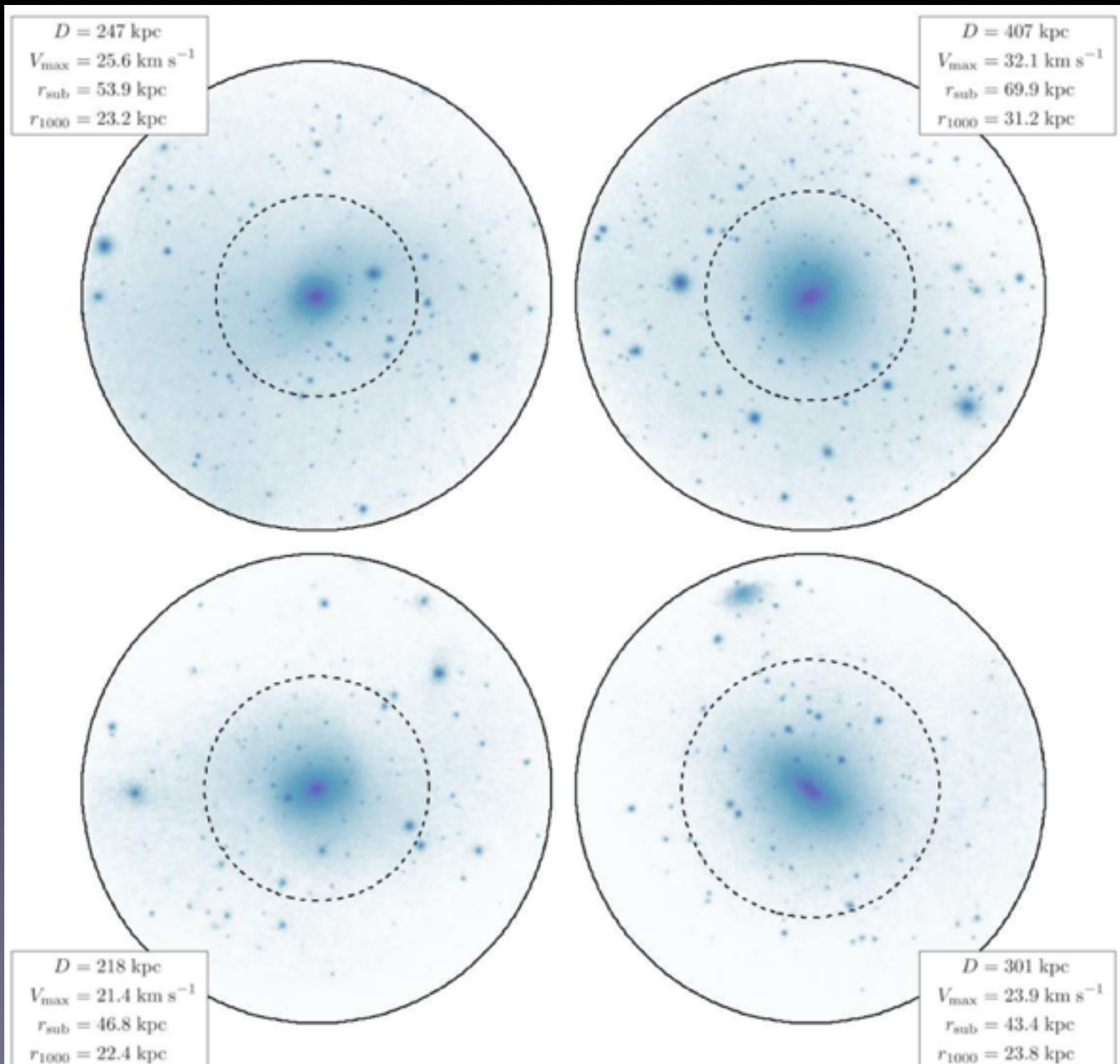
velocity function
 $N(>V) \sim V^{-3}$

annihilation signal has
not converged yet in
simulations

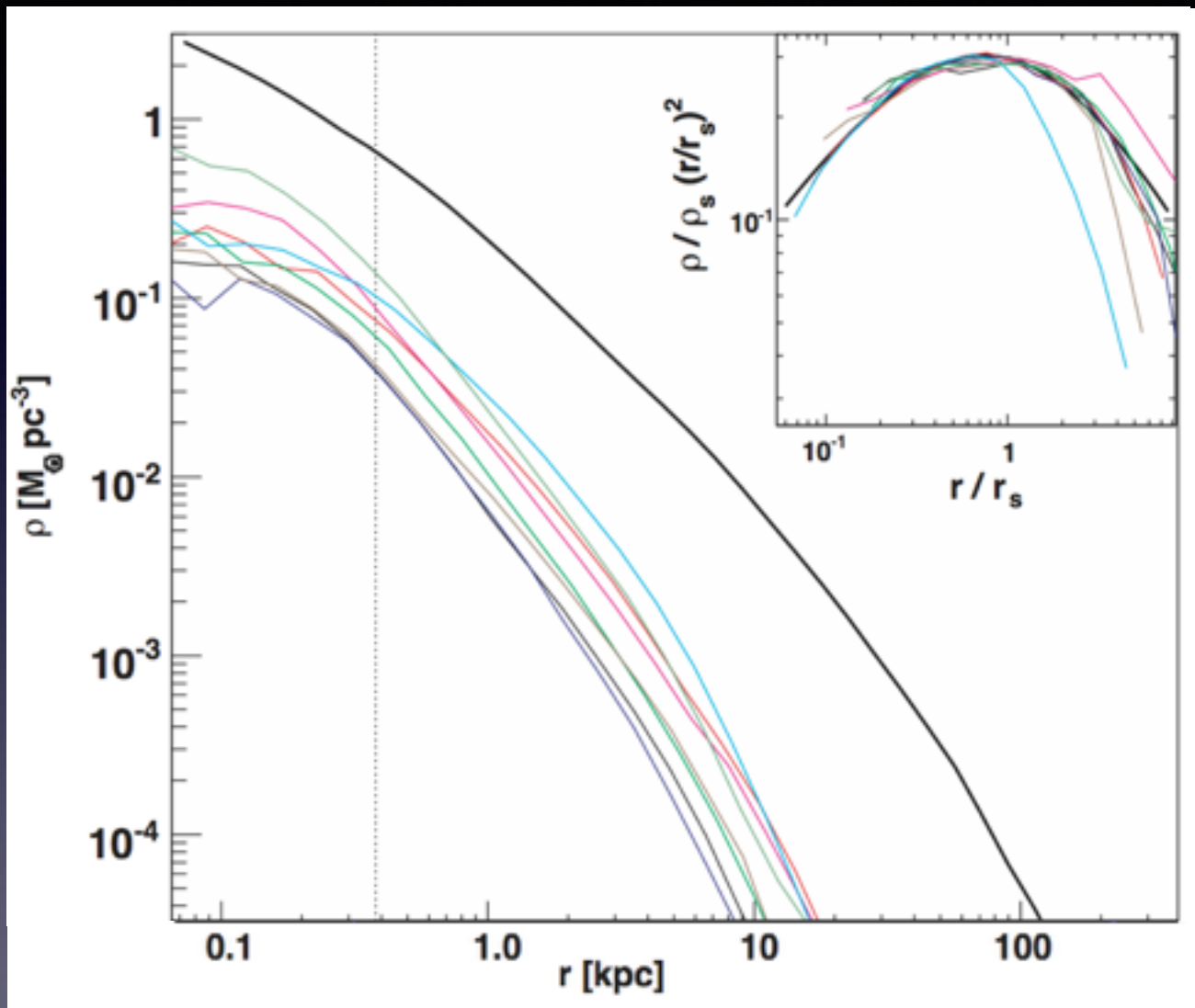
both for main halos and
for subhalos

mass functions
 $N(>M) \sim M^{-(0.9 \text{ to } 1.0)}$
give same conclusion

sub-subhalos in all well resolved subhalos



inner subhalo density profiles resemble main halo profiles



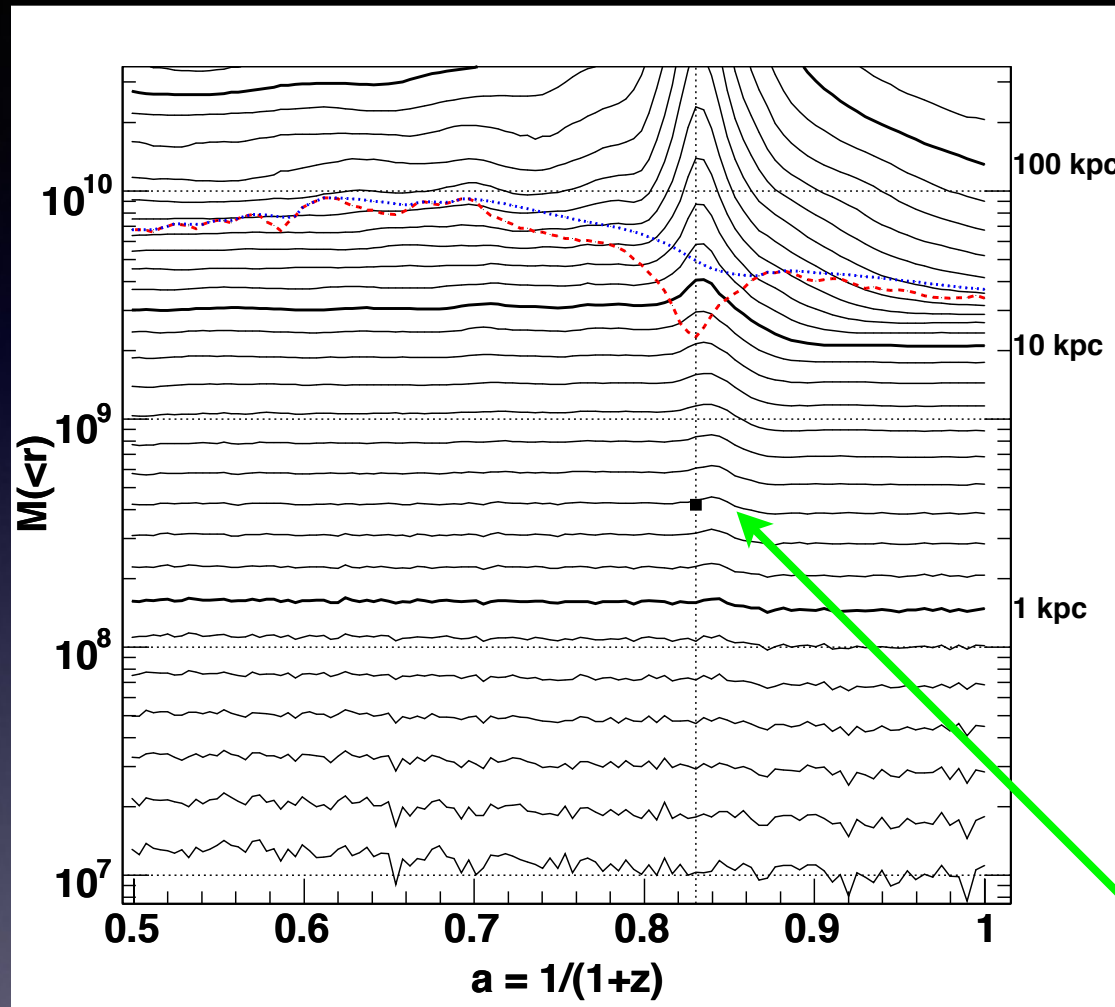
JD et al. Nature 2008

normalized profiles

overlap in inner regions

subhalos fall off steeper
in the outer parts

subhalo evolution (JD, Kuhlen, Madau, ApJ, 2007)

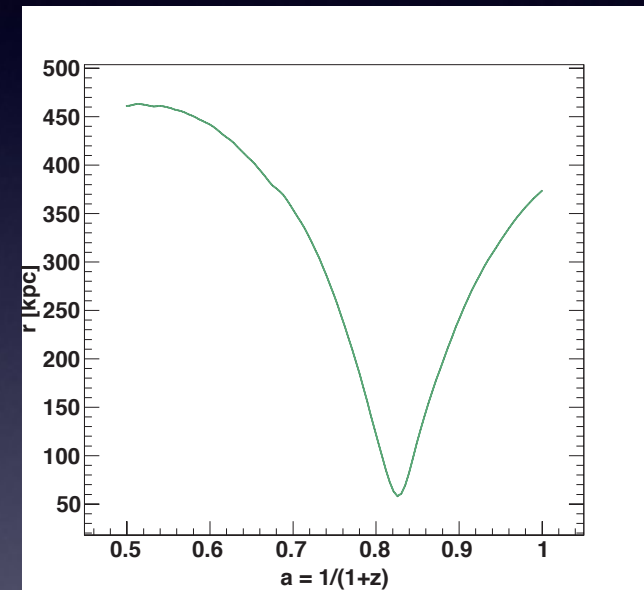


weak, long tidal shock
causes quick compression followed by expansion

mass loss increases with radius, subhalo inner regions remain unaffected

total mass in spheres around
subhalo center

this subhalo has one
pericenter passage at 56 kpc

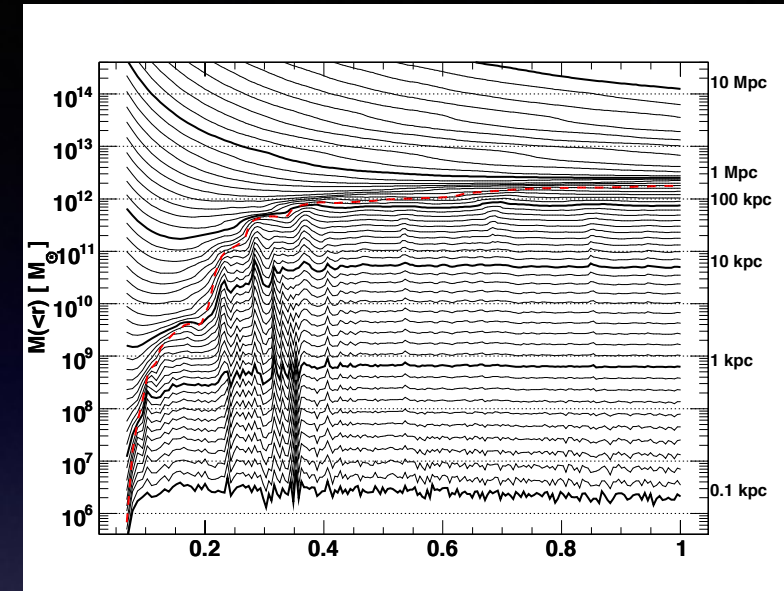
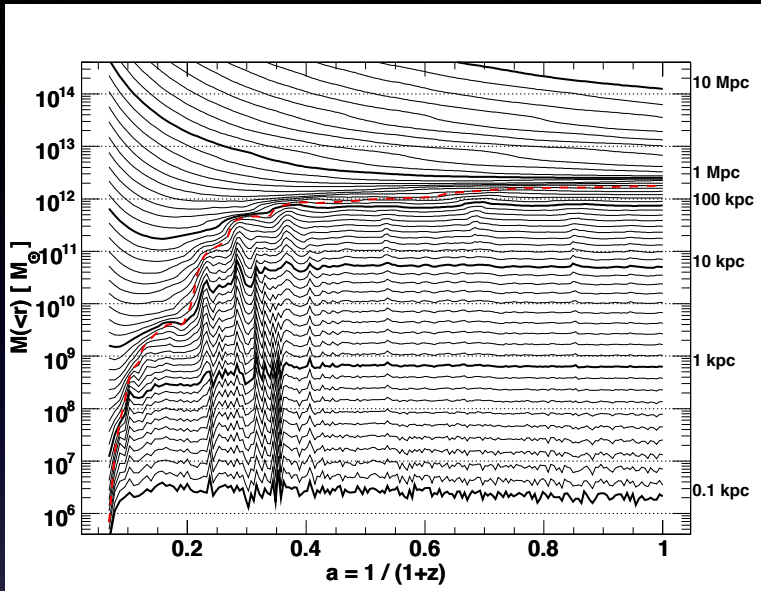


shock duration =
internal subhalo orbital time

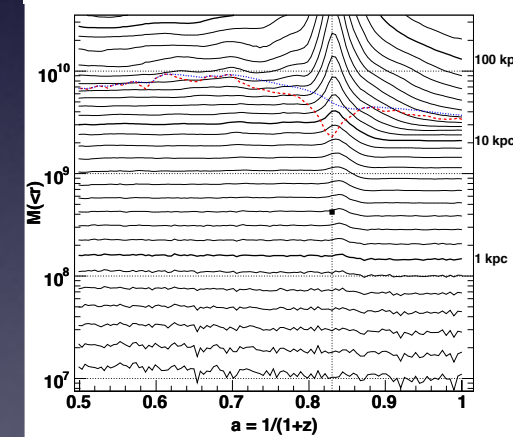
isolated halo

subhalo

formation



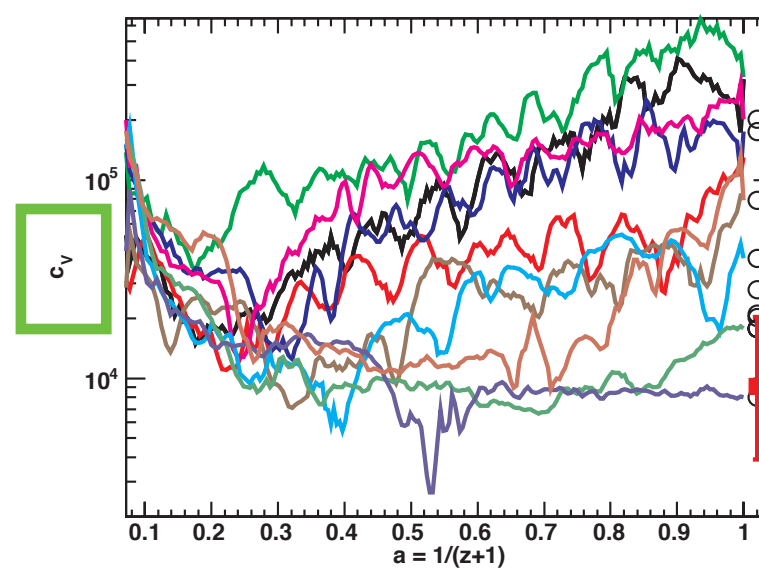
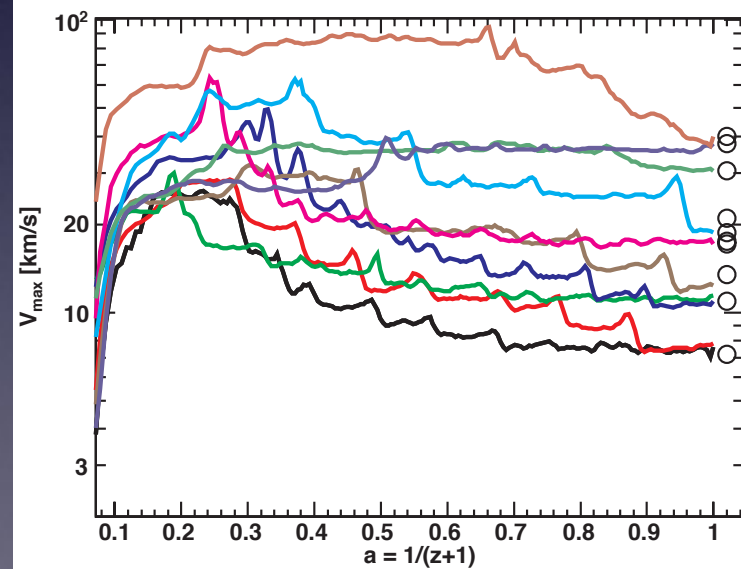
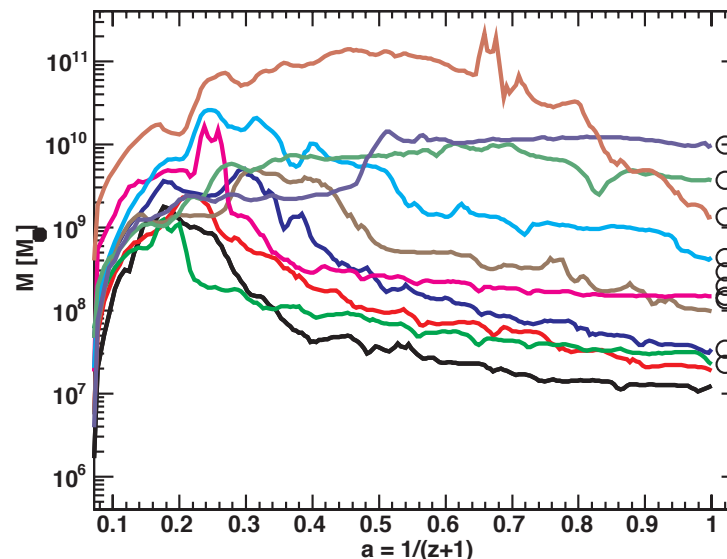
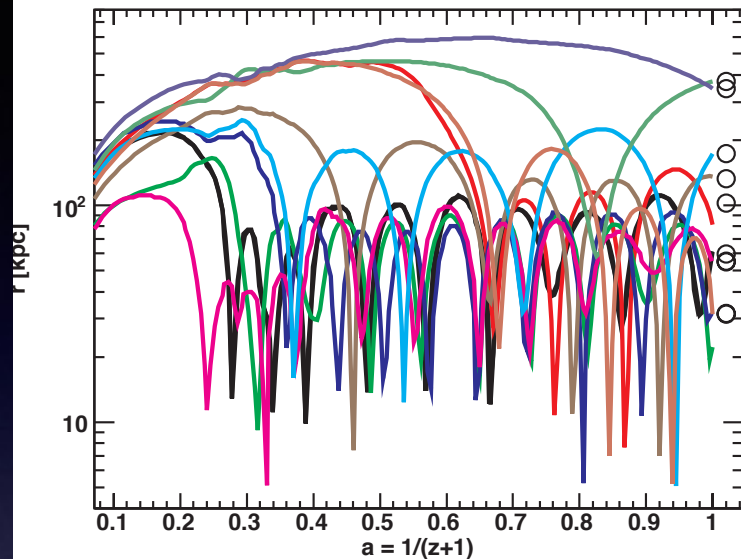
passive
evolution



tidal
stripping

same mass and substructure
distribution in the inner parts

subhalo evolution (JD, Kuhlen, Madau, ApJ, 2007)



diverse histories:

0 to 11 percenters
inner subhalos
tend to have more
of them and
starting earlier

none to very large
mass loss

concentrations
increase during
tidal mass loss

field halo
concentrations

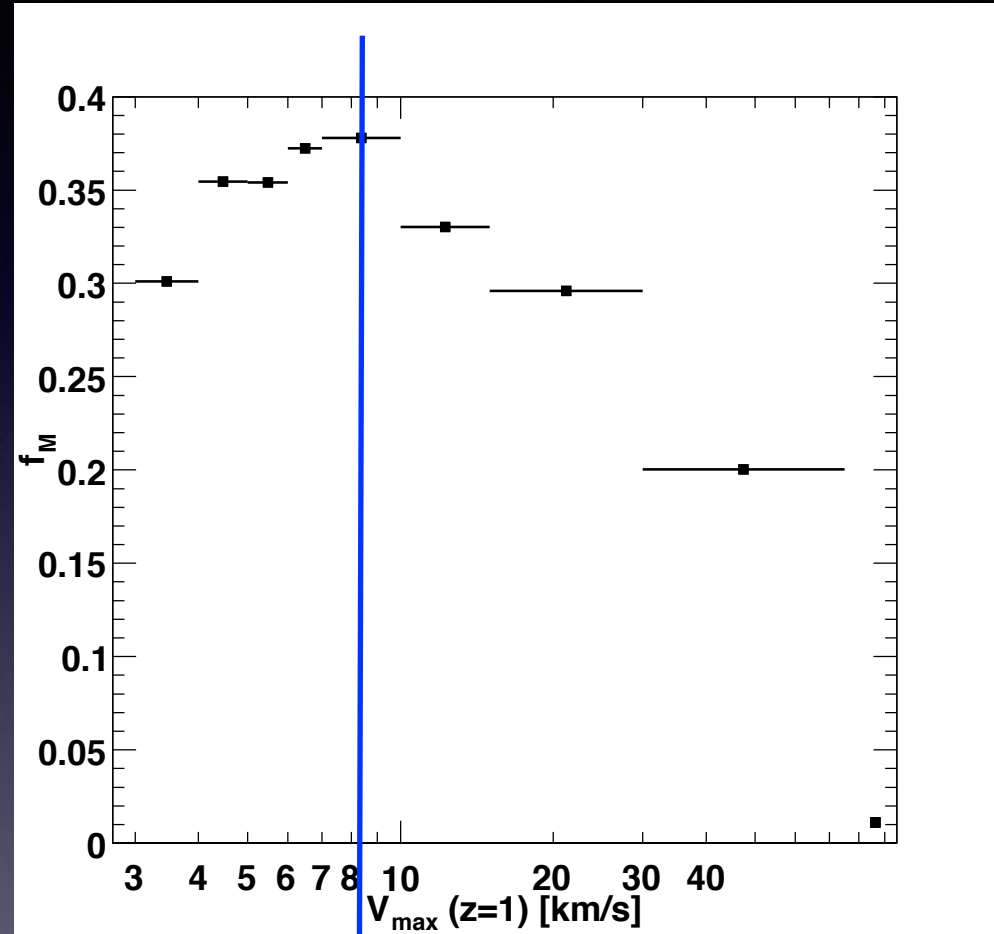
subhalo survival and merging (JD, Kuhlen, Madau, ApJ, 2007)

out of 1542 well resolved ($V_{\text{max}} > 5$ km/s)
 $z=1$ subhalos:

97 % survive until $z=0$

(only 1.3% merge into a larger subhalo)

The average mass fraction that remains
bound to them until $z=0$ depends on their
(initial) size

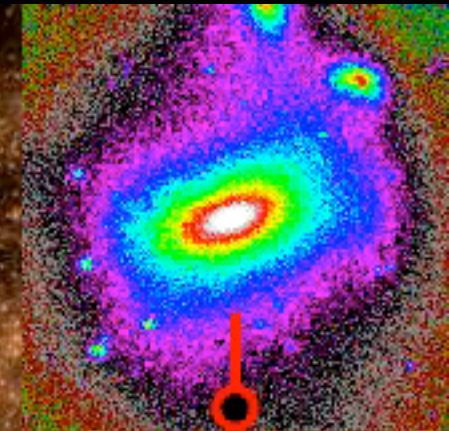


affected by numerical limitations

stronger dynamical friction

$z=2.0$

800 x 600 physical kpc



$M_t = 1.6 \times 10^{10} \text{ Mo}$

Diemand, Kuhlen, Madau 2006

where are the subhalos?

spatial distribution **depends strongly** on how the subhalo sample is selected

mass selected subhalos
are found at larger radii than
the dark matter

this 'anti-bias' is smaller in V_{\max} selected samples

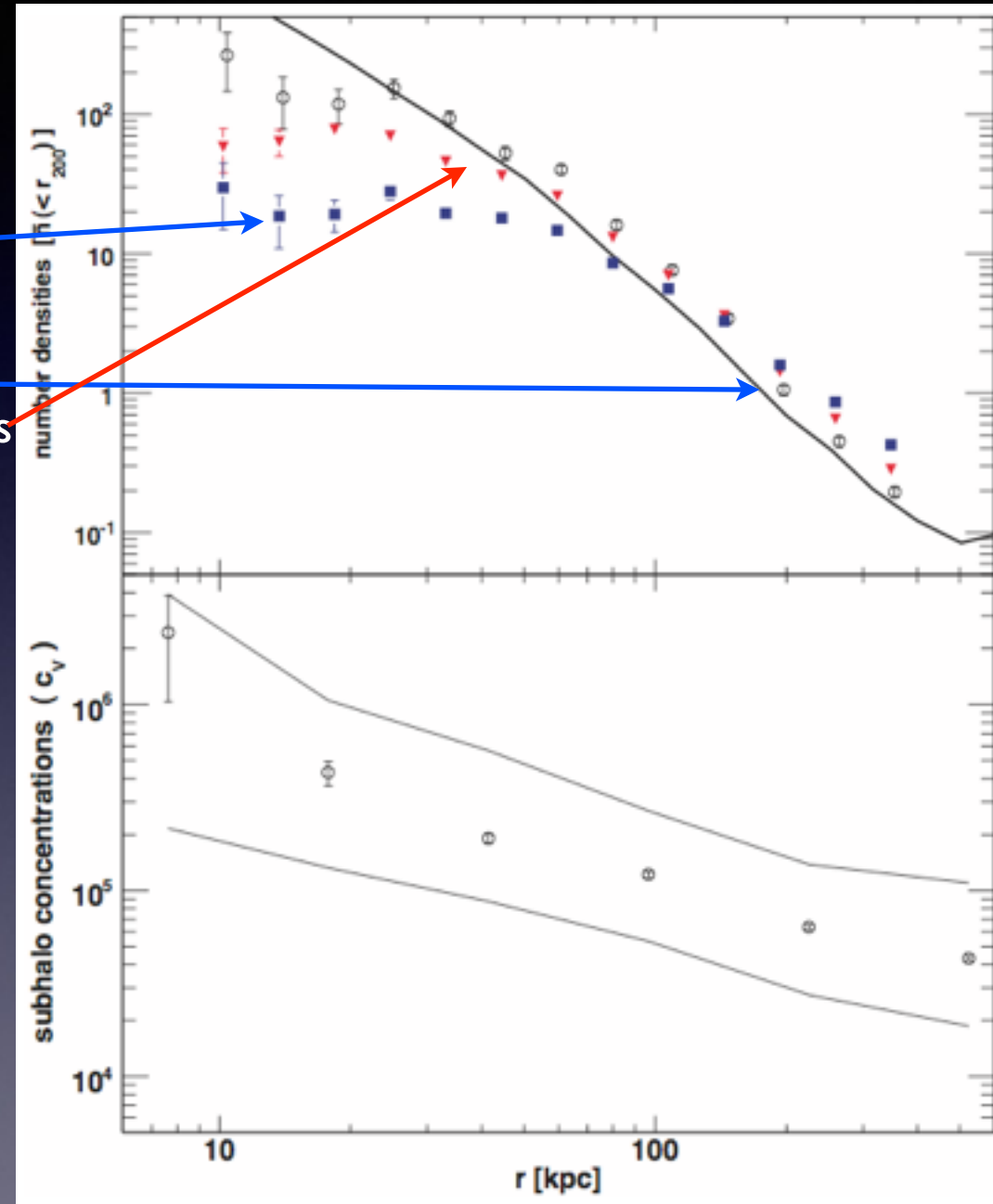
no bias when size at accretion is used
Faltenbacher & JD 2005

denser parts survive, subhalo concentrations
increase towards the galactic center

subhalo luminosity

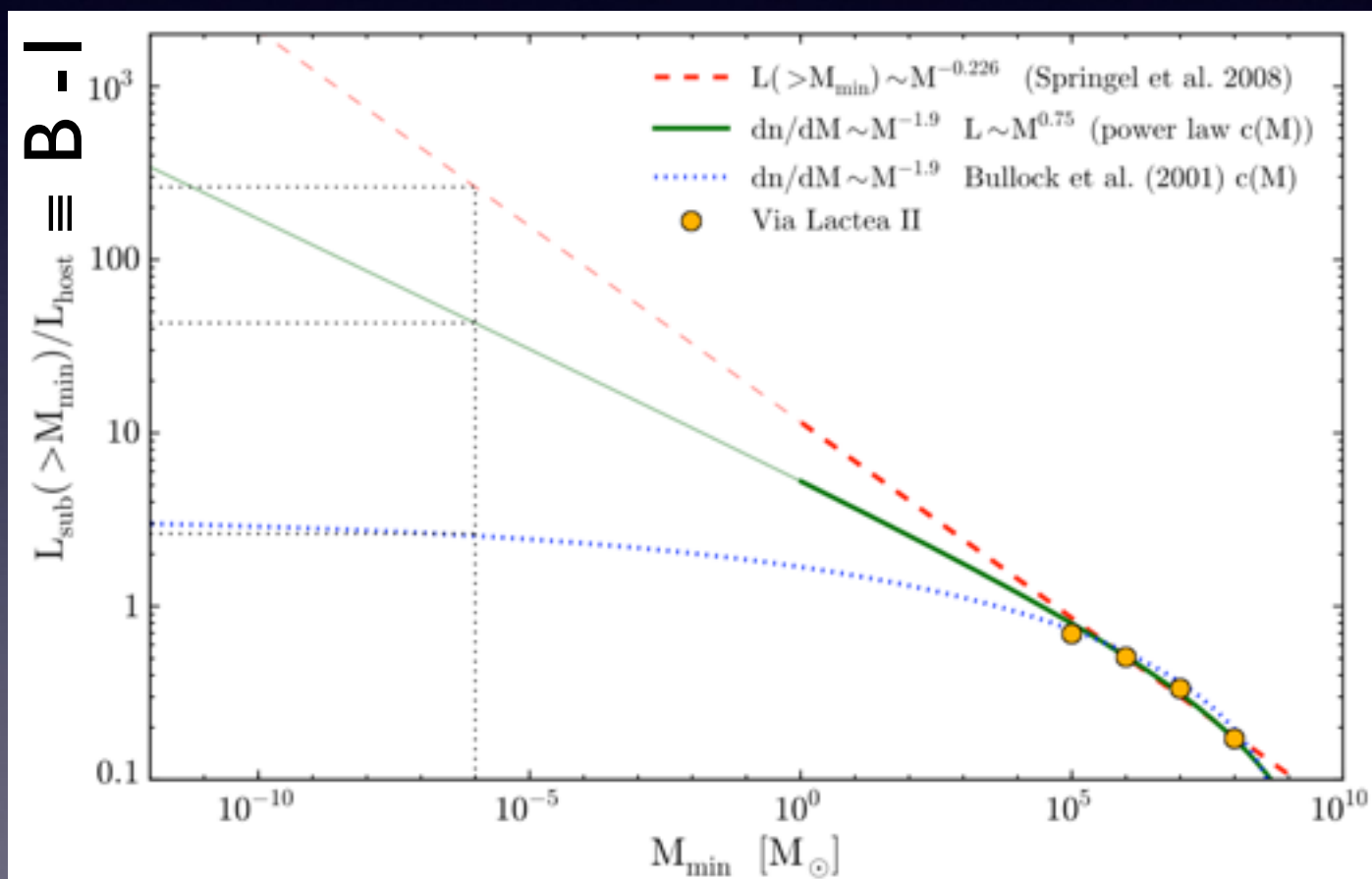
$$L \propto \rho_s^2 r_s^3 \propto V_{\max}^4 / r_{V\max} \propto V_{\max}^3 \sqrt{c_V}$$

is practically unbiased,
i.e. proportional to DM density



galaxy halo boost factor

halo boost factor: $B = \frac{\text{total halo luminosity}}{\text{spherical, smooth halo luminosity}}$



from Kuhlen et al. PDU, 2012

$B \sim 4 - 15$

JD et al ApJ 2006 and Nature 2008

maybe as high as $B \sim 30$

Kamionkowski et al. PRD 2010

Sanchez-Conde, Prada, MNRAS 2014

not ~ 1.7

Stoehr, White, Springel et al. 2003

certainly not 232

Springel et al. Nature, 2008

certainly not 100 to 5000

Gao, Frenk et al. 2012

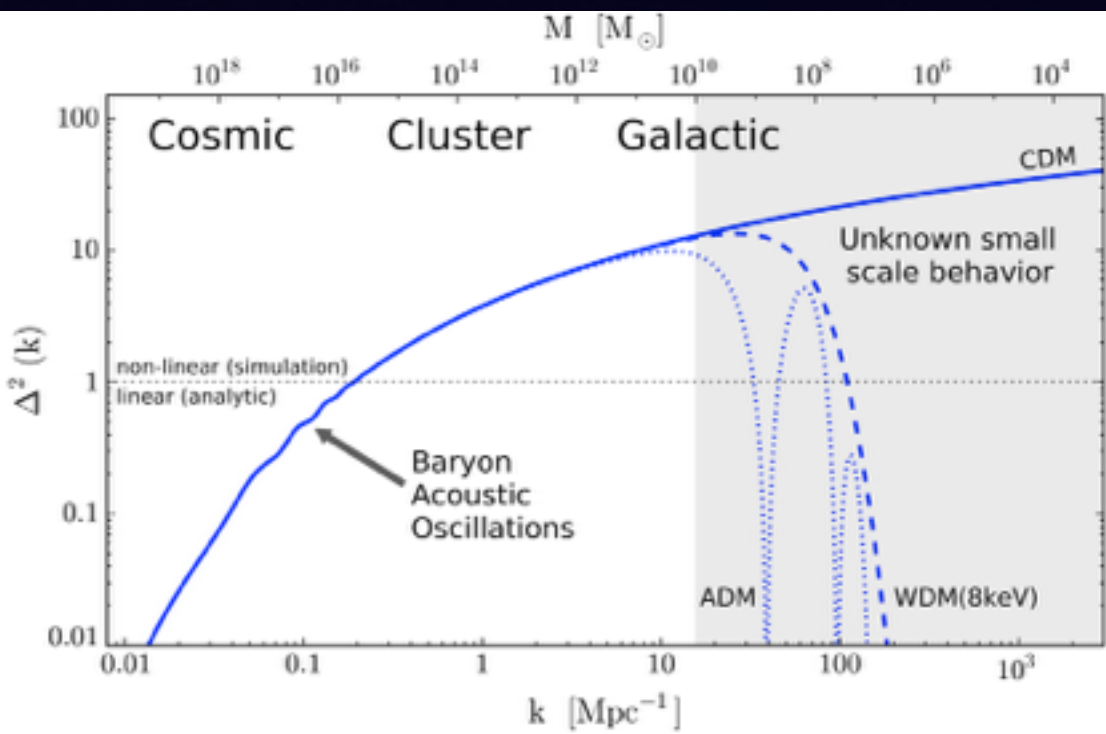
galaxy halo boost factor

$L_{\text{sub}}(>M_{\text{min}})$ and $c(M)$ are not simple power laws

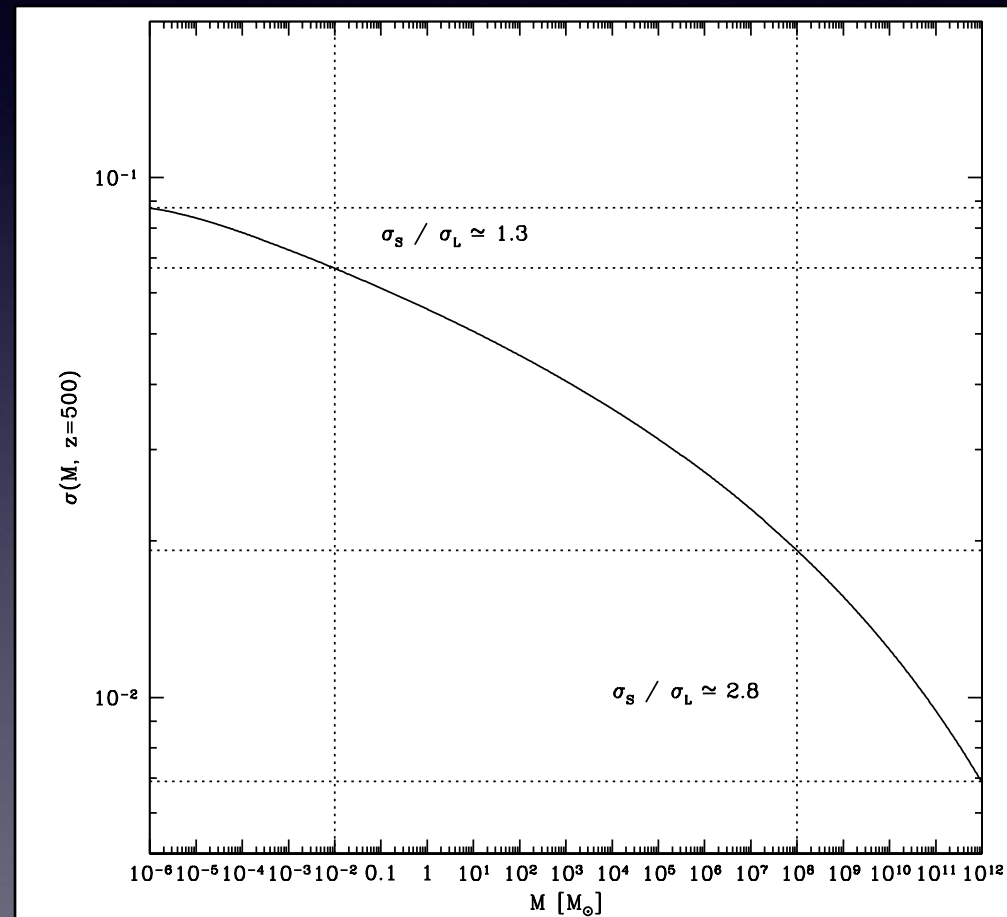
CDM power spectrum



mass fluctuations → formation times



from Kuhlen et al. 2012

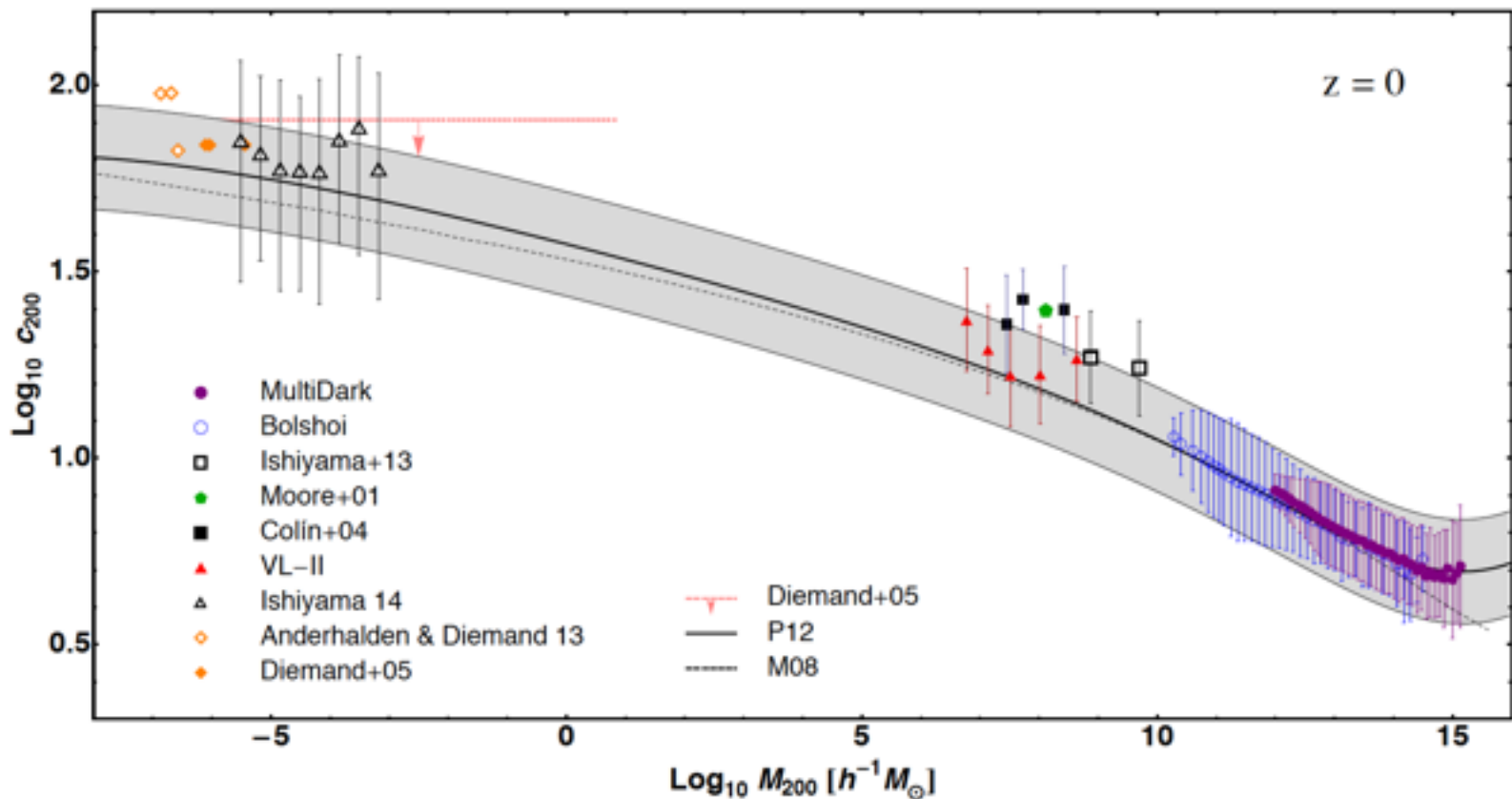


because $p(k)$, $\sigma(M)$ and $a_{\text{form}}(M)$ are not power laws.

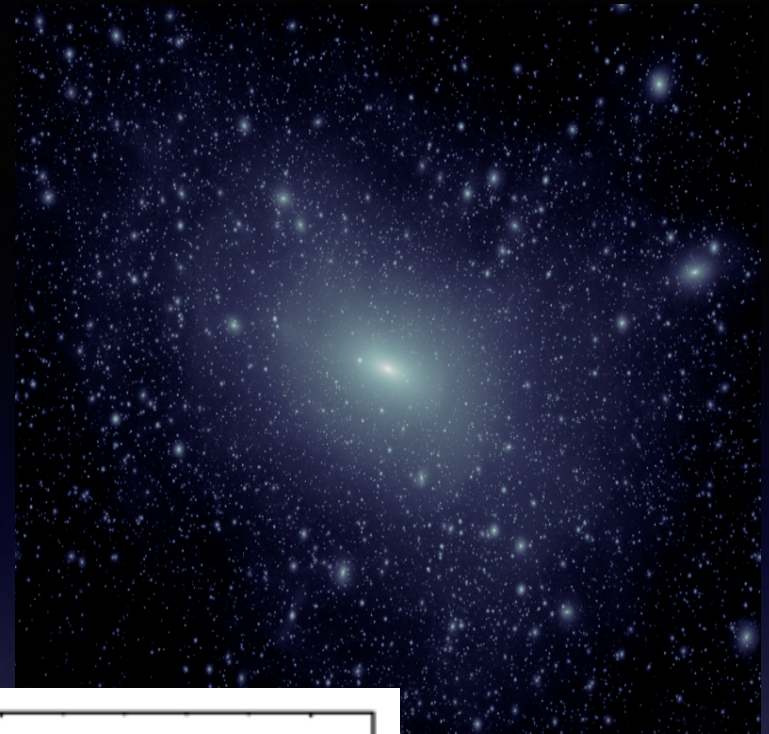
boost factors

extrapolations to smallest
CDM subhalos depends on
the concentration - mass relation

Bullock et al. 2001 or Prada et al. 2012 models
fit the simulation results well



Sanchez-Conde, Prada, MNRAS 2014



Colafrancesco, Profumo, Ullio AA 2006

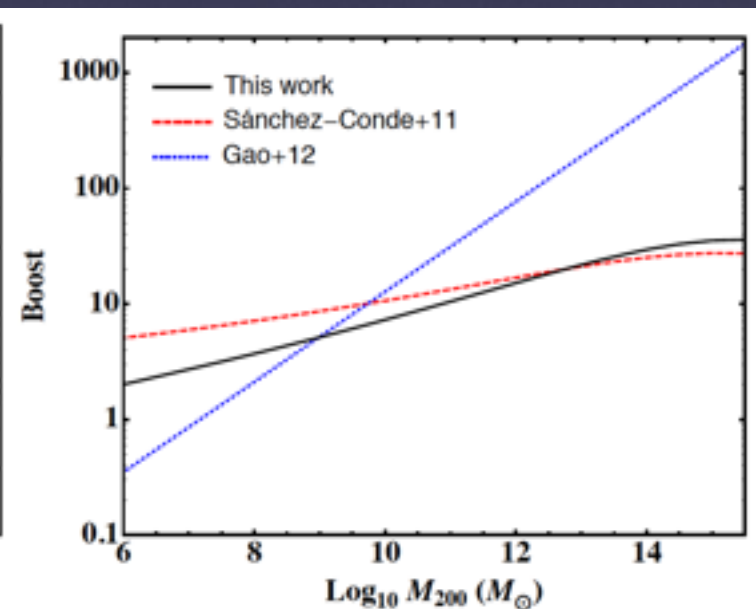
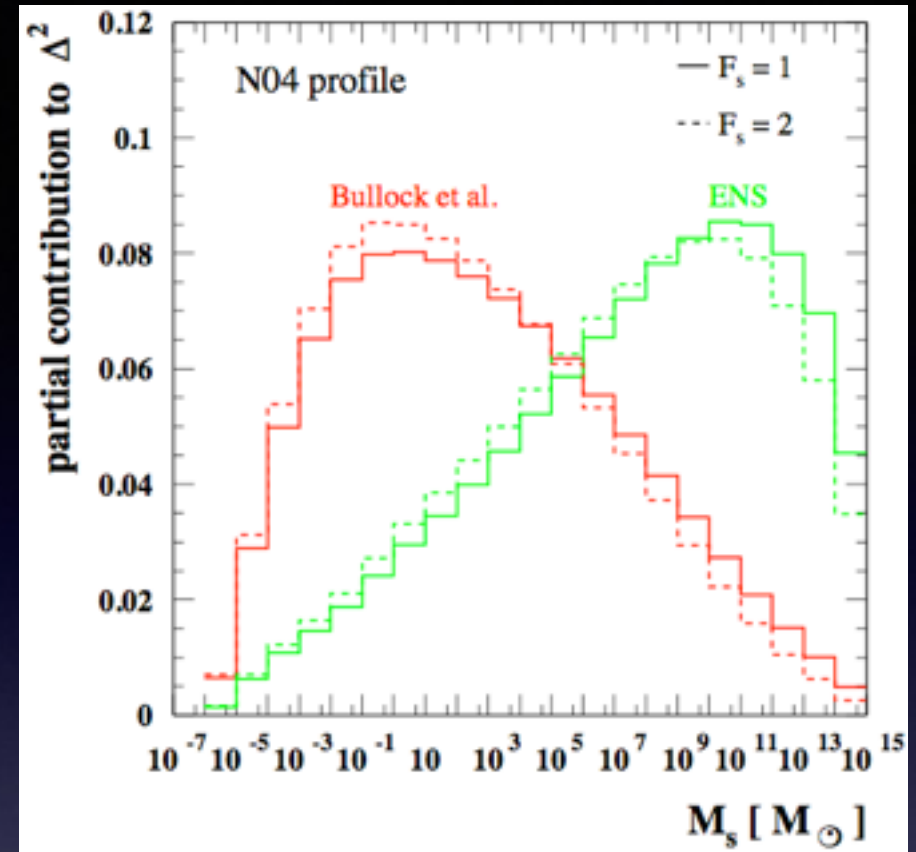
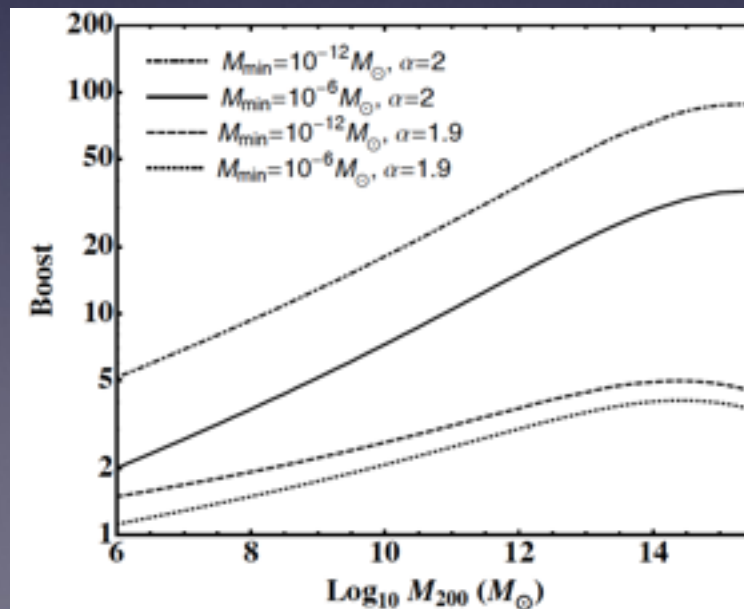
boost factors

subhalos in mass decade
around one solar mass
contribute most to
total boost

→ moderate boost: $B \sim 10$
weak dependence on CDM cutoff

Colafrancesco, Profumo, Ullio AA 2006
JD et al. 2006/08, Kamionkowski+ PRD 2010
Anderhalden & JD, 2013; Sanchez-Conde+2011, 2014

Boost $\equiv B - 1$
vs.
halo mass



boost factors depend on location

total halo luminosity

$$\text{halo boost factor} = \frac{\text{total halo luminosity}}{\text{spherical, smooth halo luminosity}} \sim 4 - 15$$

JD et al ApJ 2006 and Nature 2008

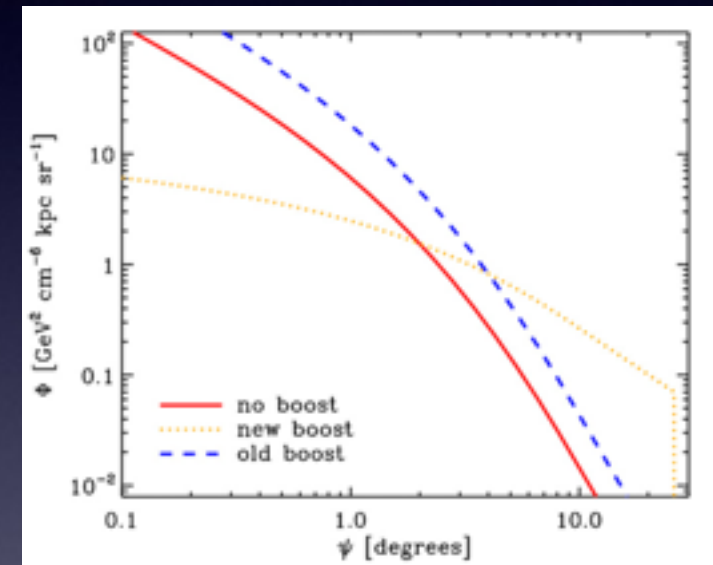
boost factors in actual observations depend on angle:

total local luminosity

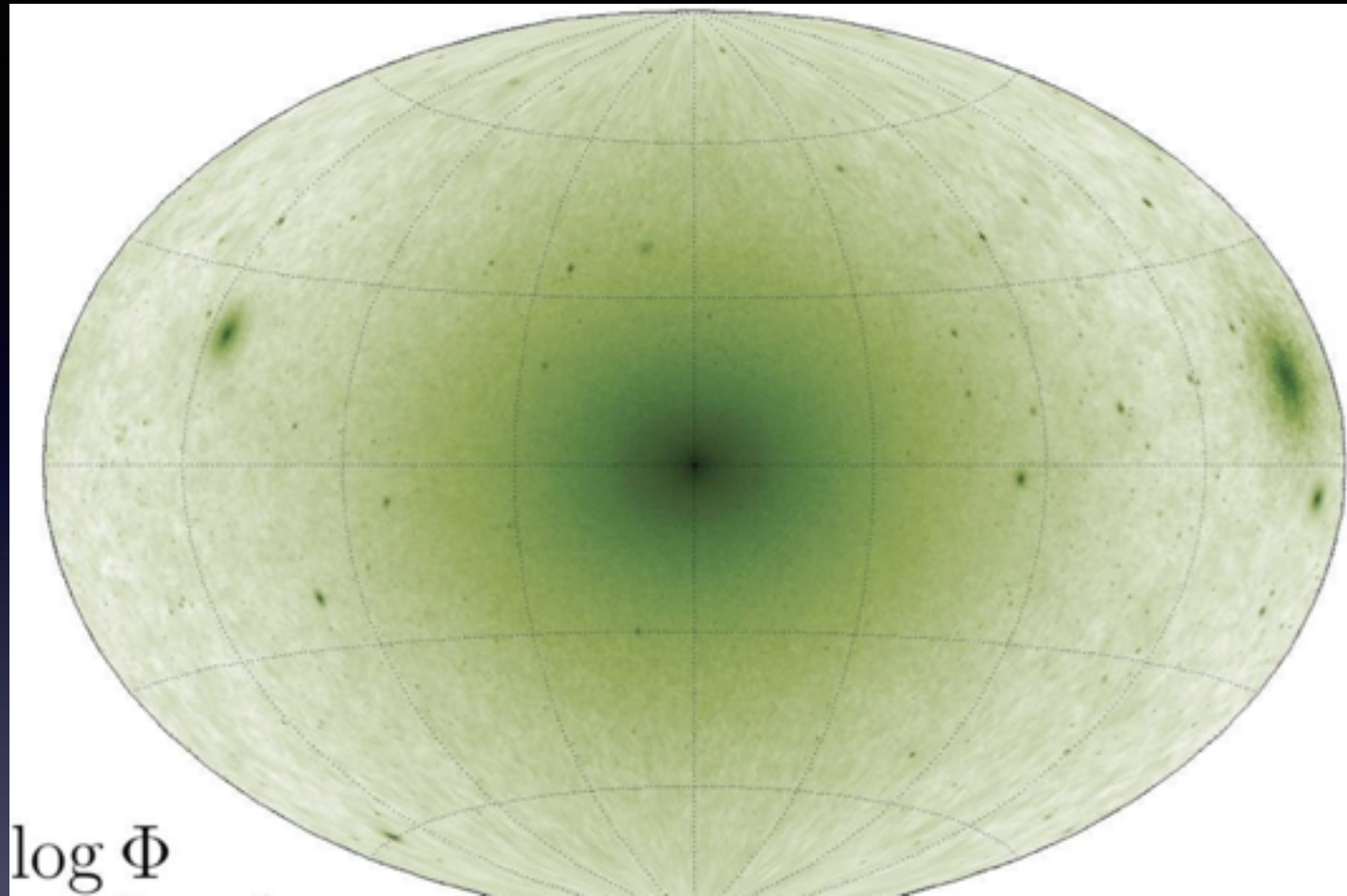
$$\text{local boost factor} = \frac{\text{total local luminosity}}{\text{smooth local halo luminosity}} \sim 1.4 \pm 0.2$$

larger than 10 in only 1% of all locations at 8 kpc
too low to explain HEAT/PAMELA e^+ excess with DM

JD et al, Nature 2008, Brun et al 2010



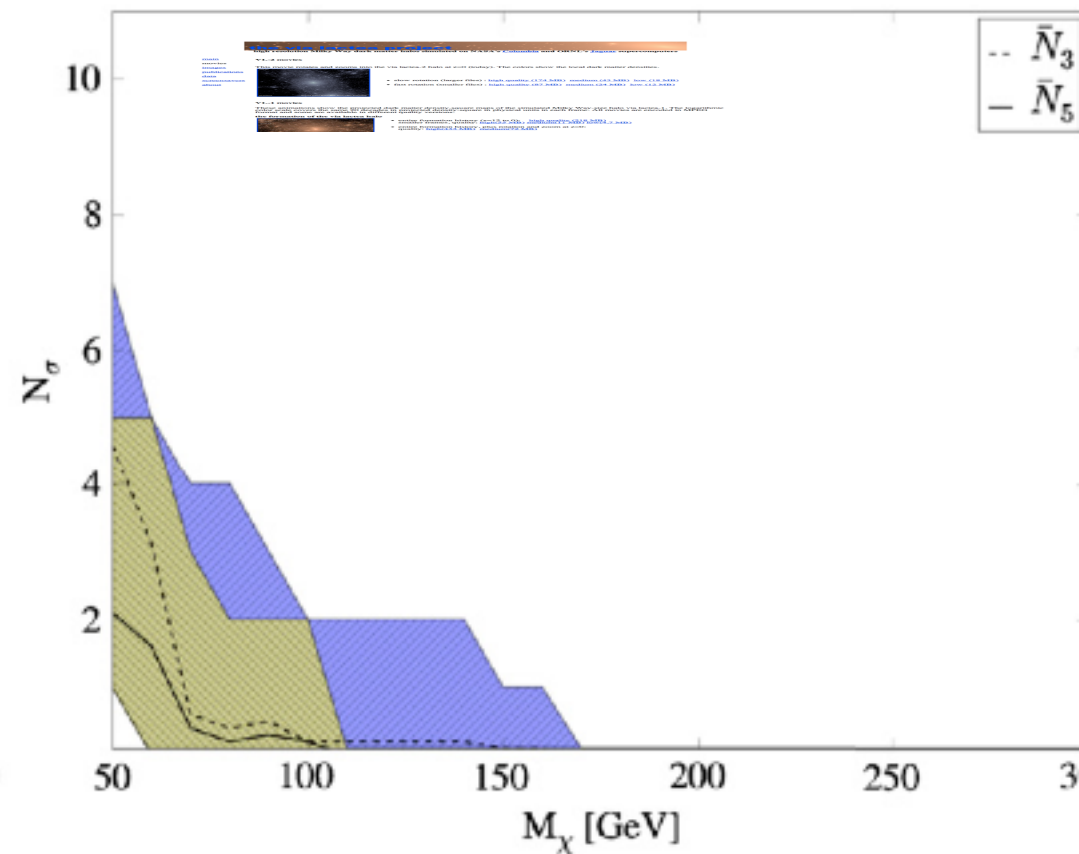
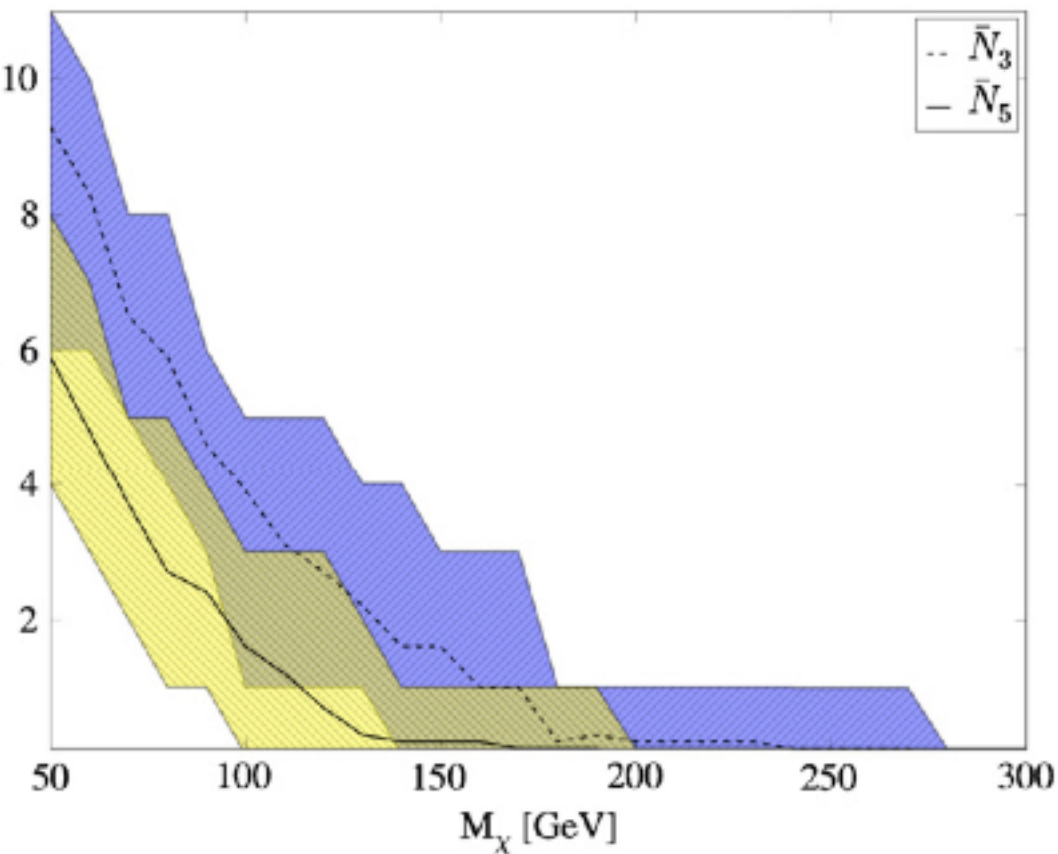
Allsky map of DM annihilation signal from via lactea II



the main halo is obviously the brightest source

but due to poorly constrained, diffuse, astrophysical foregrounds
(e.g. Strong, Moskalenko, Riemer 2004),
subhalos are the more promising gamma ray sources (Baltz et al. 2008)

Number of 3 and 5 sigma subhalo detection by Fermi over 10 years



including unresolved small sub-subhalos

assuming no sub-subhalos

small scale sub-sub-structure is not crucial for detection, but it helps.

promising numbers when using commonly assumed WIMP properties

Anderson, Kuhlen, JD, Johnson, Madau, ApJ 2011

3. other substructure

everything but subhalos,

e.g.

streams

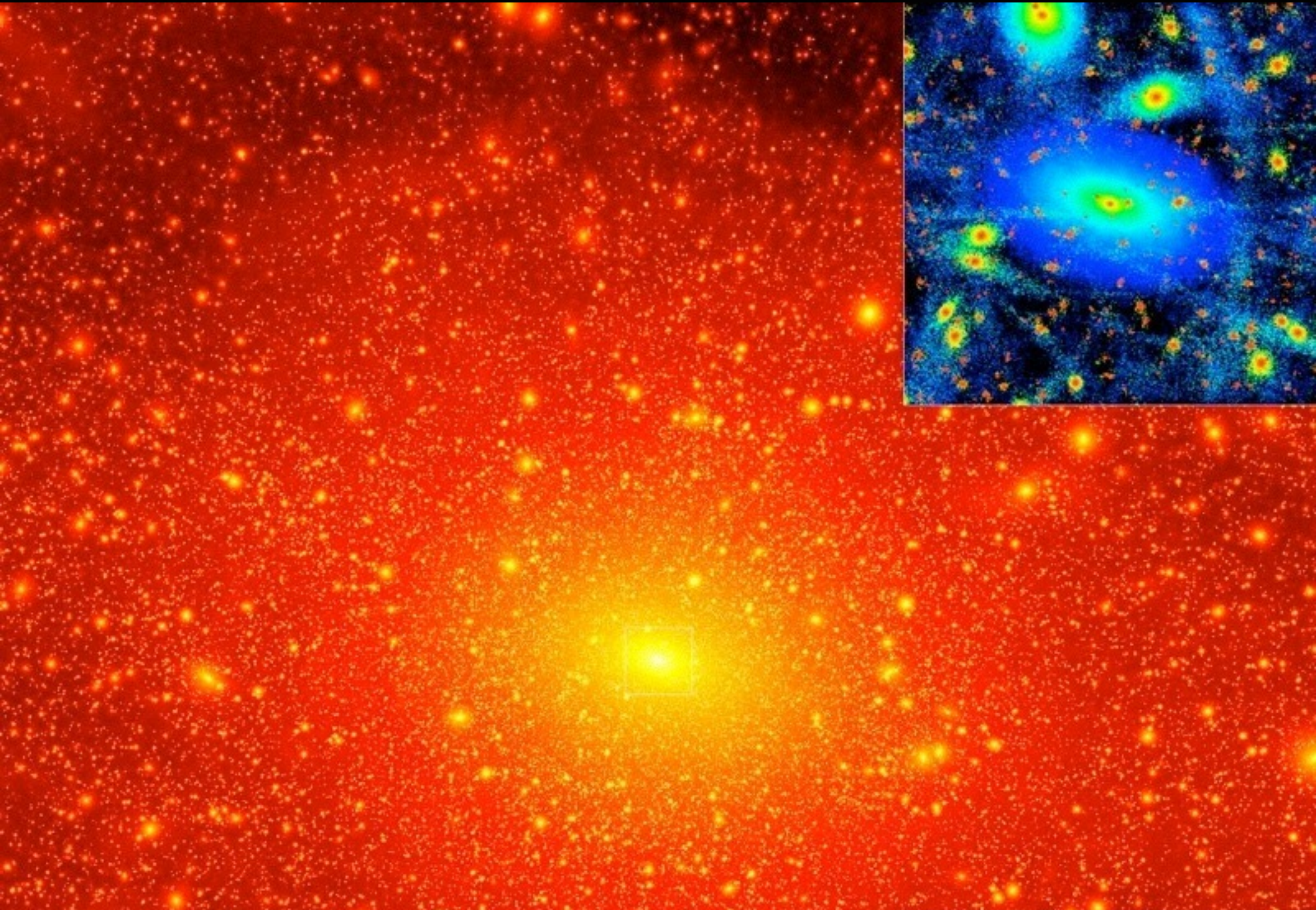
graininess

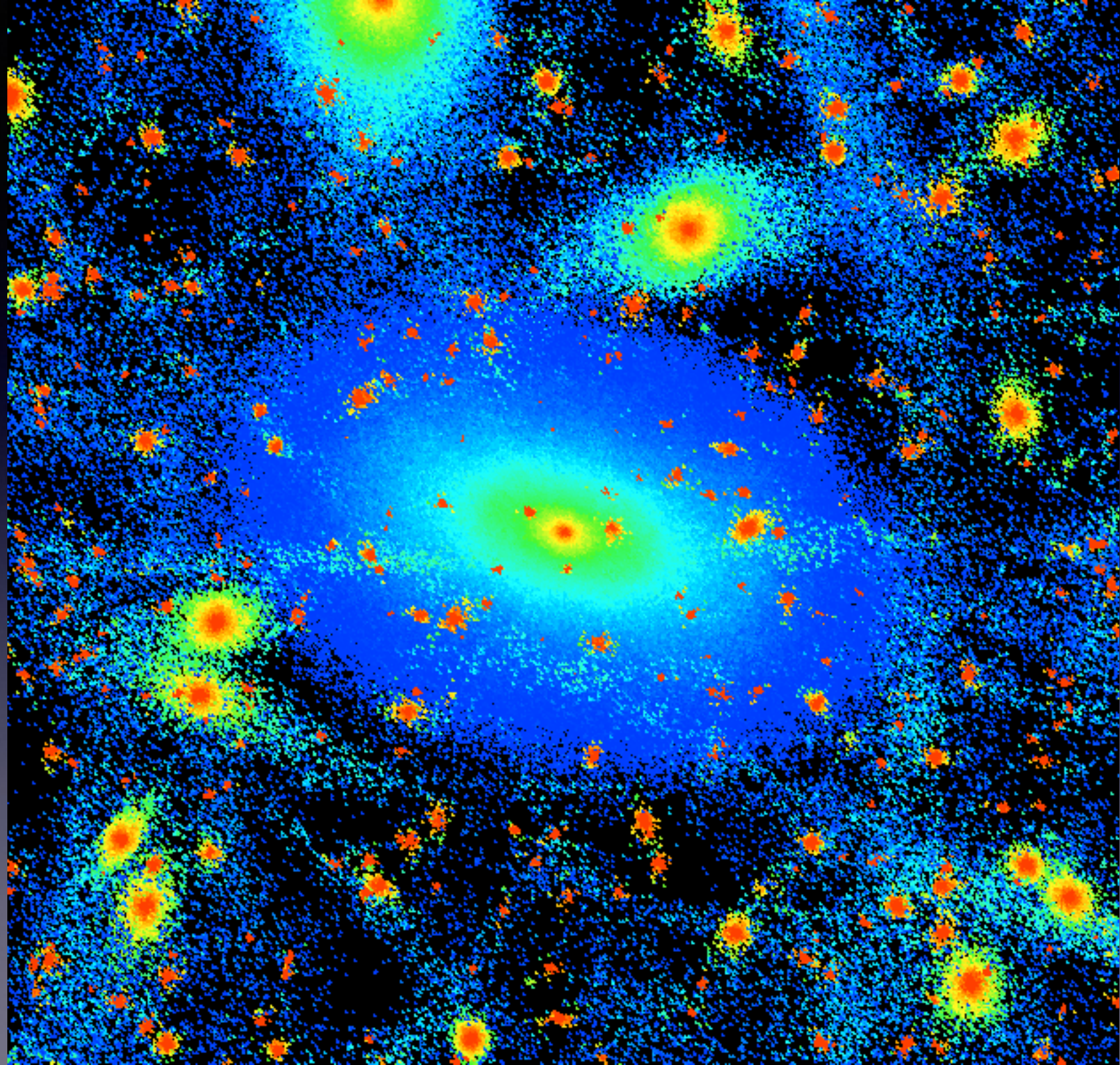
caustics

via lactea II :

local density

phase-space density

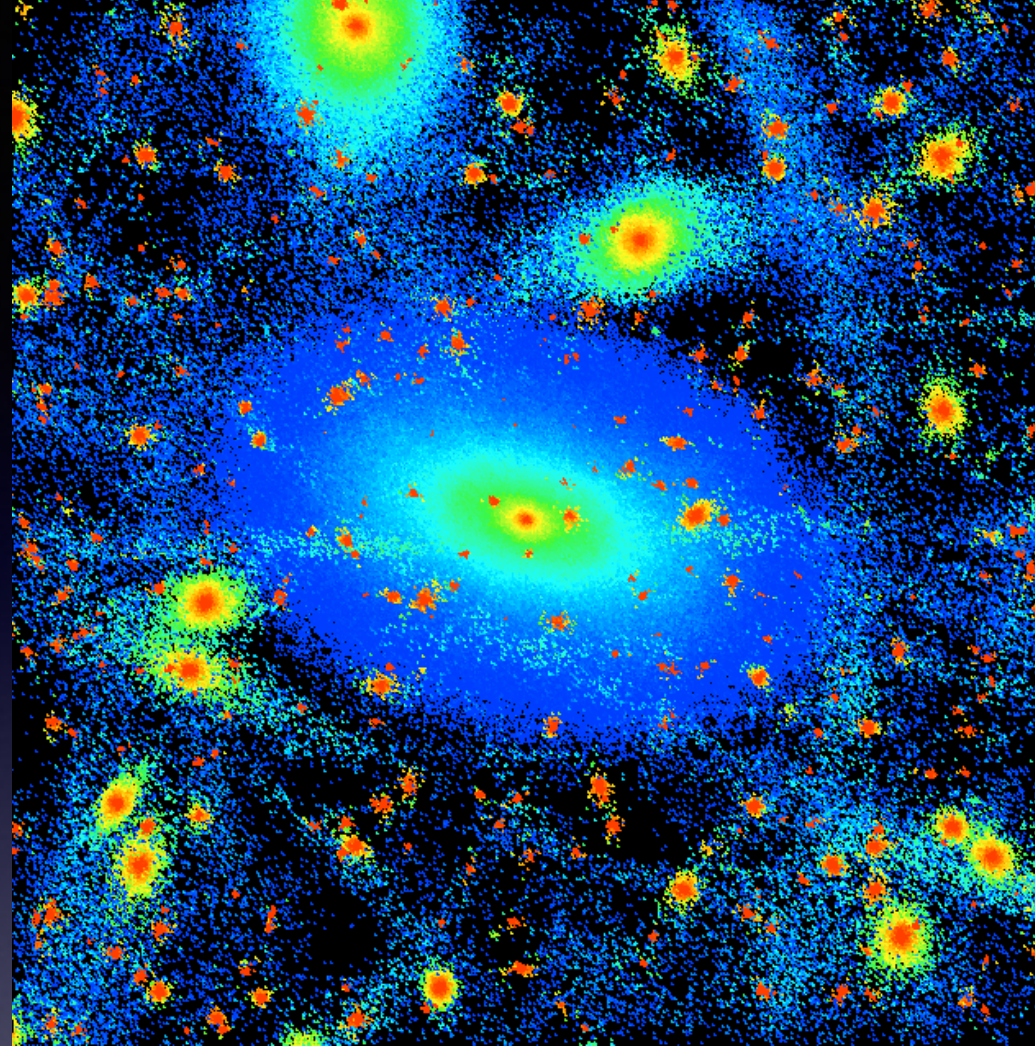




direct detection

at 8 kpc VL-II is almost smooth, there is little mass in subhalos

‘local’ kpc-scale velocity distributions are close to Gaussians



some obvious streams visible
in phase space density,
but they contain less than
0.01 of the local density

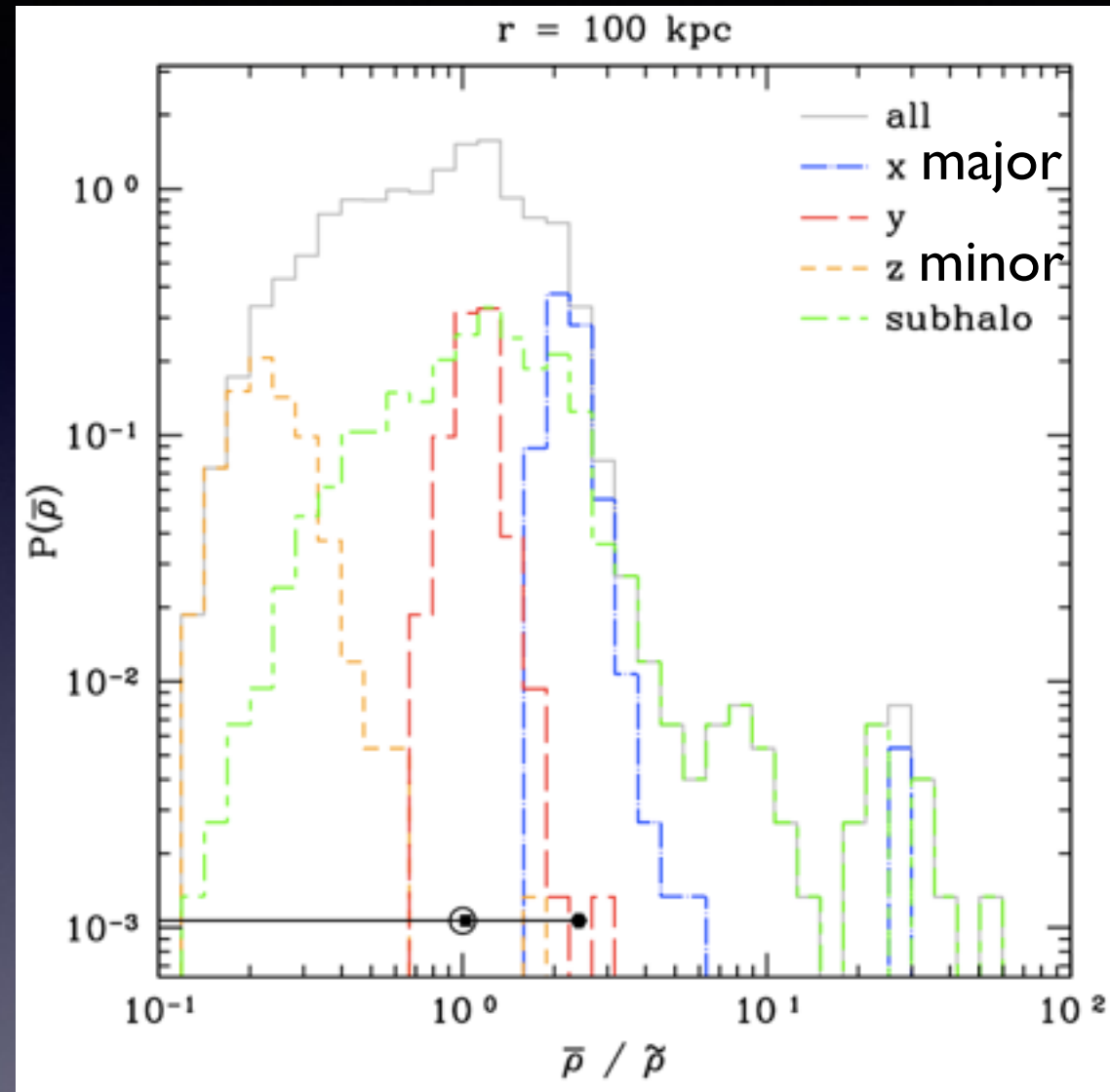
JD et al Nature 2008

additional lumpiness from tidal streams

streams are poorly mixed in the
outer halo

additional fluctuations in local
densities; more than just a smooth
triaxial halo plus subhalos

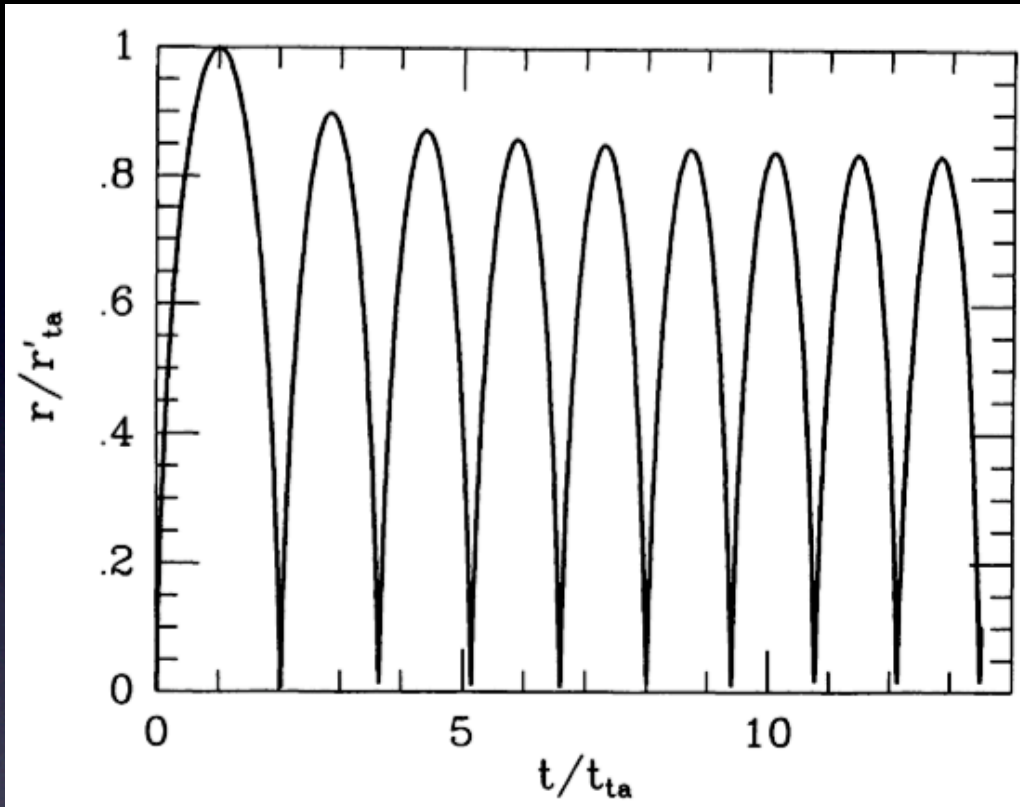
but clumpiness is still dominated
by subhalos, i.e no significant extra
annihilation boost from streams
(see also Afshordi et al. 08 | 1.1582)



Zemp, JD et al, 2009

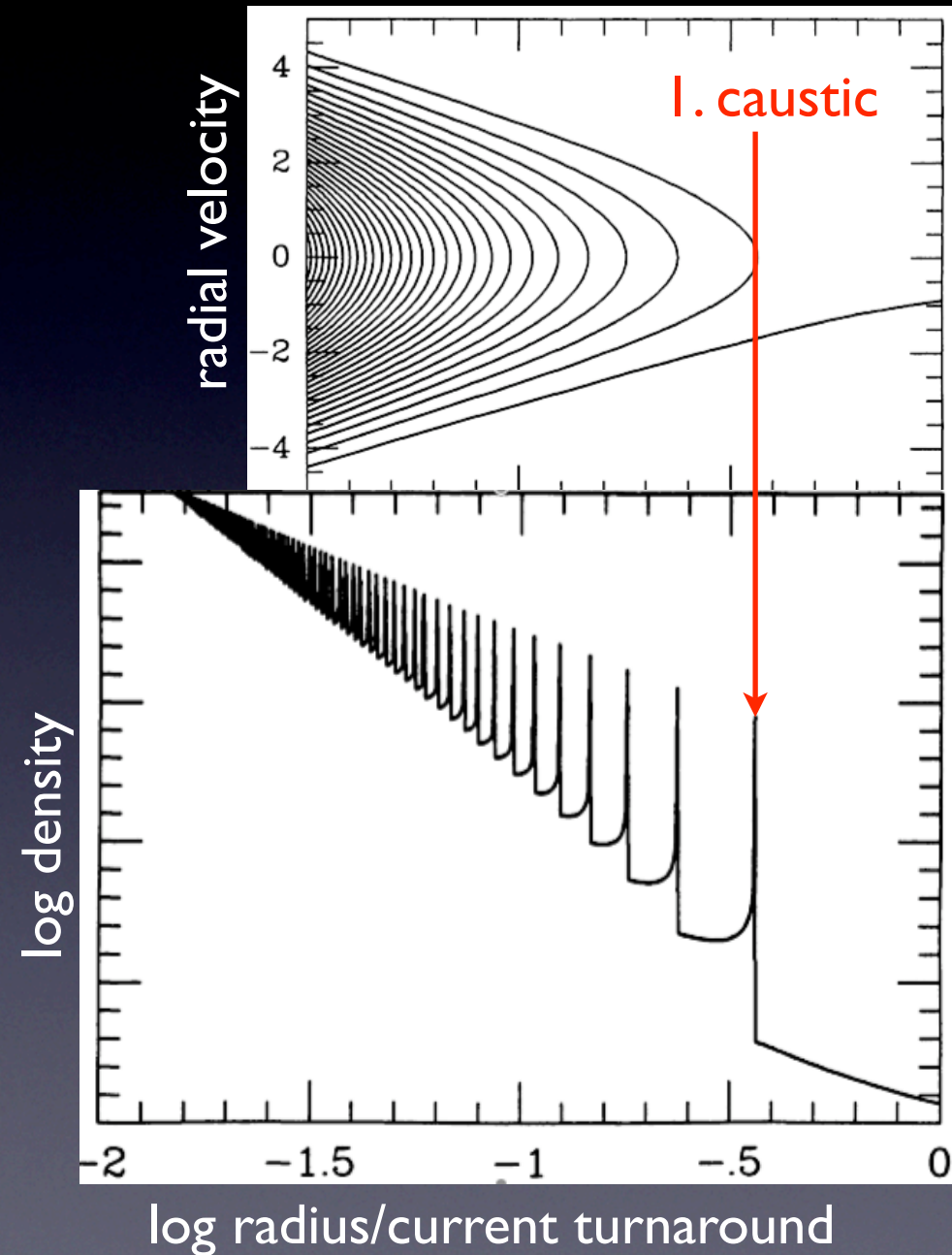
infall caustics

self-similar secondary spherical radial infall model:

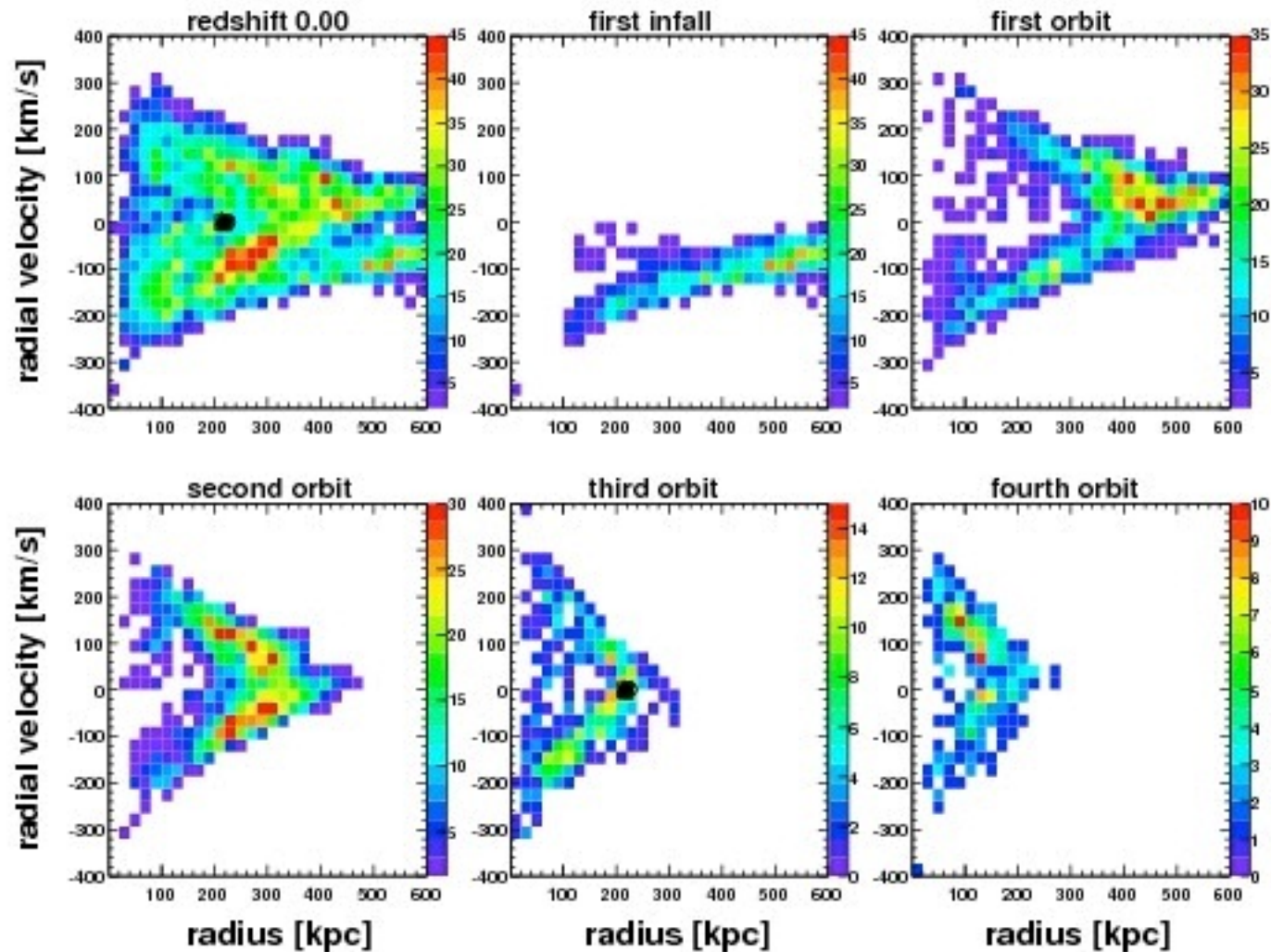


Fillmore&Goldreich 1984;Bertschinger 1985

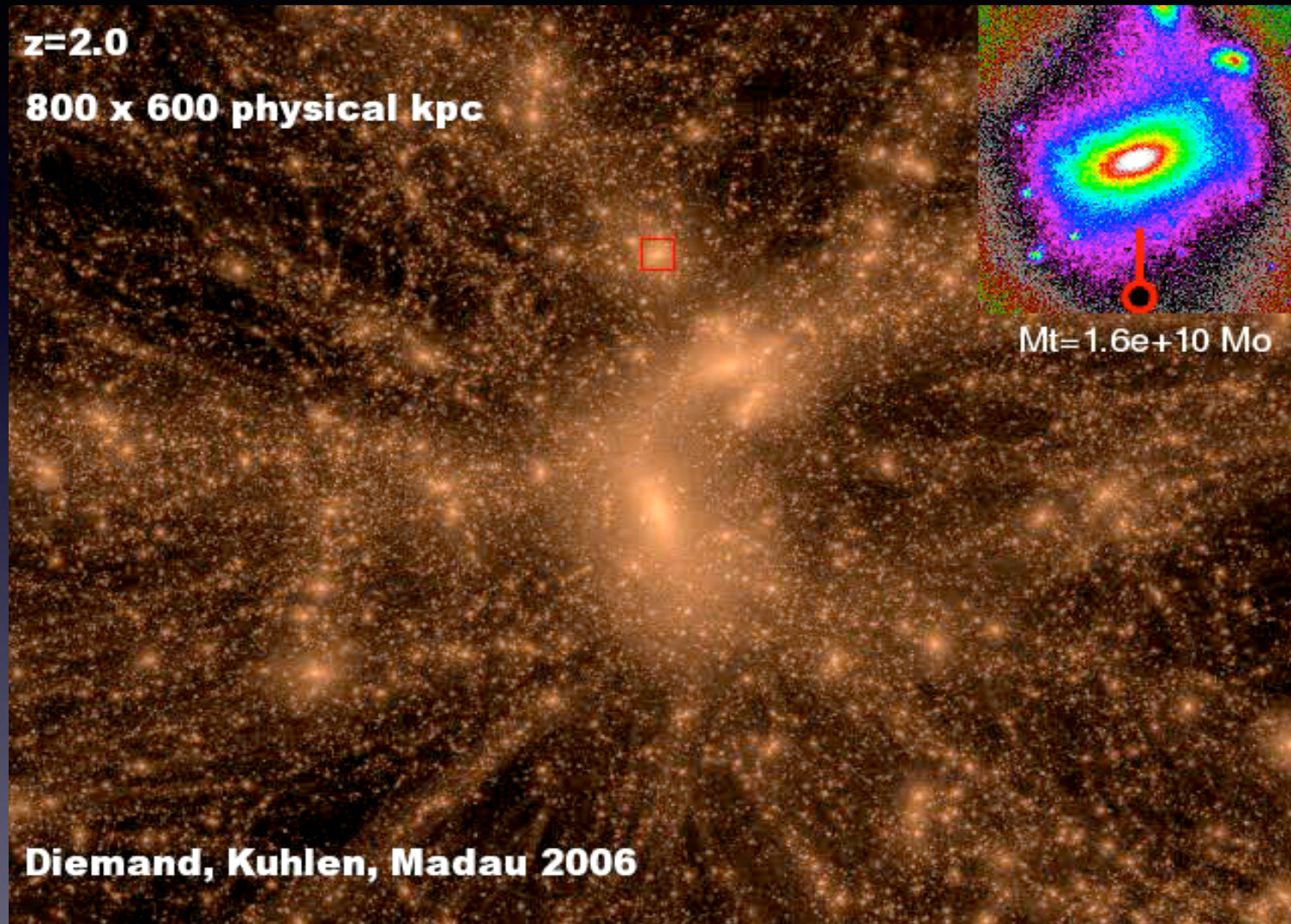
small collapse factors of 12% to 18%
 $\rho \sim r^{-2.25}$ with infinite density caustics



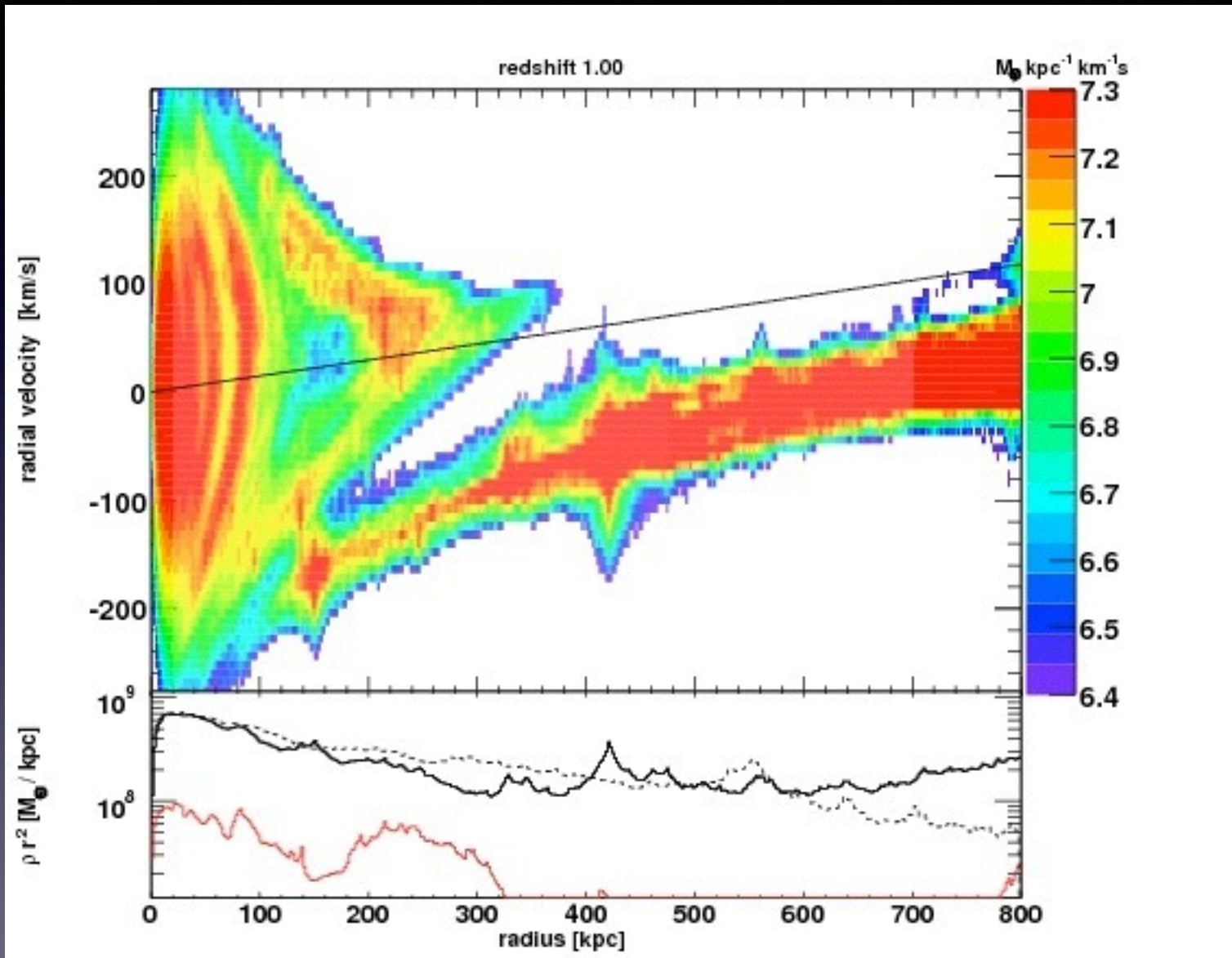
infall caustics



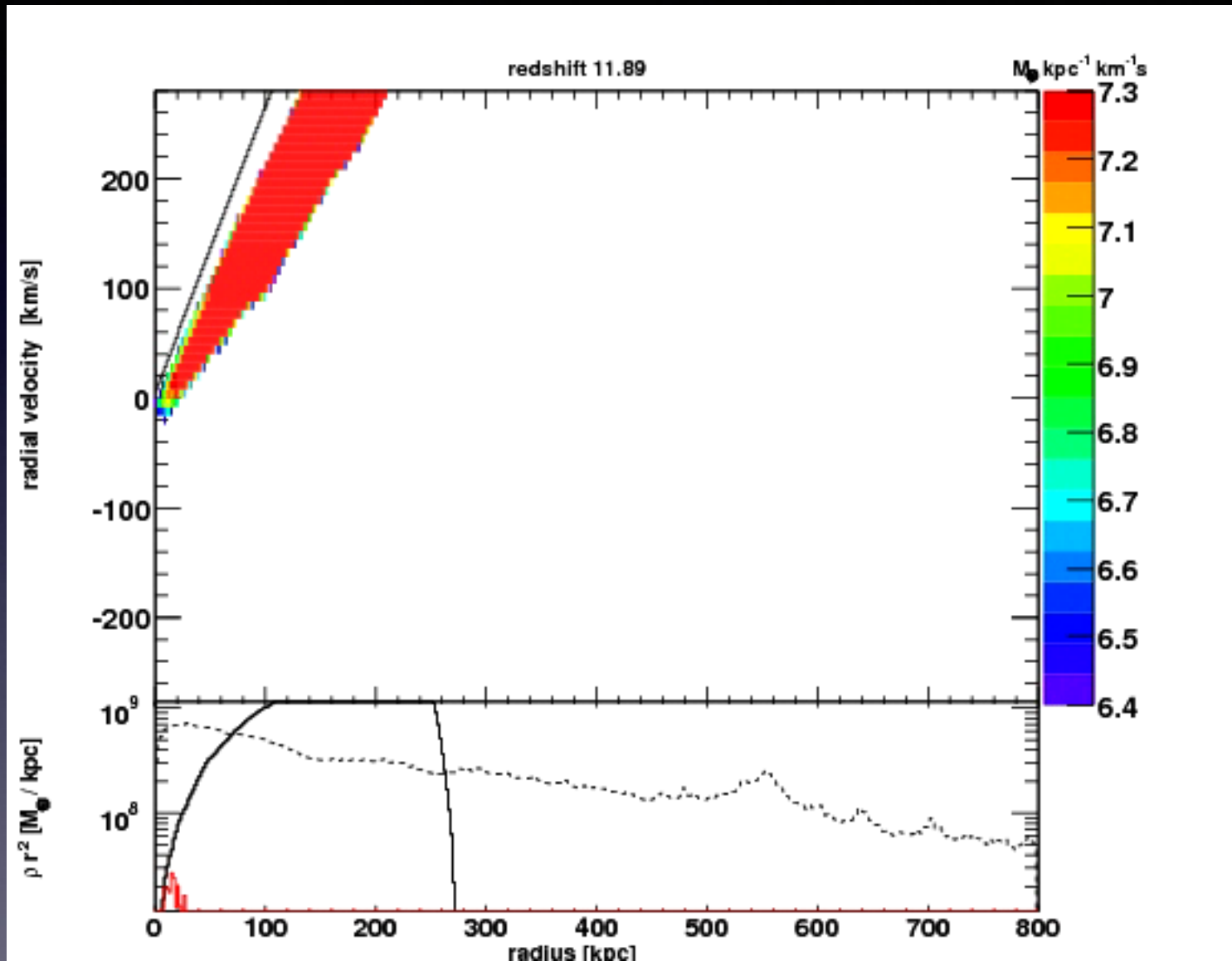
infall caustics

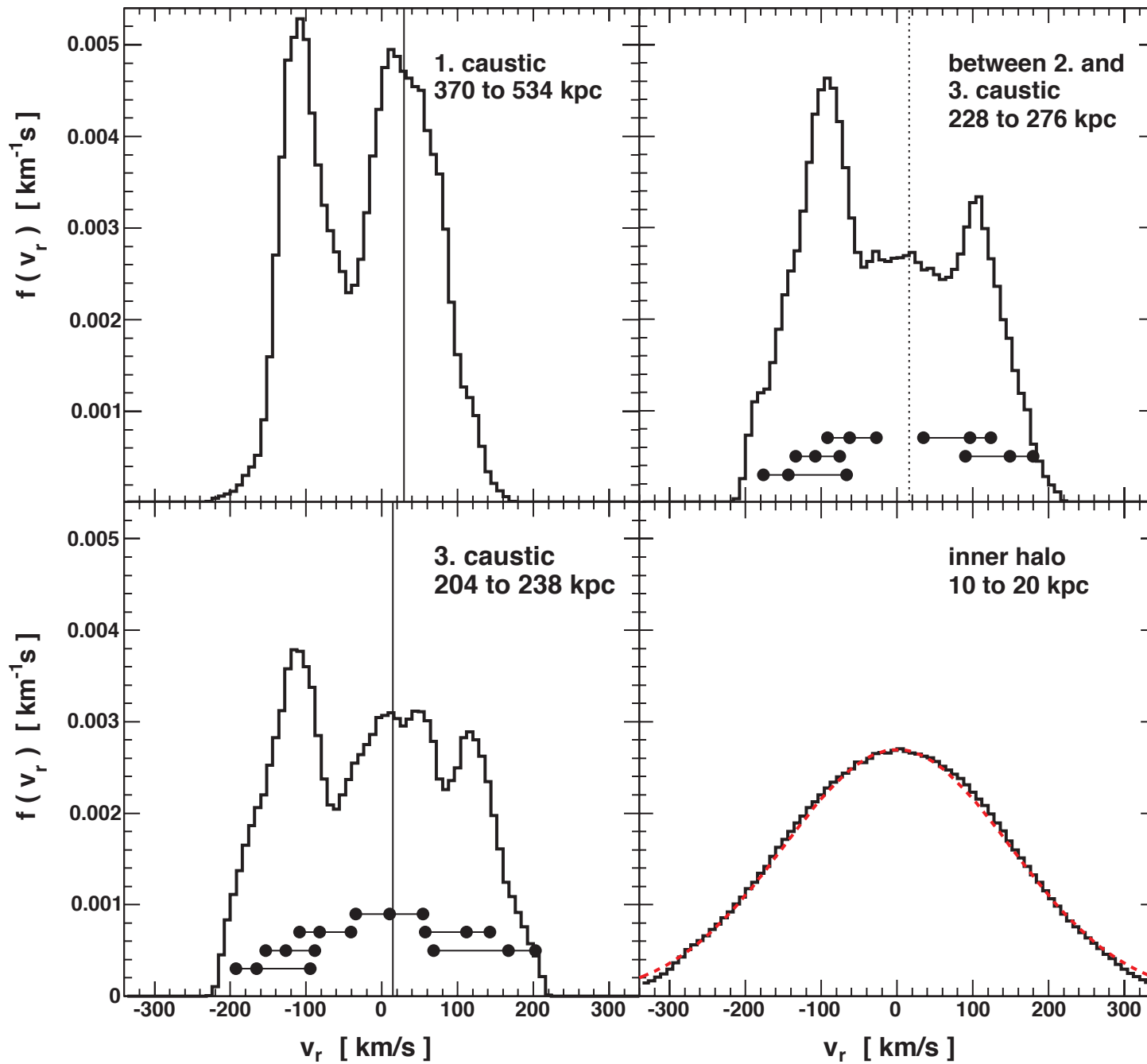


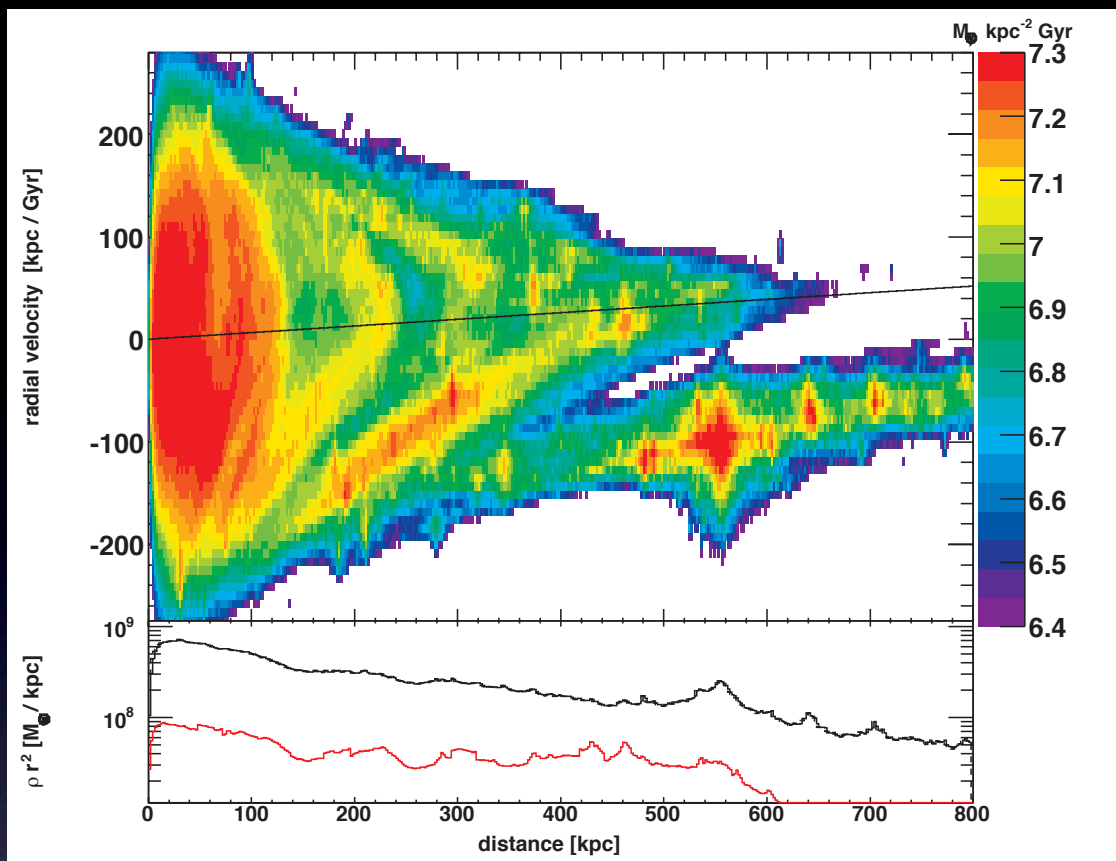
infall caustics



infall caustics







typical particles and subhalos go out to 0.8 to 0.9 of where they turned around, as in the FGB model

But the scatter is too large to allow the formation of high density caustics

only weak features in $v_r - r$ plane
detection extremely challenging!

note $r_{\text{vir}} = 289 \text{ kpc}$

$r_{k,\text{med}}$ [kpc]	$r_{k,68\%}$ [kpc]	$\frac{\Delta r_k}{r_{k,\text{med}}}$	$t_{k,\text{med}}$ [kpc]	$t_{k,68\%}$ [kpc]	$\frac{\Delta t_k}{t_{k,\text{med}}}$	$\left(\frac{r_k}{t_k}\right)_{\text{med}}$	$\left(\frac{r_k}{t_k}\right)_{68\%}$	$\left(\frac{r_k}{t_k}\right)_{\text{FGB}}$
453	370–534	0.36	491	443–551	0.22	0.92	0.77–1.12	0.876
310	242–384	0.46	343	297–407	0.32	0.93	0.57–1.24	0.864
220	204–237	0.15	261	211–316	0.40	0.84	0.67–1.10	0.856
173	137–207	0.41	222	180–266	0.39	0.78	0.58–1.25	0.843
141	110–191	0.57	179	131–229	0.55	0.78	0.52–1.46	0.832
121	89–170	0.67	157	105–201	0.61	0.81	0.54–1.46	0.834

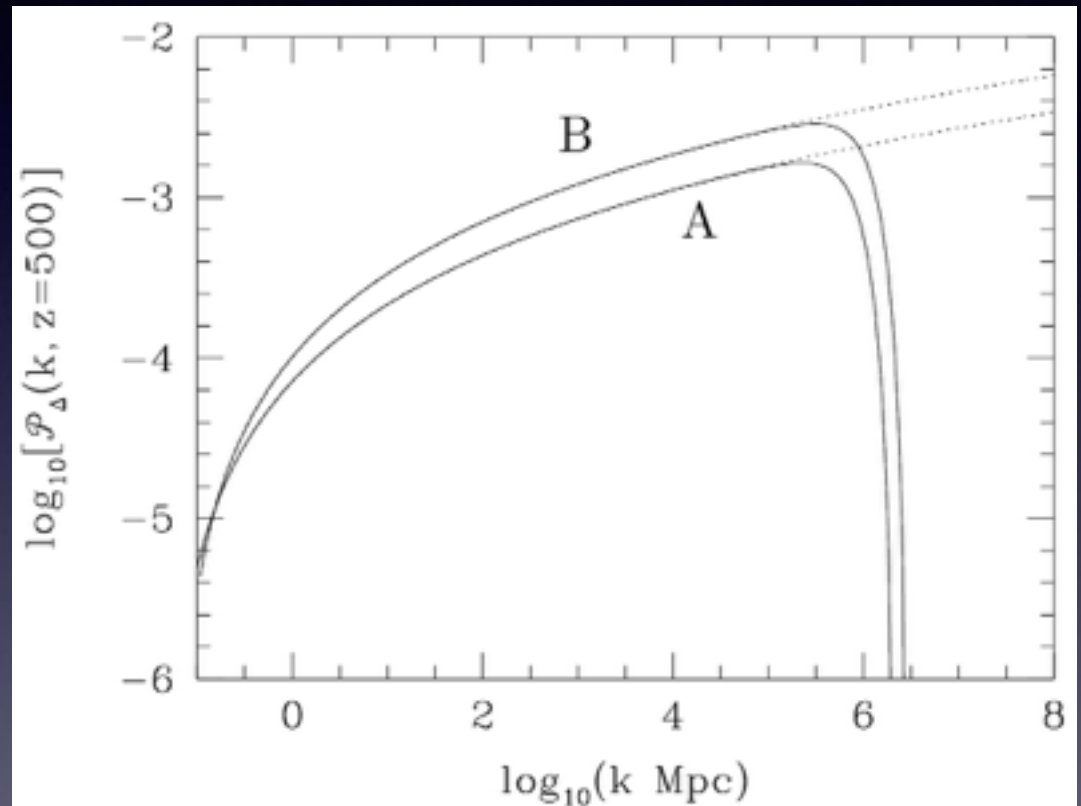
4. microhalos revisited

smallest scale CDM structures

For a 100 GeV SUSY neutralino (a WIMP)
there is a cutoff at about 10^{-6} Msun
due to free streaming

→ small, “micro”-halos should forming
around $z=40$ are the first and smallest
CDM structures

from Green, Hoffmann & Schwarz 2003



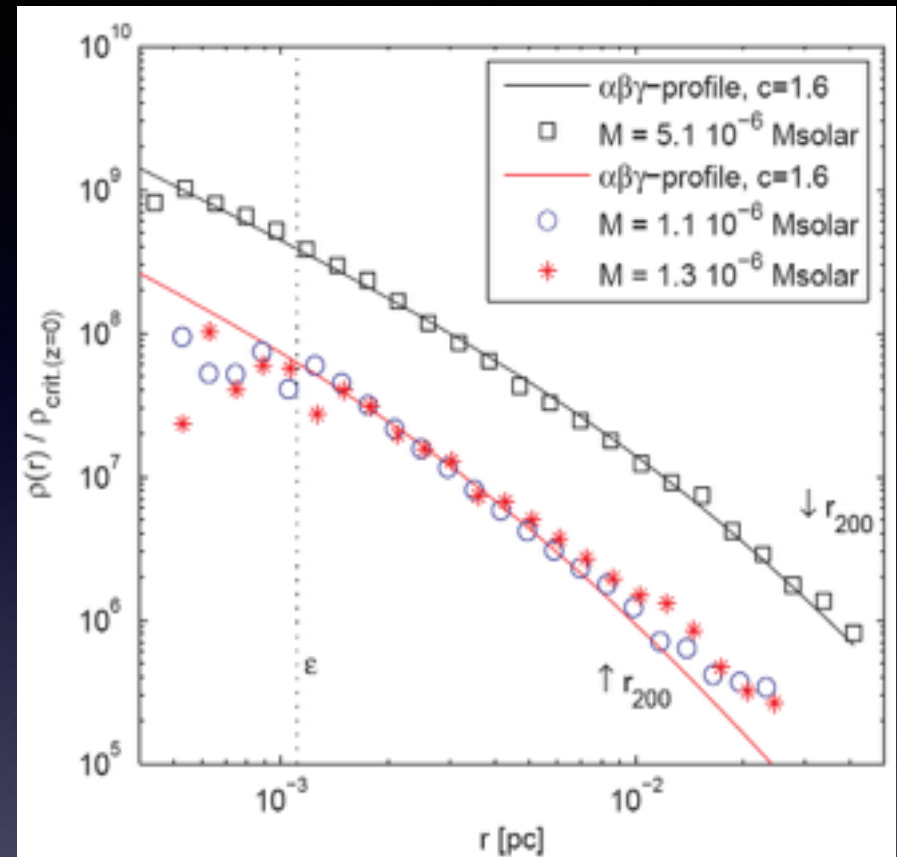
smallest scale CDM structures

CDM microhalos seem to be about as cuspy as the larger halos that formed in mergers

their concentrations $c \sim 3.3$ at $z=26$
evolve into $c \sim 90$ by $z=0$
consistent with Bullock et al. model

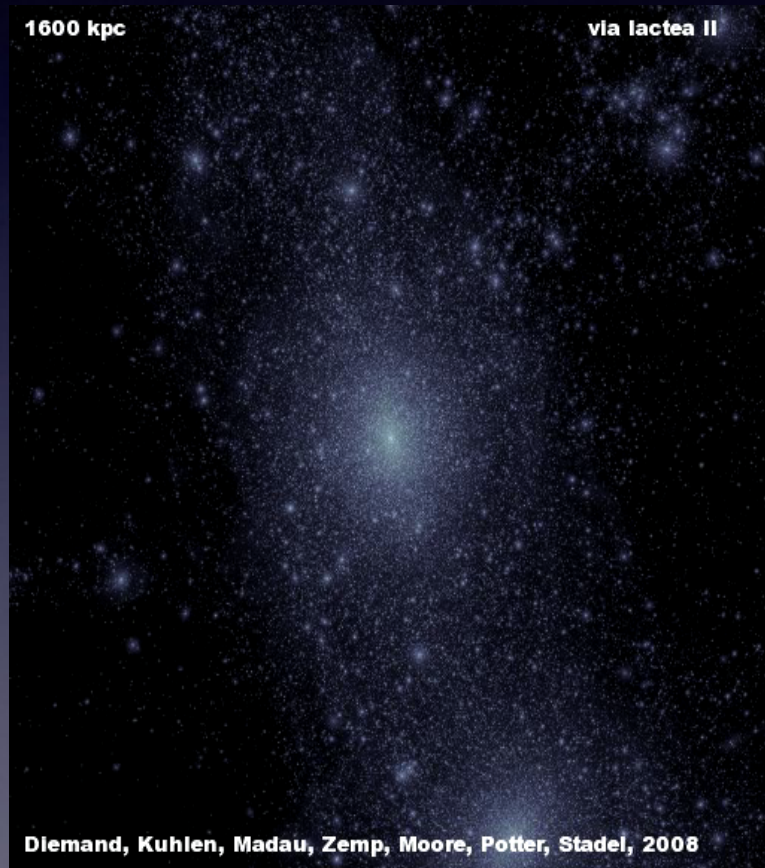
-> they are stable against tides caused by the MW potential if they live more than about 3 kpc from the galactic center
i.e. a huge number $\sim 5 \times 10^{15}$ could be orbiting in the MW halo today
(JD, Moore, Stadel, Nature 2005)

some tidal mass loss and disruption due to encounters with stars (see Goerdt et al. astro-ph/0608495)

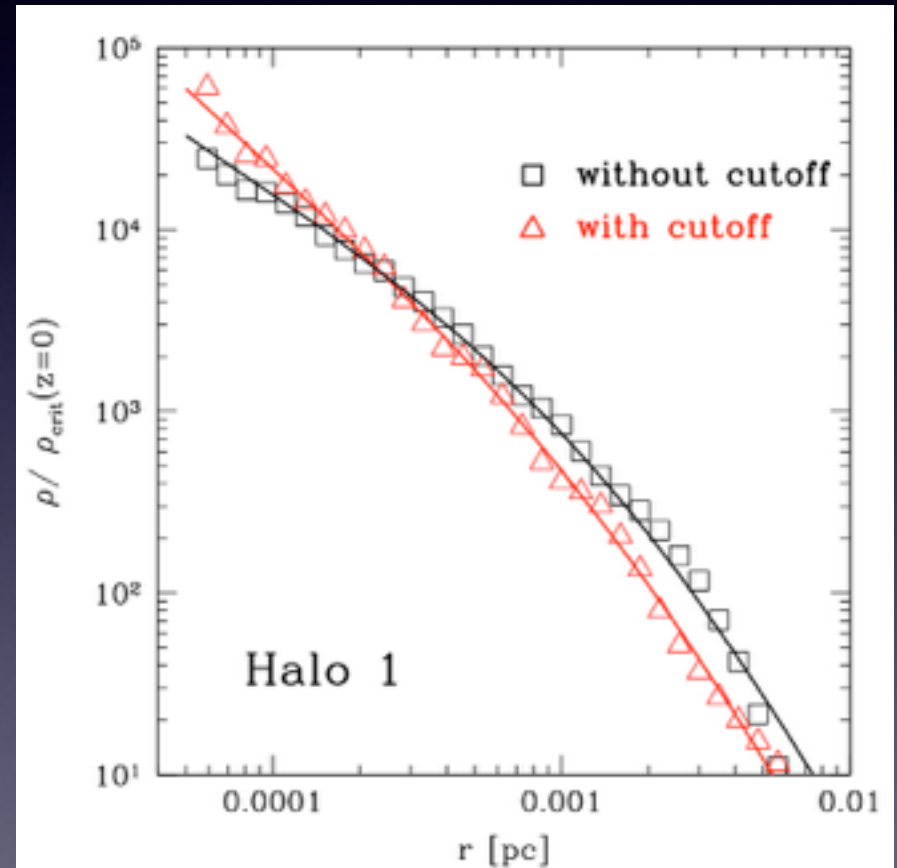


microhalo profiles depend on power spectrum

surprising result from Ishiyama et. al, ApJL, 2010:
cutoff leads to steeper profiles!

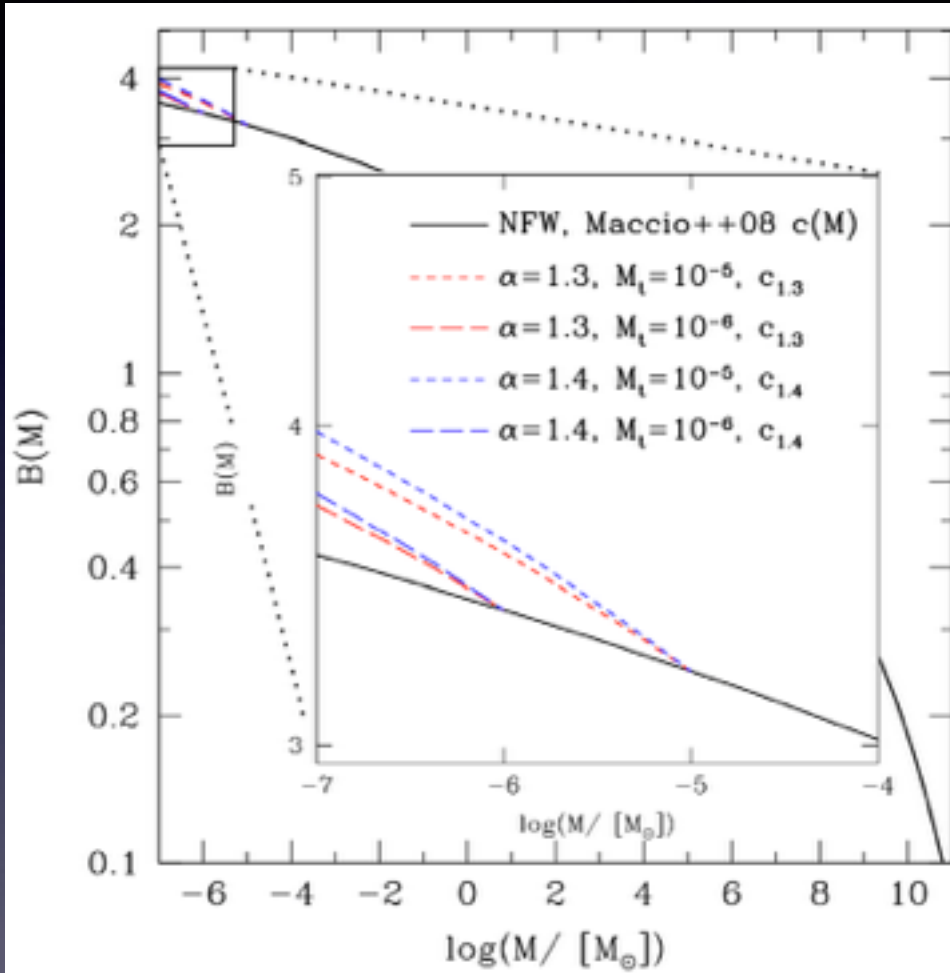


Ishiyama+, ApJL, 2010



Anderhalden & JD, arXiv:1302.0003

microhalo profiles depend on power spectrum

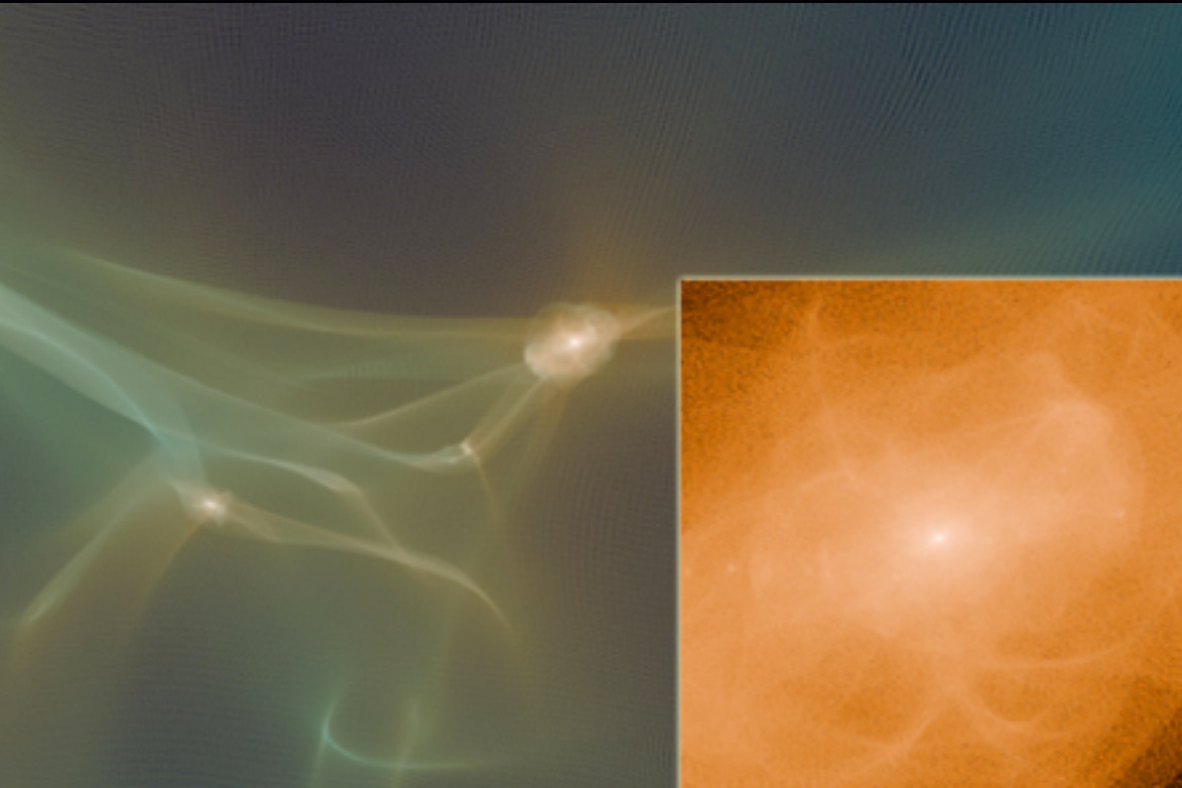


Anderhalden & JD, JCAP 2013

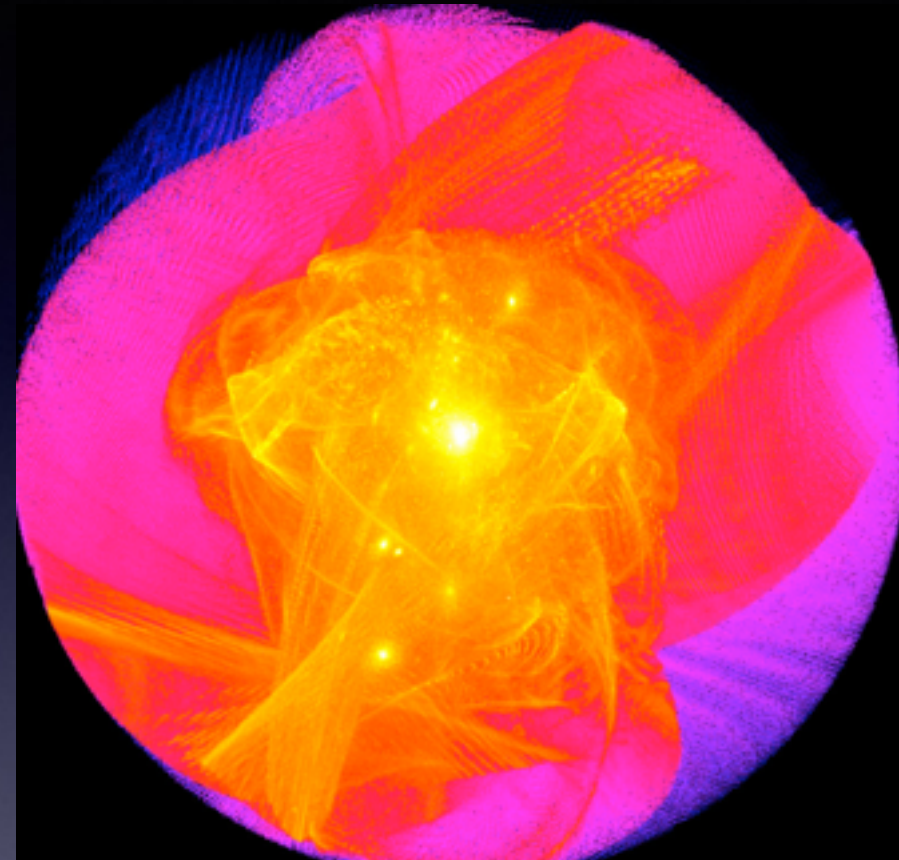
new, steeper microhalo profiles
lead to larger boost factors

the effect is quite small:
galactic halo boost increases
from 3.5 to up to 4.0

high redshift microhalos show clear infall caustics



Ishiyama+, ApJL, 2010



Anderhalden & JD, arXiv:1302.0003

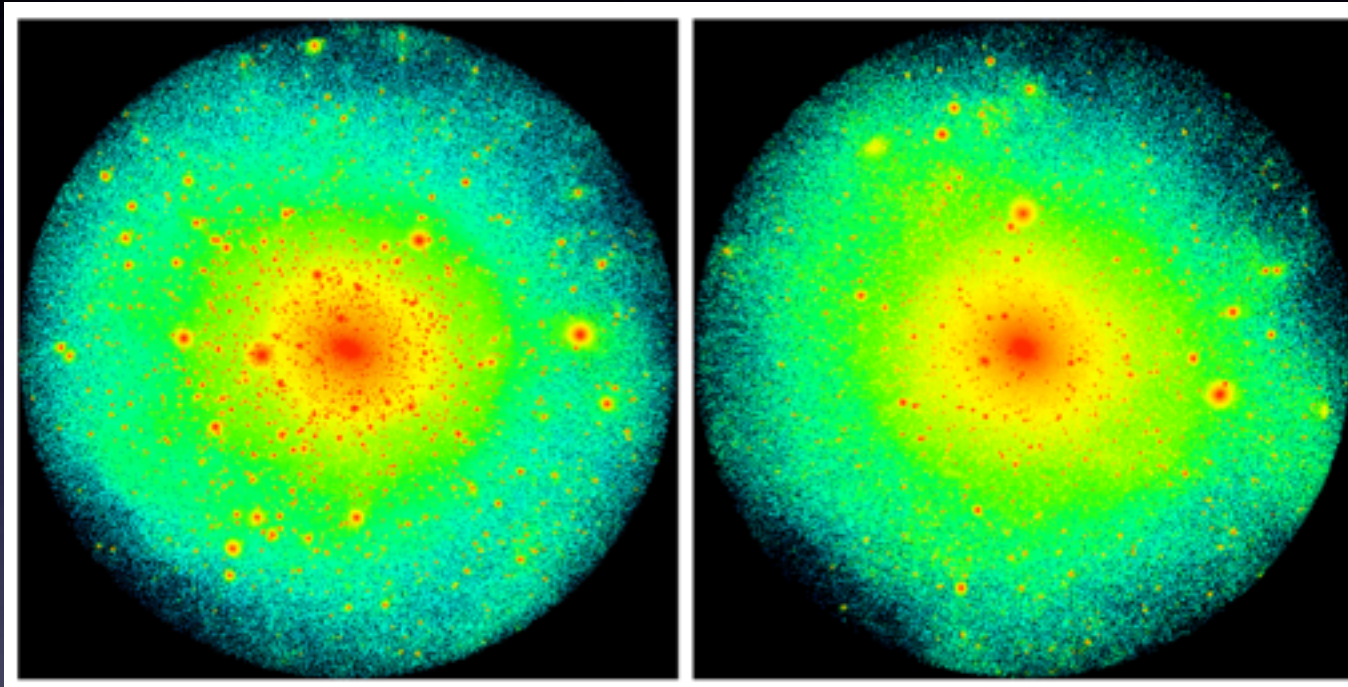
resolved caustics at $z=30$ increase the halo annihilation signal by 50%.
the effect decreases with time, unclear how much would be left at $z=0$.

summary of Λ CDM review

- tides remove subhalo mass from the outside in and lead to higher concentrations for subhalos. the effect is stronger near the galactic center
- identical density profiles and substructure abundance in the inner regions of field halos and subhalos
- small halos and subhalos contribute significantly to the total DM annihilation signal. Largest contributions per mass decade come from around solar mass scales.
- astrophysical factors in pure CDM annihilation rates are now well constrained (within a factor of two). baryons increase the uncertainty in some regions
- WIMPs with commonly assumed properties produce annihilation signals in subhalos, which should be detectable by Fermi
- other DM substructures like infall caustics and tidal streams have little effect on direct and indirect DM detection
- microhalos near the cutoff have surprisingly steep inner profiles. this increases galactic halo boost factors by a small amount (up to 15 percent)

Warm Dark Matter and Mixed Dark Matter Models

LCDM



LWDM
 $m_{\text{eff}} = 2 \text{ keV}$

for details see:

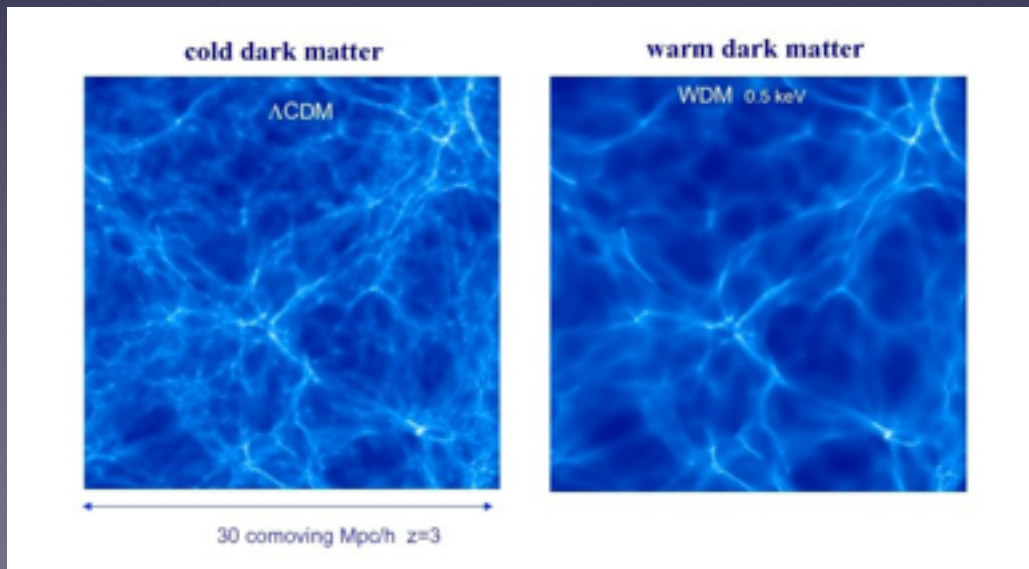
Anderhalden, Schneider, Maccio, JD, Bertone, JCAP 2012/2013

Schneider, Anderhalden, Maccio, JD, MNRAS 2014

motivation for WDM

- ◆ neutrino minimal standard model (νMSM) contains sterile neutrinos with an effective mass of a few keV
- ◆ might solve the small scale problems of CDM (e.g. Weinberg+2013):
 - cusp/core problem
 - missing satellites problem
 - too big to fail problem

while maintaining its successes on large scales



constraints from Lyman- α forest:

$$m_{\text{eff}} > 2 \text{ keV}$$

Viel et al. 2005, Seljak et al. 2006

$$m_{\text{eff}} > 3.3 \text{ keV } (2\sigma)$$

Viel et al. PRD 2013

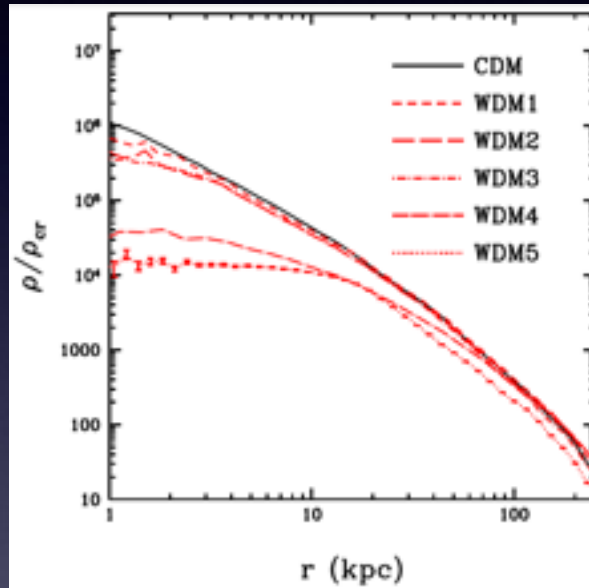
cusp / core problem

CDM predicts too high DM densities
in the inner few kpc of galaxies

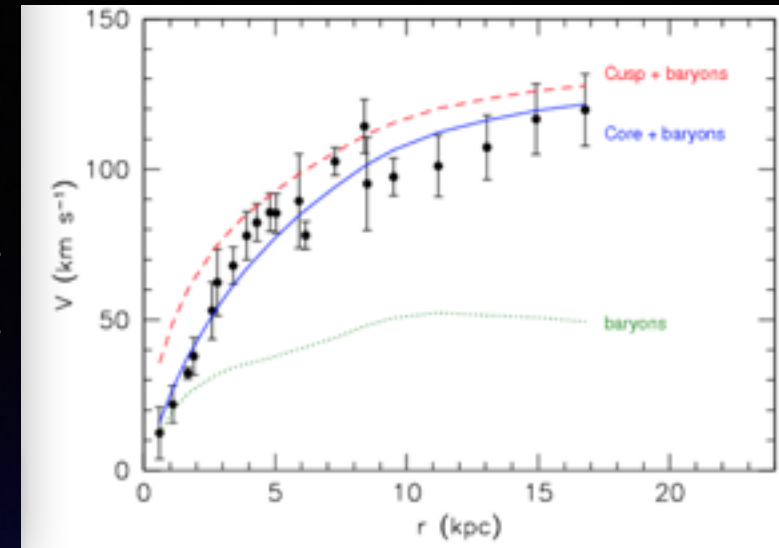
DM solutions:

needs
extreme WDM:
 $m_{\text{eff}} < 0.1$ keV
ruled out

maybe SIDM?
Rocha et al. 2013
Peter et al. 2013



Maccio et al. 2012

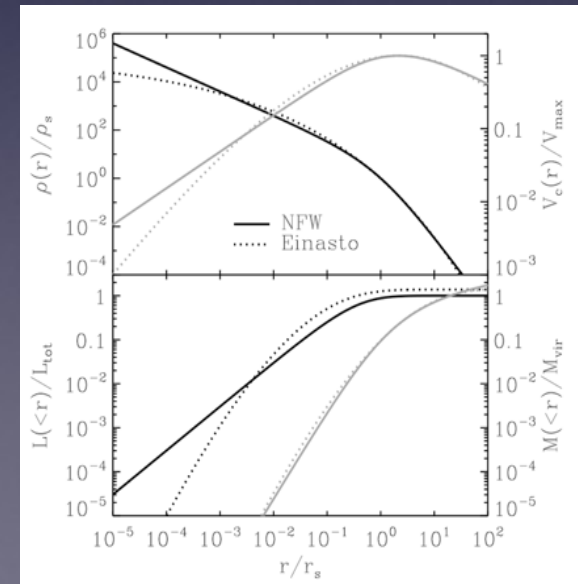


Kuzio de Naray et al. 2008

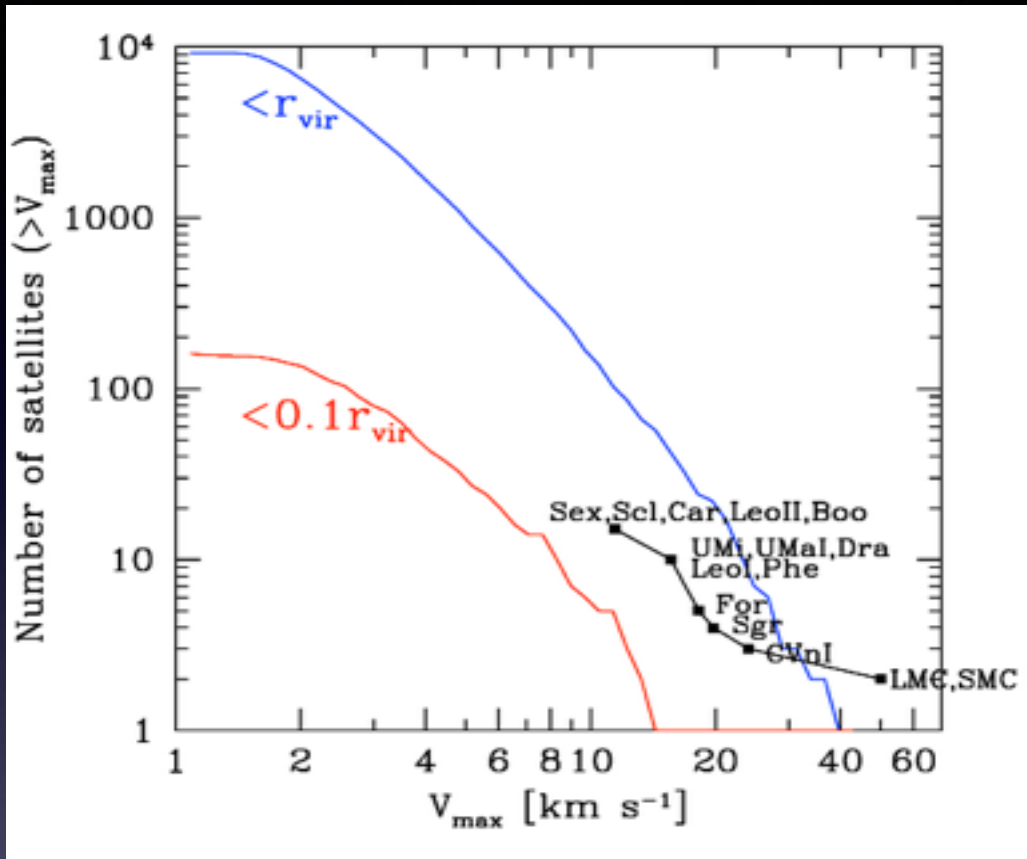
Baryonic solution:

episodic
supernova
feedback

Governato et al. 2012
Teyssier et al. 2012

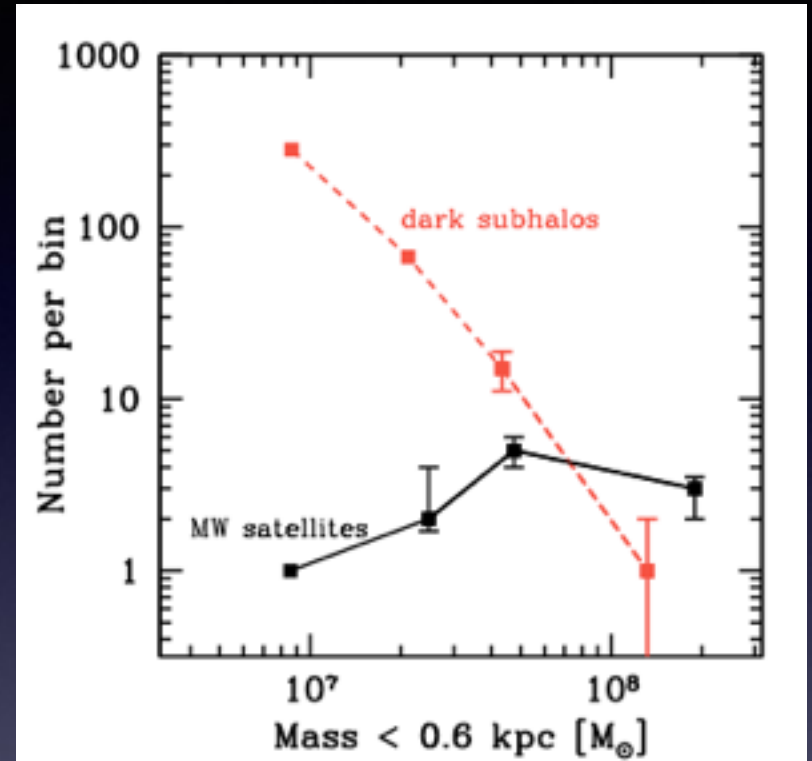


missing satellites problem (Moore+99, Klypin+99)



Madau, JD, Kuhlen 2008

the original comparisons assumed $\sqrt{3} \sigma_{1D}^* = V_{\max}$



Strigari et al. 2007

this seems to be roughly right

CDM only predicts subhalos, not dwarf galaxies. Luckily, CDM predicts (more than) enough structures to host all satellites (could be up to 1000, Tollerud et al. 2008)

Baryonic solution:

Plausible galaxy formation models roughly reproduce the observed numbers of dwarfs. Many CDM subhalos remain dark (e.g. Governato+2007/2011, Weinberg+2013)

the “too big to fail” problem (Boylan-Kolchin, Bullock, Kaplinhat, 2011/2012)

higher resolution DM simulations and better observational constraints now allow for more detailed comparisons:

dwarf satellite mass within the half light radius is well constrained (Wolf+2009)

cosmological simulations can now resolve the corresponding scales directly

mock observations confirm mass estimates, with small scatter due to subhalo shapes (Rashkov+2012)

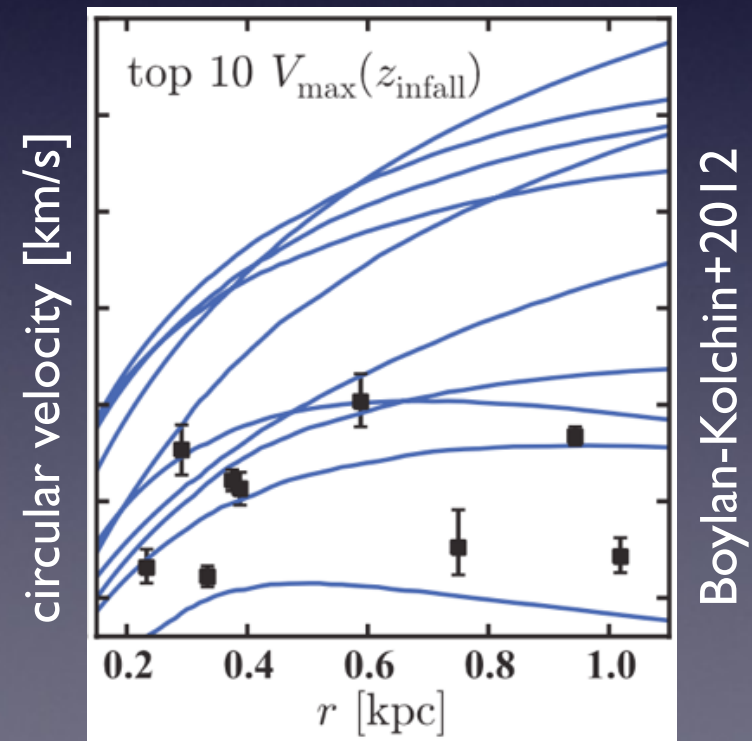
most CMD halos have
too many dense subhalos

few exceptions (Purcell&Zentner,2012)

and there is some evidence for cores in
some of these dwarf galaxies
(Walker & Penarrubia 2012, Amorisco+2013)

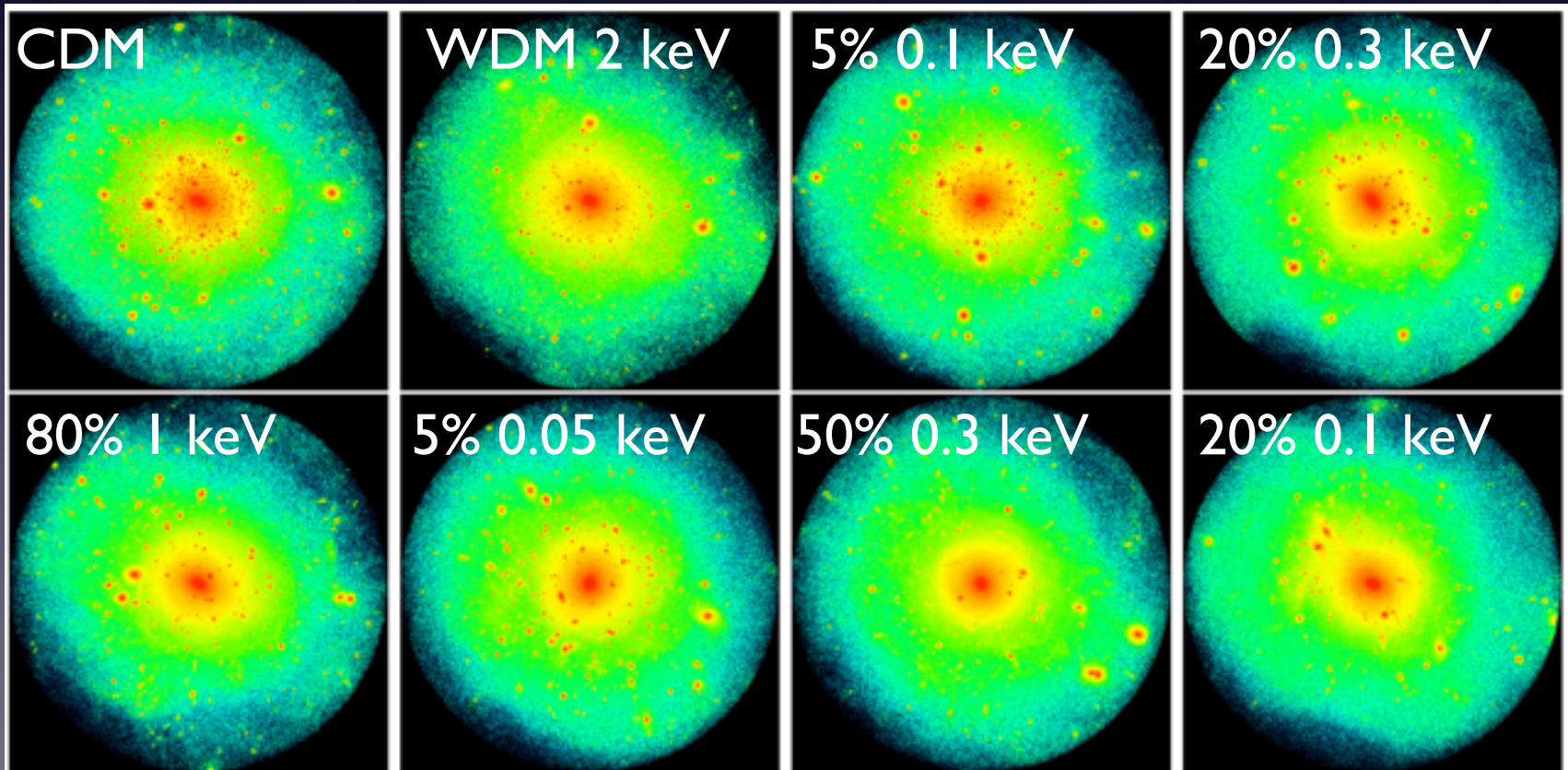
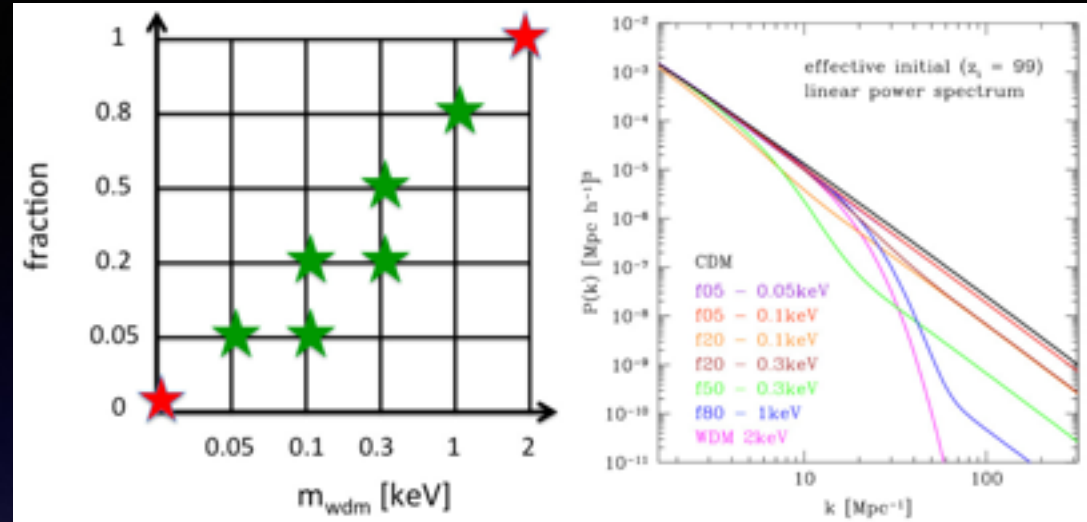
Baryonic solution?

episodic feedback too weak in these small galaxies
(Garrison-Kimmel + 2013)

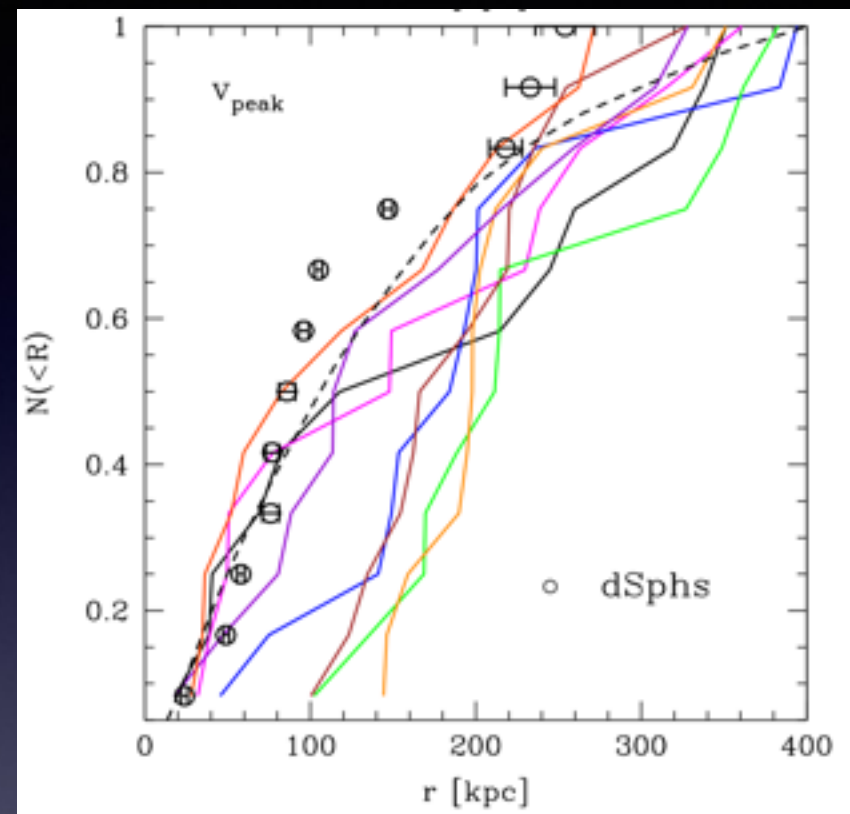
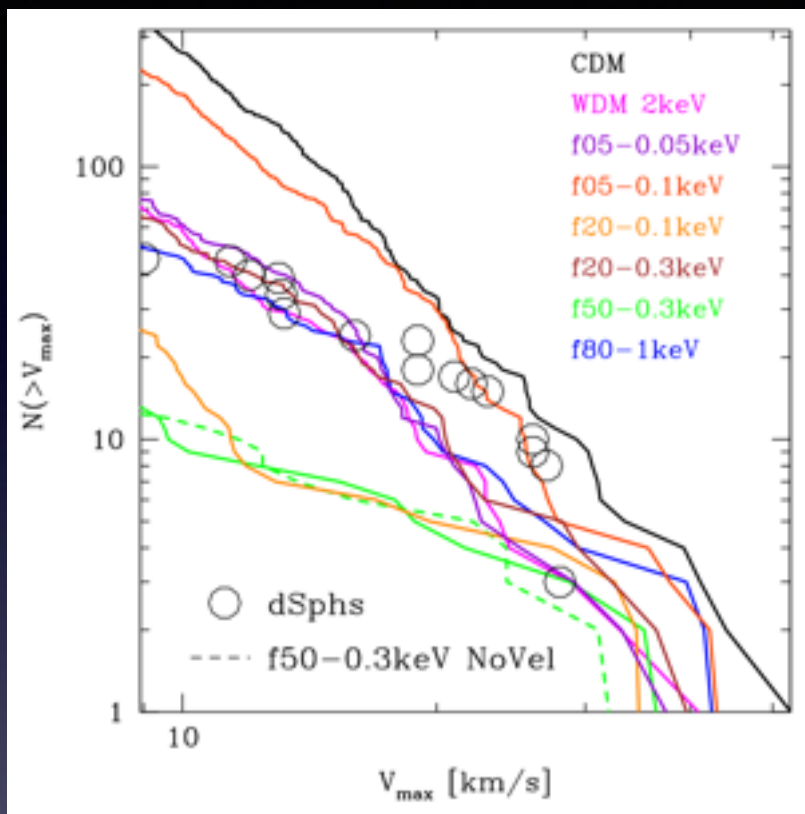


WDM and mixed C+WDM simulations

8 simulations
of the same galactic halo
DM model (marginally)
consistent with Lyman- α



abundance and radial distribution of satellites

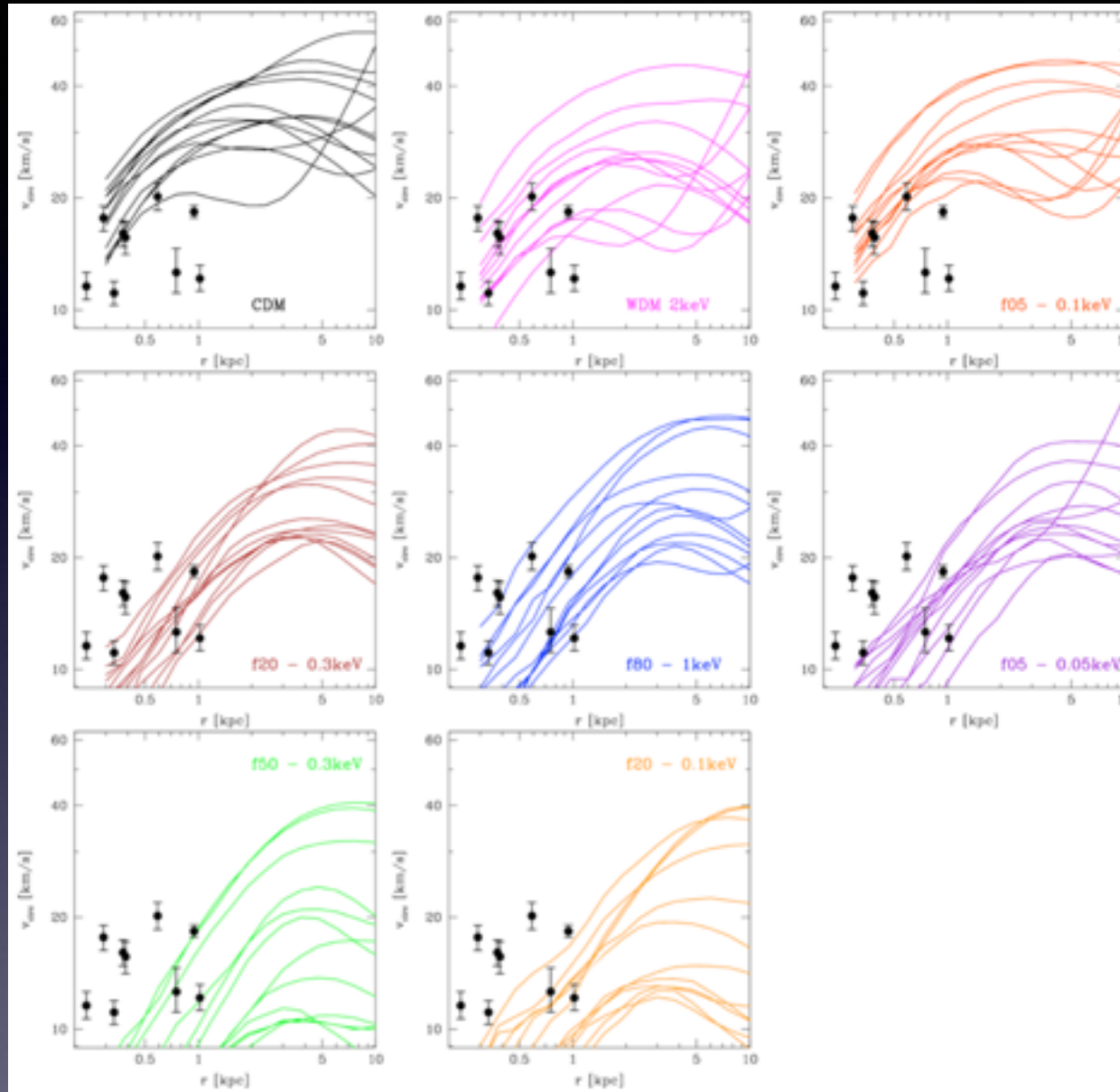


moderate WDM and C+WDM models have enough subhalos,
and with a realistic radial distribution

more extreme WDM and C+WDM models contain too few subhalos,
and they are found at larger radii than the observed dwarfs (Anderhalden+2013)

(similar WDM results in: Polisensky & Ricotti 2011, Lovell+2011)

the “too big to fail” problem (Boylan-Kolchin, Bullock, Kaplinhat, 2011/2012)



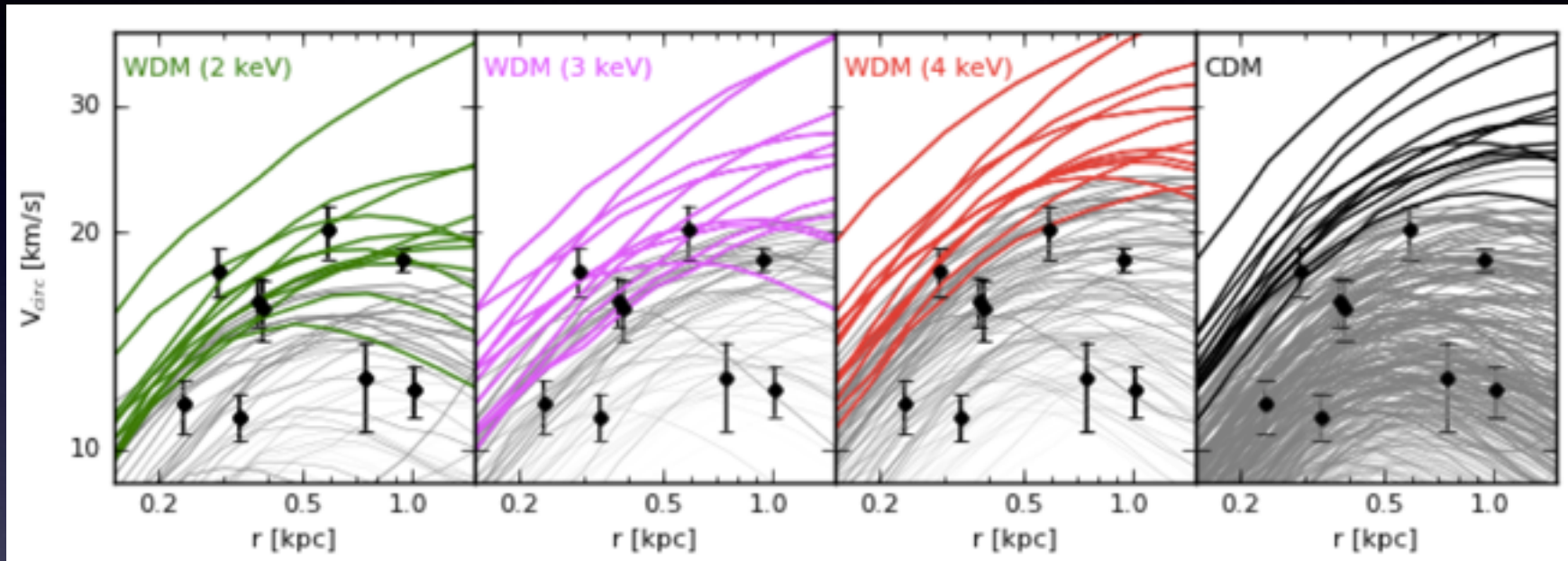
Anderhalden et al. JCAP 2013

some WDM or mixed C+WDM models do solve the problem (Lovell+2011, Anderhalden+2013)

some SIDM models also solve the problem (Vogelsberger+2012, Rocha+2013, Peter+2013)

the “too big to fail” problem (Boylan-Kolchin, Bullock, Kaplinhat, 2011/2012)

Unfortunately WDM models which solve the problem are in tension with the new Lyman- α constraint $m > 3.3$ keV (Viel+2013):



Warm dark matter does not do better than cold dark matter in solving small-scale inconsistencies

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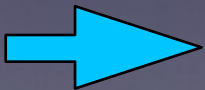
³Max Planck Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany

MNRAS, 2014, see also Polisensky & Ricotti 2014

summary of WDM and C+WDM results

- small scale problems in CDM: cusp/core, missing satellites, too big to fail
- plausible baryonic solutions within CDM exist for the first two
- too big to fail is difficult to resolve with baryonic effects (Garrison-Kimmel+2013)
- WDM cannot solve the cusp/core problem, some SIDM models can
- some WDM, C+WDM and SIDM model can resolve the too big to fail problem
- however, such WDM models are in tension with Lyman- α (Viel+2013)

(which C+WDM and SIDM are still allowed?)



DM distribution quite close to CDM predictions
on all scales probed by the baryons

- still allowed WDM has a similar cutoff scale for baryons and DM structures, which would be quite a coincidence