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Some authoritative literature about the lecture :

- BaBar physics book: <http://www.slac.stanford.edu/pubs/slacreports/slac-r-504.html>
- LHCb performance TDR: <http://cdsweb.cern.ch/record/630827?ln=en>
- A. Höcker and Z. Ligeti: CP Violation and the CKM Matrix. hep-ph/0605217
- The Belle II Physics TDR.

World Averages and Global Fits:

- Heavy Flavour Averaging Group: <http://www.slac.stanford.edu/xorg/hfag/>
- CKMfitter: <http://ckmfitter.in2p3.fr/>
- UTFit: <http://www.utfit.org/>



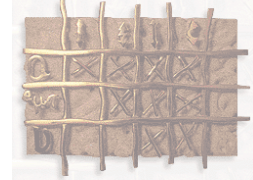
## Motivations for a two-fold approach

- I will discuss Flavour Physics and  $CP$  violation in this lecture.
- Flavours are the tag (quantum number) that you put on elementary particles, *e.g.* the  $b$  quark has the beautiful flavour.
- Electromagnetism and strong interaction are flavour-blind. Charged weak interaction breaks flavour (up / down isospin). Up and Down particles, respectively, differ only by their mass. We'll focus on the heavy elements.
- Flavour Physics is a way to study the electroweak symmetry breaking, complementary to the Higgs boson decays and properties. I hence will spend a couple of slides with a reminder of the Standard Model (SM), by the prism of its free parameters (**introduction part of the lecture**).



## Motivations for a two-fold approach

- After electroweak spontaneous symmetry brought by the scalar isospin doublet field  $\rightarrow$  the mass matrix of the quarks is defined and the couplings of flavoured fermions are characterised by the Yukawa couplings.
- After the diagonalisation the fermion mass matrix, **the mass mixing matrix** arises and shapes the couplings of the **weak charged currents**.
- $CP$  symmetry breaking is at the heart of the understanding of this mass mixing matrix (**first part of the lecture**).
- It does not saturate the interest of Flavour Physics. Several anomalies deserve comments (**second part of the lecture**). In particular rare decays of heavy-flavoured particles might be a portal to Beyond SM.



## Disclaimers

- This is an experimentalist point of view on a subject which is all about entanglements between experiment and theory.
- I won't discuss  $CP$  violation in the lepton sector nor light flavours decays and properties.
- 
- I won't have time to discuss the main machines and experiments (having been) harvesting Flavour observables. Links are provided instead.
- Most of the materials concerning global tests of the CKM matrix SM are taken from the CKMfitter group results (assumed bias) and Heavy Flavour Averaging Group (and hence the experiments themselves). I borrowed materials in presentations from colleagues which I tried to cite correctly. There are much more materials than can be covered in an hour. I append in this lectures links to more complete lectures, in case you'd like to dig further the subjects.





## Lecture's Outline

- **Part 0:** the Standard Model (SM) of particle Physics in a glance (from its free parameters).
- **Part I:**  $CP$  violation and the Cabibbo-Kobayashi-Maskawa (CKM) matrix.
- **Part II:** rare decays of heavy-flavoured particles.
- **Conclusion and Outlook:** the precision era of Flavour Physics starts.

# Introduction: SM in a glance



The free parameters of the SM:

- $SU(2)_L \otimes U(1)_Y$  unification:
  - the weak and electromagnetic coupling constants  $G_F/g_W$  and  $\alpha_{EM}$ .
- After the spontaneous breaking of the symmetry:
  - The nine masses of the fermions:  $m_f$ .
  - The masses of the electroweak gauge bosons:  $m_Z$  and  $m_W$ .
  - The scalar sector parameters:  
 $v$  (the v.e.v) and  $m_H$ .

# Introduction: SM in a glance

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## The free parameters of the SM

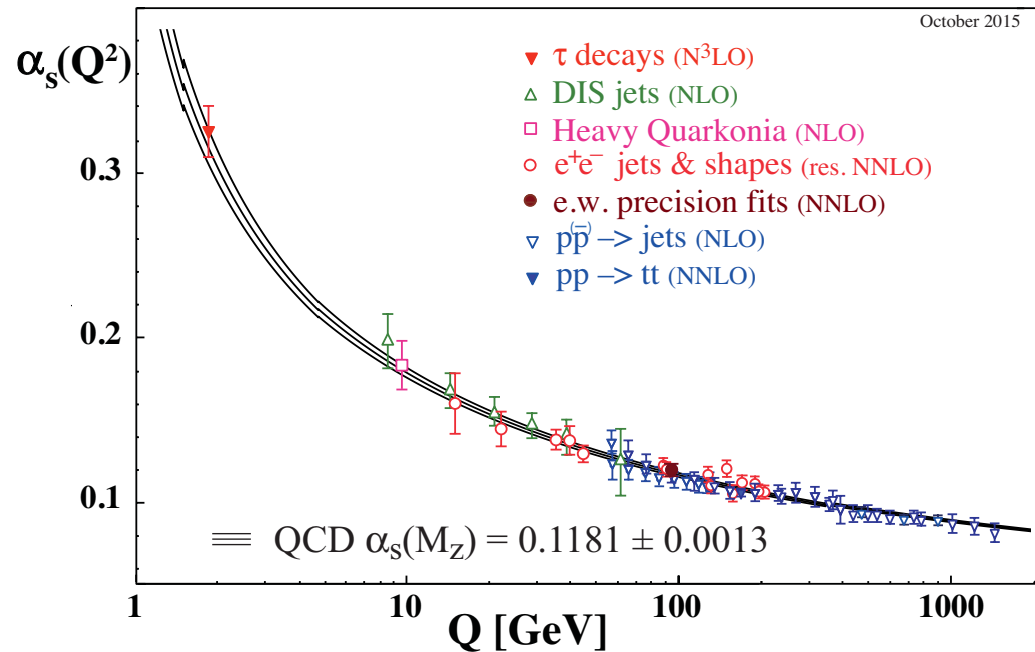
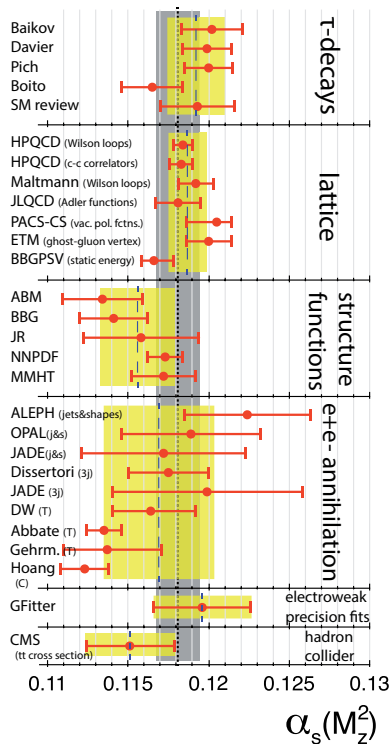
- The CKM matrix elements : it's a 3X3 complex and unitary matrix and hence can be described by means of only **4 independent parameters**. As the masses of the fermions (except for the top quark), these 4 parameters are decoupled from the rest of the theory.
- If you like QCD in (and you do), just add  $\alpha_s$  (and  $\theta_{CP}^S$  ).
- Neutrino oscillations are implying neutrinos to be massive and to mix  $\rightarrow$  7 parameters to minimally describe them.
- The number of parameters amounts to 20 (28 w/ neutrinos and strong CP). Not all of them are independent though.
- I will reorganise in the next slides the parameters and provide what we know about them.

# Introduction: SM became a theory



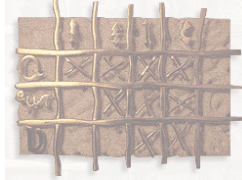
## Reorganisation:

- QCD and  $\alpha_s$ : LEP and others did great already. Limitation of the consistency test is not yet fully on the theory side for most of the determinations.



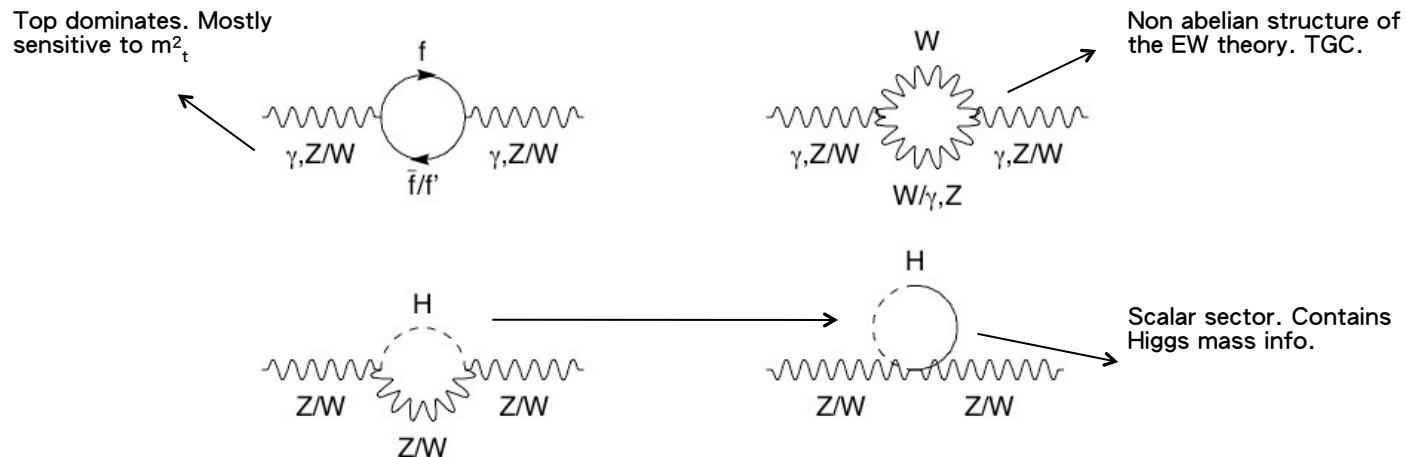
- A better  $\alpha_s$  determination is desirable, and in order for advanced predictions (QCD x-sections, Higgs decays, top mass,  $Z$  width,  $R_b$ ,  $R_l$ ).

# Introduction: SM became a theory

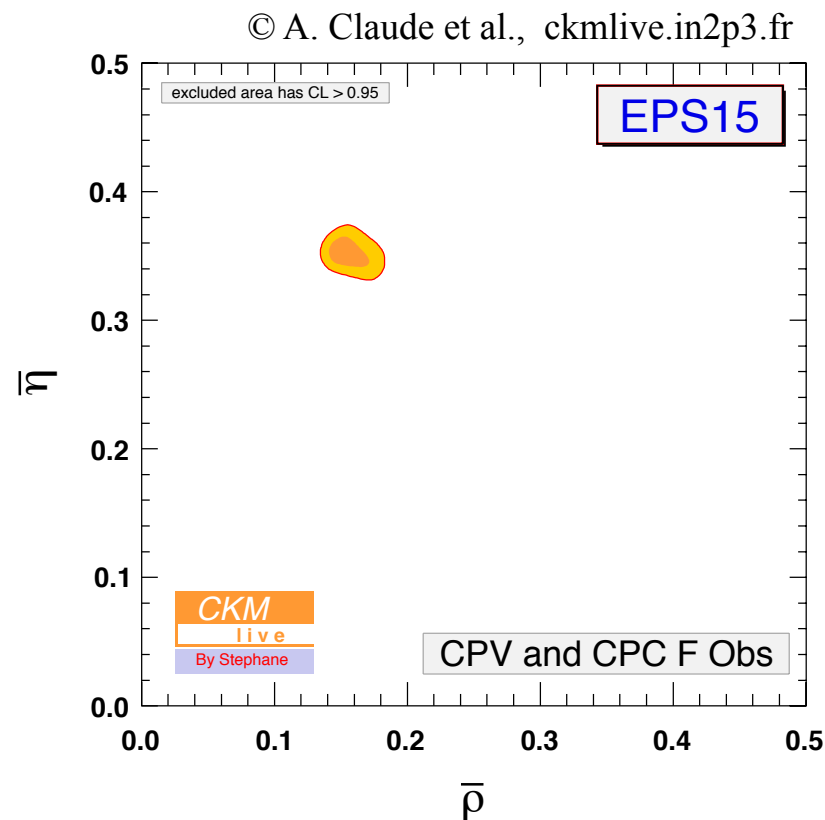


## Reorganisation:

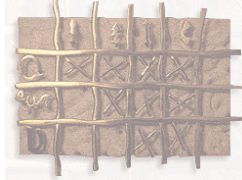
- The nine masses of the fermions:  $m_f$ .
- They are for 8 of them decoupled from the rest of the SM parameters.
- Nothing much to do here as well till the moment a theory comes with a prediction.
- The top quark has a specific status because it enters dominantly in the radiative corrections of the intermediate bosons mass propagators (in particular), *e.g.*



- The (4) CKM matrix elements (decoupled from the rest of the theory). The consistency check of the SM hypothesis in that sector is a pillar of the SM:

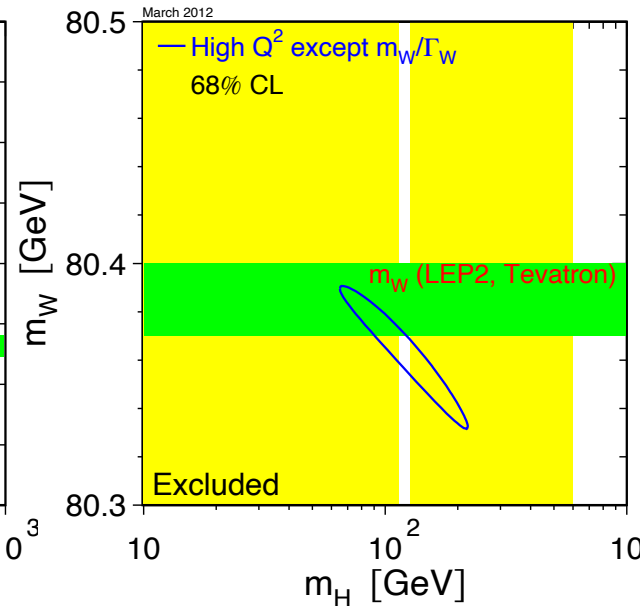
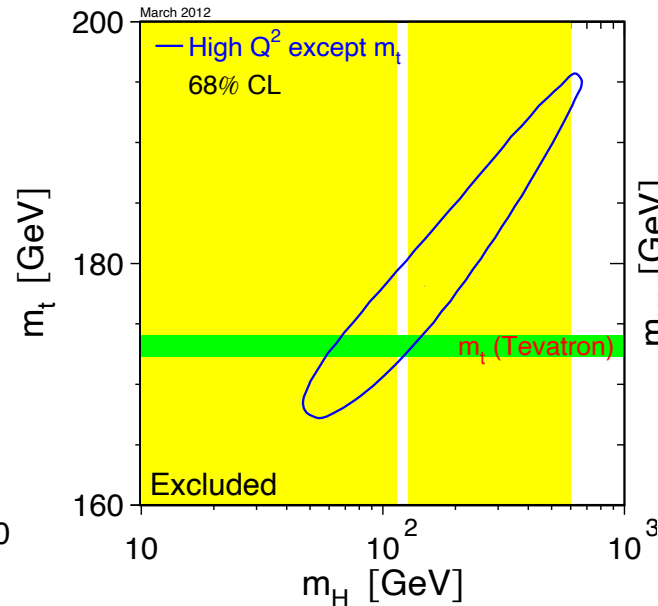
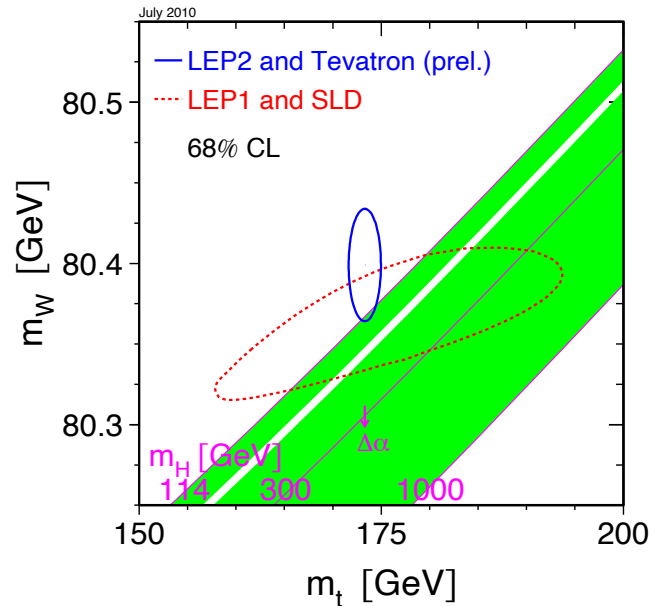


# Introduction: SM became a theory



## Reorganisation:

- The rest of the free parameters are part of the so-called electroweak precision observables consistency check. This is the other pillar of the SM. Fix  $G_F$ ,  $\alpha_{EM}$  and  $m_Z$  at their measured value and produce a prediction of  $m_{top}$ ,  $m_W$  and  $m_H$ . A tremendous success !

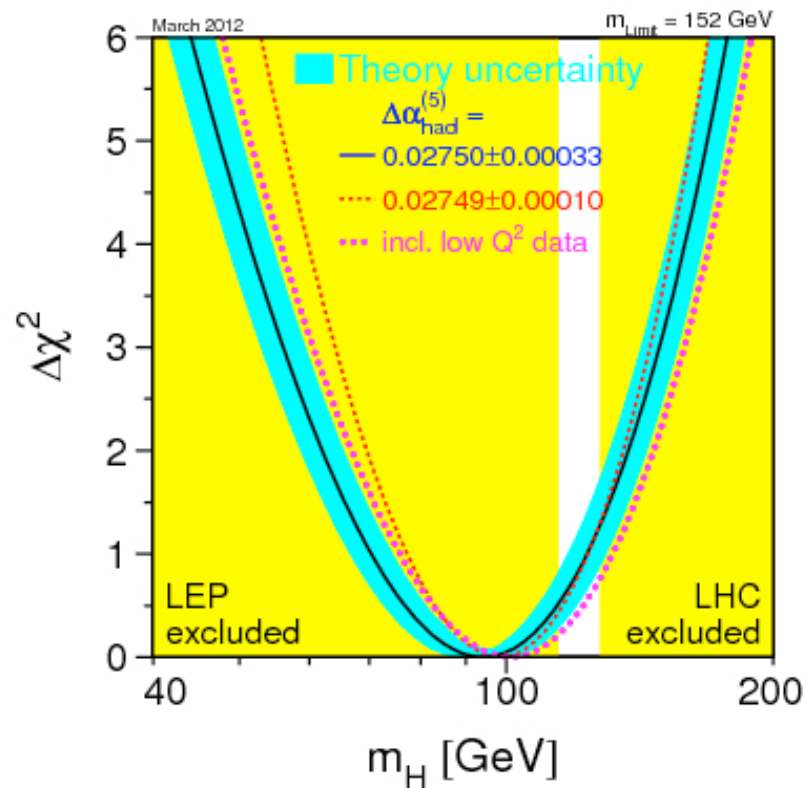
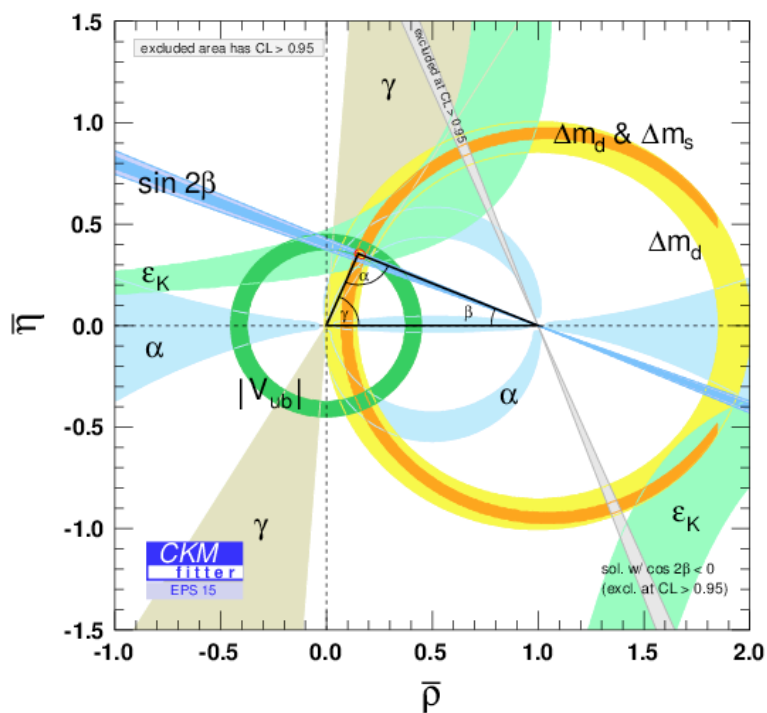


# Introduction: SM became a theory



Recap:

- Two pillars: EWPT and Flavours.



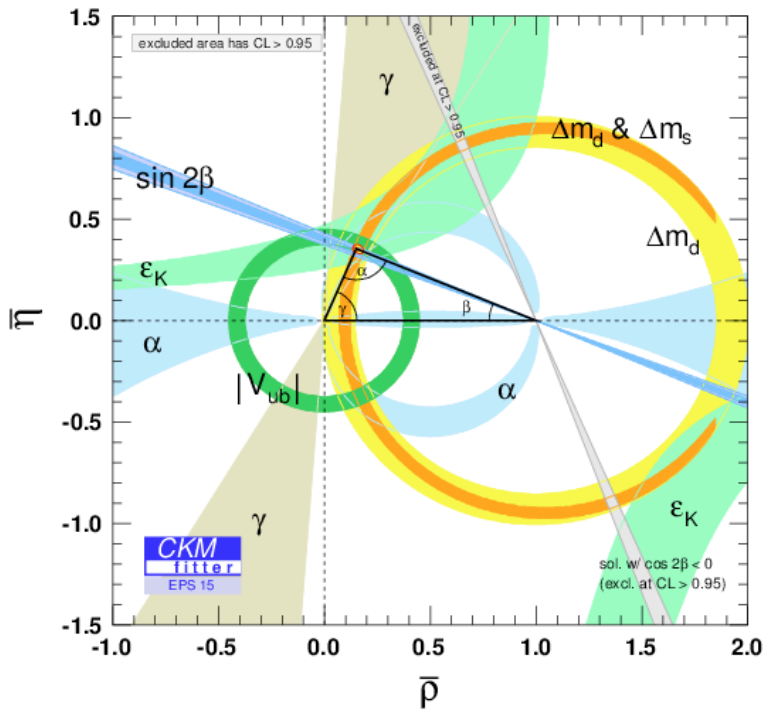


# Introduction: SM became a theory



Recap:

- Two pillars: EWPT and Flavours.

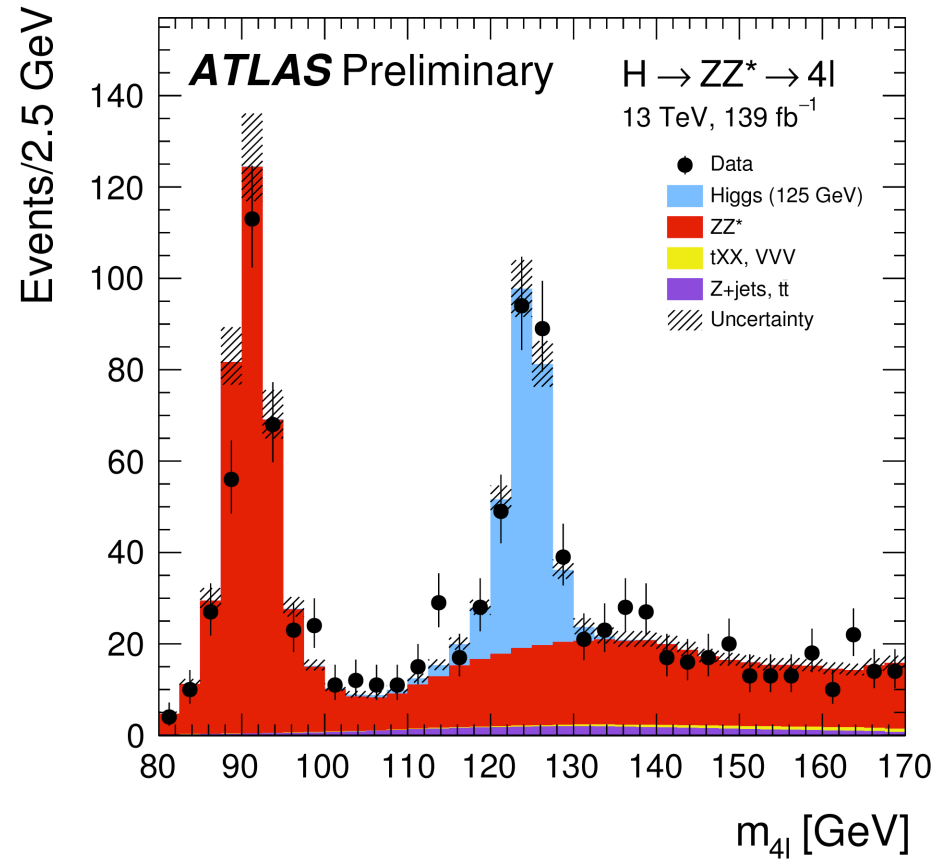
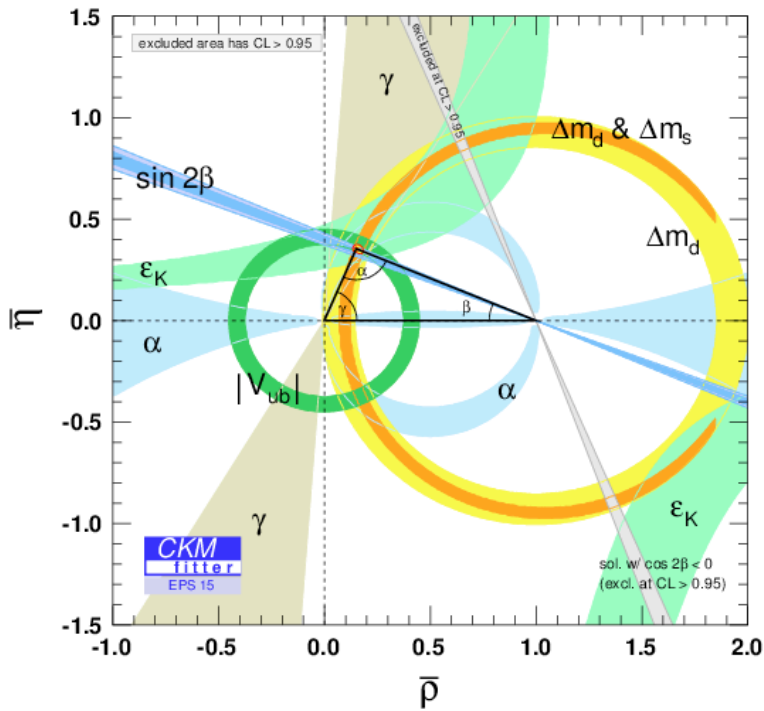


# Introduction: SM became a theory



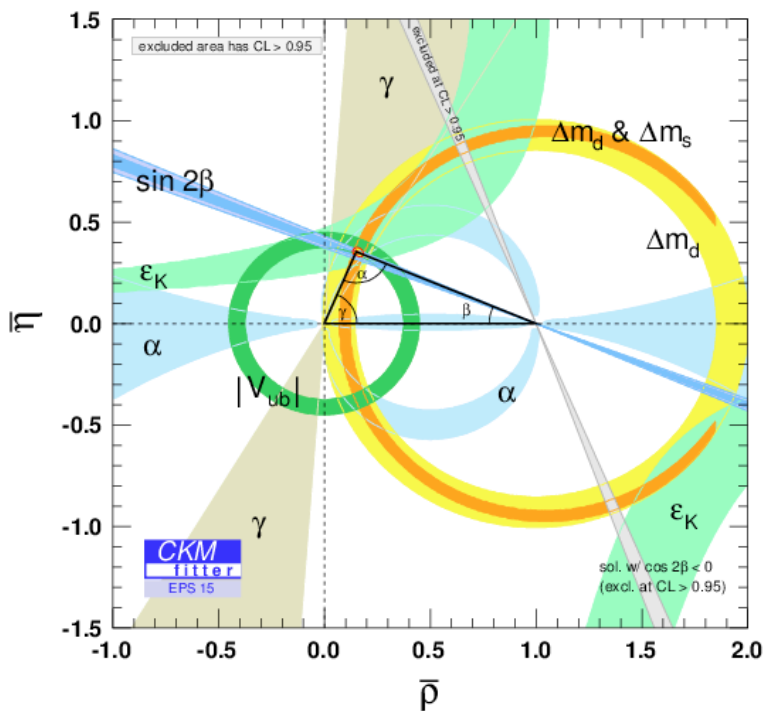
Recap:

- Two pillars: EWPT and Flavours.

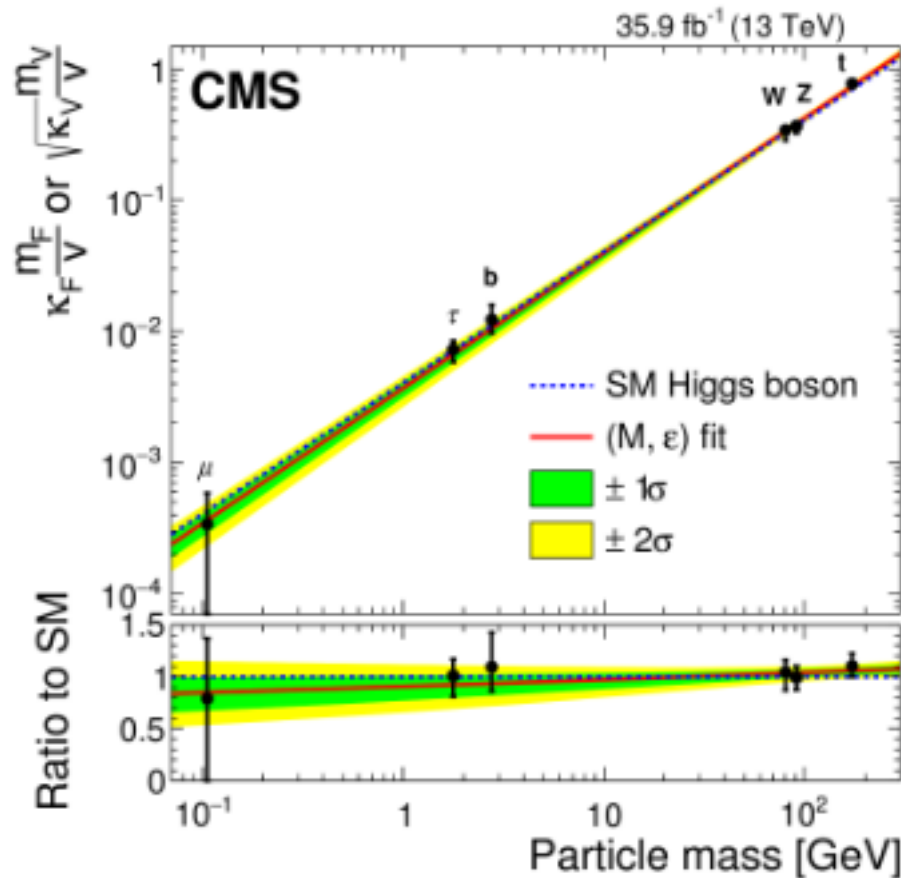


## Recap:

- Two pillars: EWPT and Flavours



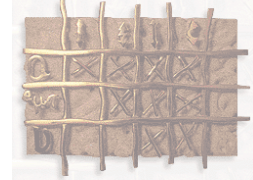
## Mass mixing matrix



## Mass matrix

# Introduction: *SM became a theory*

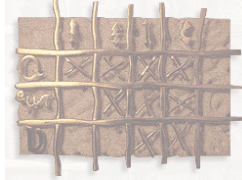
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## Lessons

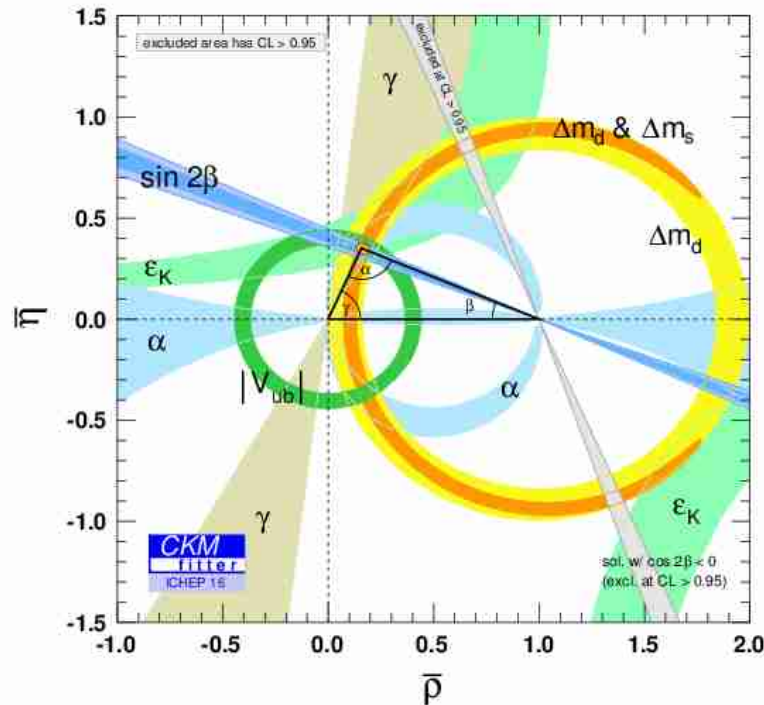
- The SM has cleared so far the attacks from LEP, TeVatron, *B*-factories, LHC and single-observables experiments. A set of anomalies though nowadays.
- There are compelling beauty arguments for Beyond Standard Model (BSM) Physics. I will overlook them.
- Instead, three indisputable measurements/observations are crying for BSM:
  - The neutrinos have a mass. Though several ways exist theoretically, it's tempting / natural to enhance the neutral particle content with right-handed states.
  - Dark matter: a nice (recent-ish) evidence for cosmological dark matter is the observation of a low surface brightness galaxy [ArXiv:1606.06291].
  - Baryonic asymmetry in the Universe is (to date) not described by SM.

# Part I — $CP$ symmetry breaking and CKM matrix



## Motivation

- In any HEP physics conference summary talk, you will find this plot, stating that (heavy) flavours and  $CP$  violation physics is a pillar of the Standard Model.

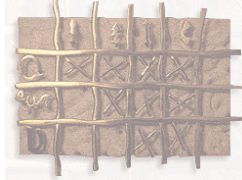


- One objective of this lecture is to undress this plot.



## A more detailed outline

1. Foundations: setting the scene, the discovery of the  $P$  and  $CP$  violation.
2. Few elements about CKM. Machine and experiments. Main observables and measurements relevant to study  $CP$  violation.
3. The global fit of the SM: CKM profile.

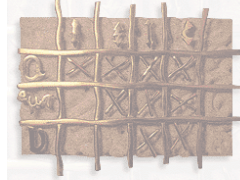


## **Why $P$ must be a good symmetry**

If a variable describing a physical system is not an observable,

one can always find a mathematical transformation which lets the physical system invariant.

An observable is conserved.



## Why $P$ must be a good symmetry

Non-observable	Mathematical transf.	Conserved quantity
Absolute spatial position	Space translation	Momentum
Absolute time	Time translation	Energy
Absolute space direction	Rotation	Angular momentum
Absolute right	Space reflexion (mirror)	Parity
Electric charge sign	$e \rightarrow -e$	Charge conjugation
Absolute time sign	$t \rightarrow -t$	Time reversal
Relative phase between electric charges	Gauge transformation	The electric charge

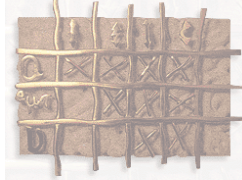




## Evidence for $P$ violation

- ✓ Before 1956 : all interactions were thought to be invariant under parity operation
- ✓ It was (quite comprehensively) tested for strong and electromagnetic interactions.
- ✓ Lee and Yang proposed an experiment to test it for weak interaction after the theta / tau puzzle.
- ✓ Designed and performed in 1956 by C.S. Wu and collaborators
- ✓ The  $\text{Co}^{60}$  experiment : *Phys. Rev.* 105, 1413-1414 (1957)





## Evidence for $P$ violation

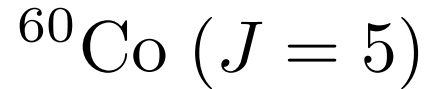
The magnetic field is directed to the right. The spins are aligned along to it.





## Evidence for $P$ violation

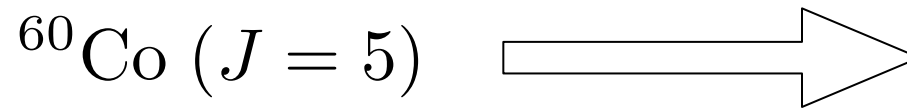
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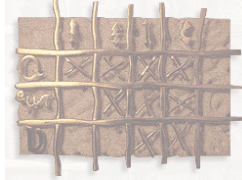




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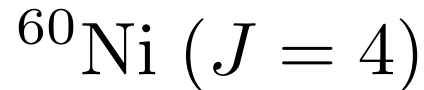
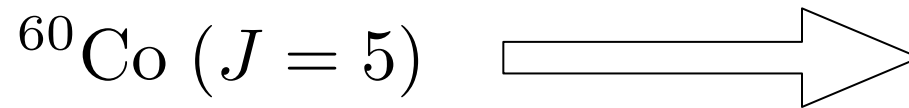
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## Evidence for $P$ violation

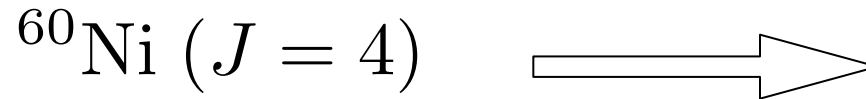
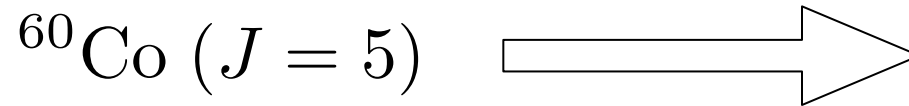
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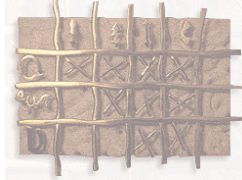




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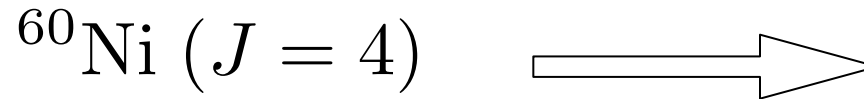
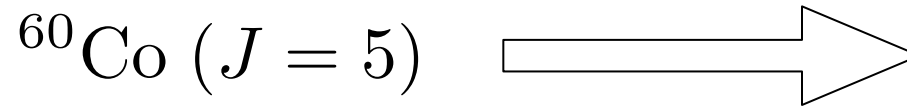
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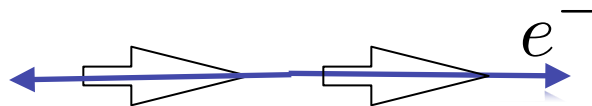
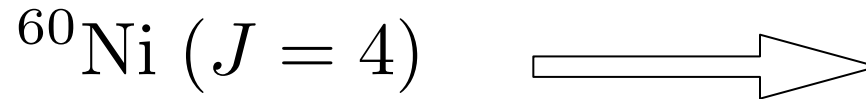
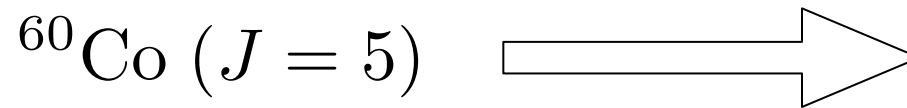
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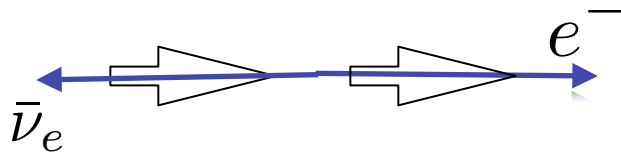
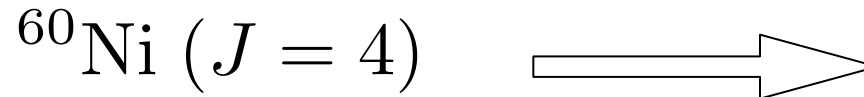
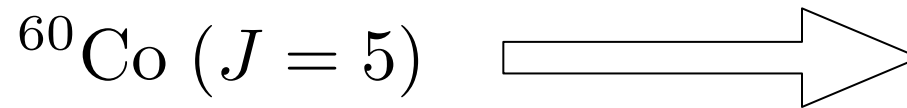


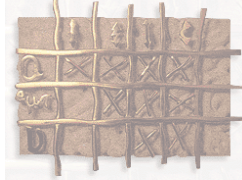




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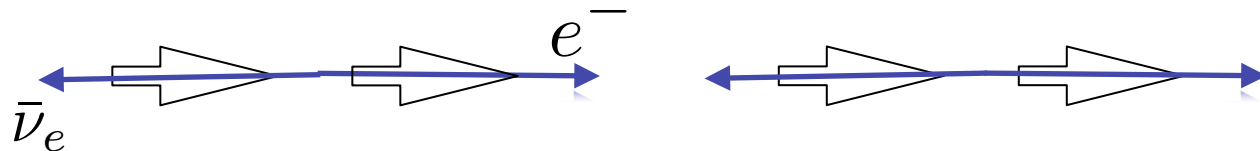
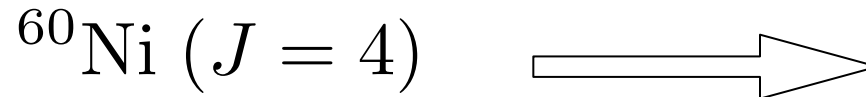
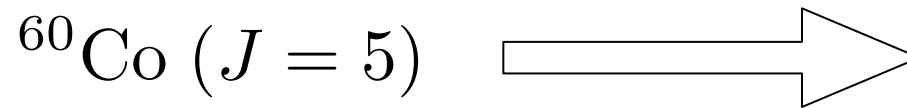
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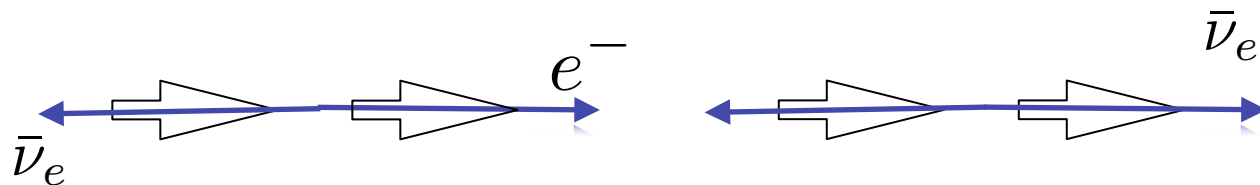
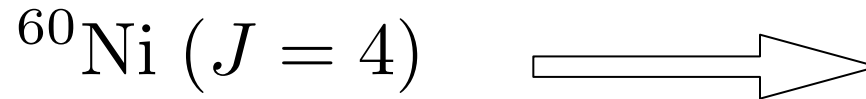
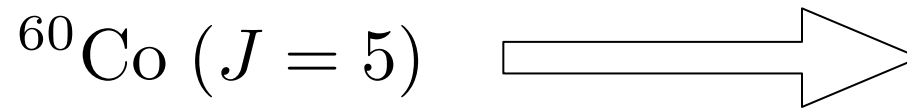
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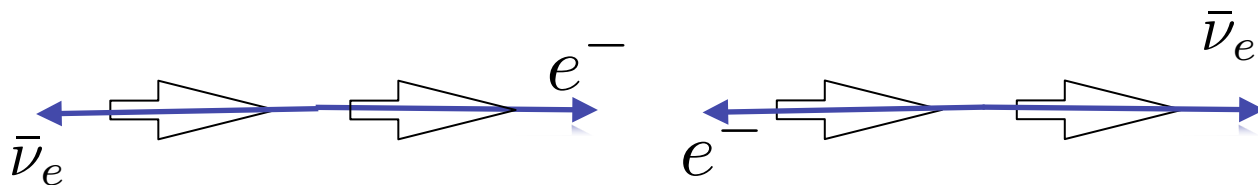
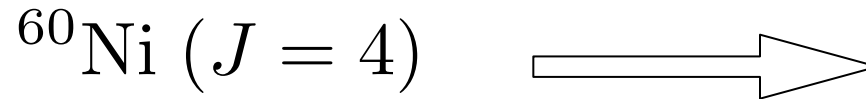
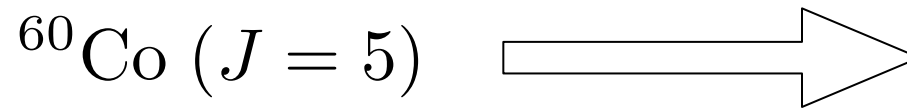
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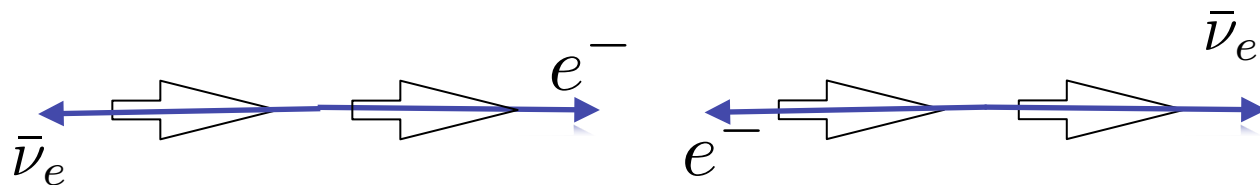
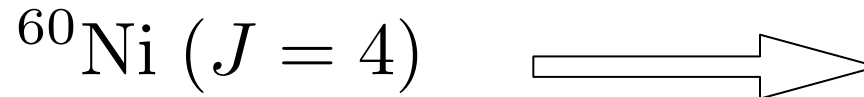
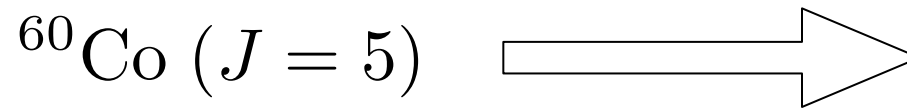
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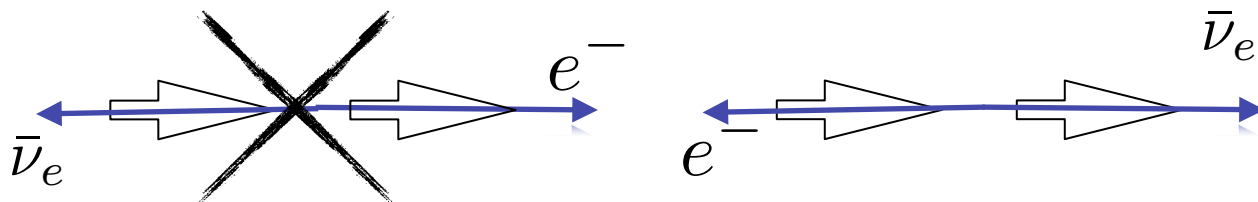
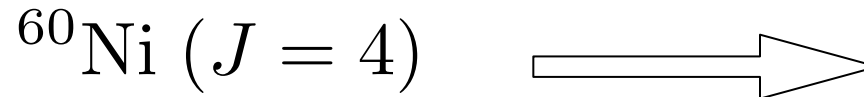
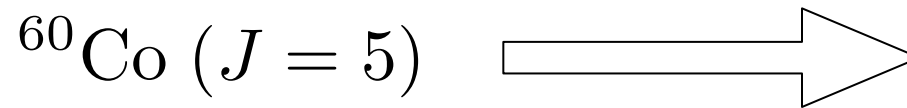


If the Nature can't distinguish left from right, then both decays are possible.



## Evidence for $P$ violation

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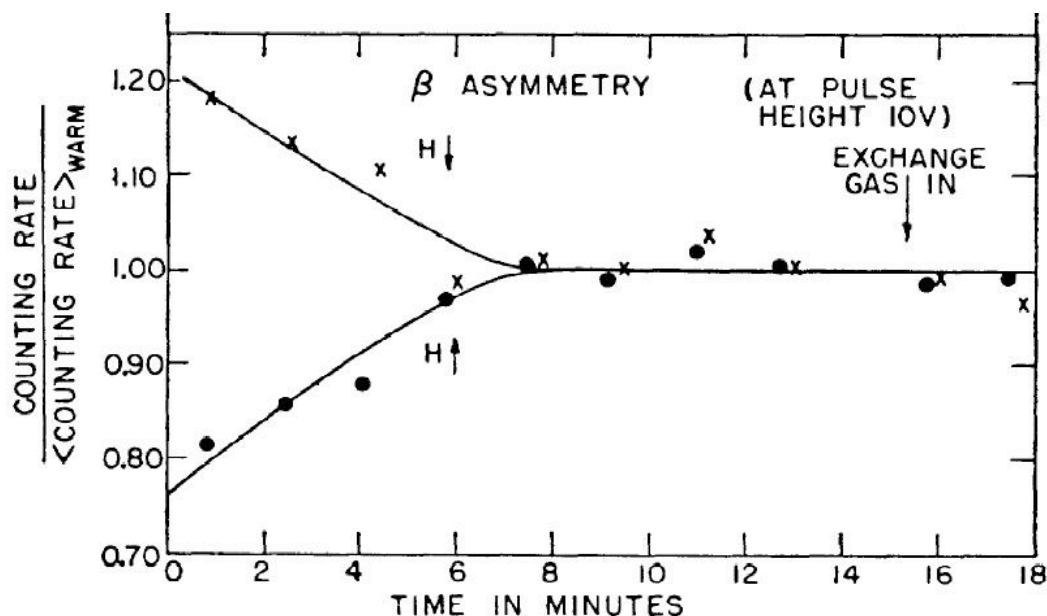


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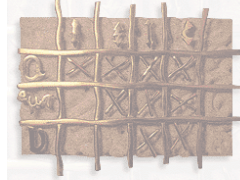
## Evidence for $P$ violation

- The magnetic field direction is changed and the rate for the electrons emission is measured in the two configurations. The asymmetry is reversed.



- The preferred chiral state is a right-handed anti-neutrino (left-handed electron).

# Foundations: parity symmetry breaking



## Evidence for $P$ violation

- The experiment was conducted during Christmas holidays 1956.
- The paper is published rightafter (2.5 pages).
- Lee and Yang receives the Nobel Prize in 1957 (sounds like this evidence was not overlooked).
- Further experiments established that  $P$  and  $C$  are maximally violated in weak charged current. This brings  $SU(2)_L$  the right symmetry of the weak interactions.

### Experimental Test of Parity Conservation in Beta Decay\*

C. S. Wu, *Columbia University, New York, New York*

AND

E. AMBLER, R. W. HAYWARD, D. D. HOPPE, AND R. P. HUDSON,  
*National Bureau of Standards, Washington, D. C.*

(Received January 15, 1957)

IN a recent paper<sup>1</sup> on the question of parity in weak interactions, Lee and Yang critically surveyed the experimental information concerning this question and reached the conclusion that there is no existing evidence either to support or to refute parity conservation in weak interactions. They proposed a number of experiments on beta decays and hyperon and meson decays which would

provide necessary evidence for parity conservation. In beta decay, one could measure the distribution of the electrons coming from polarized nuclei. If an asymmetry in the distribution between  $\theta$  and  $180^\circ - \theta$  (where  $\theta$  is the angle of orientation of the parent nuclei and the direction of the electrons) is observed, it provides proof that parity is not conserved in beta decay. An asymmetry effect has been observed in the decay of  $^{60}\text{Co}$ .

It is known for some time that  $^{60}\text{Co}$  nuclei can be polarized by the Rose-Gorter method in cerium (III) nitrate, and the degree of polarization can be measured by measuring the anisotropy of the gamma rays.<sup>2</sup> To apply this technique to the study of beta decay, two major difficulties had to be over-

### The Nobel Prize in Physics 1957



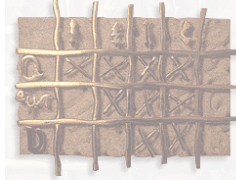
Chen Ning Yang  
Prize share: 1/2



Tsung-Dao (T.D.) Lee  
Prize share: 1/2

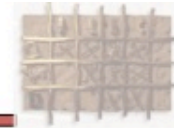
The Nobel Prize in Physics 1957 was awarded jointly to Chen Ning Yang and Tsung-Dao (T.D.) Lee "for their penetrating investigation of the so-called parity laws which has led to important discoveries regarding the elementary particles"





## Modern parity violation experiments: LEP

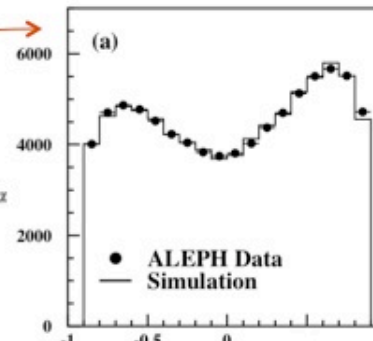
### The Standard Model Tests (Part II)



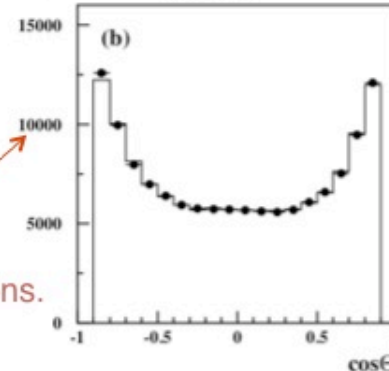
#### 3.3 The Parity-Violating forward-backward asymmetries in $e^+e^-$ .

- Then we fit the asymmetries to these data:

$$\begin{aligned}
 f_{ijkl} = & (F_{\ell,b}^{rs})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^b (1 - 2\chi_{ijkl}) x] dx \\
 & + (F_{\ell,b}^{ws})_{ijkl} \int_{-1}^1 [1+x^2 - \frac{8}{3} A_{FB}^b (1 - 2\chi_{ijkl}) x] dx \\
 & + (F_{bkg,b}^{anym})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^b (1 - 2\chi_{ijkl}) (2\eta_{ijk}^b - 1) x] dx \\
 & + (F_{\ell,c})_{ijkl} \int_{-1}^1 (1+x^2 - \frac{8}{3} A_{FB}^c x) dx \\
 & + (F_{c \rightarrow bkg}^{anym})_{ijkl} \int_{-1}^1 [1+x^2 - \frac{8}{3} A_{FB}^c (2\eta_{ijk}^c - 1) x] dx \\
 & + (F_{s \rightarrow bkg}^{anym})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^s (2\eta_{ijk}^s - 1) x] dx \\
 & + (F_{d \rightarrow bkg}^{anym})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^d (2\eta_{ijk}^d - 1) x] dx \\
 & + (F_{u \rightarrow bkg}^{anym})_{ijkl} \int_{-1}^1 [1+x^2 - \frac{8}{3} A_{FB}^u (2\eta_{ijk}^u - 1) x] dx \\
 & + (F_{bkg}^{sym})_{ijkl} \int_{-1}^1 (1+x^2) dx,
 \end{aligned}$$



Parity violation  
even seen for  
charm.




Includes QED and QCD effects.

Measuring simultaneously the mixing parameter w/ leptons.

S.Monteil

TESchool of High Energy Physics

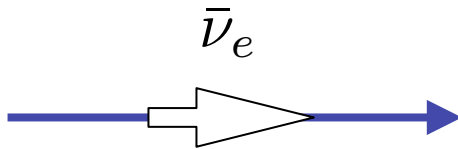
## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
  - ✓ One gets from experimental results so far the following picture:
- 
- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

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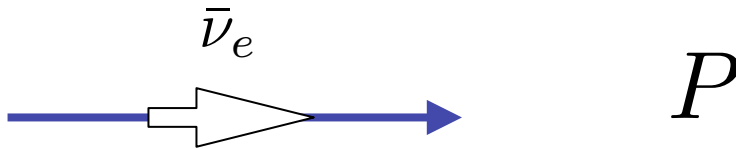


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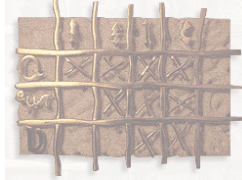


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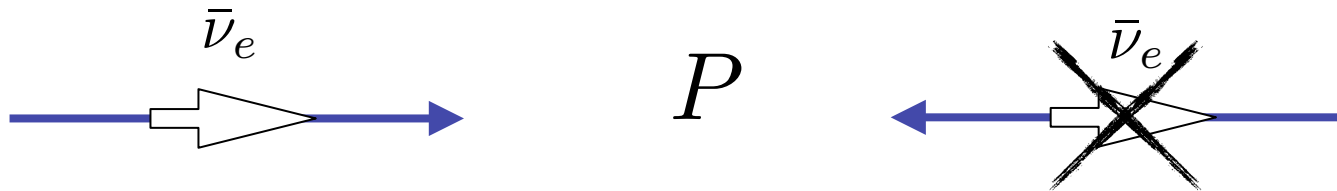


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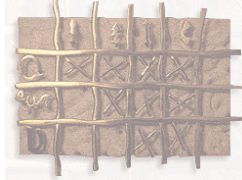


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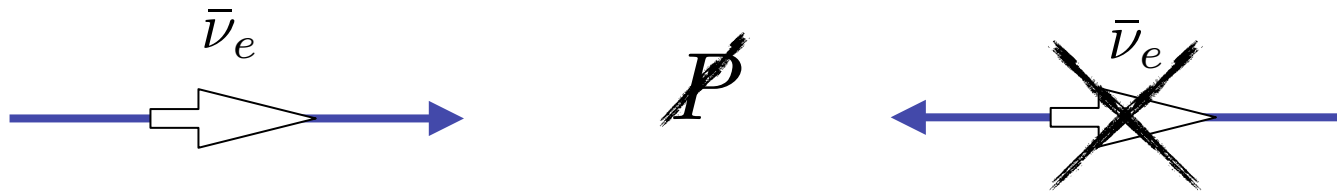


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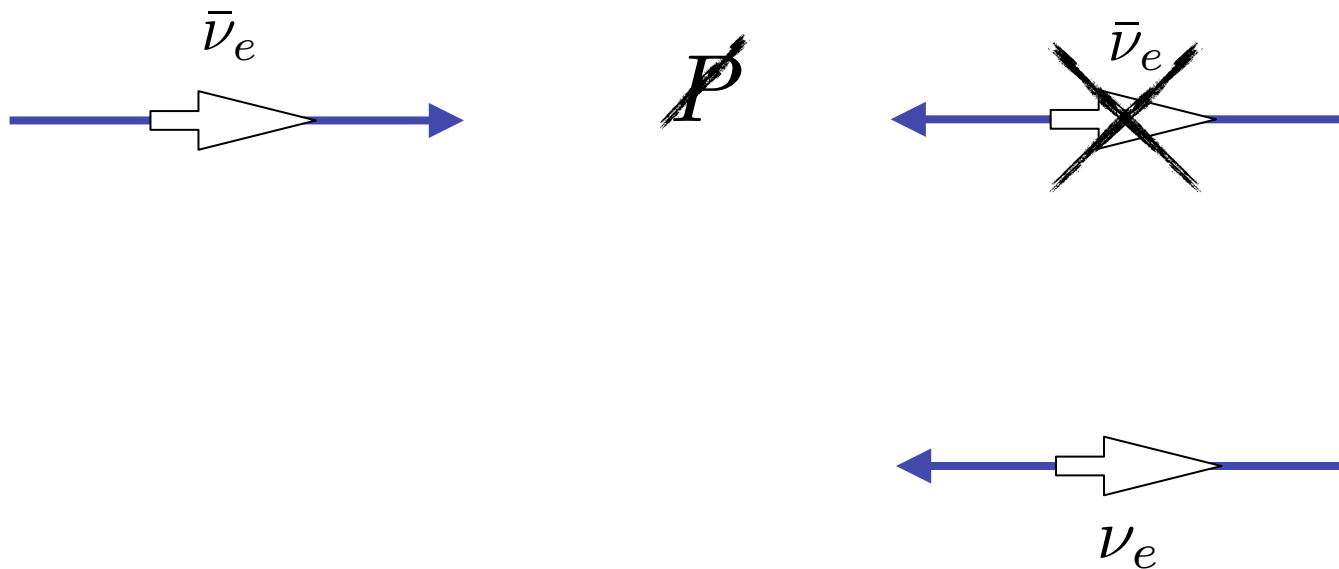


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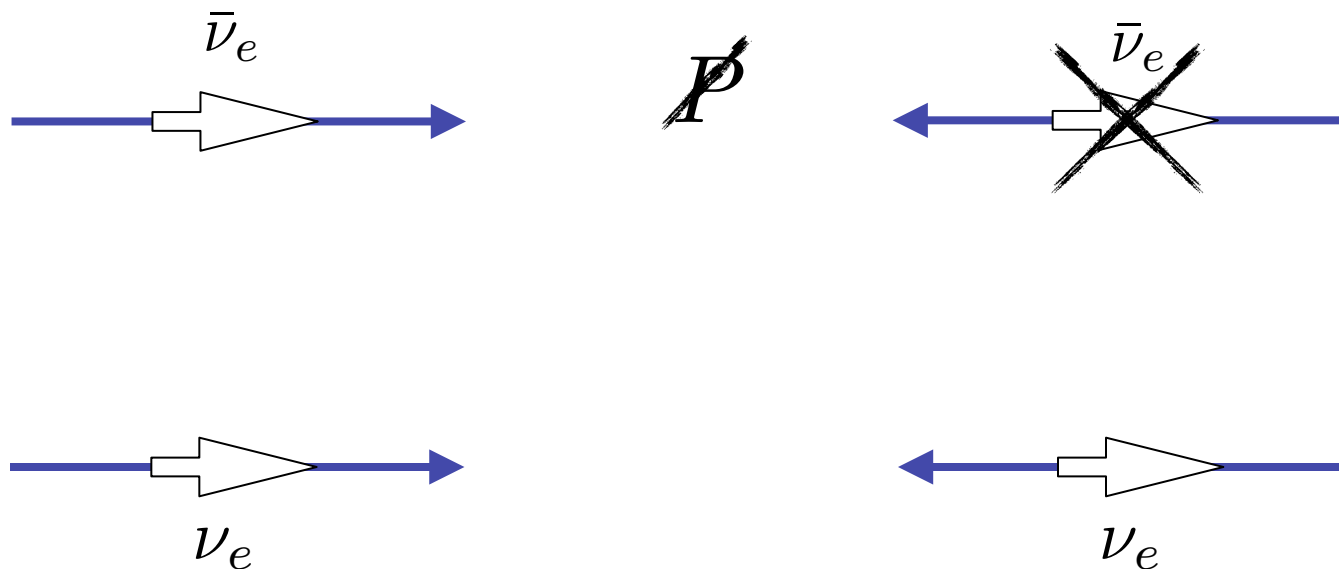
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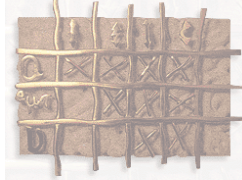


## An intermediate conclusion

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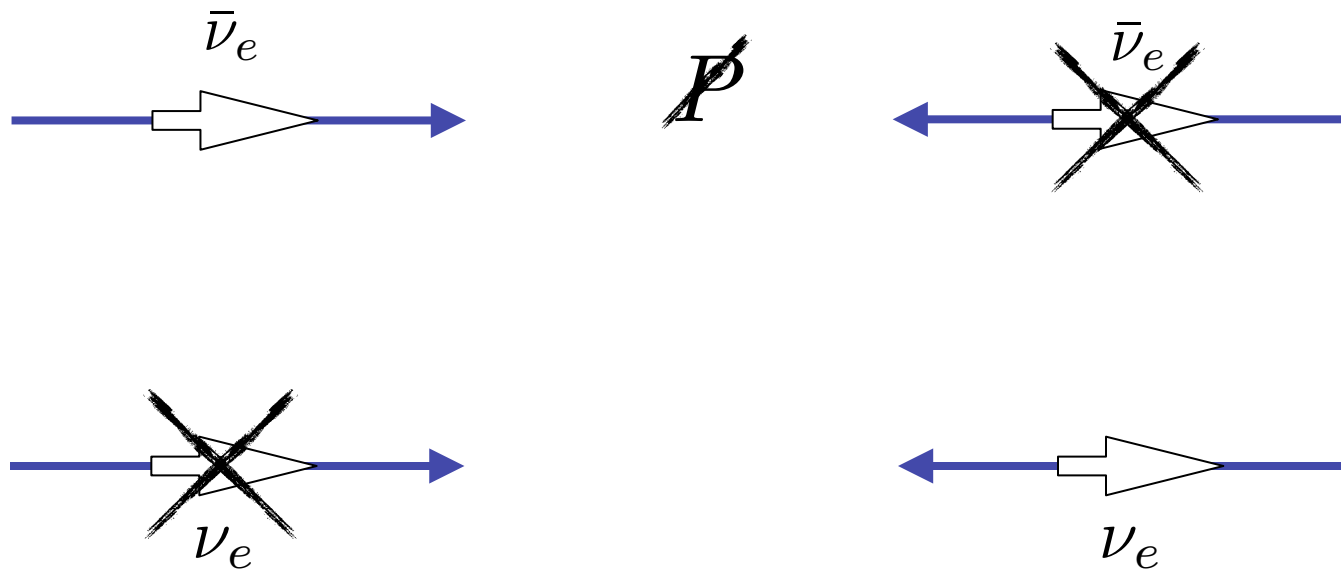


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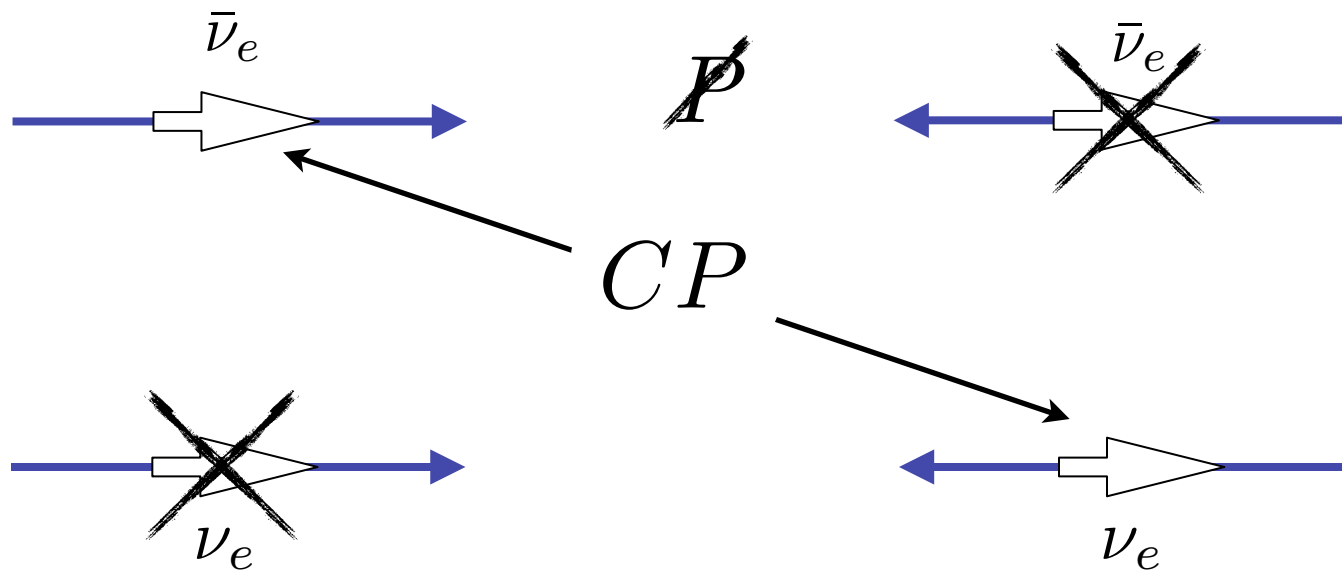


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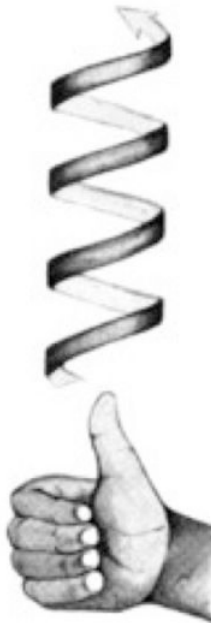


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity violation do occur elsewhere



- ✓ But those are not of fundamental nature. The right-handed DNA molecule for instance can be synthesised.



**Question: OK, parity is violated in the weak interaction. But can't we restore the left-right symmetry by considering the product  $C \times P$ ? Seems a good symmetry at least in the pion decay.**

$$\Gamma(\pi^+ \rightarrow \ell^+ \nu_\ell) = \Gamma(\pi^- \rightarrow \ell^- \bar{\nu}_\ell)$$



## Discovery of $CP$ violation.

- With simple quantum mechanics, one can show that in absence of  $CP$  violation:

$$\begin{aligned} CP|K_1\rangle &= \frac{1}{\sqrt{2}}(CP|K^0\rangle + CP|\bar{K}^0\rangle) = \frac{1}{\sqrt{2}}(|K^0\rangle + |\bar{K}^0\rangle) = +|K_1\rangle \\ CP|K_2\rangle &= \frac{1}{\sqrt{2}}(CP|K^0\rangle - CP|\bar{K}^0\rangle) = \frac{1}{\sqrt{2}}(|\bar{K}^0\rangle - |K^0\rangle) = -|K_2\rangle \end{aligned}$$

- Final states  $CP$  eigenvalues are  $+1$  ( $\pi\pi$ ) and  $-1$  ( $\pi\pi\pi$ ). If  $CP$  is a conserved quantity, one then should have:

$$\begin{aligned} K_1 &\rightarrow \pi\pi \\ K_2 &\rightarrow \pi\pi\pi. \end{aligned}$$

Which we'll identify as  $K_S^0$  and  $K_L^0$  respectively.

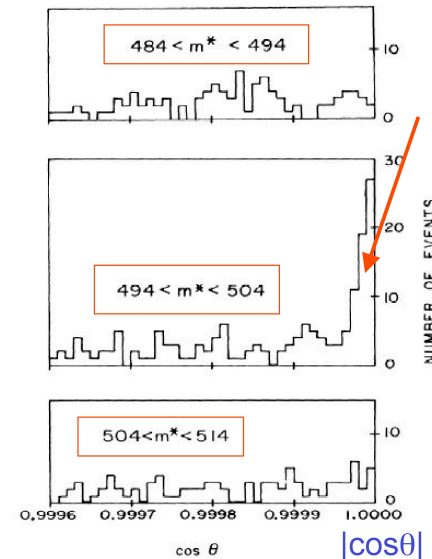
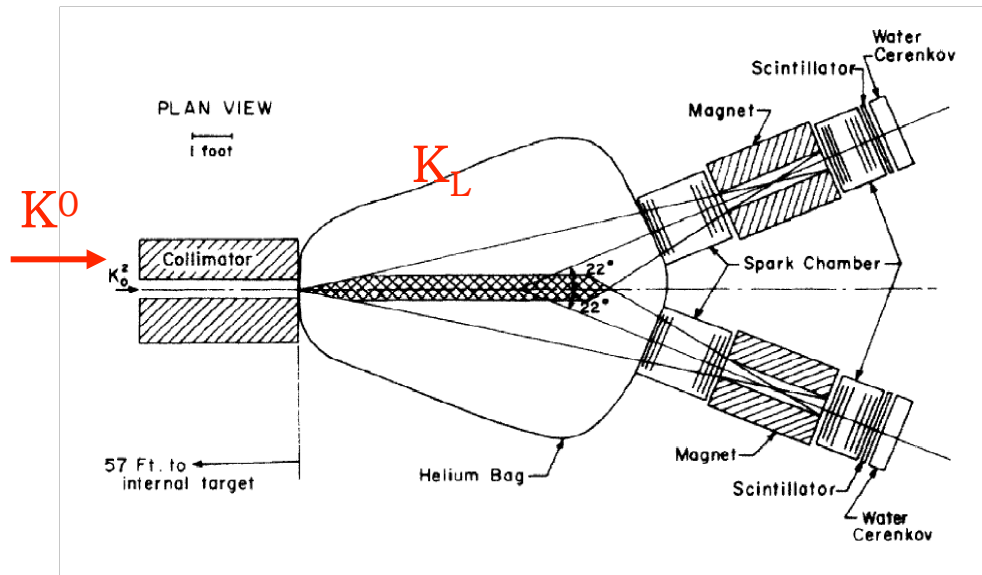
- measuring  $K_L^0$  decays into two pions ? Proof that  $CP$  symmetry is violated in weak interaction.

# Foundations: $CP$ symmetry breaking



## Discovery of $CP$ violation.

- The  $CP$  violation in kaon system: Christenson, Cronin, Fitch, Turlay. Phys. Rev. Lett. 13 (1964) 138.
- Far after the target, only the long species of  $K^0$  survive. They measured:



$$|\eta_{+-}| = \frac{A(K_L^0 \rightarrow \pi\pi)}{A(K_S^0 \rightarrow \pi\pi)} = (2.271 \pm 0.017)10^{-3}.$$



## Discovery of $CP$ violation.

Message Number 1:

The  $CP$  symmetry is violated in the mixing of neutral mesons, a pure electroweak phenomenon, e.g.

$$K^0 \longrightarrow \bar{K}^0 \neq \bar{K}^0 \longrightarrow K^0$$

1964, Brookhaven

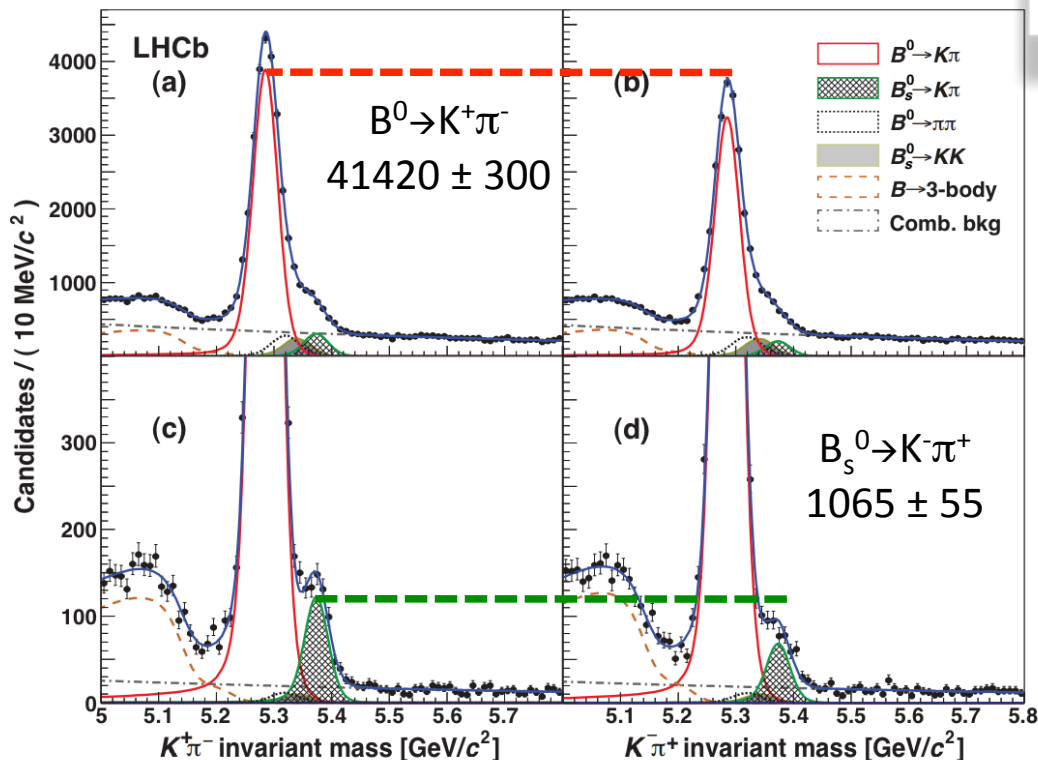




## Other discoveries of $CP$ violation.

- Compare the decay rates of self-tagged modes  $K\pi$

$$\mathcal{L} = (1/\text{fb} @ \sqrt{s} = 7 \text{ TeV})$$

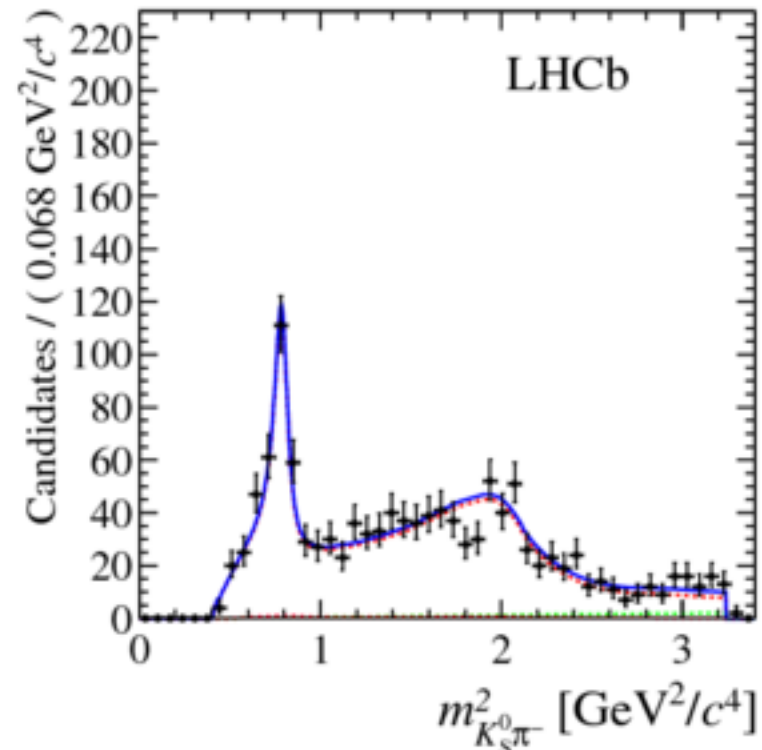
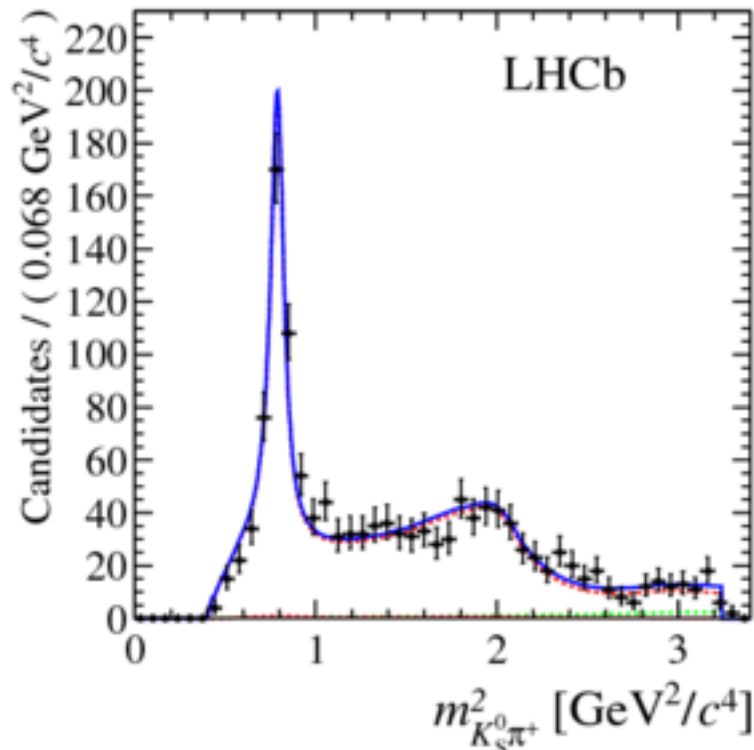


$$A_{\text{raw}}(B^0 \rightarrow K^- \pi^+) = -0.091 \pm 0.006,$$
$$A_{\text{raw}}(B_s \rightarrow K^+ \pi^-) = 0.28 \pm 0.04,$$

- Data-driven control of PID efficiencies thanks to the self-tagged mode  $D^{*+} \rightarrow D^0 (K^- \pi^+) \pi^+$
- Raw asymmetries corrected from detection asymmetry (also  $D^{*+}$  control sample).
- $B$  production asymmetry simultaneously measured from decay time distribution.



## Other discoveries of $CP$ violation.



[Phys. Rev. Lett. 120, 261801 \(2018\)](#)

$$A_{CP}(\overline{B}^0 \rightarrow K^*(892)^- \pi^+) = -0.30 \pm 0.06$$



## Other discoveries of $CP$ violation.

Message Number 2:

The  $CP$  symmetry is violated in the decay of beautiful particles, pure electroweak phenomenon, e.g.

$$B^0 \longrightarrow K^+ \pi^- \neq \bar{B}^0 \longrightarrow K^- \pi^+$$

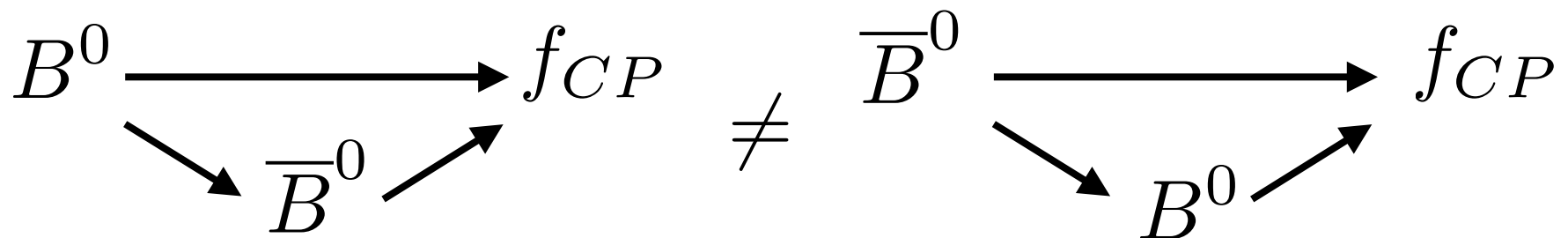
2004, B-factories



## Other discoveries of $CP$ violation.

Message Number 3:

The  $CP$  symmetry can be violated in the interplay (interference) of the two previous sources of  $CP$  violation, e.g.



2001,  $B$ -factories, will come back to that next



## Concluding this introduction

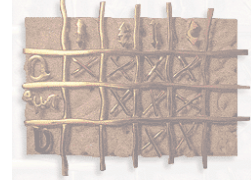
- $C$ ,  $P$  and  $CP$  are (so far) conserved in electromagnetic and strong interactions.
- $C$  and  $P$  symmetries are maximally violated by the weak interaction.
- $CP$  symmetry is slightly violated in the electroweak interaction.
- There are three ways of  $CP$  violation to manifest in the Nature so far:
  - 1) In the mixing of neutral particles (observed solely in neutral kaon mixing - 1964).
  - 2) In the decay of the beautiful and strange mesons ( $K$  and  $B_{d,s}$ , 2001 and 2004,2013 resp.).
  - 3) In the interference between decay and mixing of the beautiful particles (2001, see next chapters) .

And that's all.



## A personal comment before going to SM

- We do not have yet a (satisfactory) dynamical mechanism to explain these discrete symmetry breakings. And to my knowledge, no mathematical Physics way to do so.
- Still, what comes next is elegant.
- We'll try to make sense of the  $CP$  symmetry breaking phenomena (within the SM).



---

**The next Chapter of Part I starts at the next slide**



**The next Chapter of Part I starts at the next slide**

## **A more detailed outline**

1. Foundations: setting the scene, the discovery of the  $P$  and  $CP$  violation.
2. Few elements about CKM. Machine and experiments. Main observables and measurements relevant to study  $CP$  violation.
3. The global fit of the SM: CKM profile.





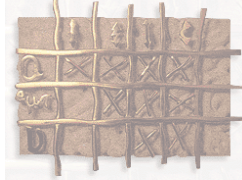
## CKM: the unitarity triangle.

- We have touched that the Higgs field gives mass to bosons (EWSB) but also fermions (quarks and leptons), through the Yukawa couplings but this is not the end of the story:

$$\mathcal{L}_{cc}^{\text{quarks}} = \frac{g}{2\sqrt{2}} W_{\mu}^{\dagger} \left[ \sum_{ij} \bar{u}_i(q_2) \gamma^{\mu} (1 - \gamma^5) V_{ij} d_j \right] + \text{h.c}$$

- After spontaneous symmetry breaking, and once the mass matrices are diagonalised, it determines also how the mass and weak eigenstates are related. This is the CKM matrix. As for the (fermion) masses, nothing is predicted except the mass matrix must be unitary and complex.

$$\begin{pmatrix} u \\ s \\ b \end{pmatrix}_{EW} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} u \\ s \\ b \end{pmatrix}_{MASS}$$



## CKM: the unitarity triangle.

- Weak eigenstates are therefore a mixture of mass eigenstates, controlled by the Cabibbo-Kobayashi-Maskawa elements  $V_{ij}$ : flavour changing charged currents between quark generations.
- This matrix is a 3X3, unitary, complex, and hence described by means of four parameters: 3 rotation angles and a phase. The latter makes possible the  $CP$  symmetry violation in the Standard Model.
- These four parameters are free parameters of the SM. As for electroweak gauge precision tests, they must be measured with some redundancy and the SM hypothesis is to be falsified by a consistency test. We will review in this lecture this overall test. But let's define first the parameters.



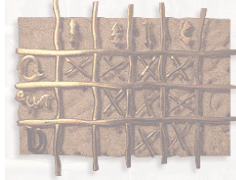
## CKM: the unitarity triangle. Parameterisation.

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Consider the Wolfenstein parametrization as in EPJ C41:1-131,2005 : unitary-exact at each order and phase- convention independent:

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}, \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad \text{and} \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}$$

- $\lambda$  is measured from  $|V_{ud}|$  and  $|V_{us}|$  in superallowed beta decays and semileptonic kaon decays, respectively.
- $A$  is further determined from  $|V_{cb}|$ , measured from semileptonic charmed  $B$  decays.
- The last two parameters are to be determined from angles and sides measurements of the CKM unitarity triangle.



## CKM: the unitarity triangle. Parameterisation.

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}, \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad \text{and} \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}$$

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4).$$

## CKM: the unitarity triangle. Representation.

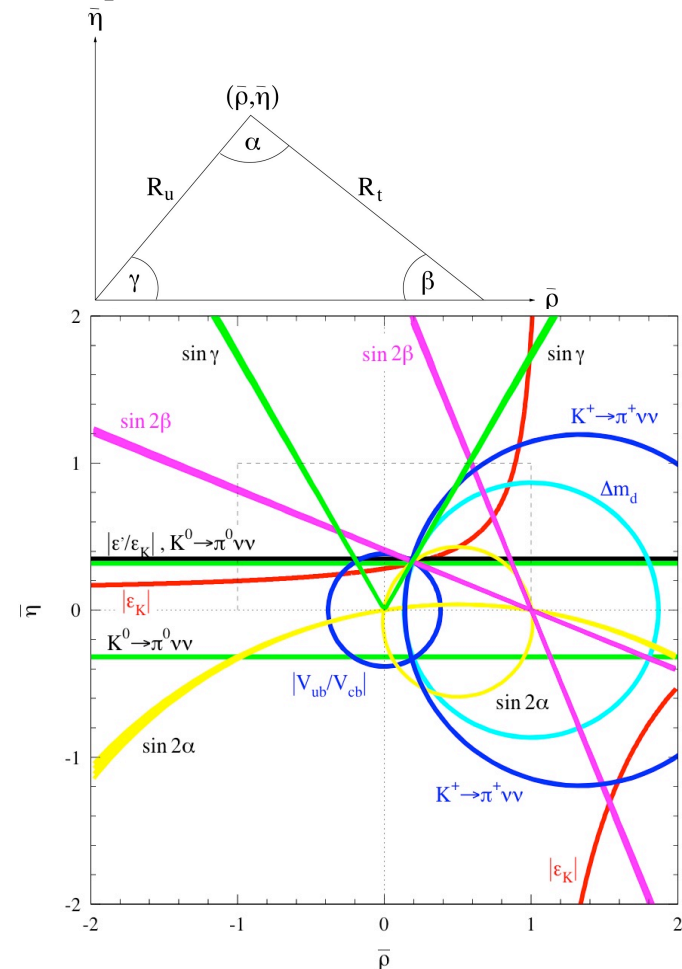
- An elegant way to represent the unitarity relations is to display them in the complex plane.

- $\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + \frac{V_{cd}V_{cb}^*}{V_{cd}V_{cb}^*} + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0.$

- The area of the triangle is half the Jarlskog invariant and measures the magnitude of the  $CP$  violation:

$$J \sum_{\sigma\gamma=1}^3 \epsilon_{\mu\nu\sigma} \epsilon_{\alpha\beta\gamma} = \text{Im}(V_{\mu\alpha} V_{\nu\beta} V_{\mu\beta}^* V_{\nu\alpha}^*) ,$$

$$J = A^2 \lambda^6 \eta (1 - \lambda^2/2) \simeq 10^{-5}$$



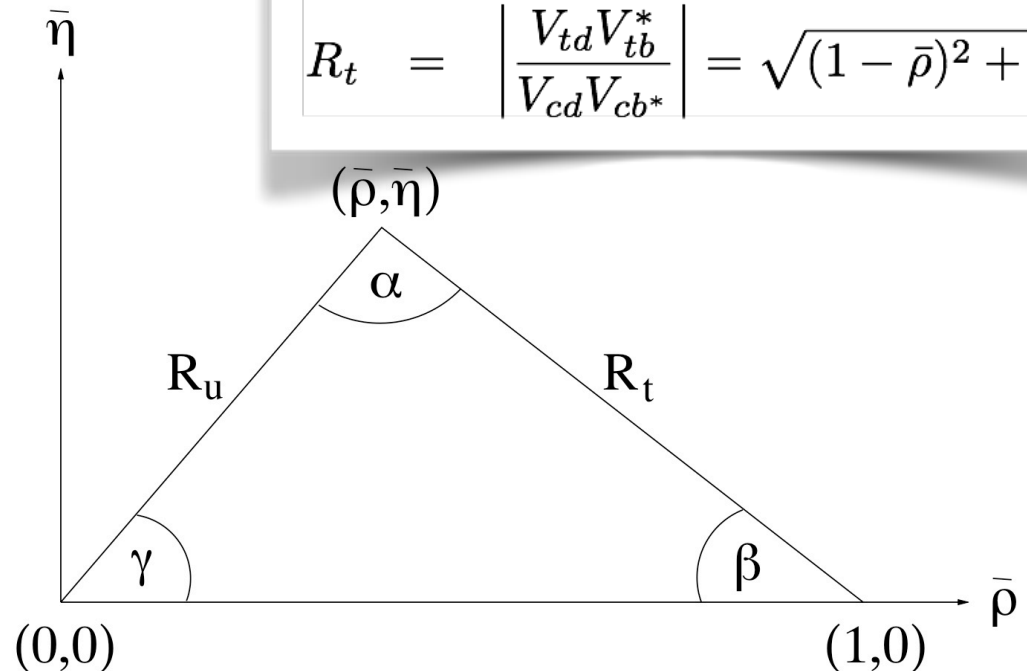


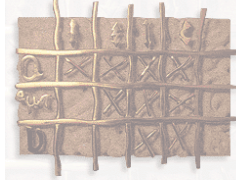
## CKM: the unitarity triangle. Definitions.

- Sides and angles of the unitarity triangle.
- Normalization given by the matrix element  $V_{cd} \cdot V_{cb}^*$ .

$$\begin{aligned}\alpha &= \arg \left( -\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right), \\ \beta &= \pi - \arg \left( \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} \right), \\ \gamma &= \arg \left( -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right).\end{aligned}$$

$$\begin{aligned}R_u &= \left| \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right| = \sqrt{\bar{\rho}^2 + \bar{\eta}^2}, \\ R_t &= \left| \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} \right| = \sqrt{(1 - \bar{\rho})^2 + \bar{\eta}^2}.\end{aligned}$$

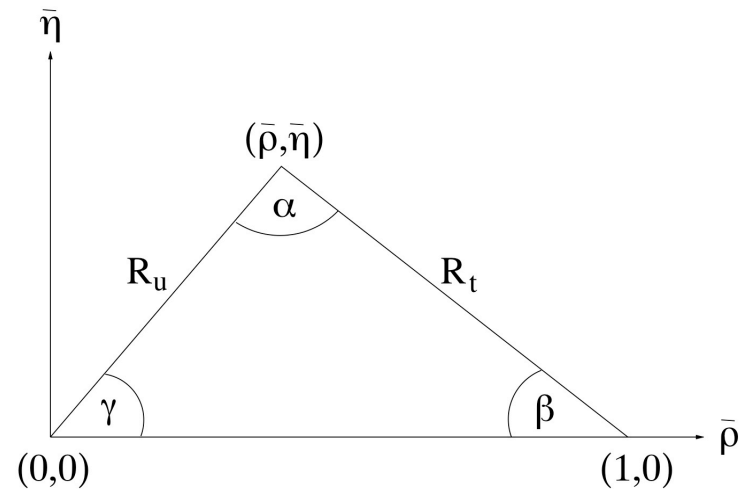




## CKM: the unitarity triangle. Definitions.

- Sides of the unitarity triangle. Towards the experimental constraints:

$$R_u = \left| \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right| = \sqrt{\bar{\rho}^2 + \bar{\eta}^2},$$
$$R_t = \left| \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} \right| = \sqrt{(1 - \bar{\rho})^2 + \bar{\eta}^2}.$$



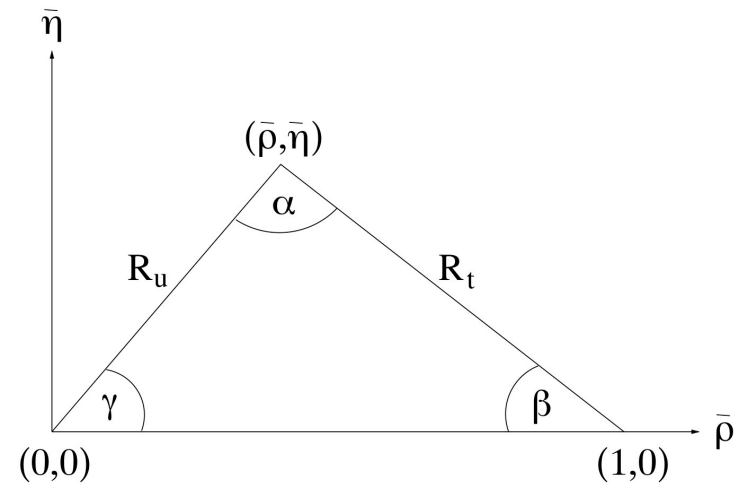
- $R_u$  is measured by the matrix elements  $V_{ub}$  and  $V_{cb}$  determined from the semileptonic decays of  $b$ -hadrons.
- $R_t$  implies the matrix element  $V_{td}$  and hence can be measured from the mixing of  $B^0$  mesons.



## CKM: the unitarity triangle. Definitions.

- Angles of the unitarity triangle. Towards the experimental constraints:

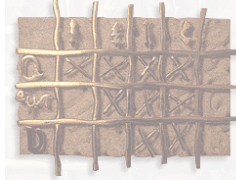
$$\begin{aligned}\alpha &= \arg \left( -\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right), \\ \beta &= \pi - \arg \left( \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} \right), \\ \gamma &= \arg \left( -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right).\end{aligned}$$



- The angle  $\beta$  is directly the weak mixing phase of the of  $B^0$  mixing.
- The angle  $\gamma$  is the weak phase at work in the charmless  $b$ -hadrons decays.
- The angle  $\alpha$  is nothing else than  $(\pi - \beta - \gamma)$  and can be exhibited in processes where both charmless decays and mixing are present.

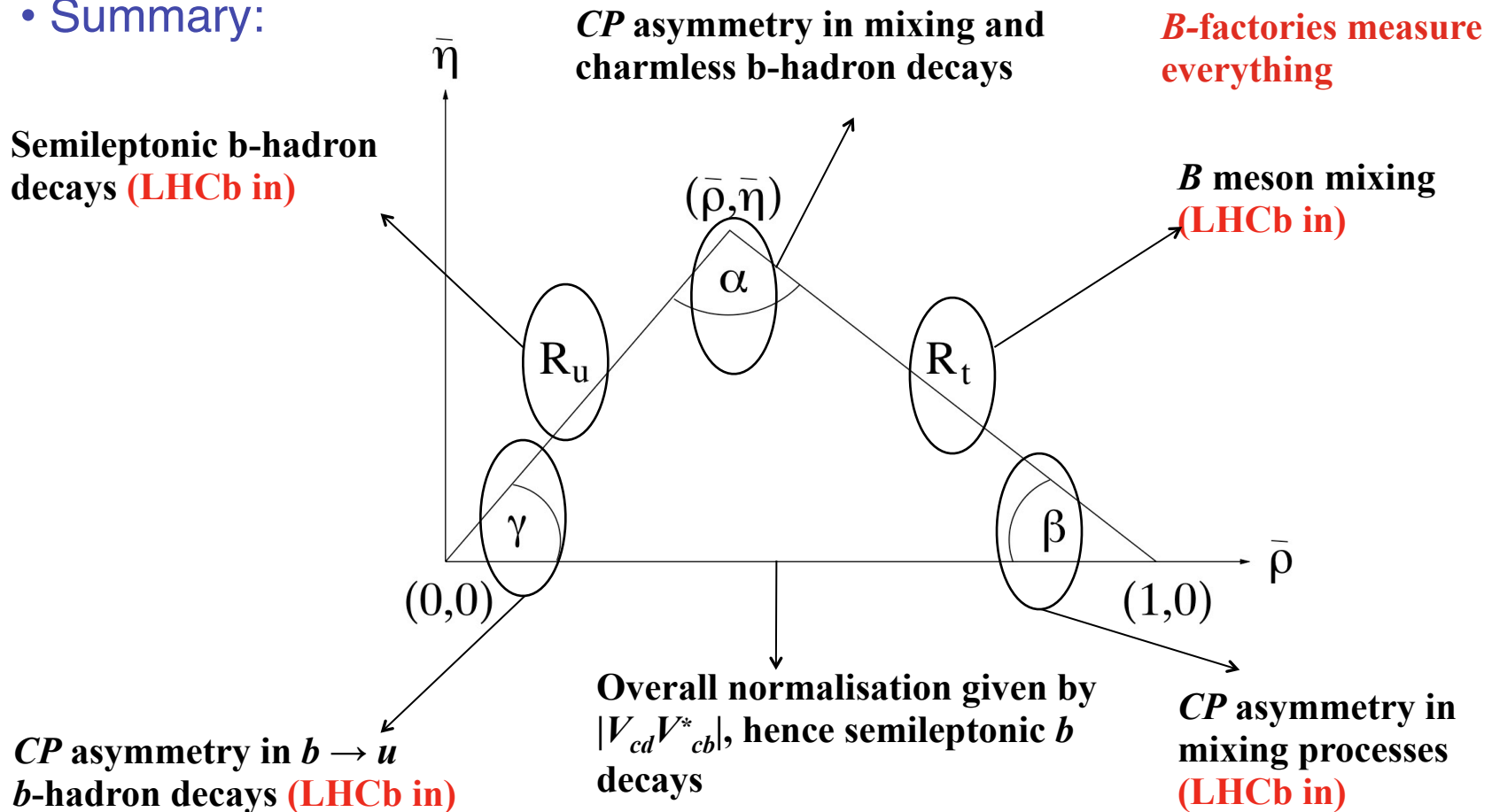
Note: a phase is not an observable. Only phase differences can be measured.

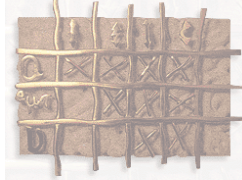




## CKM: the unitarity triangle. Experiments.

- Summary:





### **CKM: the unitarity triangle. Machine and Experiments.**

There are many machines and experiments which are interested in the Flavour Physics and  $CP$  violation. As for their pioneering role, we'll mention ARGUS (DESY, Ge), CLEO (Cornell, US) and LEP (CERN, EU) experiments. The kaon sector is not in the scope of this lecture. Major results came from NA48 (CERN, EU) and KTeV (FNAL, US) though. Japan and Cern projects for kaon physics should bring extremely valuable results. Tevatron used to provide as well world class measurements in heavy flavours physics.

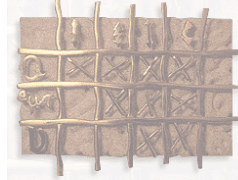
But the  $B$ -factories (now Belle II) and the LHCb experiment at LHC definitely dominate the landscape.

A complete review of the observables is given [here](#): (just click).



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**The next Chapter of Part I starts at the next slide**



# Part I — $CP$ symmetry breaking and CKM matrix

## CKM: the global fit. The observables and parameters.

- List of the inputs: in the details.
- The ones discussed in the previous link
- $\alpha, \gamma$
- Lattice parameters. And ratios.
- The tauonic  $B$  decay.

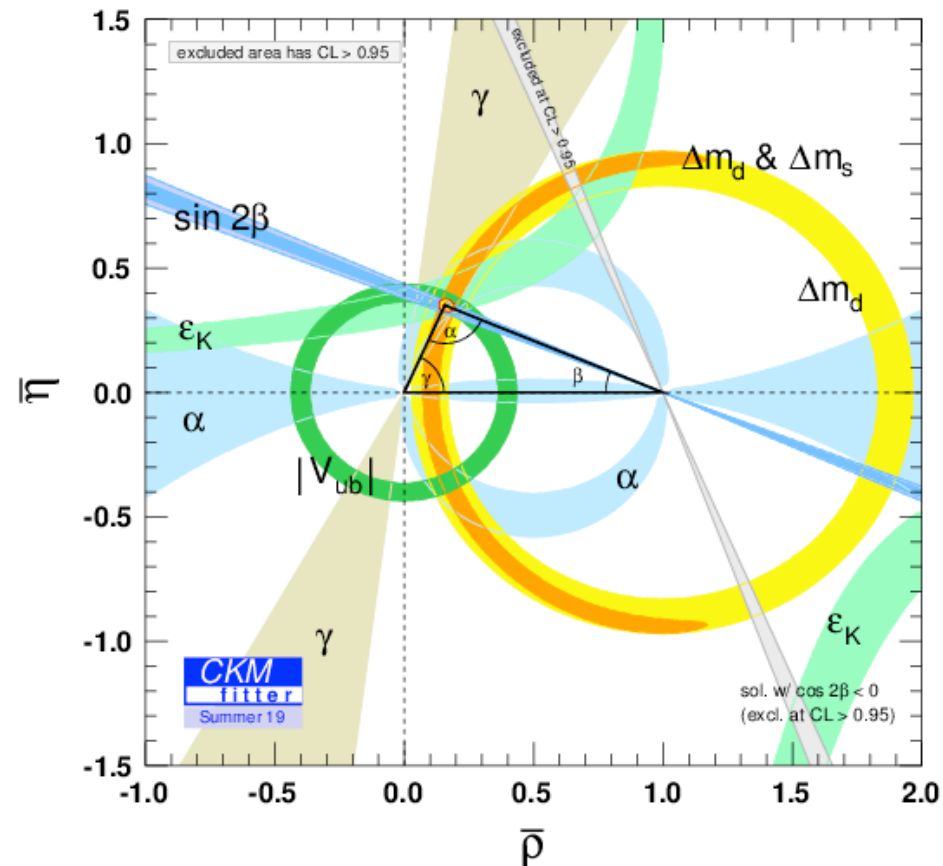
Parameter	Value $\pm$ Error(s)	Reference	Errors	
			GS	TH
$ V_{ud} $ (nuclei)	$0.97425 \pm 0.00022$	[1]	*	-
$ V_{us} $ ( $K\ell 3$ )	$0.2254 \pm 0.0013$	[2]	*	-
$ V_{ub} $	$(3.92 \pm 0.09 \pm 0.45) \times 10^{-3}$	[3, 4]	*	*
$ V_{cb} $	$(40.89 \pm 0.38 \pm 0.59) \times 10^{-3}$	[3]	*	*
$ \varepsilon_K $	$(2.229 \pm 0.010) \times 10^{-3}$	[5]	*	-
$\Delta m_d$	$(0.507 \pm 0.005) \text{ ps}^{-1}$	[3]	*	-
$\Delta m_s$	$(17.77 \pm 0.12) \text{ ps}^{-1}$	[6]	*	-
$\sin(2\beta)_{[c\bar{c}]}$	$0.673 \pm 0.023$	[3]	*	-
$S_{\pi\pi}^{+-}, C_{\pi\pi}^{+-}, C_{\pi\pi}^{00}$	Inputs to isospin analysis	[3]	*	-
$\mathcal{B}_{\pi\pi}$ all charges	Inputs to isospin analysis	[3]	*	-
$S_{\rho\rho,L}^{+-}, C_{\rho\rho,L}^{+-}, S_{\rho\rho}^{00}, C_{\rho\rho}^{00}$	Inputs to isospin analysis	[3]	*	-
$\mathcal{B}_{\rho\rho,L}$ all charges	Inputs to isospin analysis	[3]	*	-
$B^0 \rightarrow (\rho\pi)^0 \rightarrow 3\pi$	Time-dependent Dalitz analysis	[7, 8]	*	-
$B^- \rightarrow D^{(*)}K^{(*)-}$	Inputs to GLW analysis	[3]	*	-
$B^- \rightarrow D^{(*)}K^{(*)-}$	Inputs to ADS analysis	[3]	*	-
$B^- \rightarrow D^{(*)}K^{(*)-}$	GGSZ Dalitz analysis	[3]	*	-
$\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau)$	$(1.68 \pm 0.31) \times 10^{-4}$	[9]	*	-
$\bar{m}_c(m_c)$	$(1.286 \pm 0.013 \pm 0.040) \text{ GeV}$	[12]	*	*
$\bar{m}_t(m_t)$	$(165.02 \pm 1.16 \pm 0.11) \text{ GeV}$	[10]	*	*
$B_K$	$0.723 \pm 0.004 \pm 0.067$	[16]	*	*
$\alpha_s(m_Z^2)$	$0.1176 \pm 0.0020$	[5]	-	*
$\eta_{cc}$	Calculated from $\bar{m}_c(m_c)$ and $\alpha_s$	[17]	-	*
$\eta_{ct}$	$0.47 \pm 0.04$	[18]	-	*
$\eta_{tt}$	$0.5765 \pm 0.0065$	[17, 18]	-	*
$\eta_B(\overline{\text{MS}})$	$0.551 \pm 0.007$	[19]	-	*
$f_{B_s}$	$(228 \pm 3 \pm 17) \text{ MeV}$	[16]	*	*
$B_s$	$1.28 \pm 0.02 \pm 0.03$	[16]	*	*
$f_{B_s}/f_{B_d}$	$1.199 \pm 0.008 \pm 0.023$	[16]	*	*
$B_s/B_d$	$1.05 \pm 0.01 \pm 0.03$	[16]	*	*

# Part I — $CP$ symmetry breaking and CKM matrix

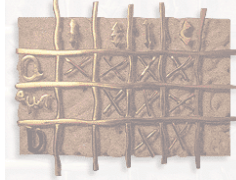


## the CKM profile

- The global picture:
- Notice to read the picture: regions outside the coloured area are excluded at 95 % Confidence Level.
- There is one and only one region of Wolfenstein parameter space which is common to all the constraints.
- In other terms, there is a remarkable consistency between all of the observables.
- The superimposed triangle is the best fit result.

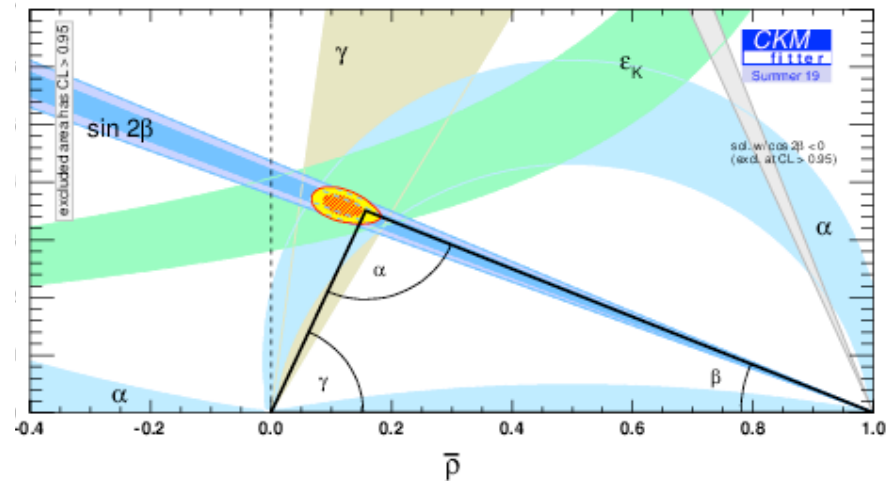
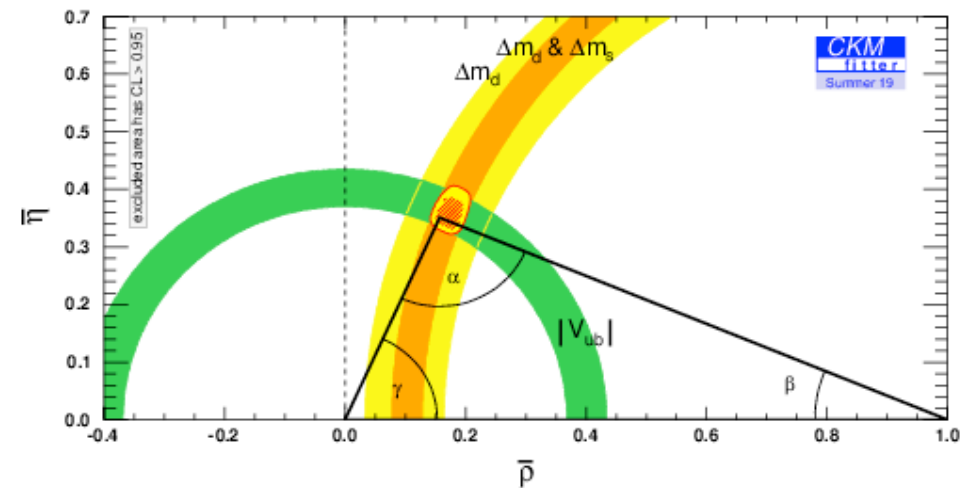


# Part I — $CP$ symmetry breaking and CKM matrix



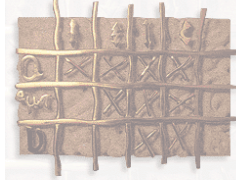
## the CKM profile

- The global picture: comparison of observables constraints.
- $CP$ -conserving against  $CP$ -violating.



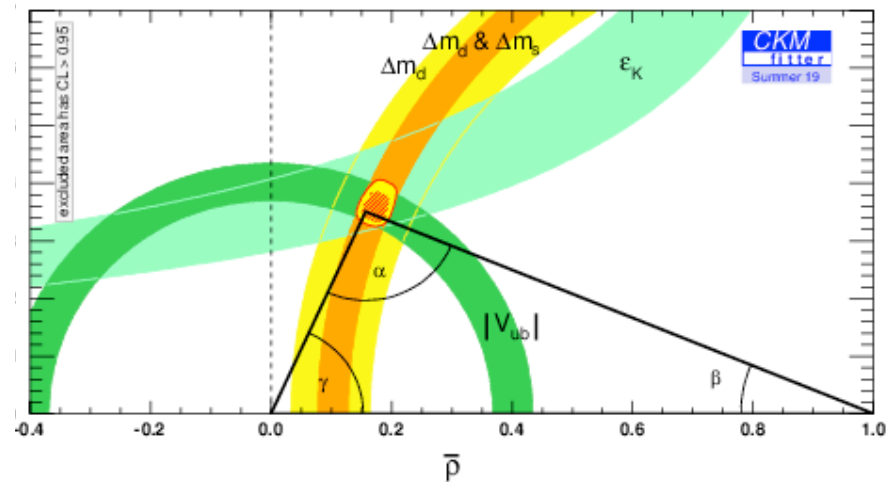
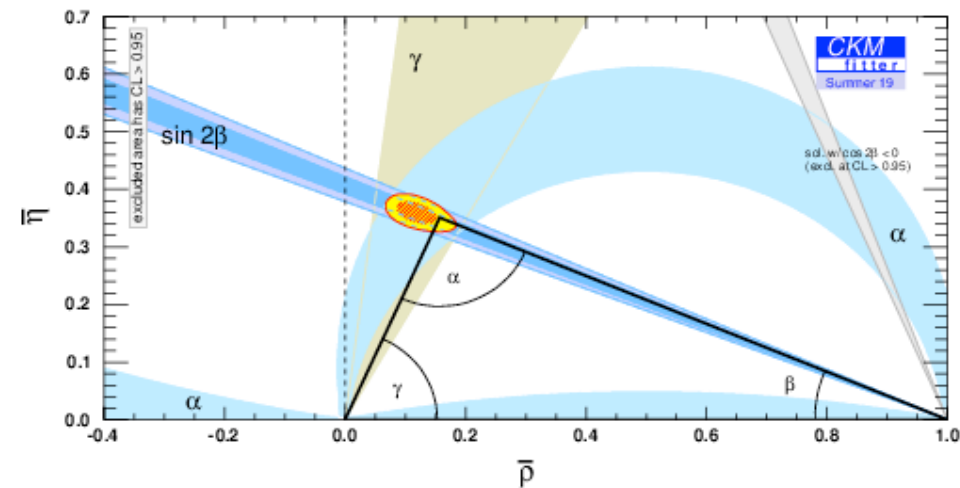
- Correct agreement.  $CP$ -conserving observables can quantify  $CP$  violation.

# Part I — $CP$ symmetry breaking and CKM matrix



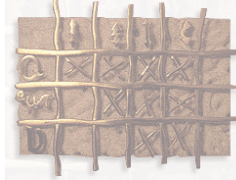
## the CKM profile

- The global picture: comparison of observables constraints.
- Angles (No theory) against No angles (Hadronic uncert.).



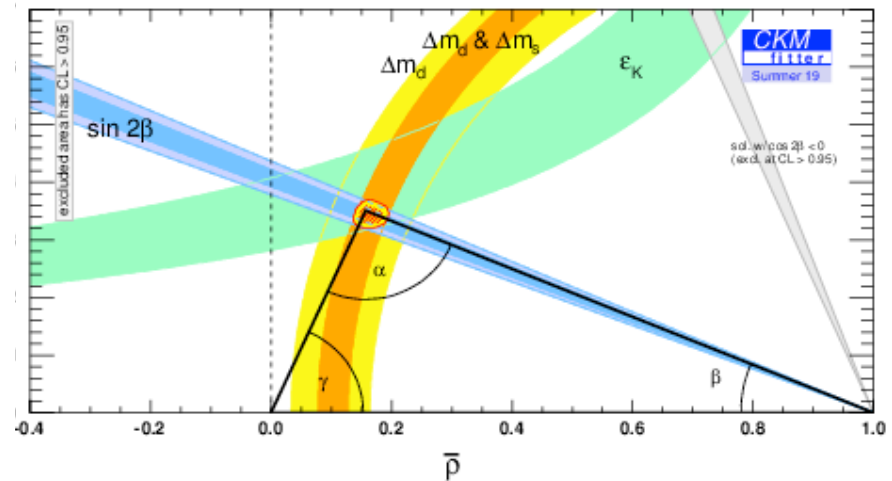
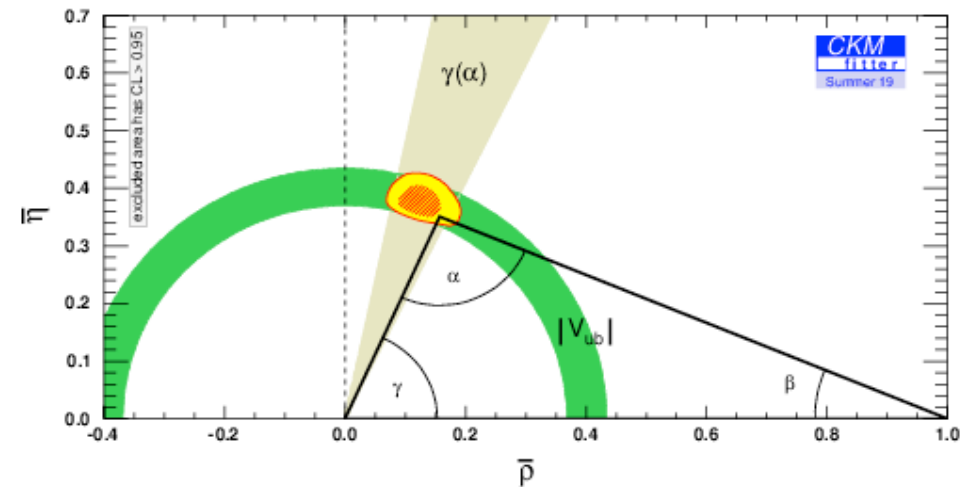
- Correct agreement. Remember that only observables with a good theoretical control are considered in the global fit.

# Part I — $CP$ symmetry breaking and CKM matrix



## the CKM profile

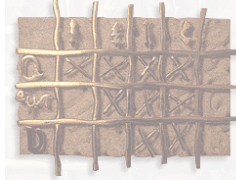
- The global picture: comparison of observables constraints.
- Trees against Loops.



- Trees are thought to be pure SM. Loops could exhibit New Physics. Fair agreement.

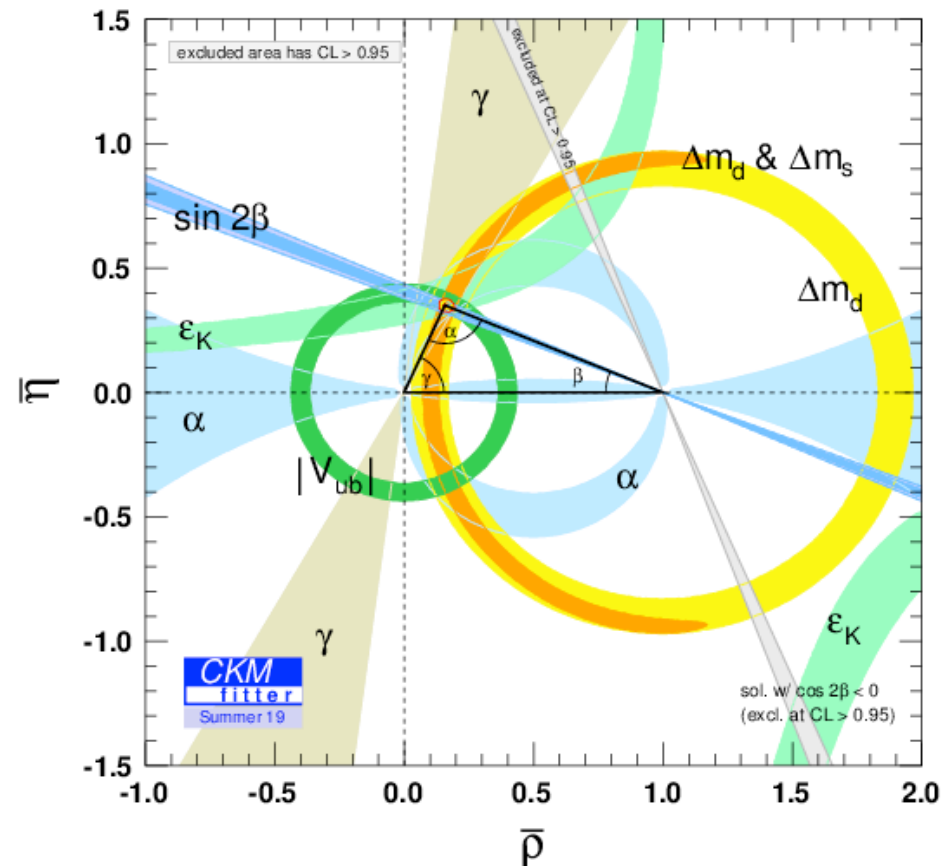


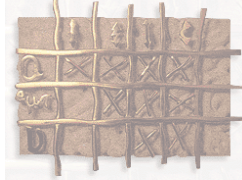
# Part I — $CP$ symmetry breaking and CKM matrix



## the CKM profile

- The global picture:
- This is a tremendous success of the Standard Model and especially the Kobayashi-Maskawa mechanism. This is simultaneously an outstanding experimental achievement by the  $B$  factories.
- CKM is at work in weak charged current.
- The KM phase IS the dominant source of  $CP$  violation in  $K$  and  $B$  system.

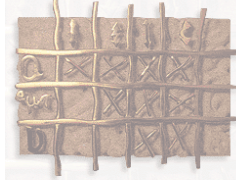




## the CKM profile: Back to the future

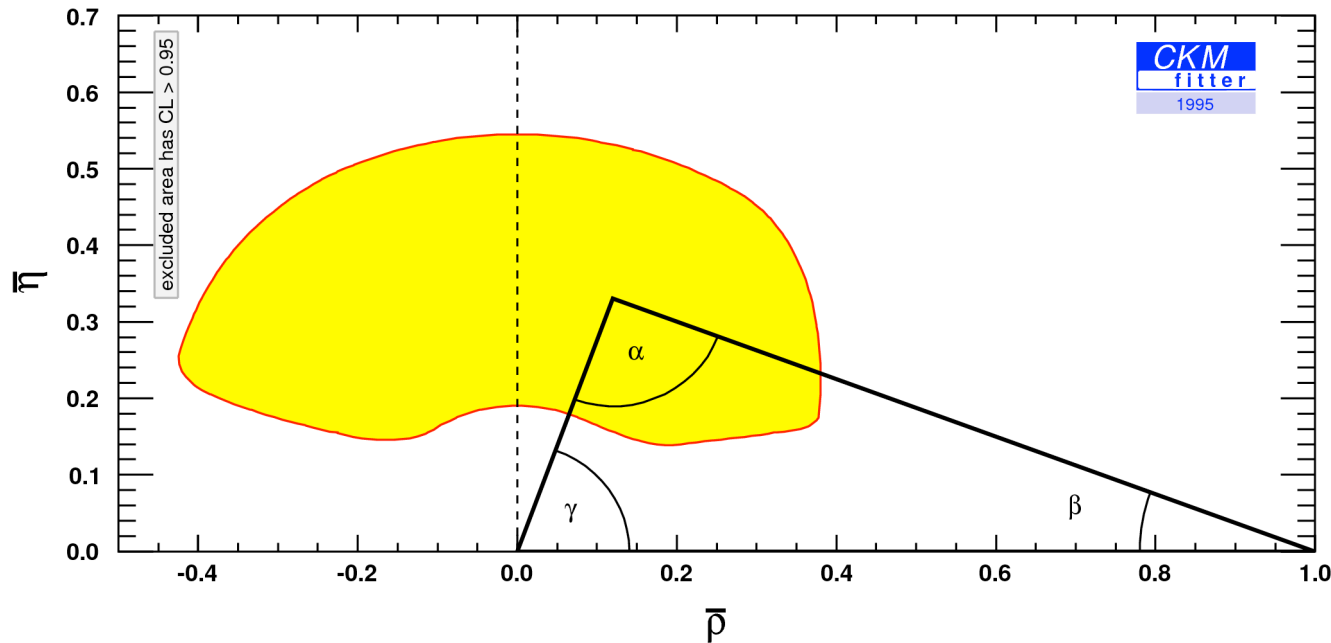
- Recreational Homework. Find the break through measurements along the past two decades.

# Part I — $CP$ symmetry breaking and CKM matrix



## the CKM profile: Back to the future

- Recreational Homework. Find the break through measurements along the past two decades.

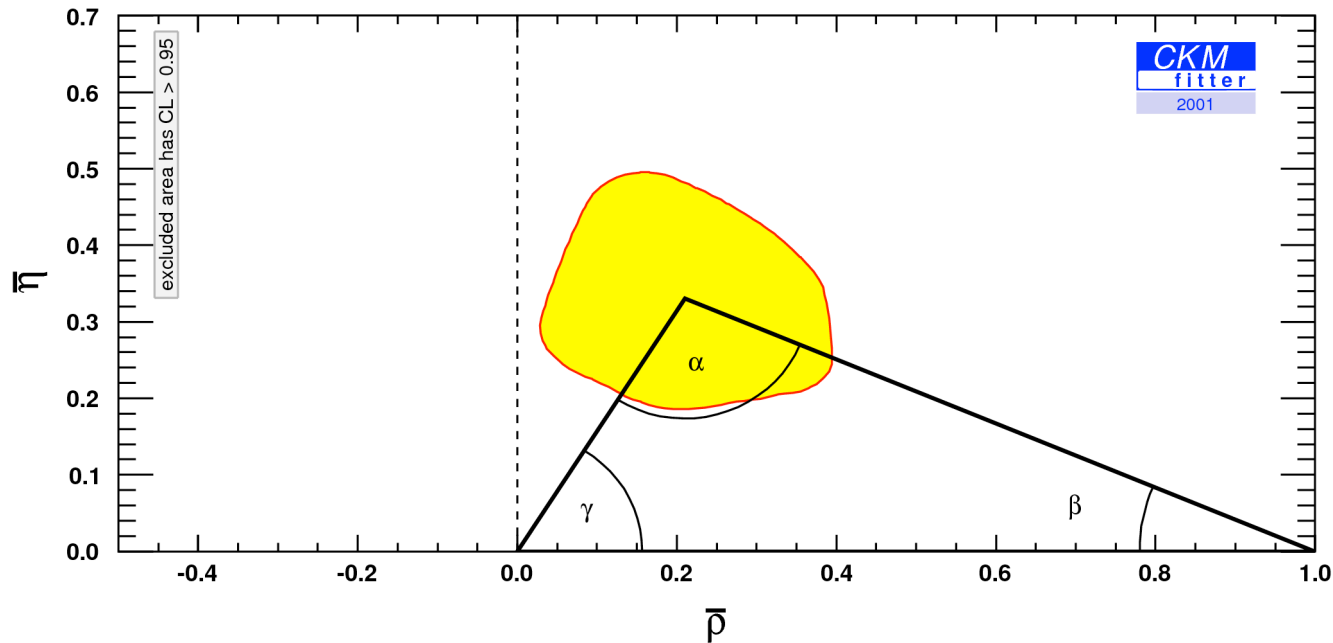


# Part I — $CP$ symmetry breaking and CKM matrix



## the CKM profile: Back to the future

- Recreational Homework. Find the break through measurements along the past two decades.

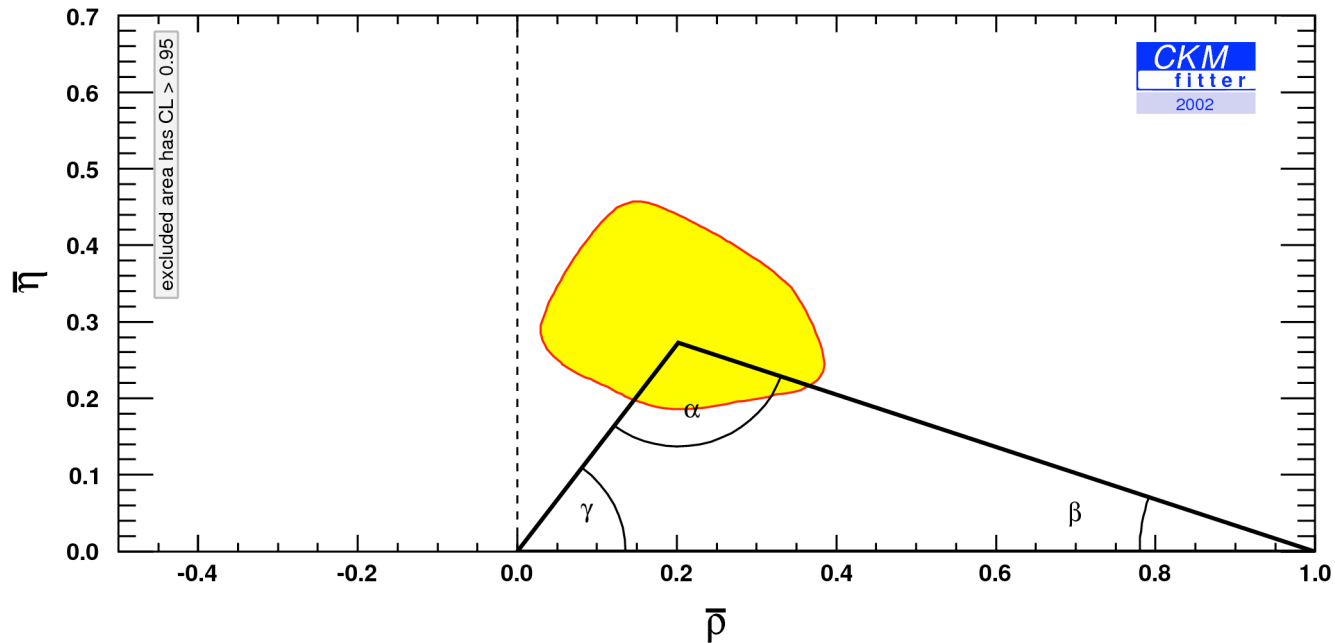


# Part I — $CP$ symmetry breaking and CKM matrix



## the CKM profile: Back to the future

- Recreational Homework. Find the break through measurements along the past two decades.

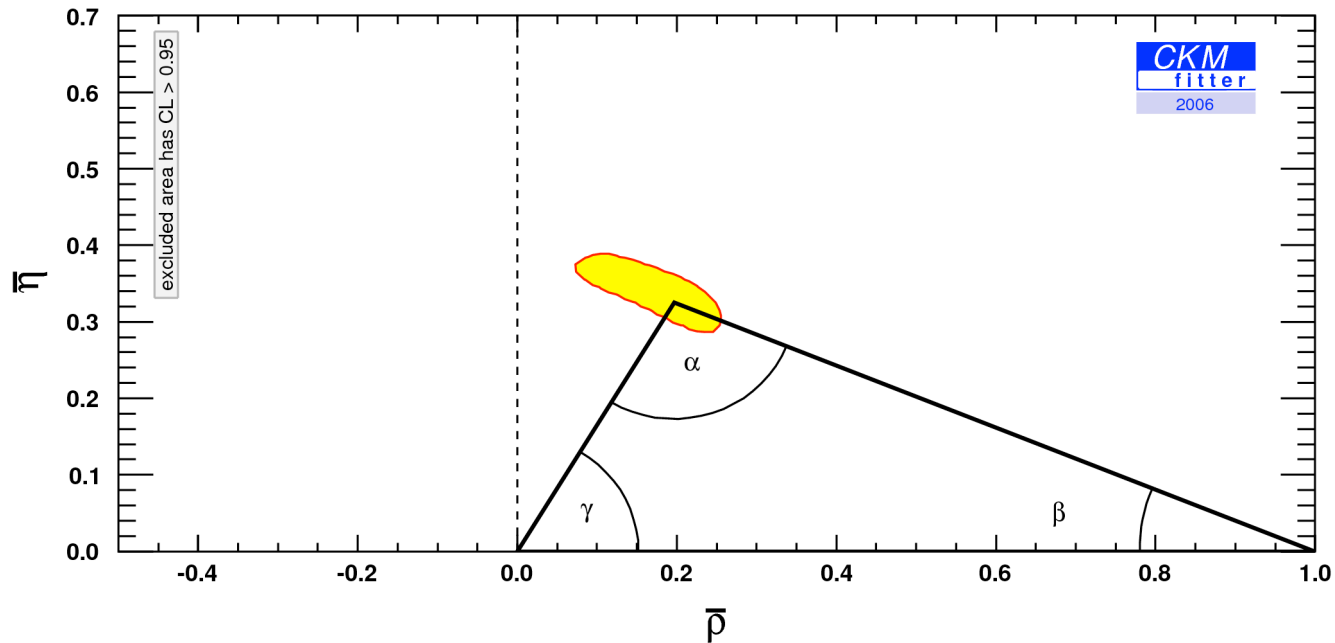


# Part I — $CP$ symmetry breaking and CKM matrix

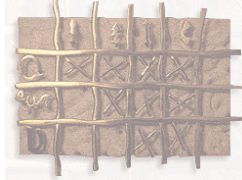


## the CKM profile: Back to the future

- Recreational Homework. Find the break through measurements along the past two decades.

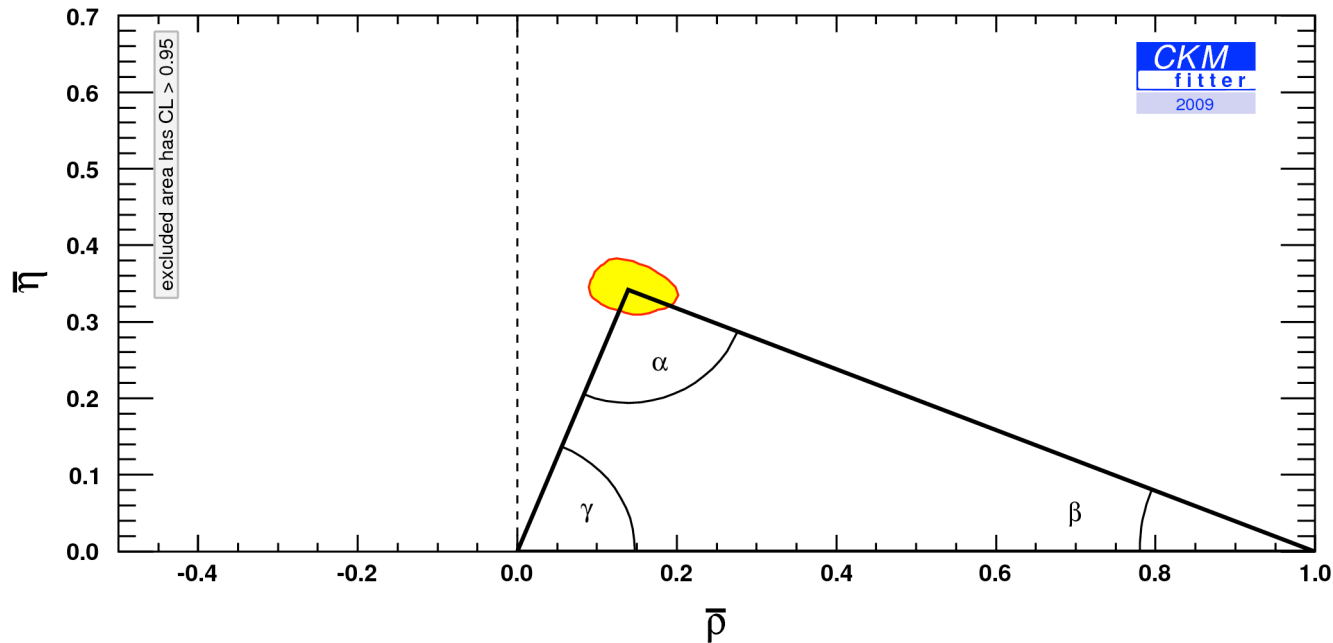


# Part I — $CP$ symmetry breaking and CKM matrix

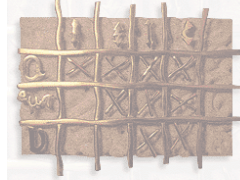


## the CKM profile: Back to the future

- Recreational Homework. Find the break through measurements along the past two decades.

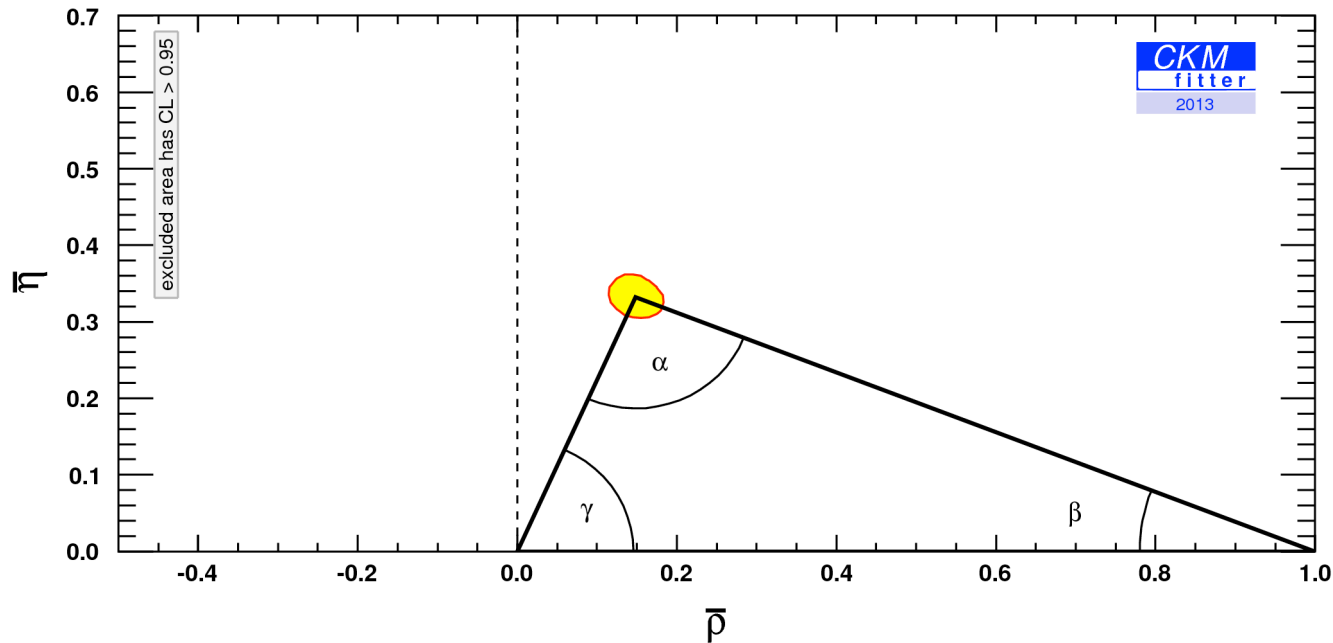


# Part I — $CP$ symmetry breaking and CKM matrix



## the CKM profile: Back to the future

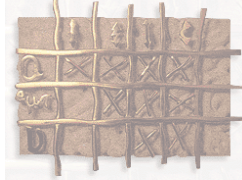
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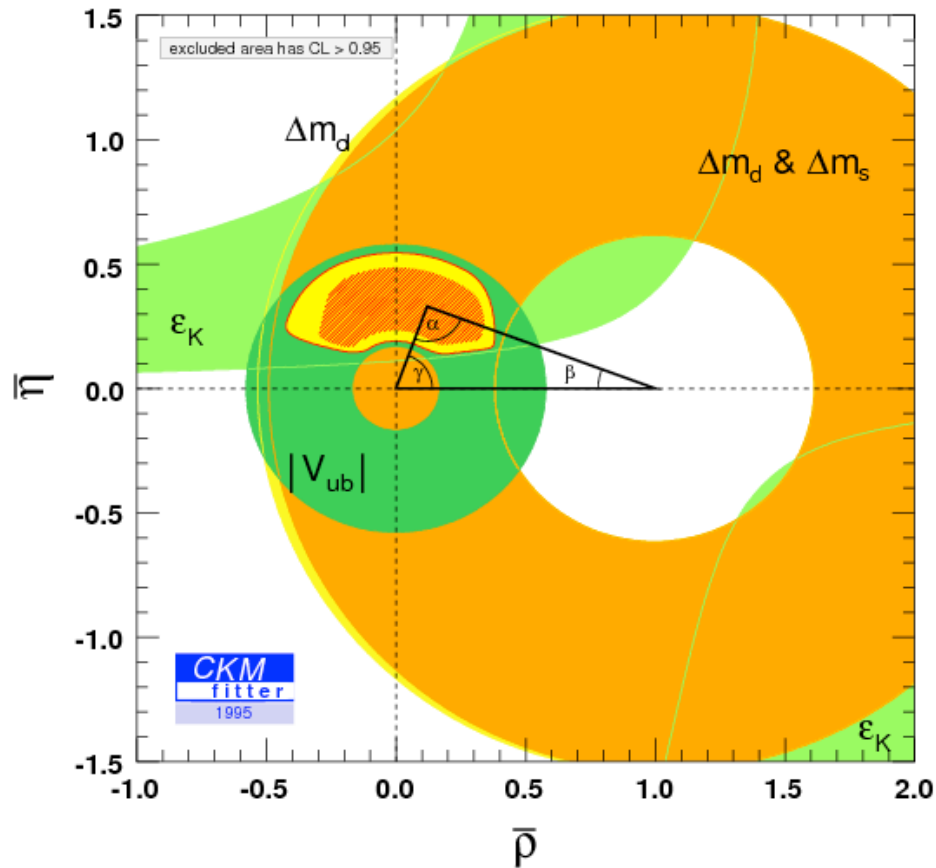




## the CKM profile: Back to the future

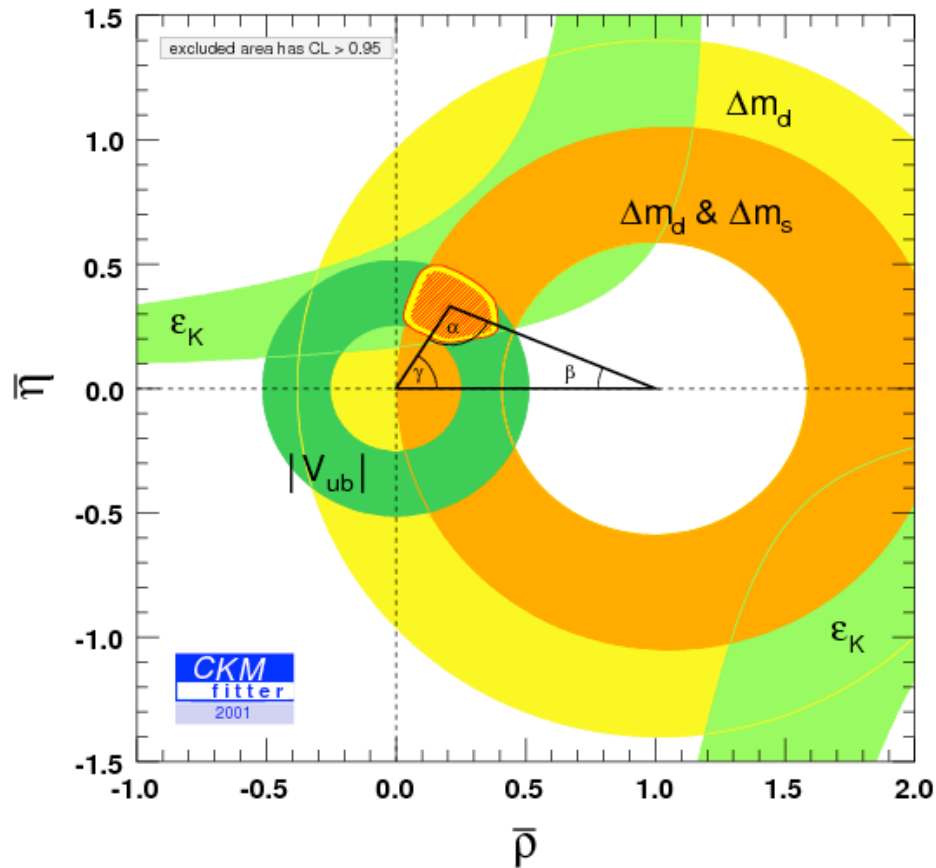


## the CKM profile: Back to the future



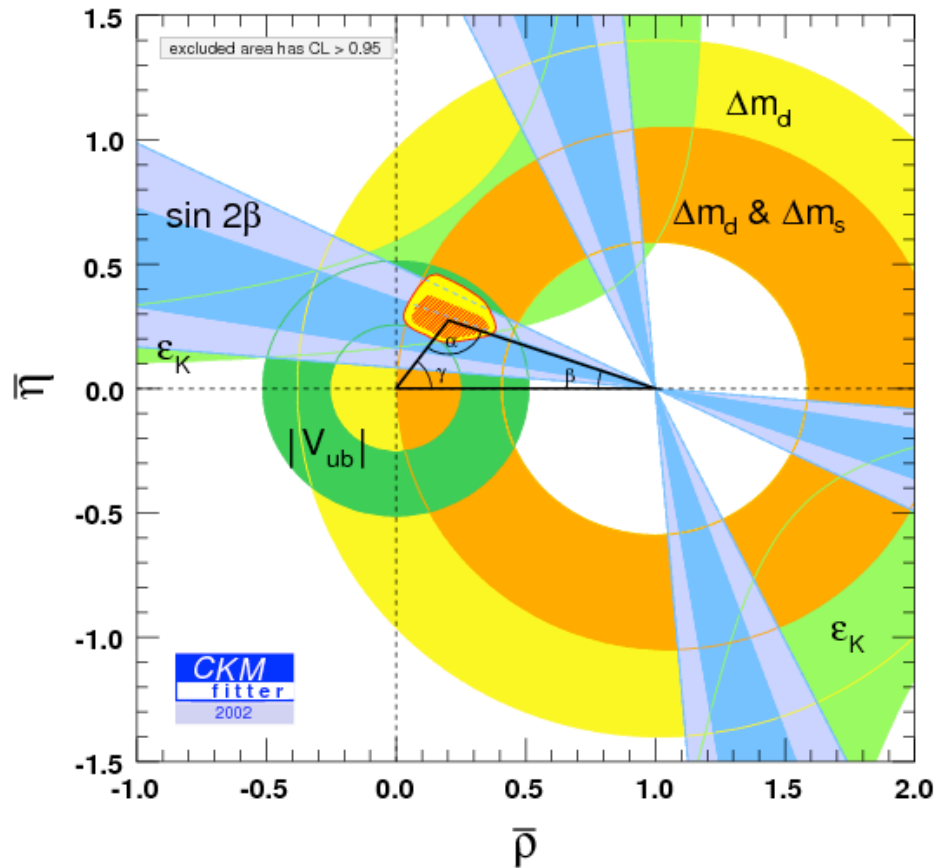


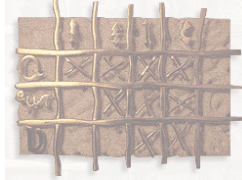
## the CKM profile: Back to the future



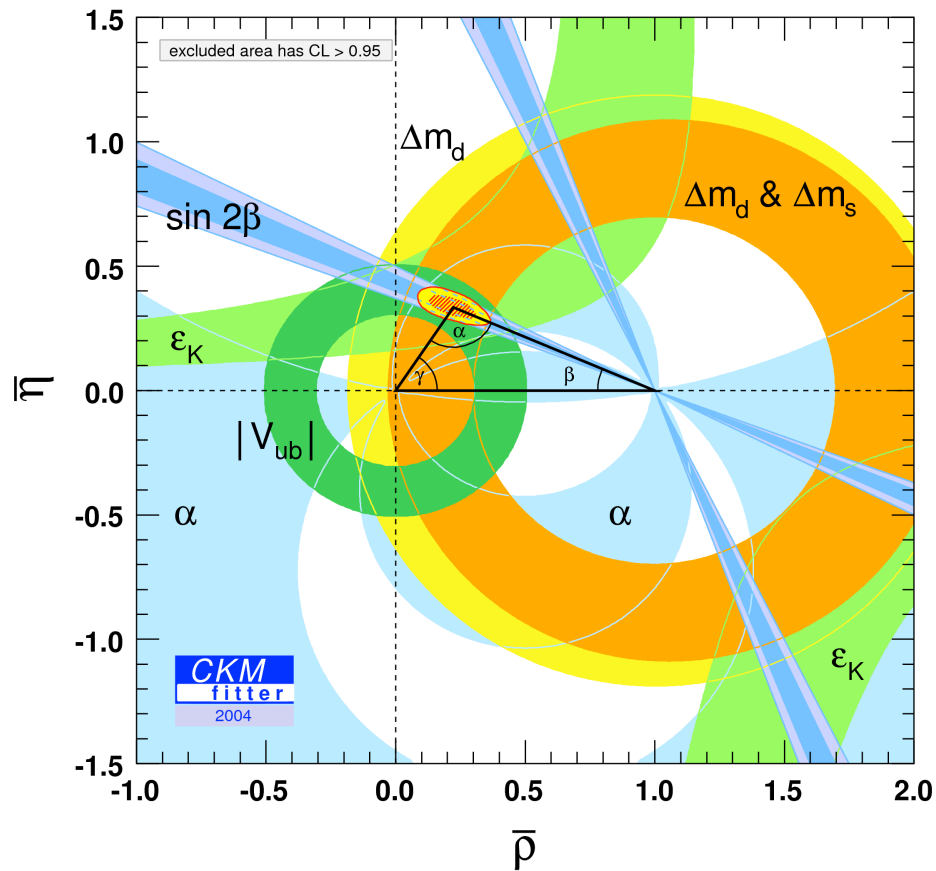


## the CKM profile: Back to the future



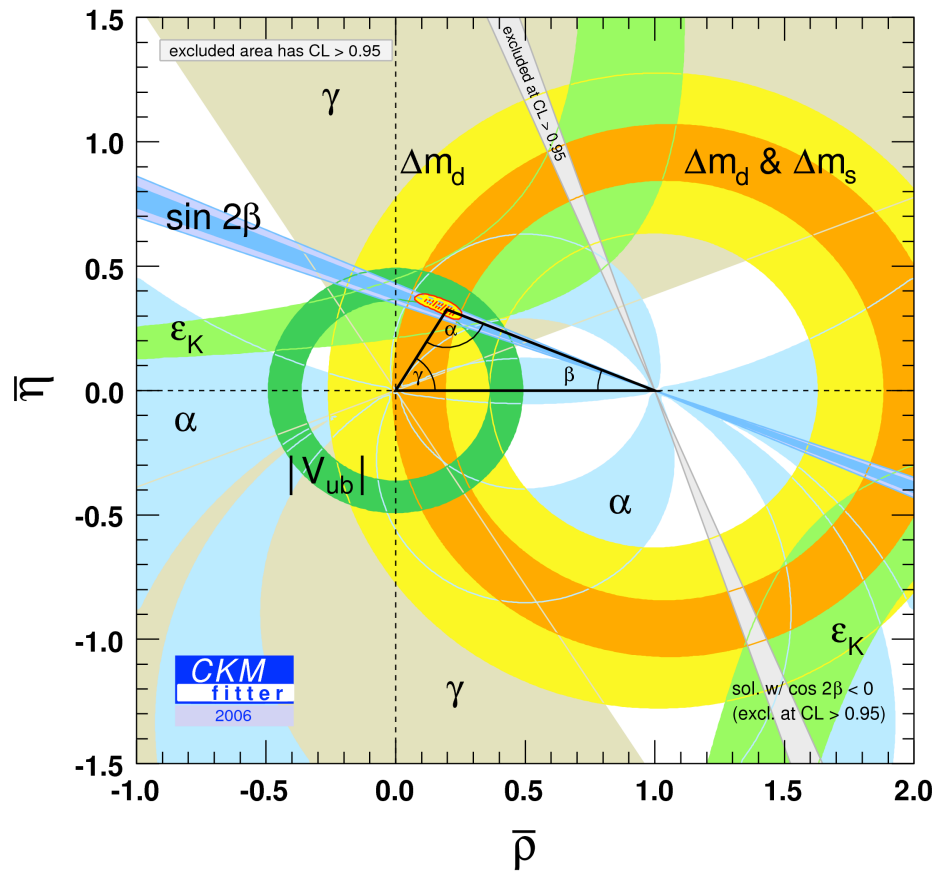


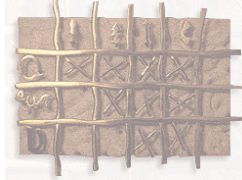
## the CKM profile: Back to the future



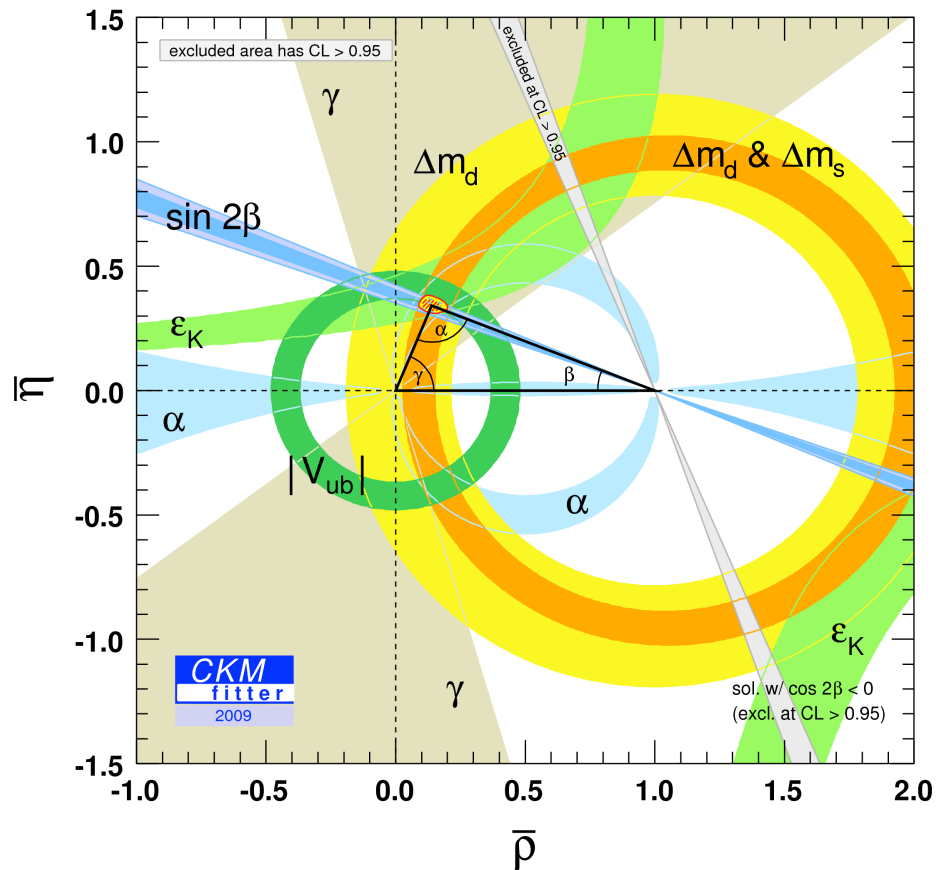


## the CKM profile: Back to the future



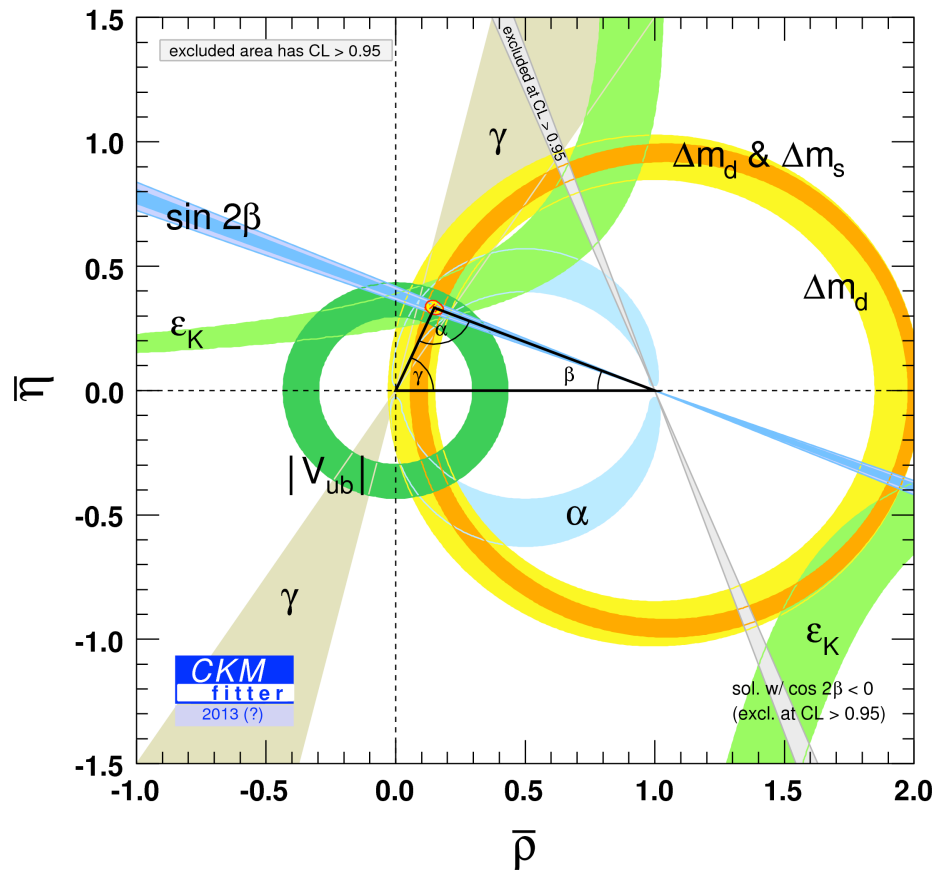


## the CKM profile: Back to the future





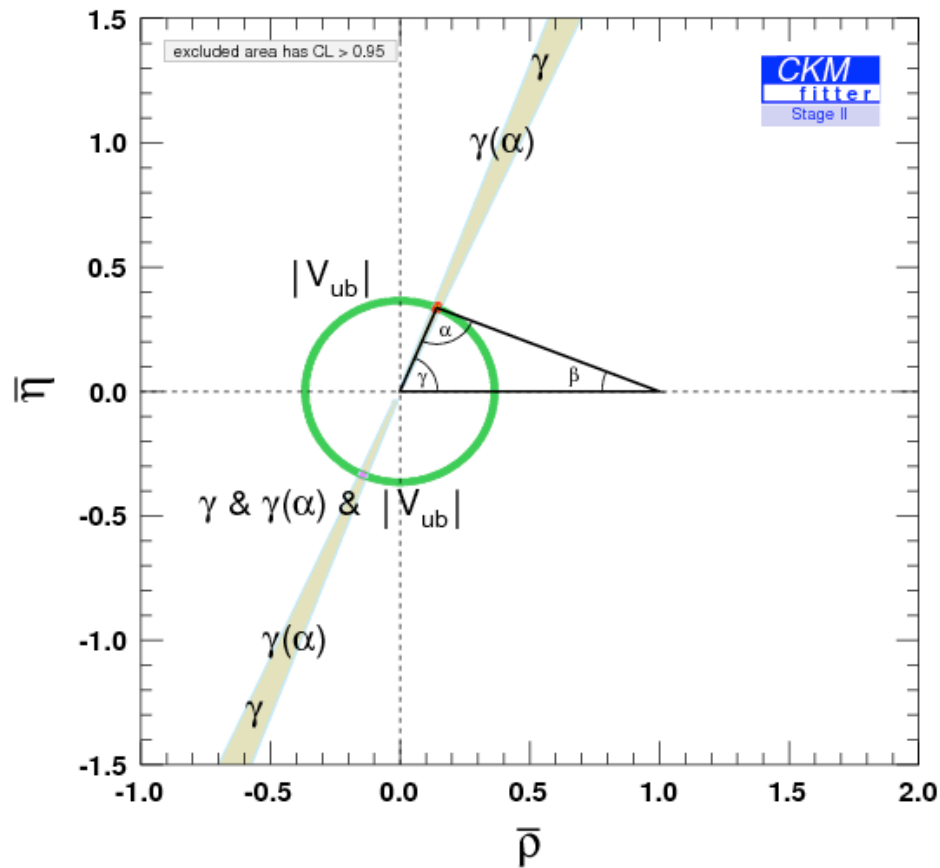
## the CKM profile: Back to the future







## the CKM profile: Back to the future





## the CKM profile: Back to the future

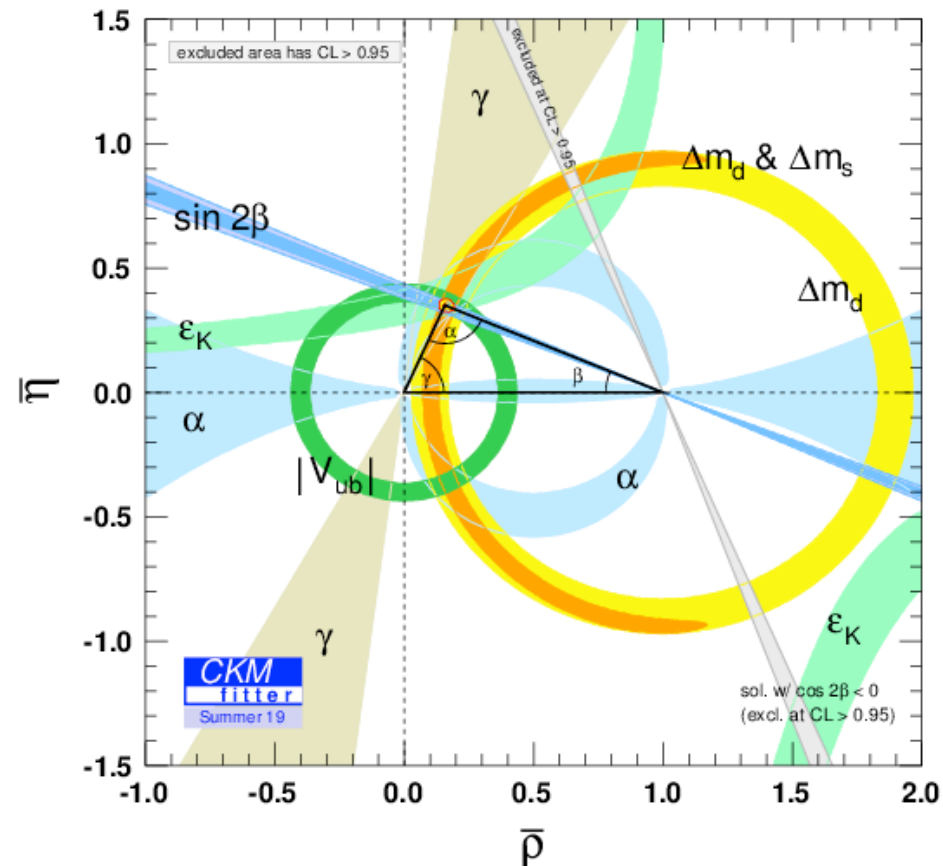
- 1995: starting point given by the top quark mass measurement.  $K$  and  $B$  mixings can be predicted.
- 2001: pre- $B$ -factories era. LEP/CLEO based UT. Comparison with kaon mixing gives a consistency check.
- 2002:  $CP$  violation in the interference between decay and mixing is observed. This is the first true consistency test of the Standard Model.
- 2004: alpha angle is constrained.
- 2006:  $\Delta m_s$  (and first gamma angle constraint).
- 2013: LHCb dominating the gamma measurement.
- 2028: Super Flavour Factory (SuperKEKB) and LHCb (upgrade): additionally LQCD improvement. A New Physics perspective.

# Part I — $CP$ symmetry breaking and CKM matrix

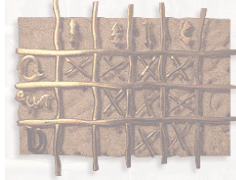


## Standard Model predictions

- Now that the Standard Model hypothesis is validated [Validated does not mean that the SM is THE theory: it means that it passed the statistical test !!!] it's relevant to make the metrology of the CKM parameters.
- Additionally, perform consistency checks. Exclude the meas. of the observable you want to predict from the global fit and ... compare !
- Please pick your favourite around here: <http://ckmfitter.in2p3.fr>.



# Part I — $CP$ symmetry breaking and CKM matrix



## Standard Model predictions

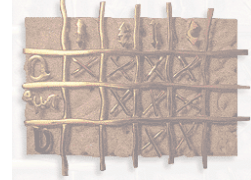
- Predictions can be made on single observables not present in the global fit but depending on the CKM parameters.

- Here is an example of such predictions Phys.Rev. D84 (2011) 033005

- LHCb and Belle II can measure some of these observables: null test of the SM hypothesis.

- To date, all measurements are aligned with the predictions. I will critically examine this statement in a minute.

Charged Leptonic Decays				
$\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$	$(16.8 \pm 3.1) \cdot 10^{-5}$	[4]	$(7.57^{+0.98}_{-0.61}) \cdot 10^{-5}$	2.8
$\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu)$	$< 10^{-6}$	[10]	$(3.74^{+0.44}_{-0.38}) \cdot 10^{-7}$	-
$\mathcal{B}(D_s^+ \rightarrow \tau^+ \nu_\tau)$	$(5.29 \pm 0.28) \cdot 10^{-2}$	[10]	$(5.44^{+0.05}_{-0.17}) \cdot 10^{-2}$	0.5
$\mathcal{B}(D_s^+ \rightarrow \mu^+ \nu_\mu)$	$(5.90 \pm 0.33) \cdot 10^{-3}$	[10]	$(5.39^{+0.21}_{-0.22}) \cdot 10^{-3}$	1.3
$\mathcal{B}(D^+ \rightarrow \mu^+ \nu_\mu)$	$(3.82 \pm 0.32 \pm 0.09) \cdot 10^{-4}$	[9]	$(4.18^{+0.13}_{-0.20}) \cdot 10^{-4}$	0.6
Neutral Leptonic $B$ decays				
$\mathcal{B}(B^0 \rightarrow \pi^+ \pi^-)$	$< 32 \cdot 10^{-9}$	[10]	$(7.73^{+0.37}_{-0.31}) \cdot 10^{-7}$	-
$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$	$< 2.8 \cdot 10^{-9}$	[10]	$(3.64^{+0.17}_{-0.31}) \cdot 10^{-9}$	-
$\mathcal{B}(B_s^0 \rightarrow e^+ e^-)$	$< 4.1 \cdot 10^{-3}$	[10]	$(8.54^{+0.16}_{-0.72}) \cdot 10^{-14}$	-
$\mathcal{B}(B_d^0 \rightarrow \tau^+ \tau^-)$	$< 6 \cdot 10^{-9}$	[10]	$(2.36^{+0.12}_{-0.21}) \cdot 10^{-8}$	-
$\mathcal{B}(B_d^0 \rightarrow \mu^+ \mu^-)$	$< 8.3 \cdot 10^{-9}$	[10]	$(1.13^{+0.06}_{-0.11}) \cdot 10^{-10}$	-
$\mathcal{B}(B_d^0 \rightarrow e^+ e^-)$	$< 8.3 \cdot 10^{-9}$	[10]	$(2.64^{+0.13}_{-0.24}) \cdot 10^{-15}$	-
$B_q - \bar{B}_q$ mixing observables				
$\Delta\Gamma_s/\Gamma_s$	$0.092^{+0.051}_{-0.054}$	[10]	$0.179^{+0.067}_{-0.071}$	0.1
$a_{\text{SL}}^d$	$(-47 \pm 46) \cdot 10^{-4}$	[10]	$(-6.5^{+1.9}_{-1.7}) \cdot 10^{-4}$	0.8
$a_{\text{SL}}^s$	$(-17 \pm 91^{+12}_{-23}) \cdot 10^{-4}$	[26]	$(0.29^{+0.09}_{-0.08}) \cdot 10^{-4}$	0.2
$a_{\text{SL}}^s - a_{\text{SL}}^d$	-		$(6.8^{+1.9}_{-1.7}) \cdot 10^{-4}$	-
$\sin(2\beta)$	$0.678 \pm 0.020$	[10]	$0.832^{+0.033}_{-0.033}$	2.7
$2\beta_s$	$[0.04; 1.04] \cup [2.16; 3.10]$	[27]	$0.0363^{+0.0016}_{-0.0015}$	-
	$0.76^{+0.36}_{-0.28} \pm 0.02$	[28]		
Radiative $B$ decays				
$\mathcal{B}(B_d \rightarrow K^*(892)\gamma)$	$(43.3 \pm 1.8) \cdot 10^{-6}$	[10]	$(64^{+22}_{-21}) \cdot 10^{-6}$	1.2
$\mathcal{B}(B^- \rightarrow K^{*-}(892)\gamma)$	$(42.1 \pm 1.5) \cdot 10^{-6}$	[10]	$(66^{+21}_{-20}) \cdot 10^{-6}$	1.1
$\mathcal{B}(B_s \rightarrow \phi\gamma)$	$(57^{+21}_{-18}) \cdot 10^{-6}$	[10]	$(65^{+31}_{-24}) \cdot 10^{-6}$	0.1
$\mathcal{B}(B \rightarrow X_s\gamma)/\mathcal{B}(B \rightarrow X_c\ell\nu)$	$(3.346 \pm 0.247) \cdot 10^{-3}$	[10]	$(3.03^{+0.34}_{-0.32}) \cdot 10^{-3}$	0.2
Rare $K$ decays				
$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$(1.75^{+1.15}_{-1.05}) \cdot 10^{-10}$	[29]	$(0.854^{+0.116}_{-0.068}) \cdot 10^{-10}$	0.8



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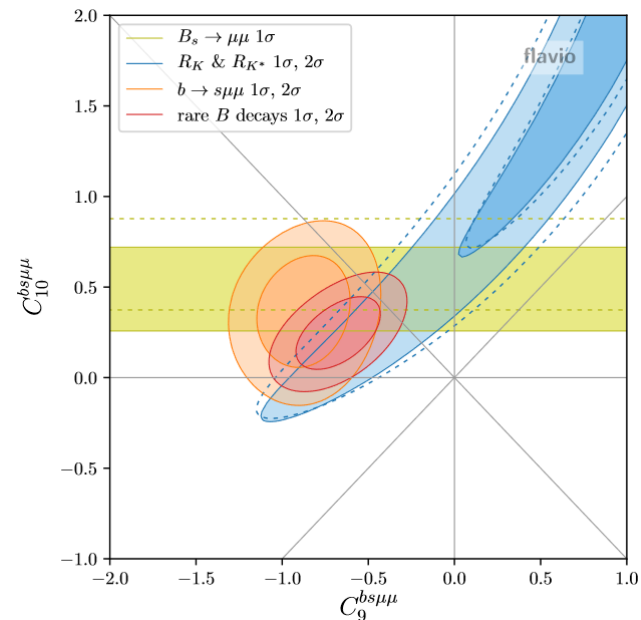
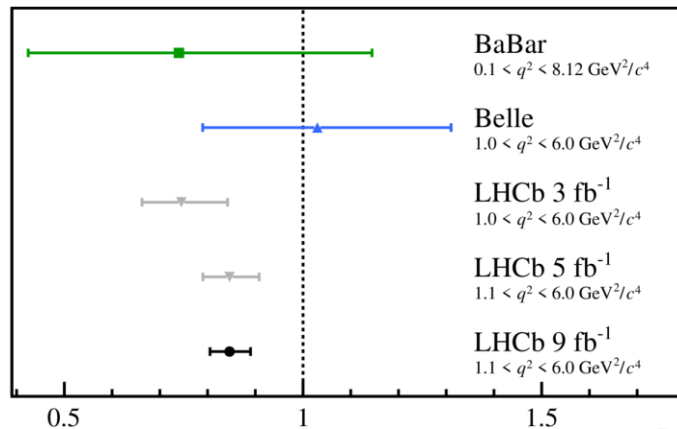
**The Part II starts at the next slide**

# Part II — Rare decays of heavy-flavoured particles



## Motivation

- In any recent HEP physics conference summary talk, you will find these kinds of plot, stating that we are #CautiouslyExcited



- The second objective of this lecture is to undress those plots.



### **Why are rare decays interesting?**

- Rare decays correspond to loop-level weak processes, usually at rates lower than  $O(10^{-6})$
- They do not happen at tree-level in the SM.
- They are as such strongly suppressed:
  - the mass of the virtual mediating particles.
  - the factoring CKM elements.
- Beyond the SM, new (well, unraveled yet) particles can contribute, by contrast, at tree-level. We think they are much heavier than the known mediating particles but could bring significant contributions. Ideal laboratory to search indirectly for those !



### Why are rare decays interesting?

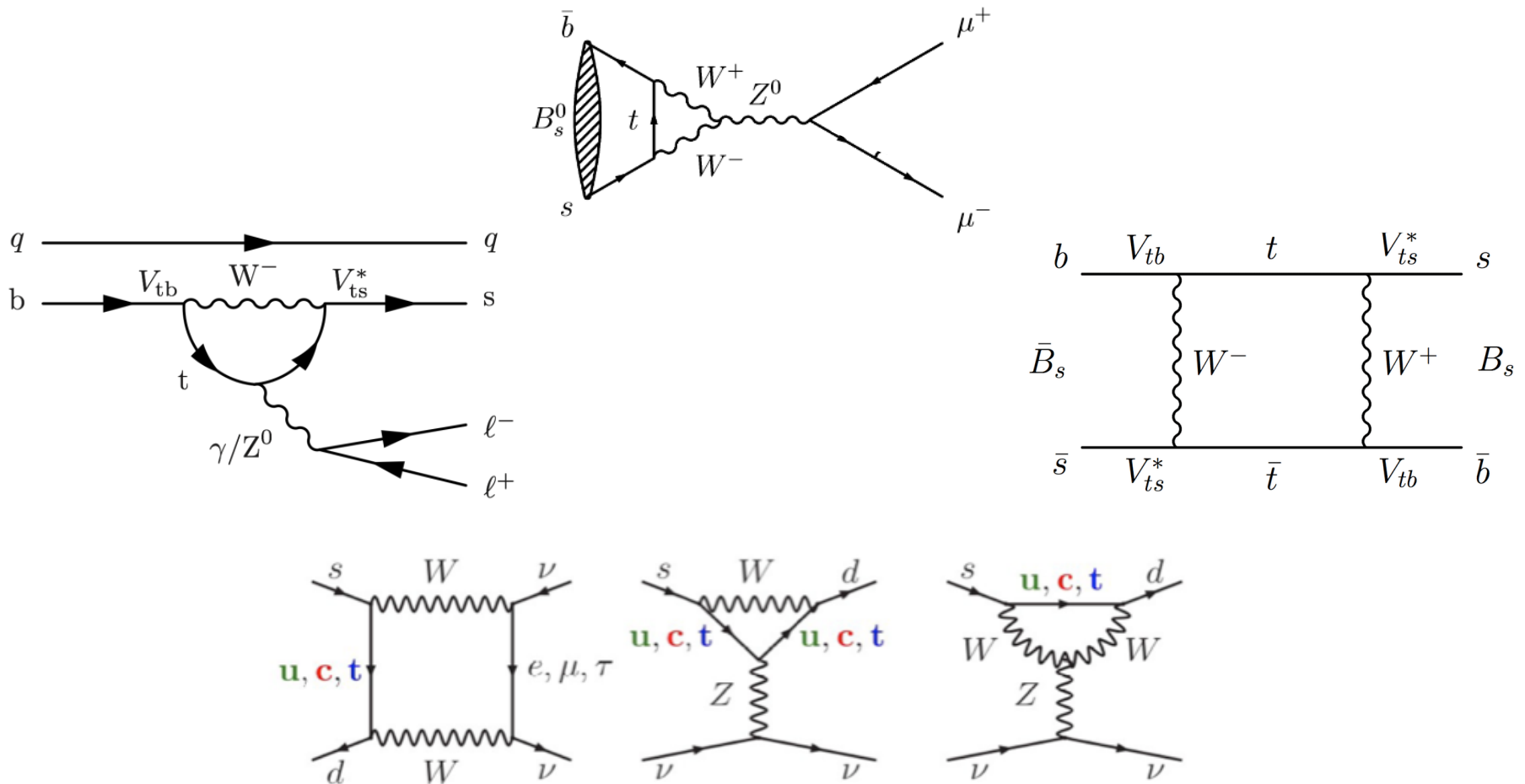
- A personal selection of historical break-throughs related to rare decays:
  - The  $CP$  violation discovery we just studied.
  - The Flavour-Changing Neutral Current  $K^0 \rightarrow \mu\mu$  absence [well,  $O(10^{-9})$ ] yielded the prediction of the  $c$  quark.
  - The oscillation frequency  $B^0$ —anti- $B^0$  suggested the existence of the  $t$  quark (with a mass  $> 50$  GeV).
  - The transition  $b \rightarrow s \gamma$  suggests a high-mass  $H^\pm$ , should a potential charged Higgs in two-Higgs doublet model exist.
- When a discovery (or closure) path is relevant, it's worth pursue it!



# Part II — Rare decays of heavy-flavoured particles



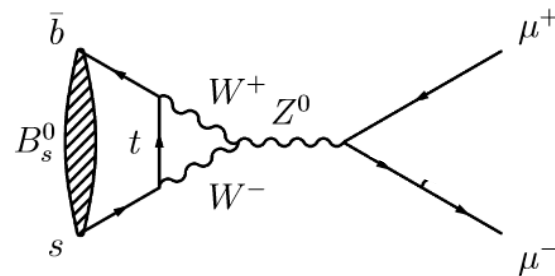
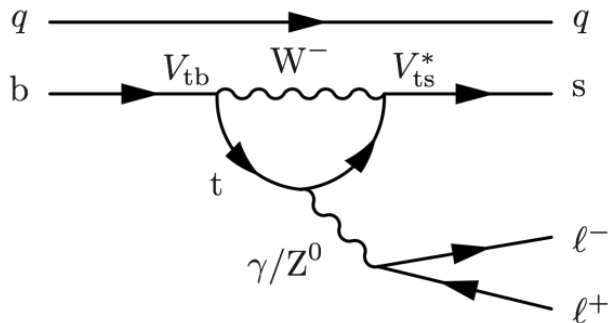
**Let's write some diagrams in the SM**



# Part II — Rare decays of heavy-flavoured particles

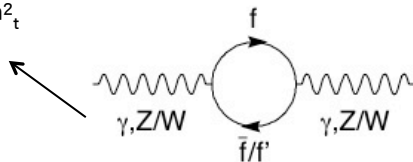


## Let's write some diagrams in the SM

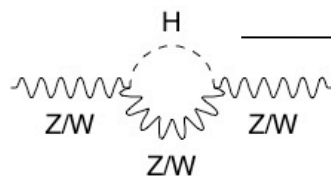
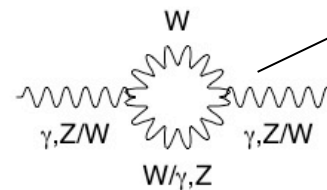


## Remember half an hour ago: same Physics to probe

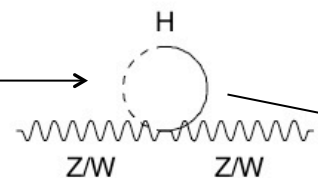
Top dominates. Mostly sensitive to  $m_t^2$



Non abelian structure of the EW theory. TGC.



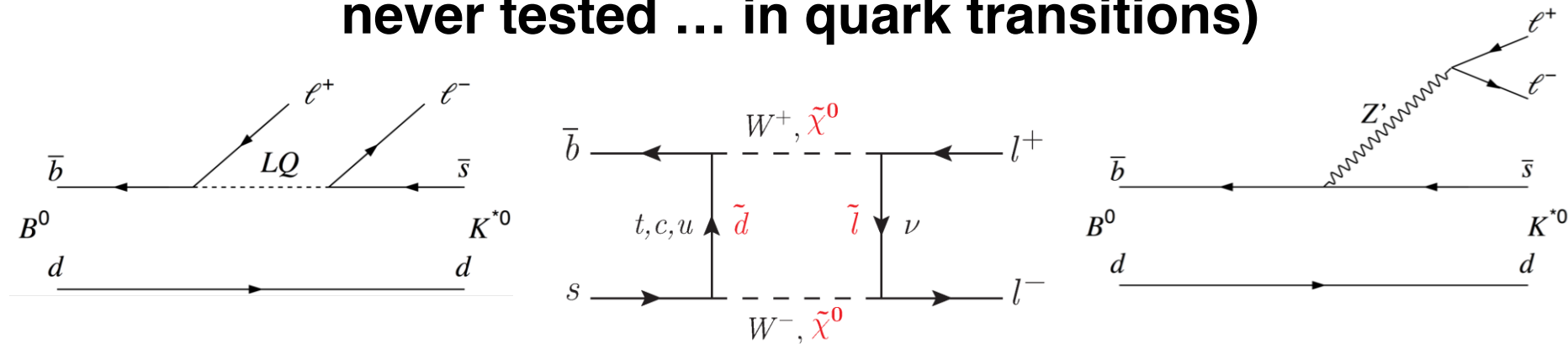
Scalar sector. Contains Higgs mass info.



## Part II — Rare decays of heavy-flavoured particles



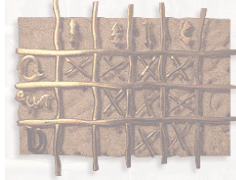
**Let's write some diagrams BSM (the outermost were never tested ... in quark transitions)**



**The menu of observables comes next**

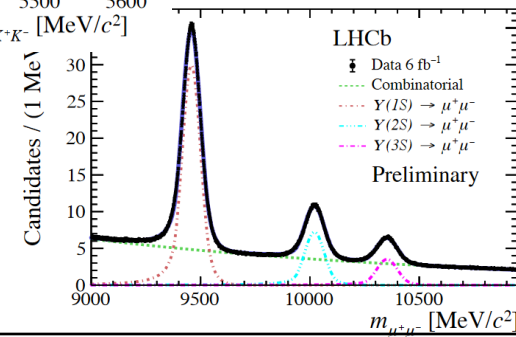
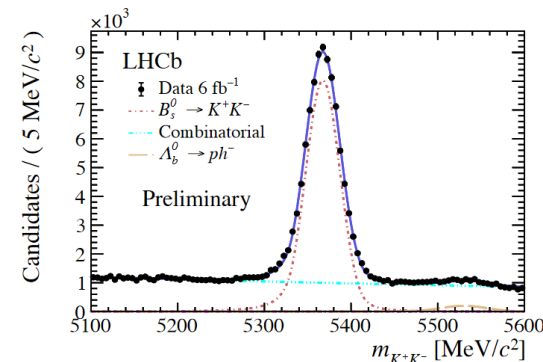
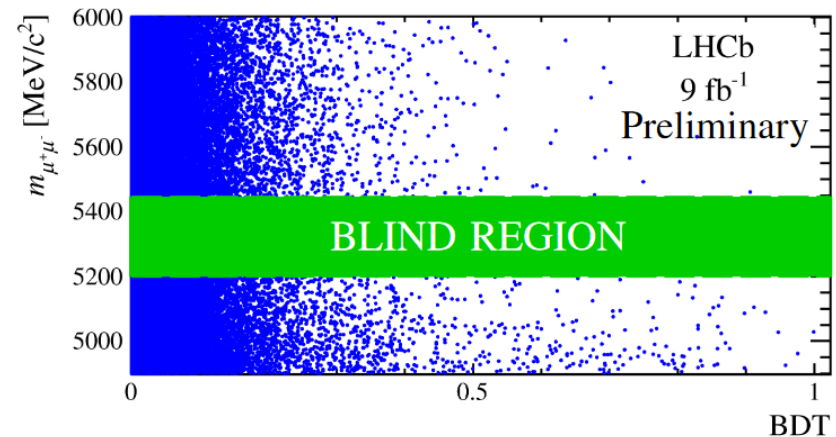
- The search for Flavour-Changing Neutral Current  $B_s^0 \rightarrow \mu\mu$
- The Flavour-Changing Neutral Currents  $b \rightarrow s \ell \ell$ 
  - Lepton universality observables
  - Angular observables
  - Branching fractions
- A glance at  $b \rightarrow c \tau \nu$  decay rates

# Part II — $B_s \rightarrow \mu\mu$ (ex. of LHCb-PAPER-2021-007)

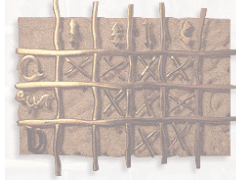


## • Strategy

- Use full Run 1 + Run 2 data
- Muon pairs with invariant-mass  $m \in [4.9, 6.0]$  GeV
- Use the topological properties of the decay / good displaced vertex
- Suppress misidentification of particles with tight PID and muon detector requirements
- Calibrate mass and width of signals
- Signal region blind until analysis is finalised

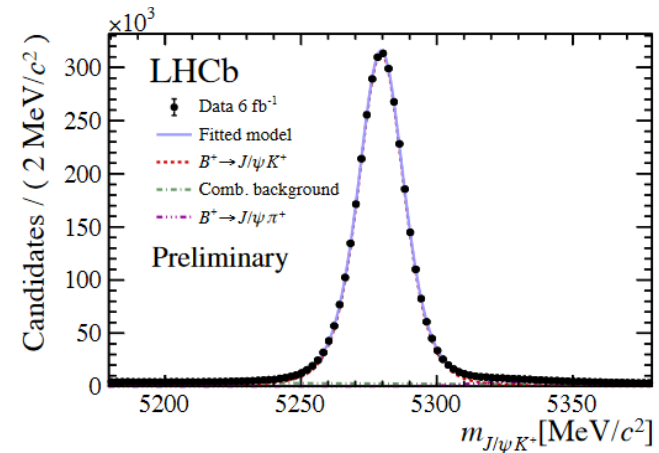
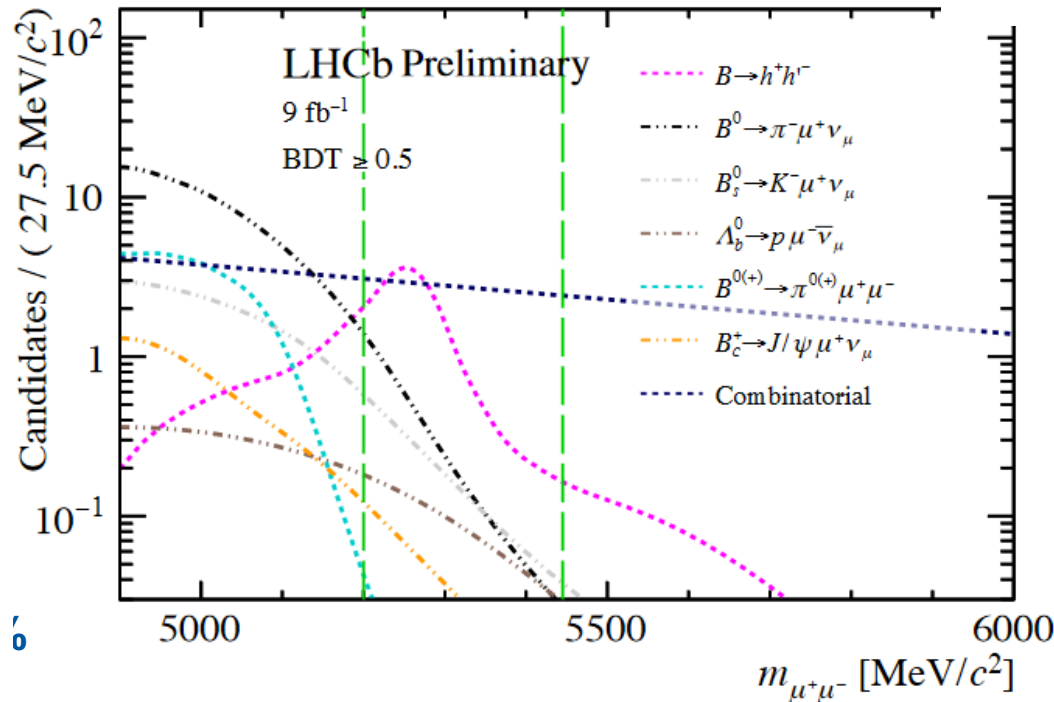


# Part II — $B_s \rightarrow \mu\mu$ (ex. of LHCb-PAPER-2021-007)



- Strategy:
  - Normalise the yields to known branching fractions
  - Analysis of backgrounds

$$\mathcal{B}(B_{d,s}^0 \rightarrow \mu^+ \mu^-) = \underbrace{\frac{\mathcal{B}_{norm}}{N_{norm}}}_{\alpha_d} \times \underbrace{\frac{\epsilon_{norm}}{\epsilon_{sig}}}_{\alpha_s} \times \underbrace{\frac{f_{norm}}{f_{d,s}}}_{\alpha_s} \times N_{B_{d,s}^0 \rightarrow \mu^+ \mu^-}$$



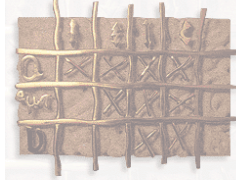
## Part II — $B_s \rightarrow \mu\mu$ (ex. of LHCb-PAPER-2021-007)

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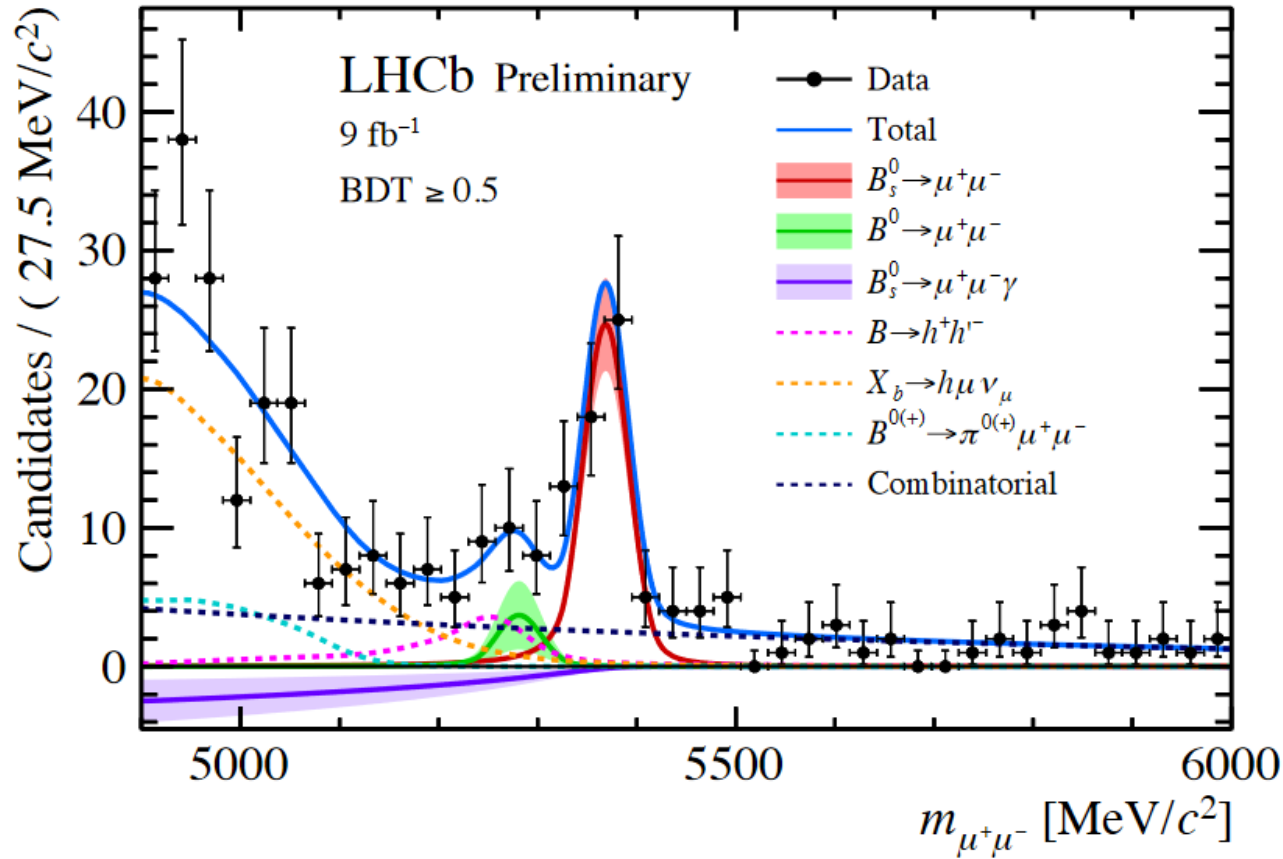


- Results:

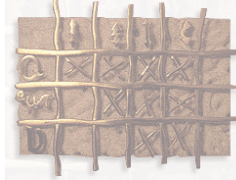
## Part II — $B_s \rightarrow \mu\mu$ (ex. of LHCb-PAPER-2021-007)



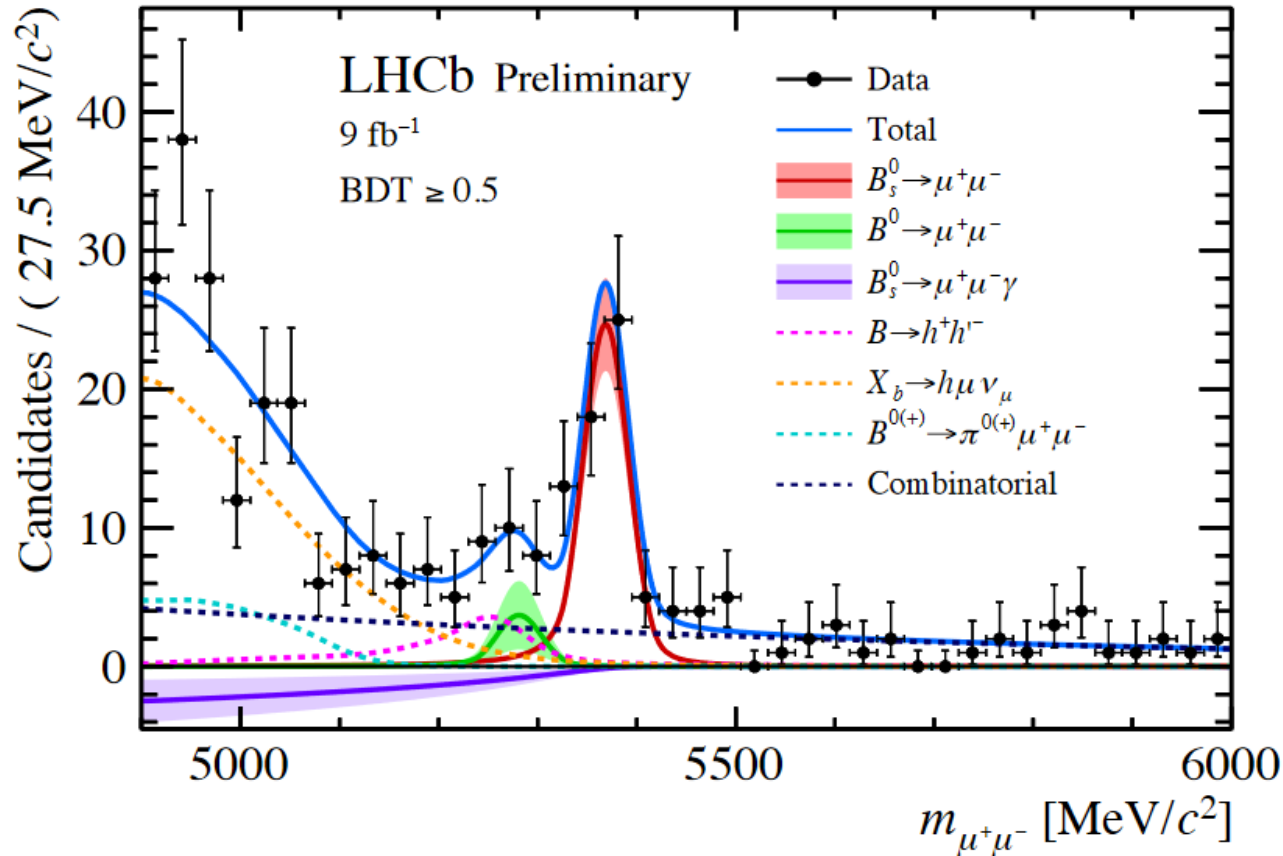
- Results:



## Part II — $B_s \rightarrow \mu\mu$ (ex. of LHCb-PAPER-2021-007)



- Results:

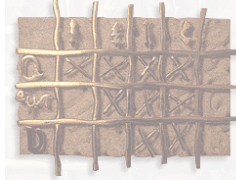


$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) \times 10^9 = 3.09^{+0.46}_{-0.43} {}^{+0.15}_{-0.11},$$

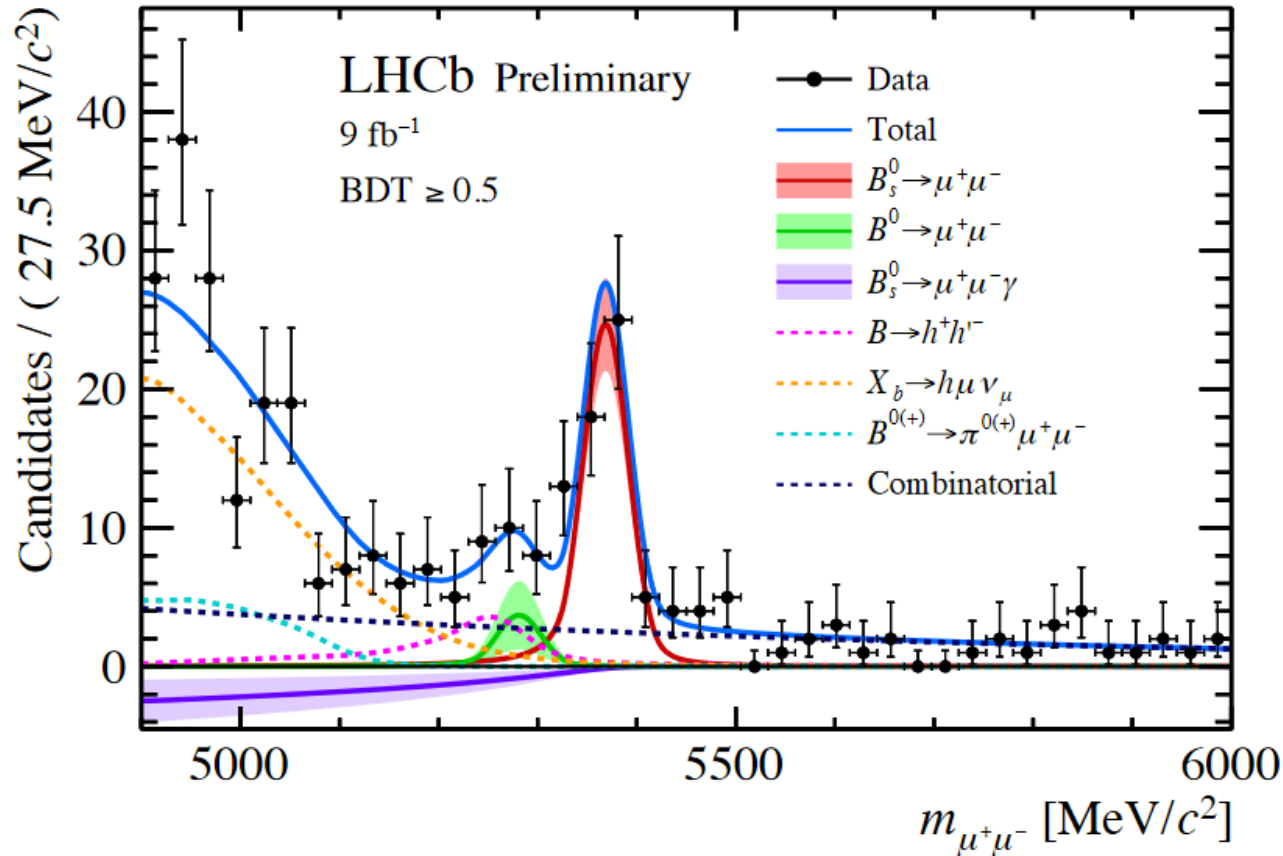
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) \times 10^9 = 3.27^{+0.12}_{-0.16}.$$



# Part II — $B_s \rightarrow \mu\mu$ (ex. of LHCb-PAPER-2021-007)



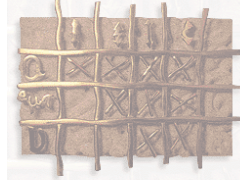
## • Results:



$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) \times 10^9 = 3.09^{+0.46}_{-0.43} {}^{+0.15}_{-0.11}, \quad \text{Exp.}$$

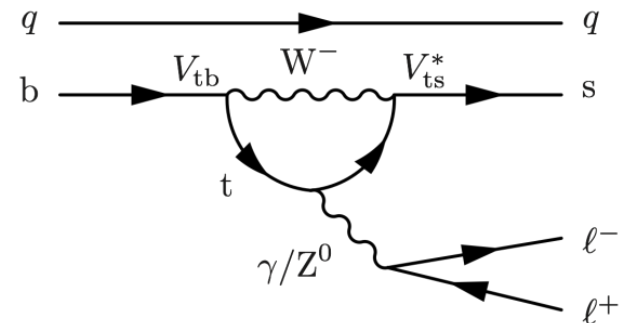
$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) \times 10^9 = 3.27^{+0.12}_{-0.16}. \quad \text{SM.}$$

## Part II — $b \rightarrow s \mu \mu$ and $b \rightarrow s e e$



- Not an annihilation, two quarks left in the final state
- This defines an ensemble of possible decays to study: since LHCb is the place to look at and that charged particles are preferred, one has

- $B^+ \rightarrow K^+ \ell \ell$ ,  $B^+ \rightarrow K^{*+} \ell \ell$  ( $K^{*+} \rightarrow K_S \pi^+$ )
- $B^0 \rightarrow K^{*0} \ell \ell$
- $B_s \rightarrow \phi \ell \ell$
- $\Lambda_b \rightarrow \Lambda^* \ell \ell$  ( $\Lambda^* \rightarrow p K^-$ )

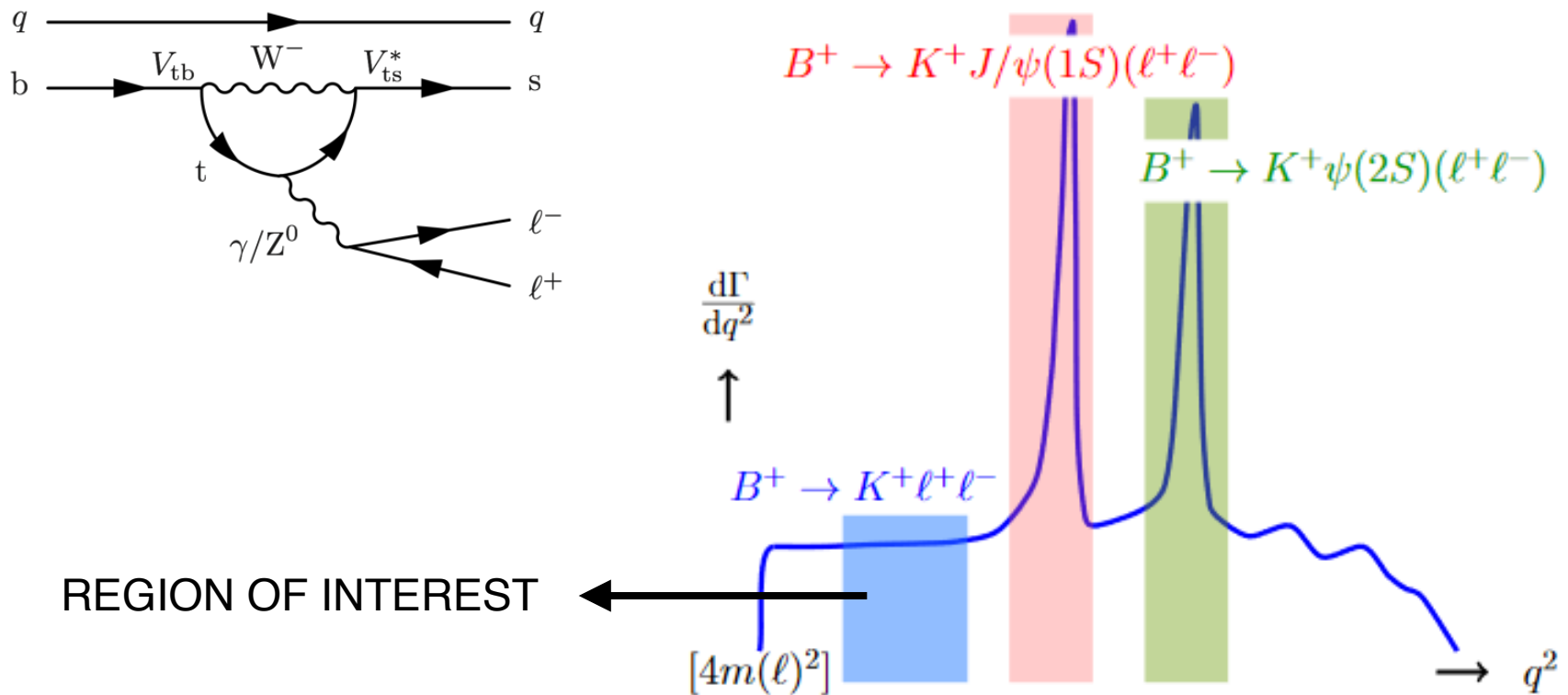


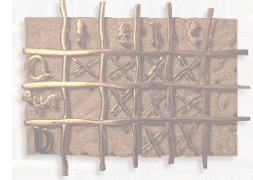
- One can:
  - Compare rates into electrons with muons (Test of the Lepton Flavour Universality LFU — theoretically clean)
  - Analyse the angular distributions of the decays with muons.
  - Measure the branching fractions

## Part II — $b \rightarrow s \mu \mu$ and $b \rightarrow s e e$



The key physics quantity to study the decay is the invariant-mass of the dilepton pair, so-called  $q^2$  :





## Part II — $b \rightarrow s\mu\mu$ and $b \rightarrow see$ — LFU tests

- It consists in comparing the rates of the decays into electrons and muons.
- Theoretical prediction is safe and straightforward (close to unity, mild dependence as function of  $q^2$ ).
- Experimental measurements (at least at LHCb) is challenging: electrons and muons are not selected with the same triggers, the reconstruction of the electrons suffer from bremsstrahlung photons etc ...
- Yet, one can measure double ratios ! *e.g.* :

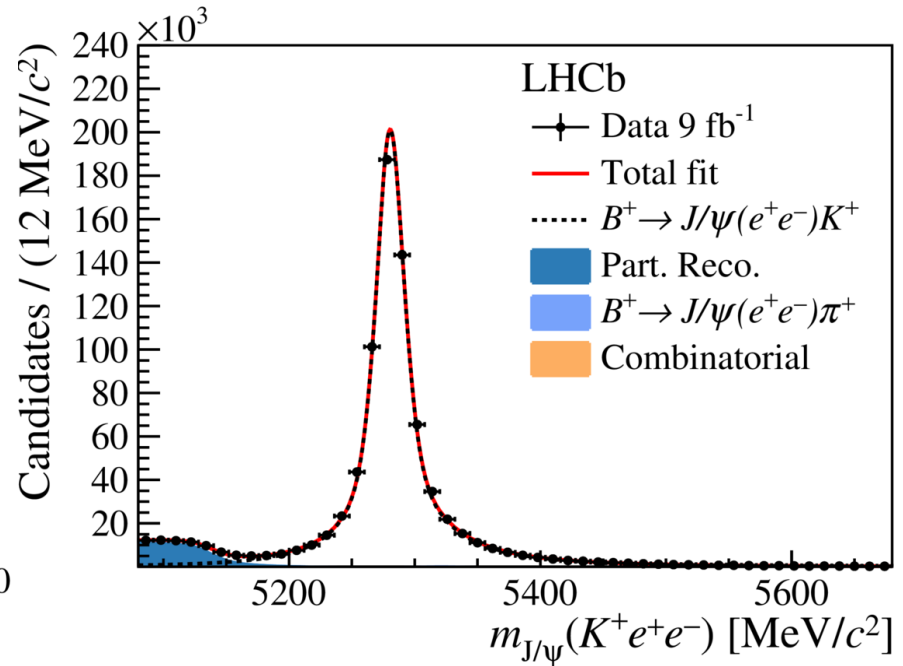
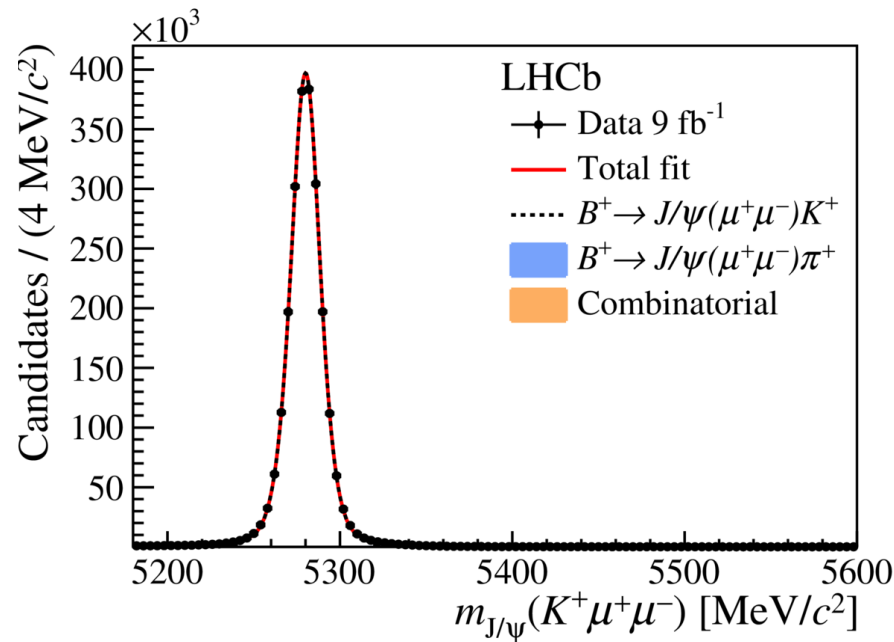
$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(\mu^+ \mu^-))} \bigg/ \frac{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{\mathcal{B}(B^+ \rightarrow K^+ J/\psi(e^+ e^-))}$$

- Factors out efficiency systematics. Residual mismodellings calibrated with data control samples. J/Psi does not decay weakly.

## Part II — $b \rightarrow s \mu \mu$ and $b \rightarrow s e e$ — LFU tests



### Calibration modes:



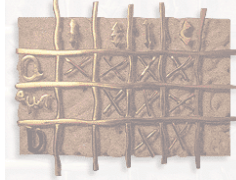
The ratio of the two must be unity.

$$r_{J/\psi} = 0.981 \pm 0.020 \text{ (stat + syst)}$$

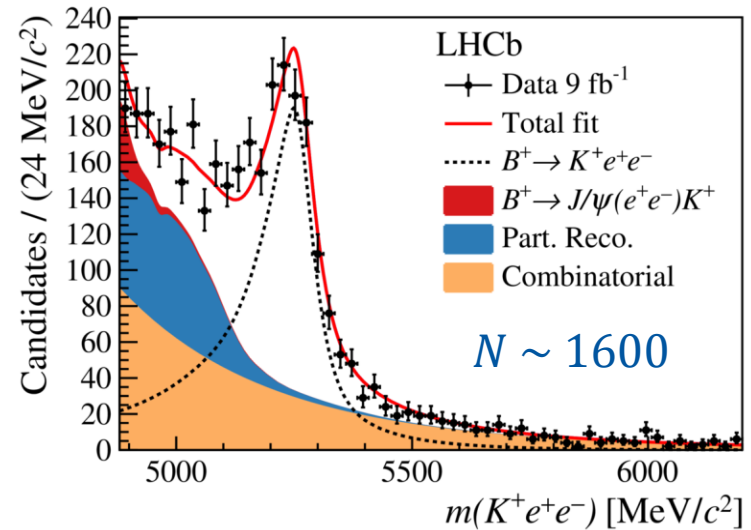
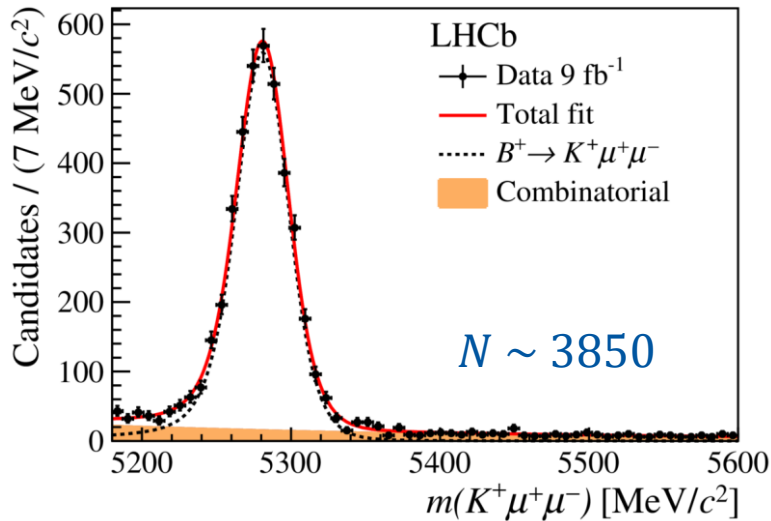
Double ratio with Psi(2S) can be determined

$$R_{\psi(2S)} = 0.997 \pm 0.011 \text{ (stat + syst)}$$

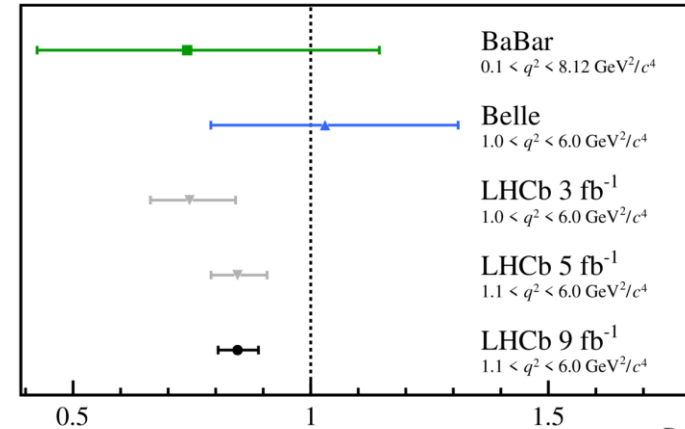
# Part II — LFU tests (ex. of LHCb-PAPER-2021-004)



## Results:



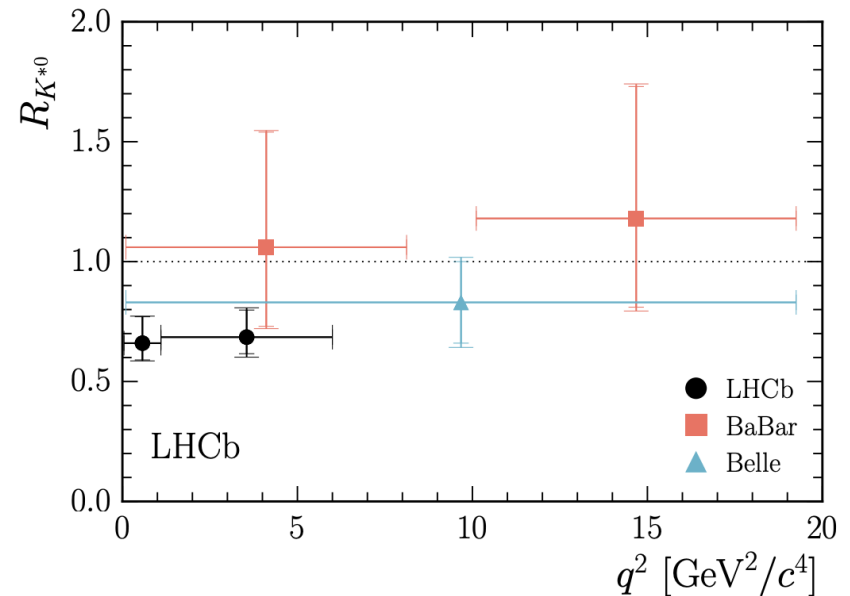
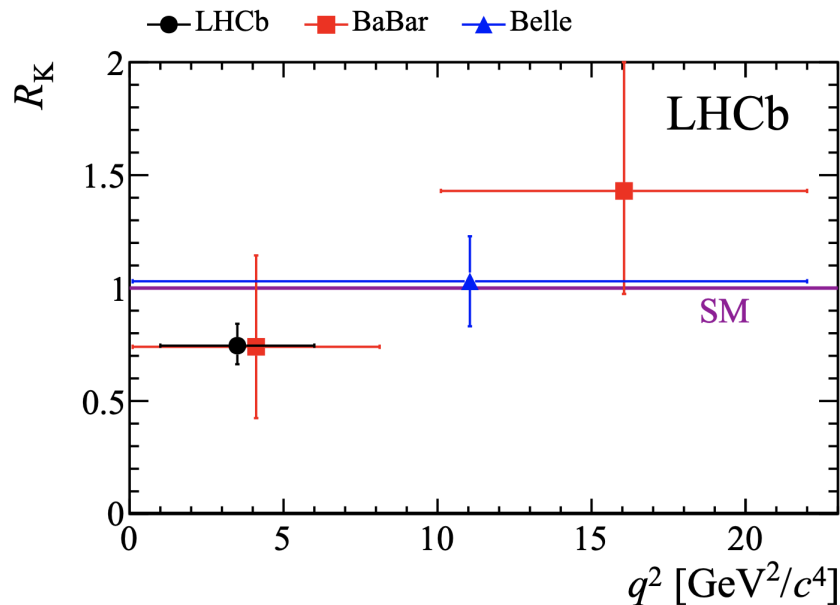
$$R_K = 0.846^{+0.042}_{-0.039} {}^{+0.013}_{-0.012}$$



## Part II — LFU tests (bigger picture)



- Results: same pattern observed previously in  $R_{K^*}$  (and  $R_{\rho K}$ )

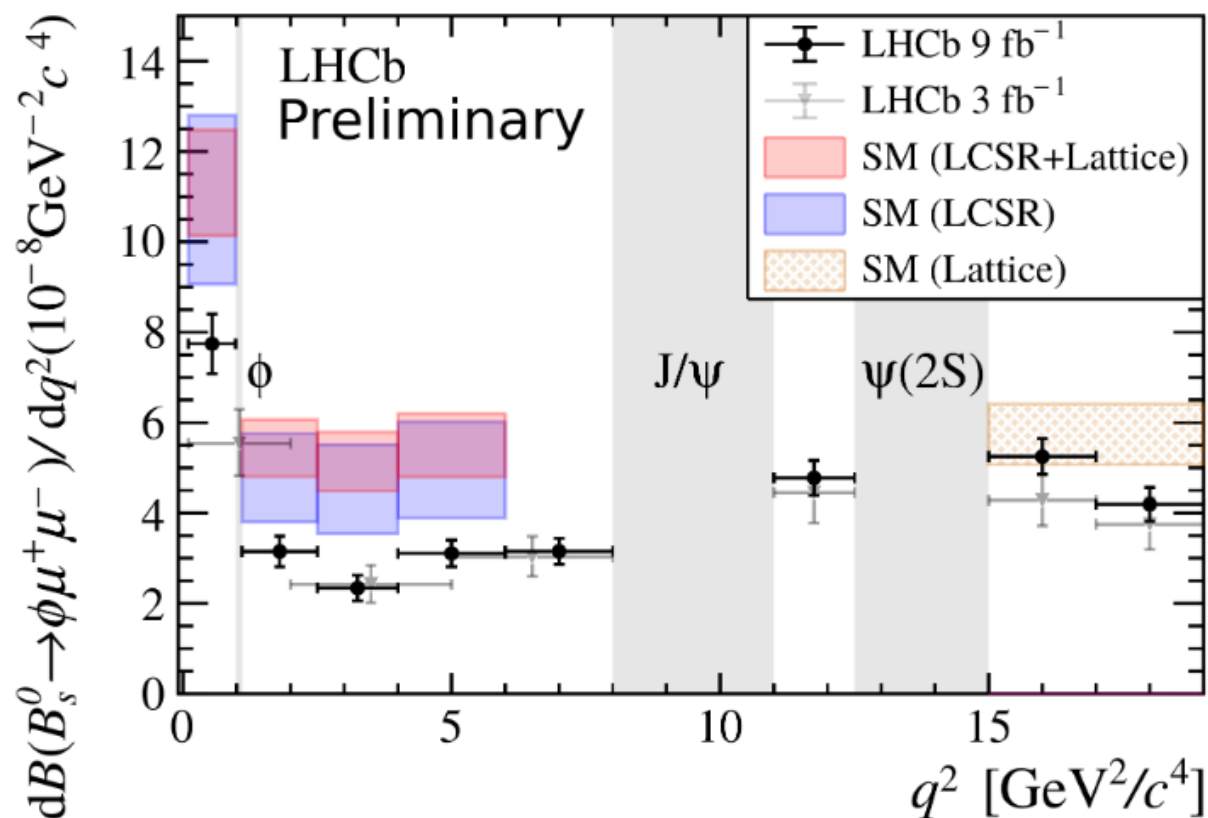


- Demands a further scrutiny. Updates are expected soon. Belle II will enter the game in the next years.
- And it comes on existing anomalous terrain.

## Part II — Branching fractions



- Comment: absolute branching fraction prediction precisions are plagued by hadronic parameters uncertainties.
- Results: yet, a consistent pattern is observed here as well. The muon rate is systematically lower than the prediction. A spring result as example.

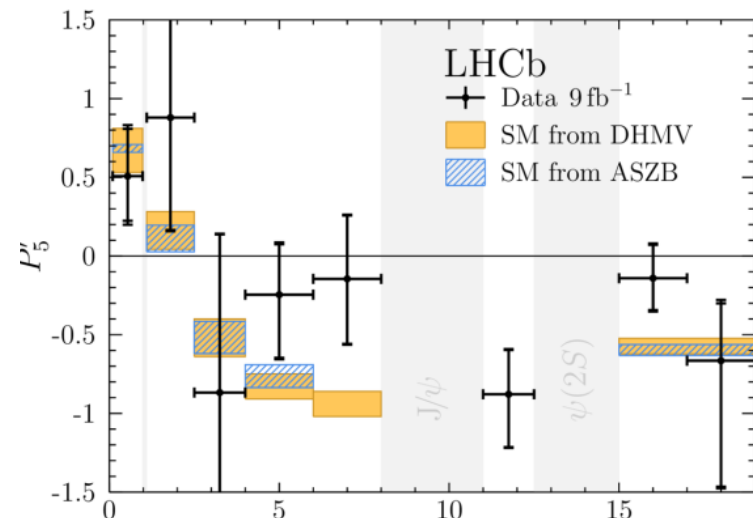
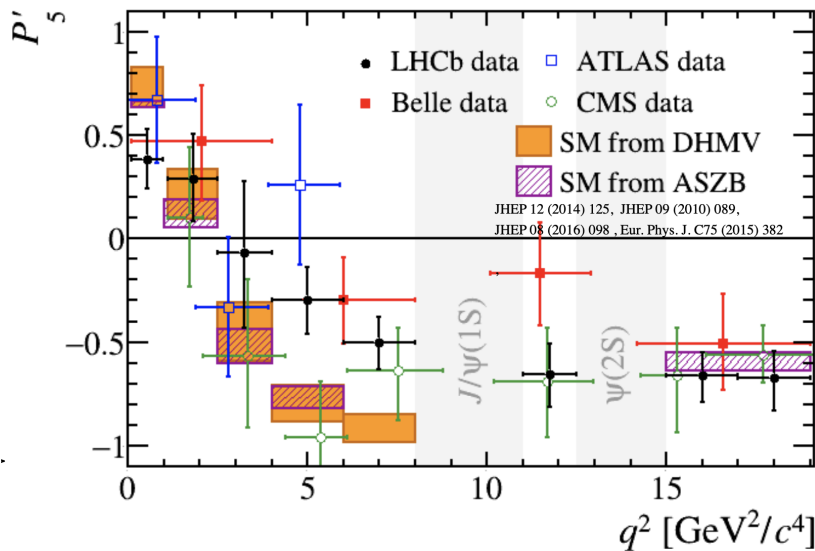




## Part II — Angular analyses



- Comment: again significant QCD uncertainties in the prediction. Immense efforts were spent to factor most of them out though.
- 
- Results: another place where tensions with the SM arise.



## Part II — $b \rightarrow c \tau \nu$ decay rates

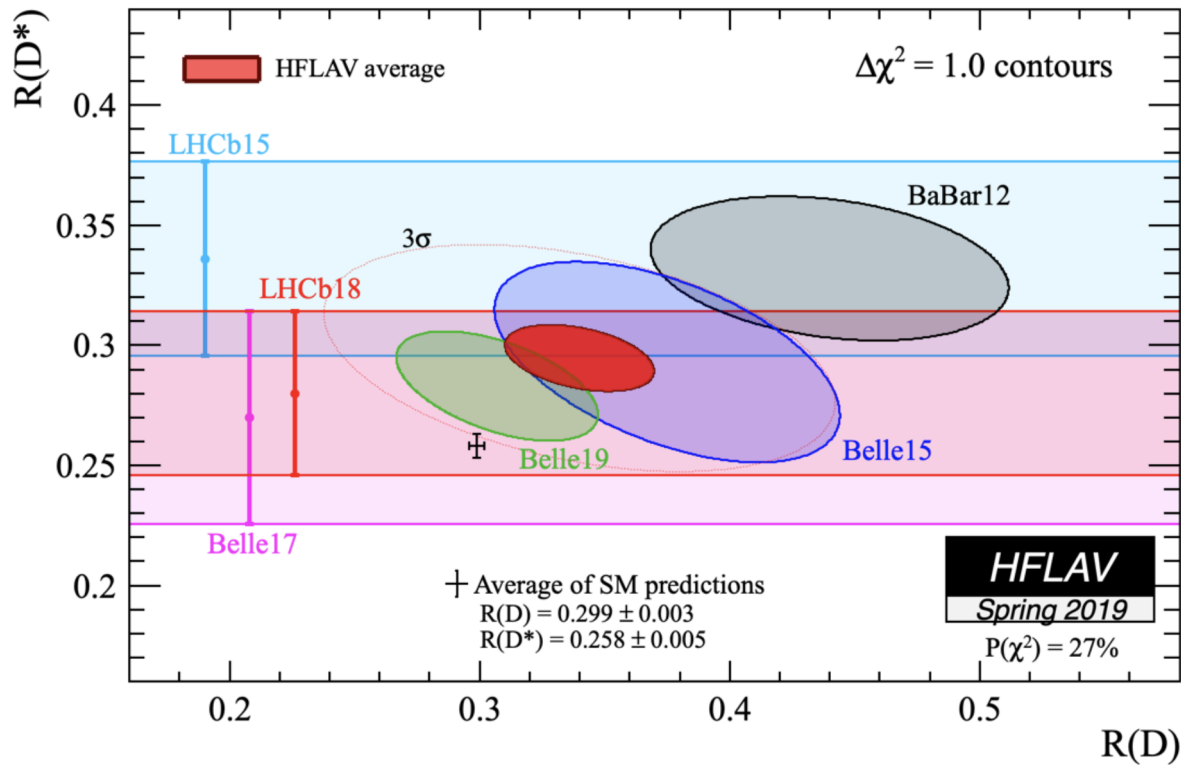


- Definition:

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$

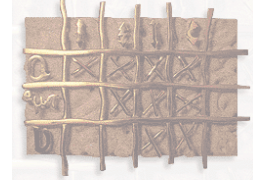
- Results:

$$R_D(\text{th}) = 0.299 \pm 0.003 ; R_D(\text{exp}) = 0.340 \pm 0.030,$$
$$R_{D^*}(\text{th}) = 0.258 \pm 0.005 ; R_{D^*}(\text{exp}) = 0.295 \pm 0.014.$$



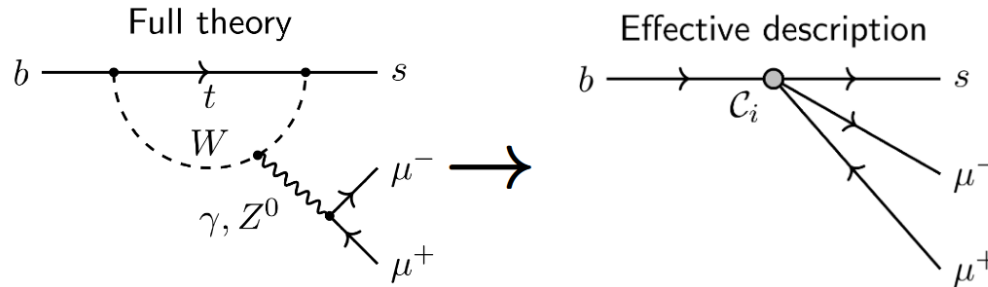
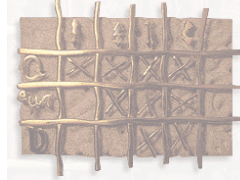
- Interpretation: if true, BSM Physics coupled preferentially to tau.

## Part II — Rare decays anomalies interpretation



- There are anomalies in  $b \rightarrow c \tau \nu$  and  $b \rightarrow s \mu \mu$  transitions.
- The level of these anomalies is about three standard deviations departures from the SM predictions.
- Each anomaly can receive a more or less appealing phenomenological interpretation.
- Instead, can we aim at qualifying the departure in a model-independent way ? For instance, asking the question: are these anomalies consistent?
- The answer is YES ! By means of Effective Field Theory. It consists of the SM Lagrangian + non-renormalisable operators (actually dimension 6 operators at first). This approach is valid as far as one can integrate out the heavy fields.

# Part II — Rare decays anomalies interpretation



- The relevant operators are:

$$\mathcal{O}_7^{ij} = \frac{e m_{d_j}}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} P_R d_j) F^{\mu\nu},$$

$$\mathcal{O}_9^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \gamma^\mu P_L d_j) (\bar{\ell} \gamma_\mu \ell')$$

$$\mathcal{O}_{10}^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \gamma^\mu P_L d_j) (\bar{\ell} \gamma_\mu \gamma_5 \ell'),$$

$$\mathcal{O}_S^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i P_R d_j) (\bar{\ell} \ell'),$$

$$\mathcal{O}_P^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i P_R d_j) (\bar{\ell} \gamma_5 \ell'),$$

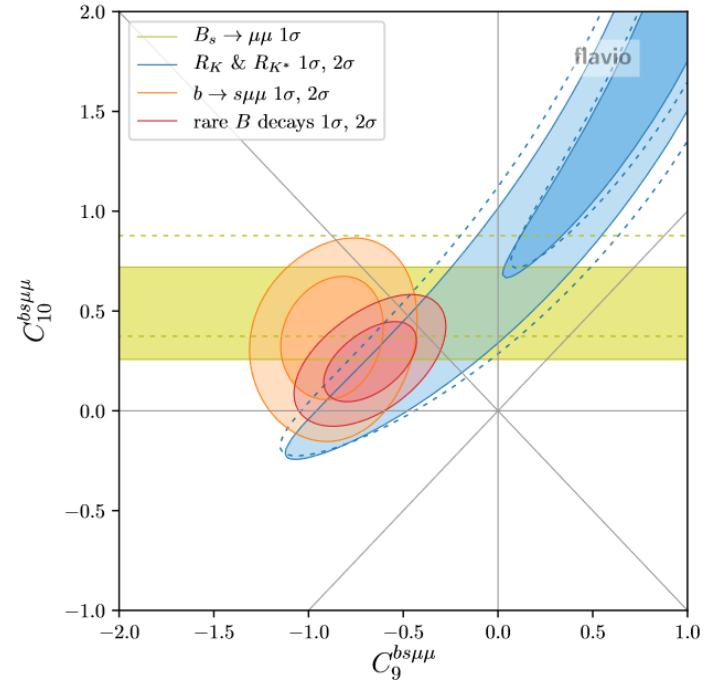
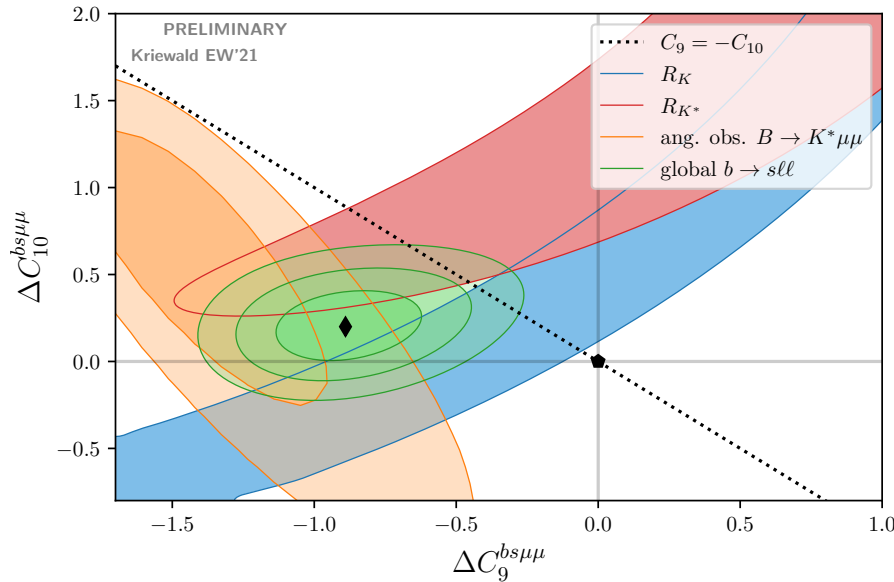
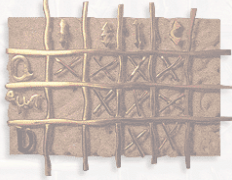
$$\mathcal{O}_T^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} d_j) (\bar{\ell} \sigma^{\mu\nu} \ell'),$$

$$\mathcal{O}_{T5}^{ij;\ell\ell'} = \frac{e^2}{(4\pi)^2} (\bar{d}_i \sigma_{\mu\nu} d_j) (\bar{\ell} \sigma^{\mu\nu} \gamma_5 \ell')$$

- The effective operators are coming with effective coupling constants, denoted the Wilson coefficients (fully calculable for their SM component, careful at the running with the scale  $\mu$ )

$$\mathcal{L}_{\text{eff}} \propto \frac{4G_F}{\sqrt{2}} \sum_k C_k(\mu) \mathcal{O}_k(\mu).$$

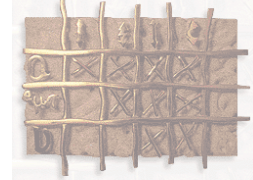
# Part II — Rare decays anomalies interpretation



- Multiple global fits in the literature (I picked here 2012.13241 and arXiv:2103.13370, many others around). Significance of the departure with SM flirts with 5 standard deviations.
- They all tell the same: the anomalies provide a consistent pattern and require a modification of the SM  $C_9$ .

## Part III — Conclusion and outlook

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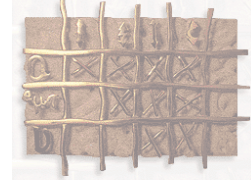
- The observation of  $P$  and  $CP$  violation has shaped our understanding of the elementary interactions.
- All the  $CP$ -conserving and  $CP$ -violating observables are accounted for in the Kobayashi-Maskawa paradigm, embodied in the SM. This makes a pillar of the SM.
- A single  $CP$ -violating phase allows to comprehend the meson decays and mixing asymmetries phenomena. The advent of Belle II and the continuation of LHCb will allow to enter the precision era and test further the paradigm (and hopefully shake it).
- Meanwhile, rare decays of heavy-flavoured particles have been analysed meticulously. Anomalies are reported and find an appealing (common) explanation. Here again, the advent of Belle II and the continuation of LHCb shall unravel BSM Physics if the anomalies stand.

## Part III — Conclusion and outlook

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- It was thought by numbers of the HEP community that the supersymmetry would appear at the turn-on of the LHC. This did not happen. A “light” narrow scalar was indeed discovered but it looks \*to date\* like the Brout-Englert-Higgs boson of the Standard Model.
- The experimentalists among you have entered the field at exciting times. Orphan of the no-lose theorem, the path towards the answers to fundamental questions will be again shaped by experimental breakthroughs.
- Flavour Physics (and precision physics) is a key player in this scrutiny, with the emerging anomalies we have discussed.
- The next generation experimental tools are presently thought of. I would have loved to talk to you in front of the Nazare waves about the Future Circular Collider 100 km long european-based project ! **Looking forward the occasion to meet in person.**



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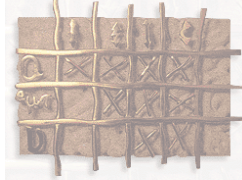
**Back-ups / Les renforts**  
**(The complete introduction about**  
***P* and *CP* symmetries follows)**





## A more detailed outline

1. Introduction: setting the scene. History and recent past of the parity violation experiments. The discovery of the  $CP$  violation.
2. Few elements about CKM. Machine and experiments. Main observables and measurements relevant to study  $CP$  violation.
3. The global fit of the SM: CKM profile.
4. New Physics exploration with current data: two examples.



Some authoritative literature about the lecture :

- ✓ Lee, T.D. and Yang, C.N. (1956) *Question of parity conservation in weak interactions*, Phys. Rev. 104(1): 254-258 (1956).
- ✓ The  $^{60}\text{Co}$  experiment: Phys. Rev. 105, 1413-1414 (1957)
- ✓ The  $^{152}\text{Eu}$  experiment: Phys. Rev. 109, 1015 (1958).



## The foundations

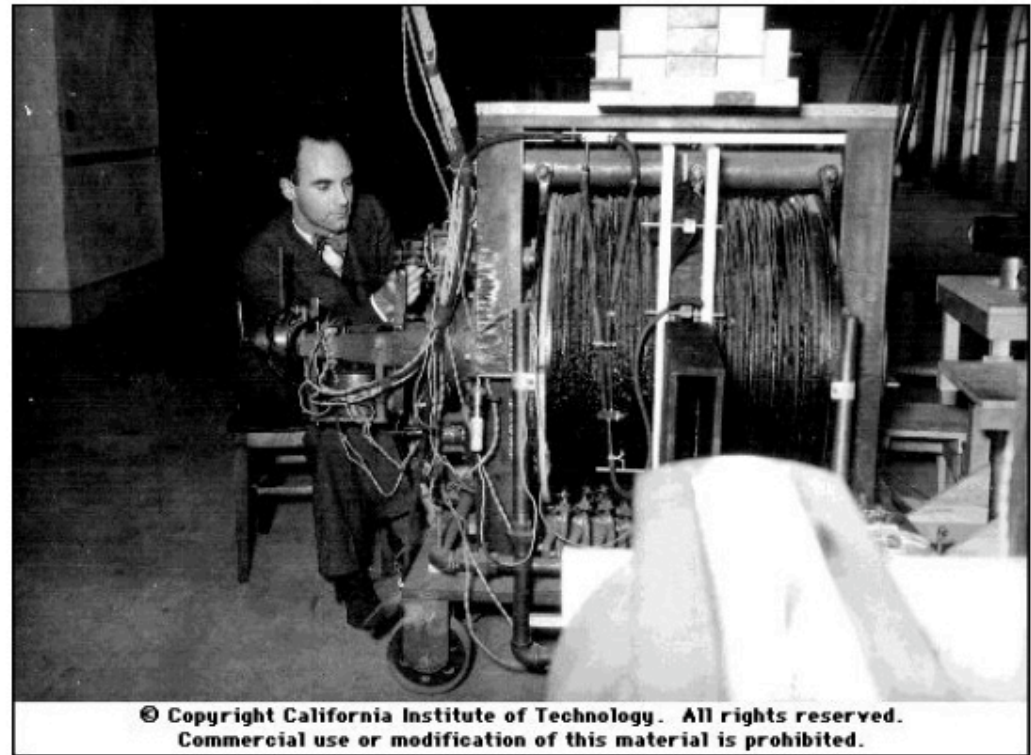
1. Antimatter discovery – C. Anderson.
2. The parity violation measurement – C.S. Wu.
3. The parity violation measurement – Goldhaber et al.
4. The emergence of the V-A theory. Premises of  $SU(2)_L$ .
5. Recent parity violation measurements at LEP/SLD.
6. Selection of  $CP$  violation phenomena.



## Antimatter exists.

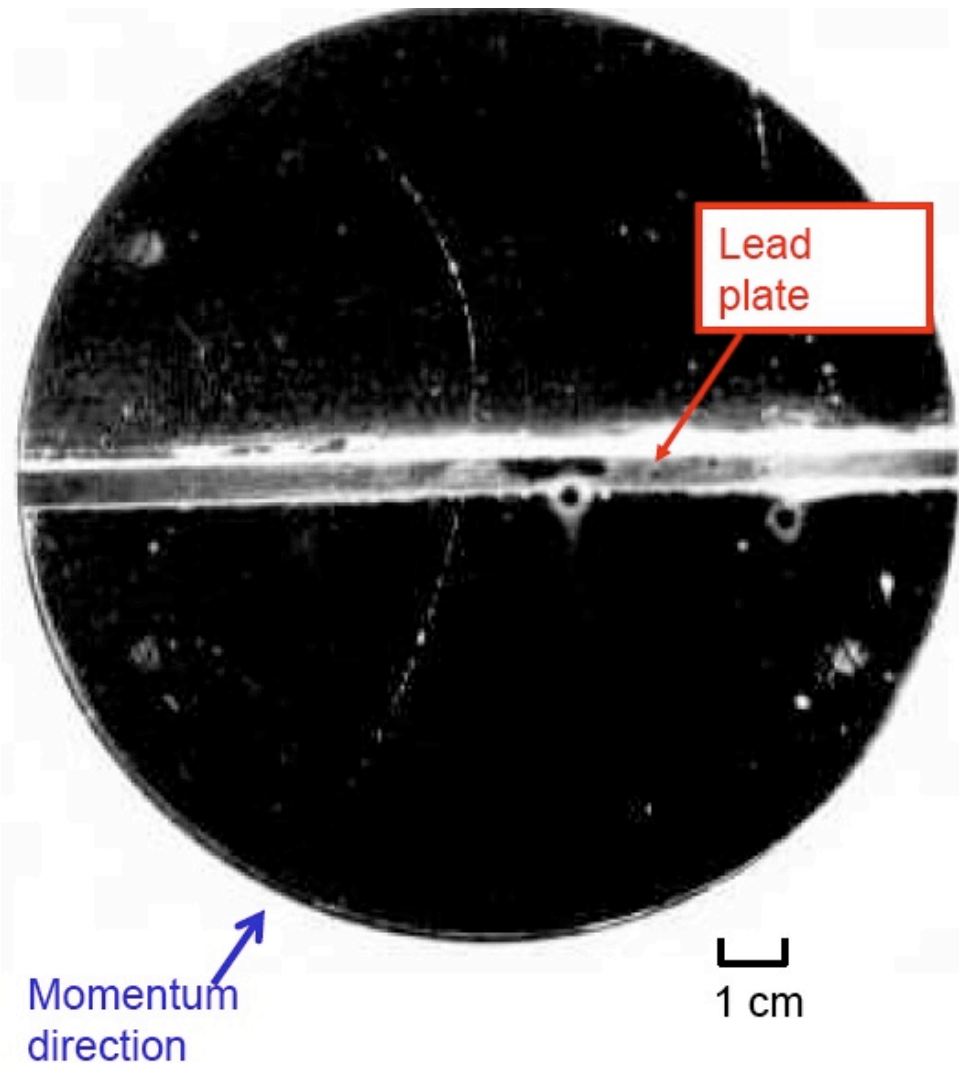
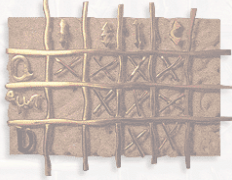
In 1929, P.A.M. Dirac solves the free motion of a relativistic spin 1/2 particle (electron or proton). It happened that there should exist a solution of negative energy, which he interpreted as an antiparticle.

$$\text{Dirac spin } 1/2 : (i\gamma^\mu \partial_\mu - m)\psi = 0$$



Anderson at work: discovery of the positron in 1932.

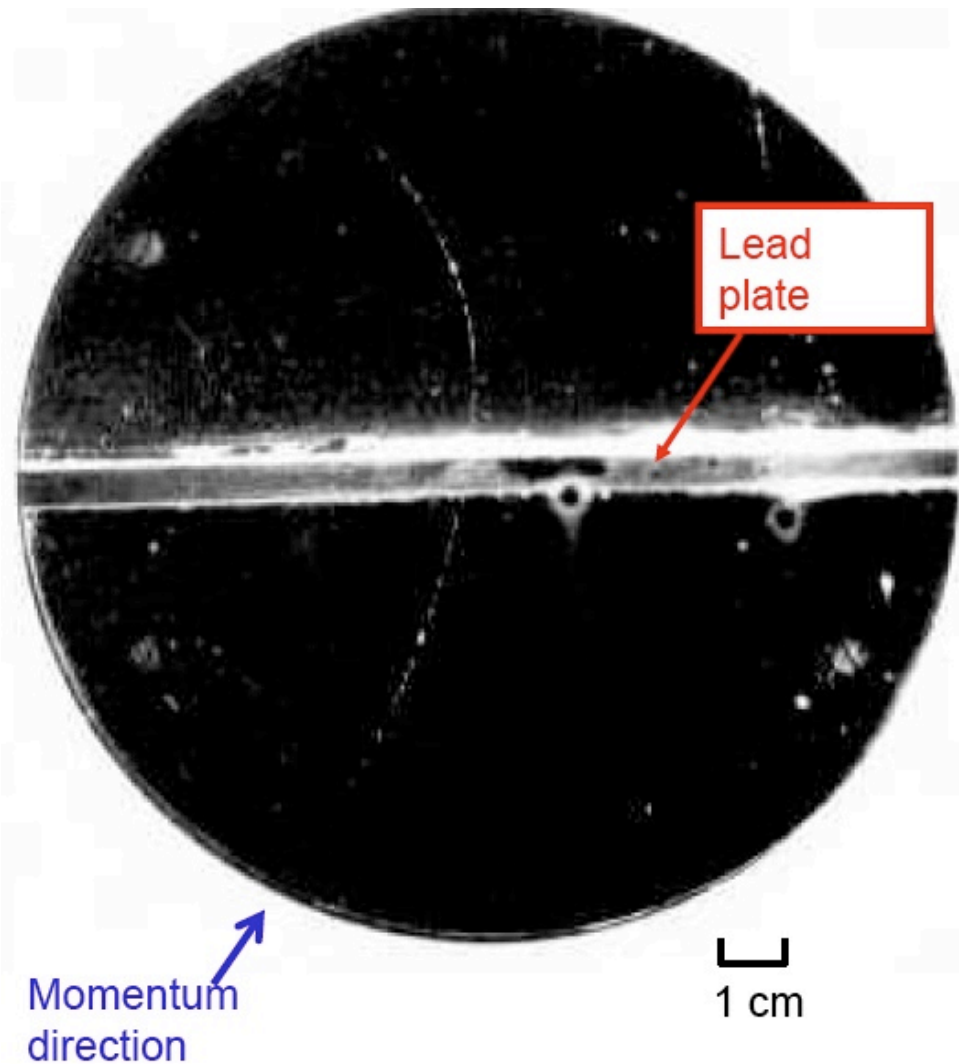
# Parity symmetry breaking



# Parity symmetry breaking



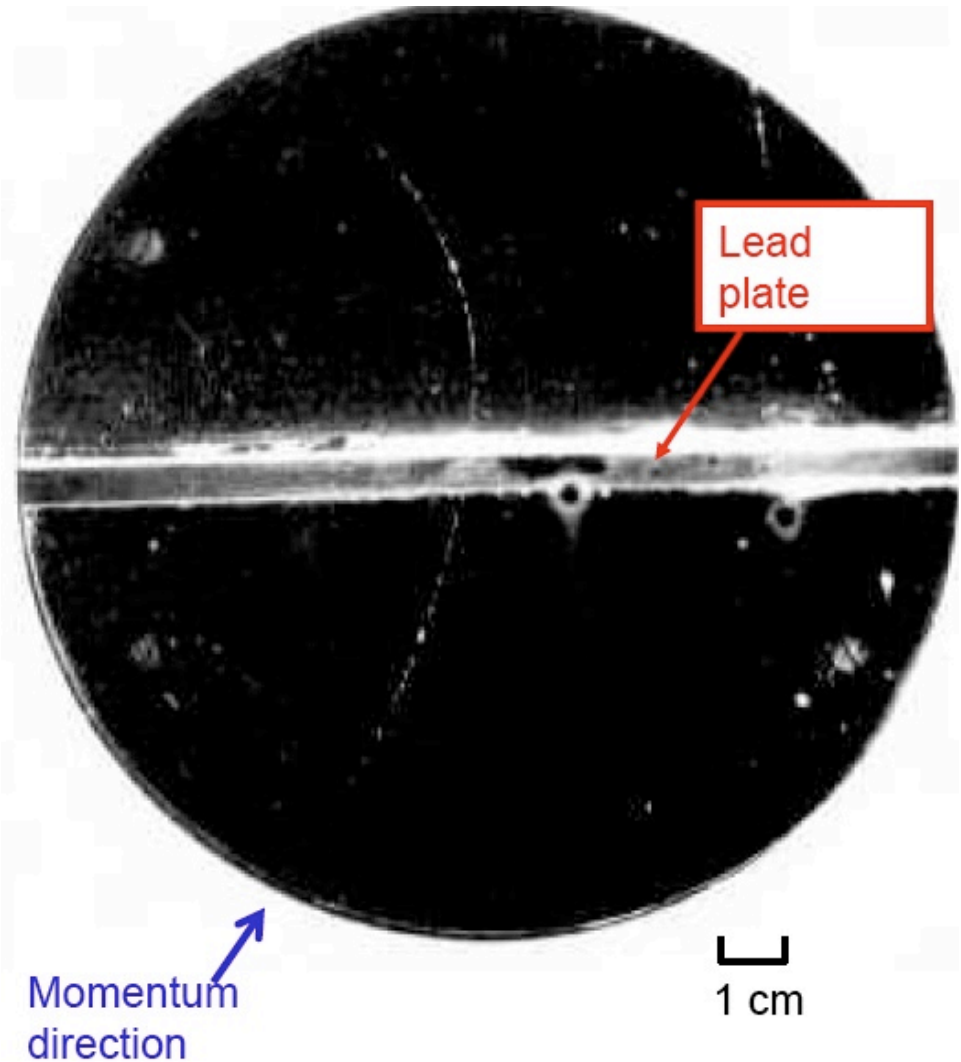
- The radius of curvature is smaller above the plate. The particle is slowed down in the lead → the particle is incoming from the bottom.



# Parity symmetry breaking



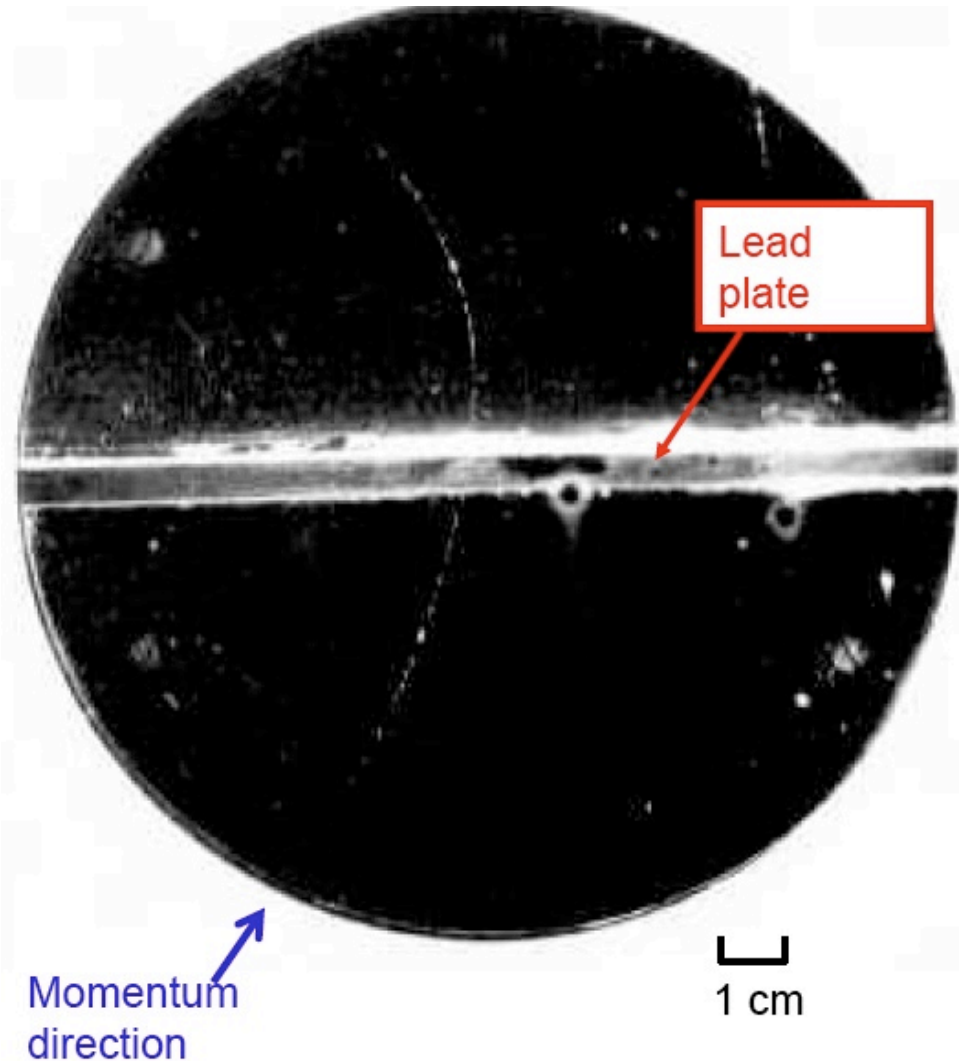
- The radius of curvature is smaller above the plate. The particle is slowed down in the lead → the particle is incoming from the bottom.
- The magnetic field direction is known:  
→ positive charge



# Parity symmetry breaking

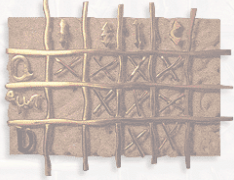


- The radius of curvature is smaller above the plate. The particle is slowed down in the lead → the particle is incoming from the bottom.
- The magnetic field direction is known:  
→ positive charge
- From the density of the drops one can measure the ionizing power of the particle → minimum ionizing particle.

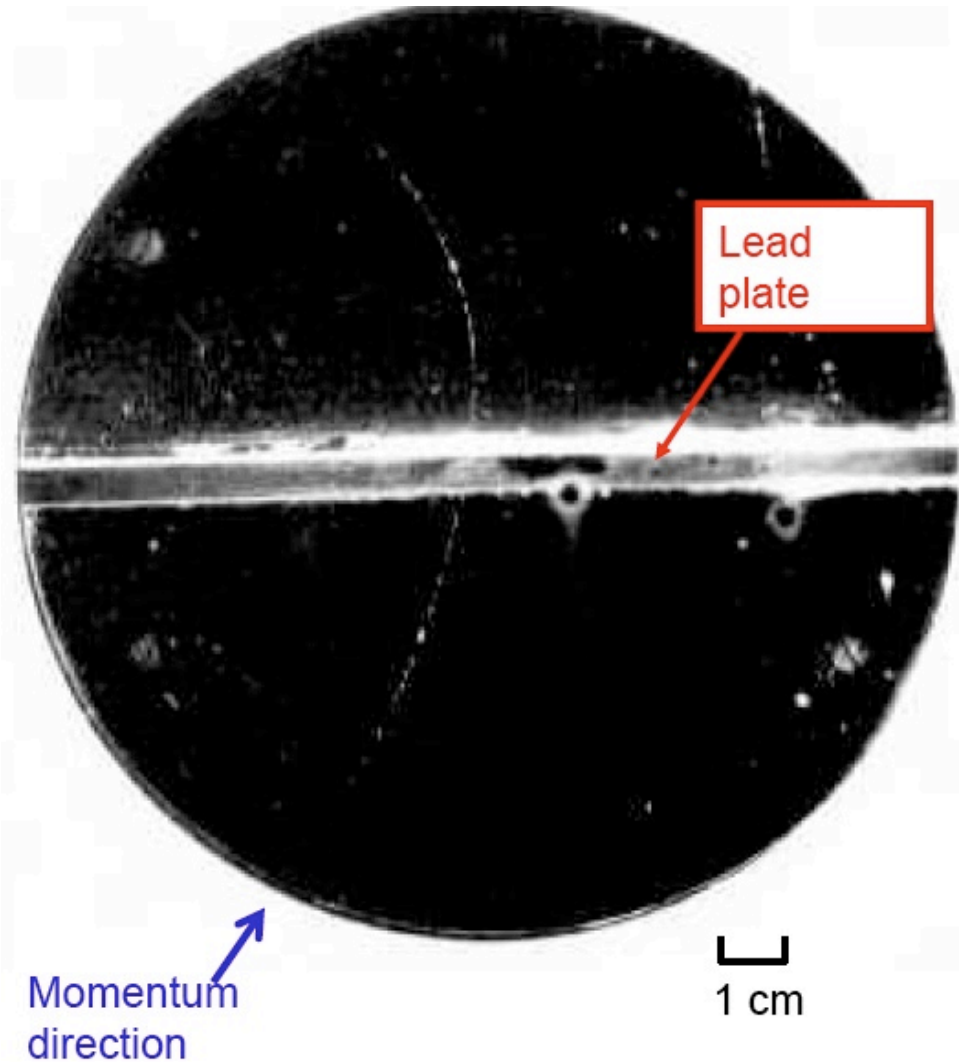




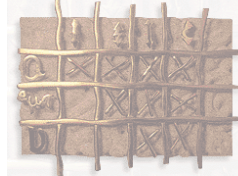
# Parity symmetry breaking



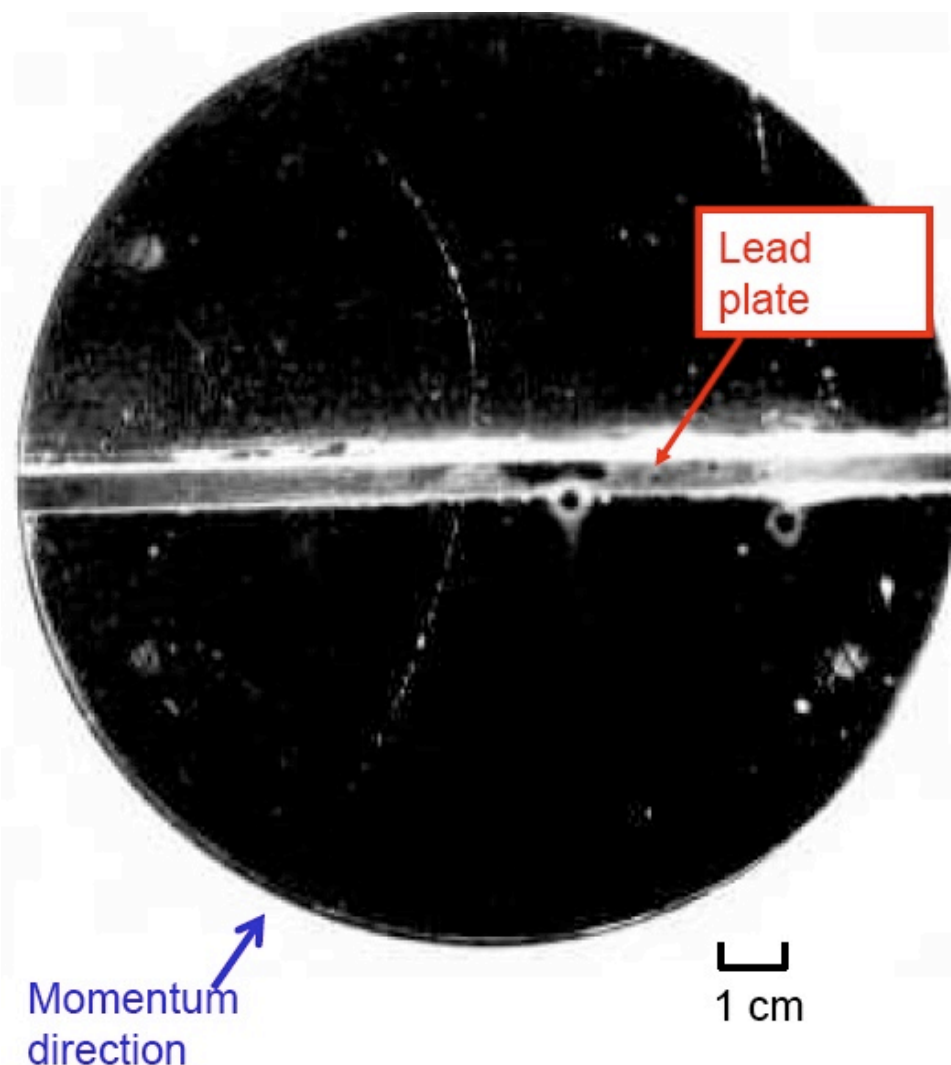
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- Similar ionizing power before and after the plate → same particle on the 2 sides.



# Parity symmetry breaking



- The radius of curvature is smaller above the plate. The particle is slowed down in the lead → the particle is incoming from the bottom.
- The magnetic field direction is known:  
→ positive charge
- From the density of the drops one can measure the ionizing power of the particle → minimum ionizing particle.
- Similar ionizing power before and after the plate → same particle on the 2 sides.
- Curvature measurement after the lead: particle of  $\sim 23\text{MeV}$  → it is not a non-relativistic proton because it would have lost all its energy after  $\sim 5\text{mm}$  (a track of  $\sim 5\text{ cm}$  is observed).





## Why $P$ must be a good symmetry

A variable describing a physical system is not an observable.

One can always find a mathematical transformation which lets the physical system invariant.

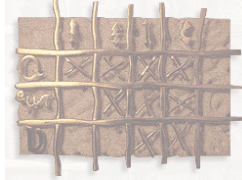
An observable is conserved.

# Parity symmetry breaking



## Why $P$ must be a good symmetry

Non-observable	Mathematical transf.	Conserved quantity
Absolute spatial position	Space translation	Momentum
Absolute time	Time translation	Energy
Absolute space direction	Rotation	Angular momentum
Absolute right	Space reflexion (mirror)	Parity
Electric charge sign	$e \rightarrow -e$	Charge conjugation
Absolute time sign	$t \rightarrow -t$	Time reversal
Relative phase between electric charges	Gauge transformation	The electric charge



## Evidence for $P$ violation

- ✓ Before 1956 : all interactions were thought to be invariant under parity operation
- ✓ It was (quite comprehensively) tested for strong and electromagnetic interactions.
- ✓ Lee and Yang proposed an experiment to test it for weak interaction after the theta / tau puzzle.
- ✓ Designed and performed in 1956 by C.S. Wu and collaborators
- ✓ The  $\text{Co}^{60}$  experiment : *Phys. Rev.* 105, 1413-1414 (1957)

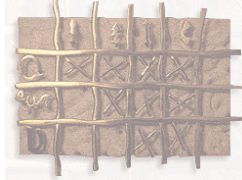




## Evidence for $P$ violation

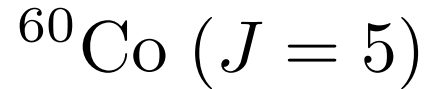
The magnetic field is directed to the right. The spins are aligned along to it.





## Evidence for $P$ violation

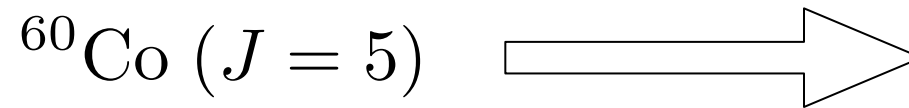
The magnetic field is directed to the right. The spins are aligned along to it.





## Evidence for $P$ violation

The magnetic field is directed to the right. The spins are aligned along to it.

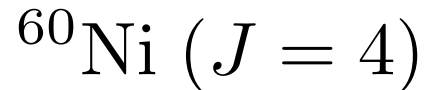
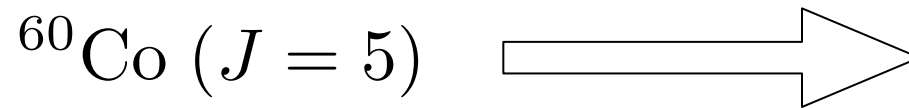


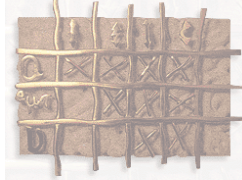




## Evidence for $P$ violation

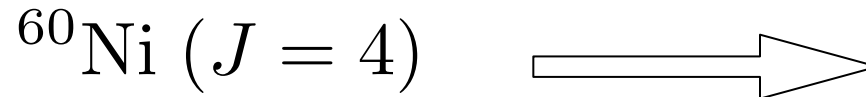
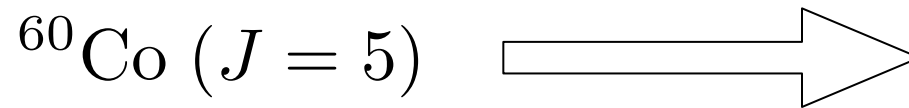
The magnetic field is directed to the right. The spins are aligned along to it.





## Evidence for $P$ violation

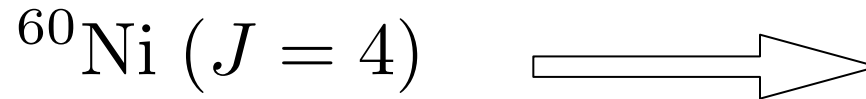
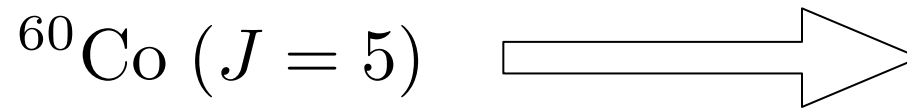
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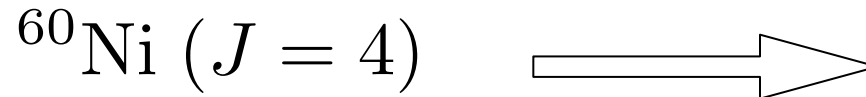
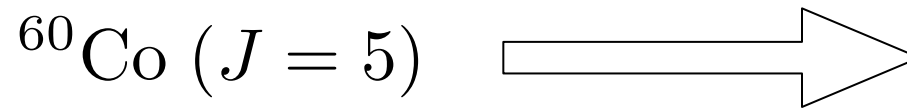
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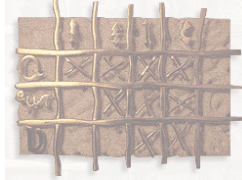




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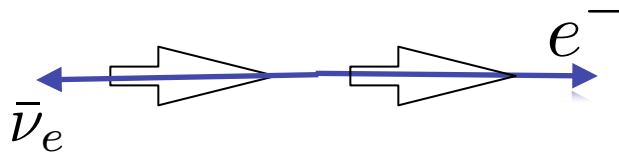
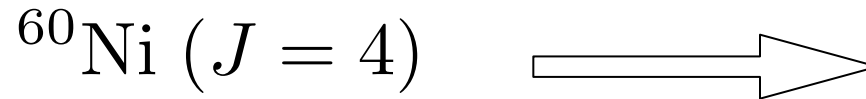
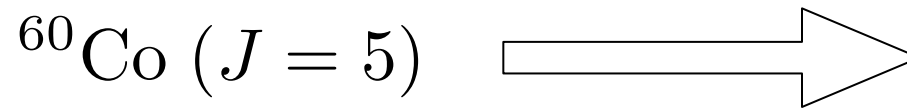
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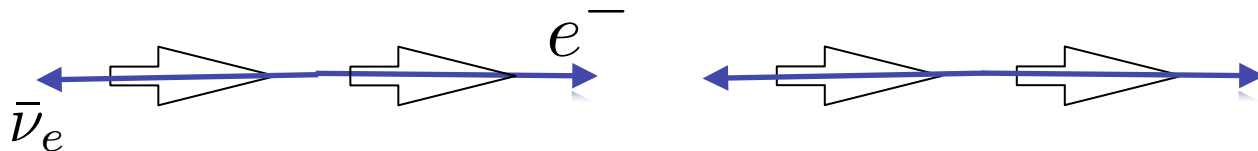
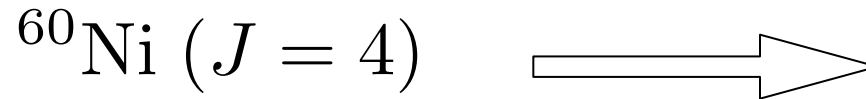
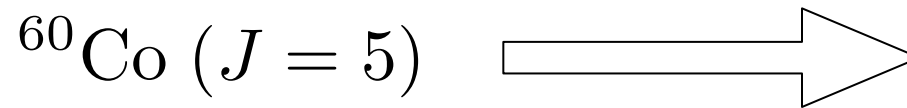
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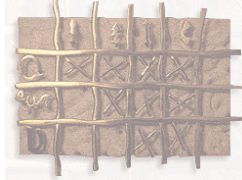




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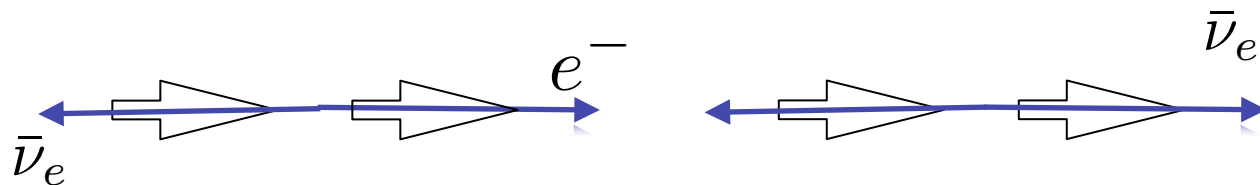
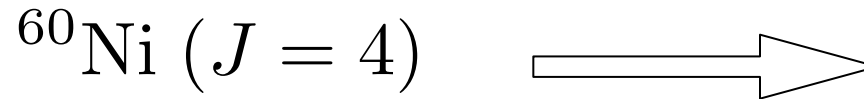
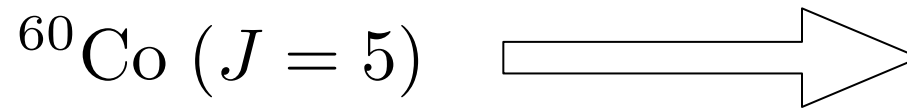
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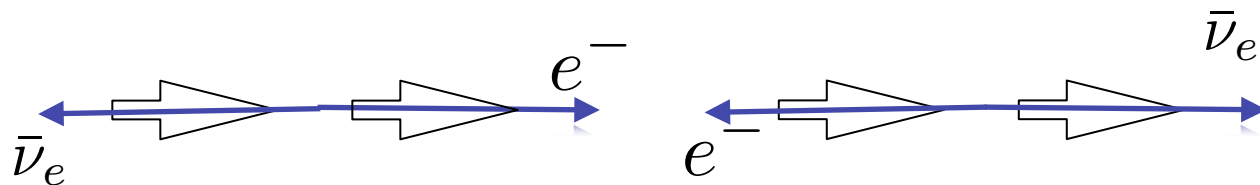
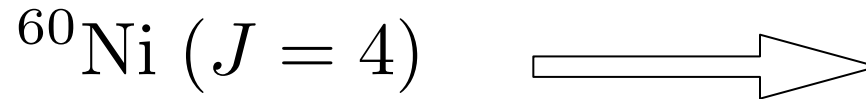
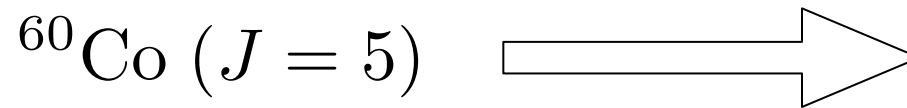
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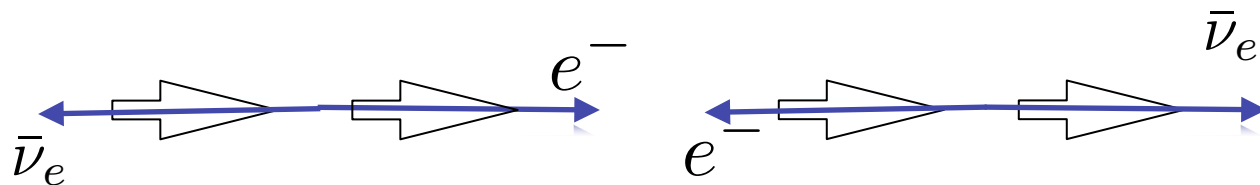
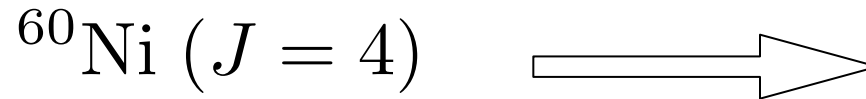
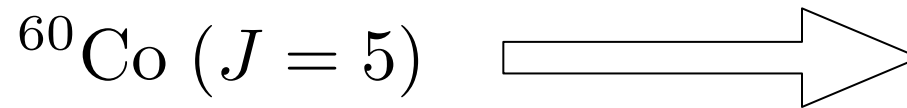




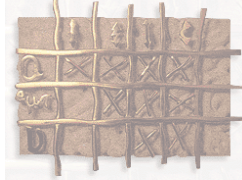


## Evidence for $P$ violation

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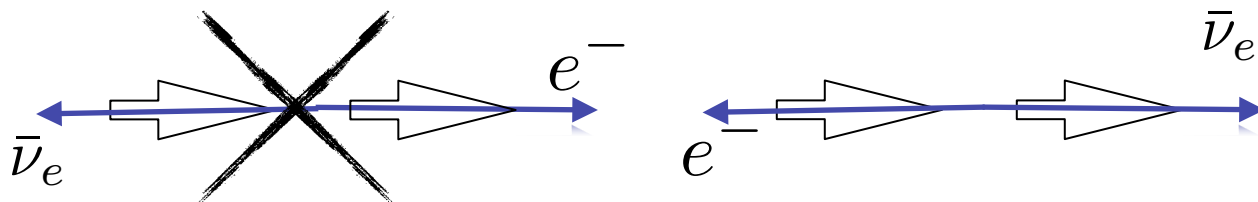
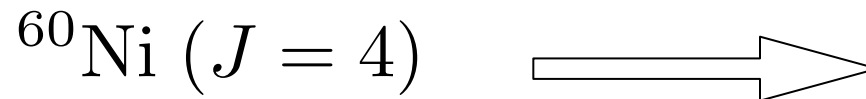
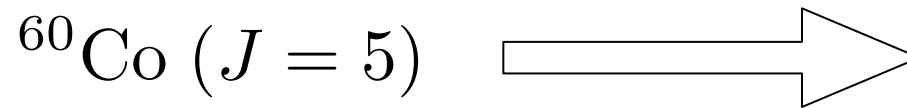


If the Nature can't distinguish left from right, then both decays are possible.

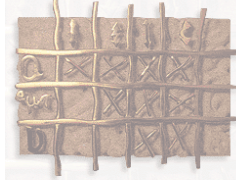


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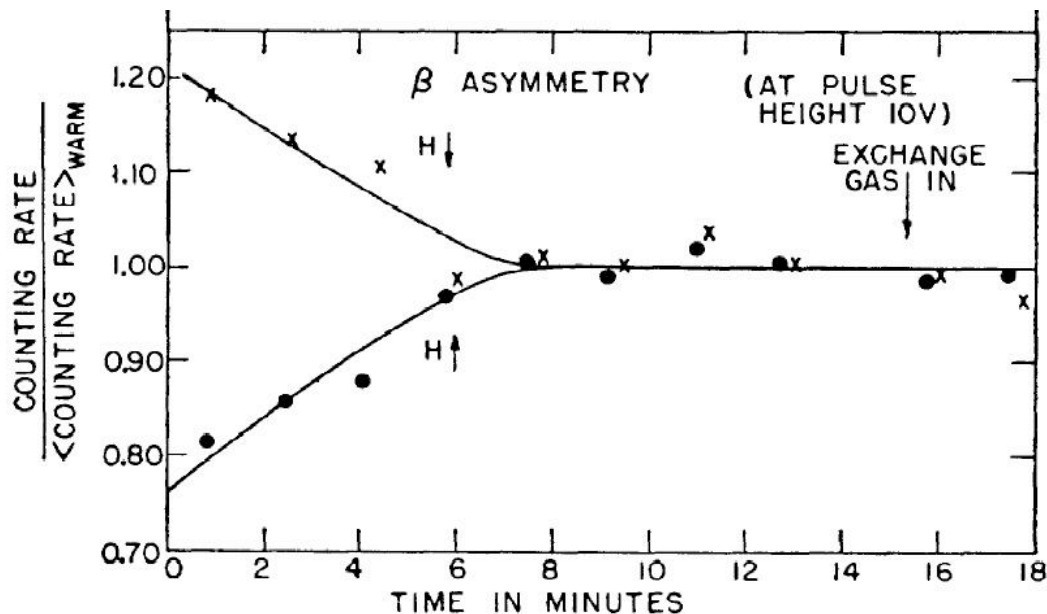


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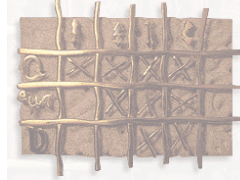
## Evidence for $P$ violation

- The magnetic field direction is changed and the rate for the electrons emission is measured in the two configurations. The asymmetry is reversed.



- The preferred chiral state is a right-handed anti-neutrino (left-handed electron).

# Parity symmetry breaking



## Evidence for $P$ violation

- The experiment was conducted during Christmas holidays 1956.
- The paper is published rightafter (2.5 pages).
- Lee and Yang receives the Nobel Prize in 1957 (sounds like this evidence was not overlooked).

### Experimental Test of Parity Conservation in Beta Decay\*

C. S. Wu, *Columbia University, New York, New York*

AND

E. AMBLER, R. W. HAYWARD, D. D. HOPPE, AND R. P. HUDSON,  
*National Bureau of Standards, Washington, D. C.*

(Received January 15, 1957)

IN a recent paper<sup>1</sup> on the question of parity in weak interactions, Lee and Yang critically surveyed the experimental information concerning this question and reached the conclusion that there is no existing evidence either to support or to refute parity conservation in weak interactions. They proposed a number of experiments on beta decays and hyperon and meson decays which would

provide necessary evidence for parity conservation. In beta decay, one could measure the distribution of the electrons coming from polarized nuclei. If an asymmetry in the distribution between  $\theta$  and  $180^\circ - \theta$  (where  $\theta$  is the angle of orientation of the parent nuclei and the direction of the electrons) is observed, it provides proof that parity is not conserved in beta decay. An asymmetry effect has been observed in the decay of  $^{60}\text{Co}$ .

It is known for some time that  $^{60}\text{Co}$  nuclei can be polarized by the Rose-Gorter method in cerium (balt) nitrate, and the degree of polarization can be measured by measuring the anisotropy of the gamma rays.<sup>2</sup> To apply this technique to the study of beta decay, two major difficulties had to be over-

### The Nobel Prize in Physics 1957



Chen Ning Yang  
Prize share: 1/2



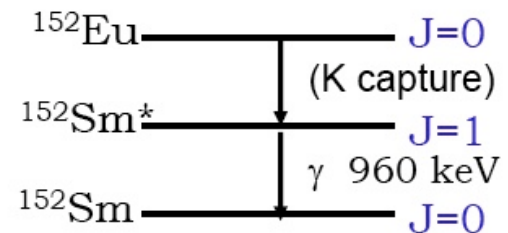
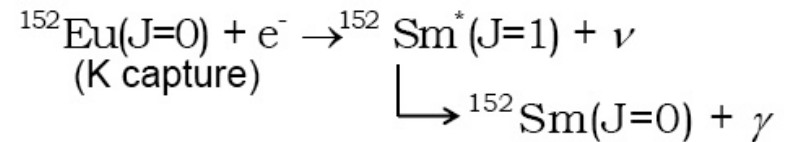
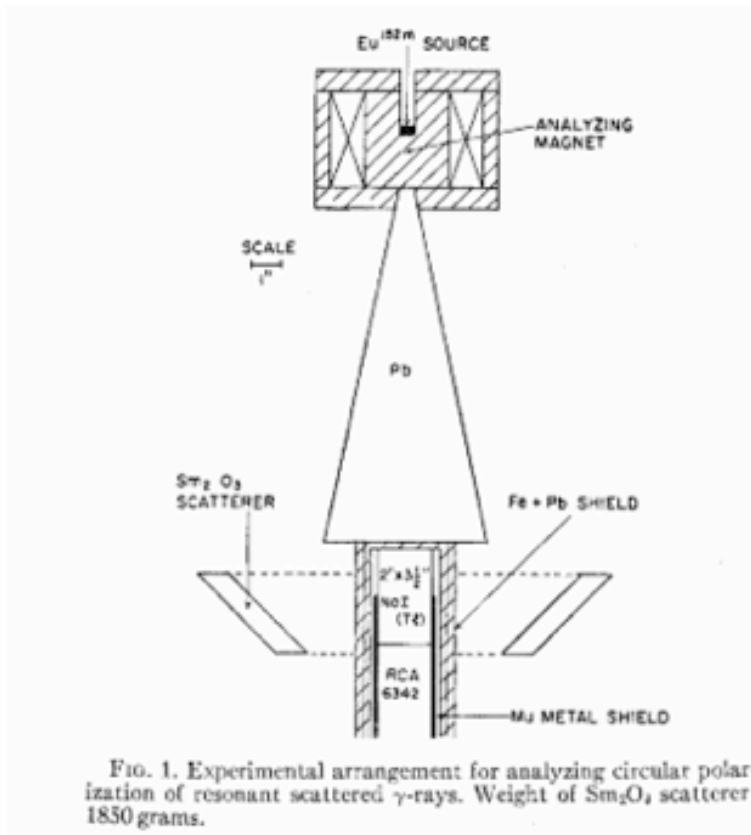
Tsung-Dao (T.D.) Lee  
Prize share: 1/2

The Nobel Prize in Physics 1957 was awarded jointly to Chen Ning Yang and Tsung-Dao (T.D.) Lee "for their penetrating investigation of the so-called parity laws which has led to important discoveries regarding the elementary particles"



## Neutrinos are left-handed

The Goldhaber experiment:



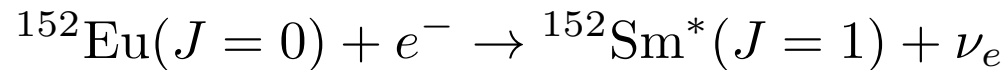
*The spins of all final states particles are constrained. The gammas aligned with the  $^{152}\text{Sm}$  are selected and their polarization is measured.*



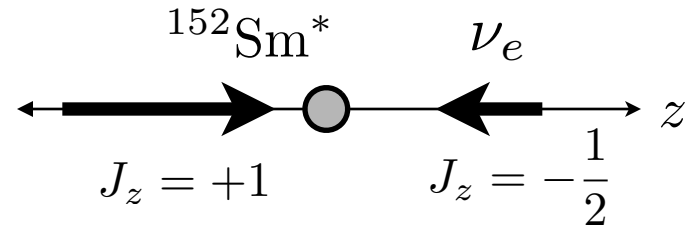
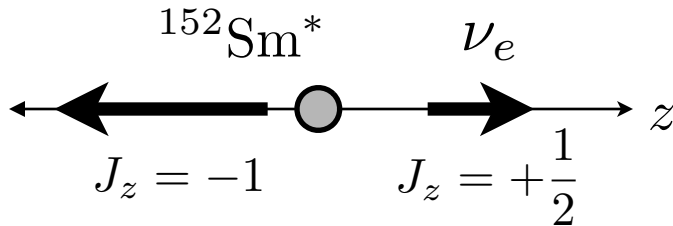
## Neutrinos are left-handed

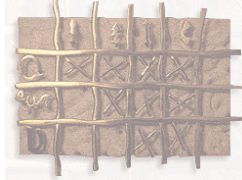
### The Goldhaber experiment:

We write down the spin constraints: the spin of the electron defines the initial and the final states. We shall end up with a one-half spin projection.



Two configurations are possible:





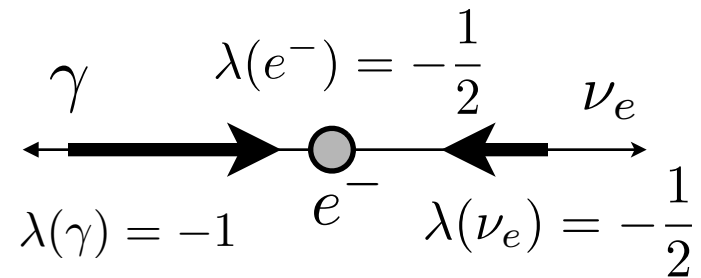
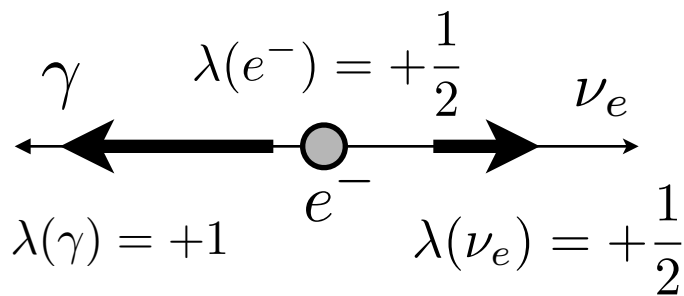
## Neutrinos are left-handed

The Goldhaber experiment:  $^{152}\text{Eu}(J = 0) + e^- \rightarrow ^{152}\text{Sm}^*(J = 1) + \nu_e$

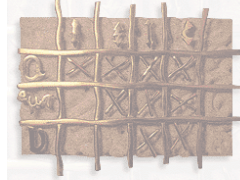
The above *K*-capture is followed by the excited Samarium decay:

$$^{152}\text{Sm}^*(J = 1) \rightarrow ^{152}\text{Sm}(J = 0) + \gamma$$

The gamma (as a massless vector boson) has two possible polarisations, which manifest in the two and only two possible configurations of helicities:



From the gamma polarization measurement, Goldhaber et al. show that only left-handed neutrinos are found (i.e, the second configuration) in  $\beta$  decays. Goldhaber, Grodzins, Sunyar, Phys. Rev. 109, 1015 (1958).



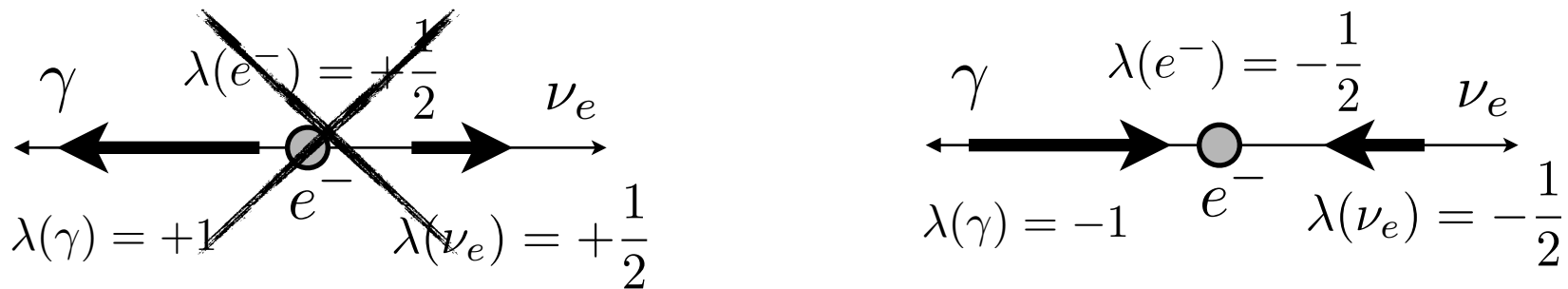
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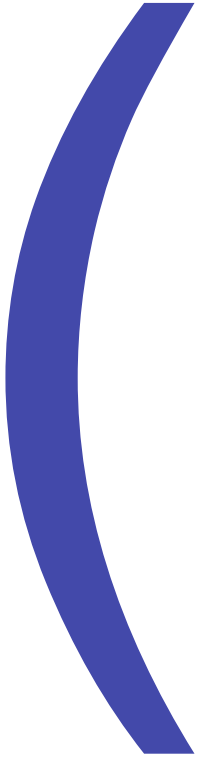


# Parity symmetry breaking

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Aparté: what is helicity? What is chirality?



# Parity symmetry breaking



Aparté: what is helicity? What is chirality?

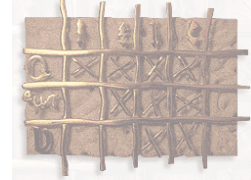
Let's have a look first to the solutions ( $E > 0$ ) of Dirac equation written in the Pauli-Dirac basis:

$$\gamma^0 = \begin{pmatrix} I & 0 \\ 0 & -I \end{pmatrix} \quad \gamma^k = \begin{pmatrix} 0 & \sigma_k \\ -\sigma_k & 0 \end{pmatrix} \quad \gamma^5 = \begin{pmatrix} 0 & I \\ I & 0 \end{pmatrix}$$

For the sake of the simplicity of the notation, I consider the momentum along the  $z$  coordinate only.

$$u_1 = \sqrt{E + m} \begin{pmatrix} 1 \\ 0 \\ \frac{p}{E+m} \\ 0 \end{pmatrix} \quad u_2 = \sqrt{E + m} \begin{pmatrix} 0 \\ 1 \\ 0 \\ -\frac{p}{E+m} \end{pmatrix}$$

# Parity symmetry breaking



Aparté: what is helicity? What is chirality?

$$\hat{h} = \frac{1}{2} \vec{p} \cdot \vec{\sigma} = \frac{1}{2} p \cdot \begin{pmatrix} \sigma_3 & 0 \\ 0 & \sigma_3 \end{pmatrix} \quad \sigma_3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

$$\hat{h} = \frac{p}{2} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} \quad u_1 = \sqrt{E+m} \begin{pmatrix} 1 \\ 0 \\ \frac{p}{E+m} \\ 0 \end{pmatrix}$$

$$u_2 = \sqrt{E+m} \begin{pmatrix} 0 \\ 1 \\ 0 \\ -\frac{p}{E+m} \end{pmatrix}$$

$$\hat{h} \cdot u_1 = \frac{1}{2} u_1 ,$$

$$\hat{h} \cdot u_2 = -\frac{1}{2} u_2 .$$

$u_1$  and  $u_2$  are helicity eigenstates

# Parity symmetry breaking



Aparté: what is helicity? What is chirality?

Let's project those states with the chirality projectors:

$$u_1 = \sqrt{E+m} \begin{pmatrix} 1 \\ 0 \\ \frac{p}{E+m} \\ 0 \end{pmatrix}$$

$$u_2 = \sqrt{E+m} \begin{pmatrix} 0 \\ 1 \\ 0 \\ -\frac{p}{E+m} \end{pmatrix}$$

$$P_L = \frac{1}{2}(1 - \gamma^5) = \begin{pmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & -1 \\ -1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{pmatrix} \quad P_R = \frac{1}{2}(1 + \gamma^5) = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{pmatrix}$$

$$P_L u_1 = \frac{1}{2} \sqrt{E+m} \begin{pmatrix} 1 - \frac{p}{E+m} \\ 0 \\ -1 + \frac{p}{E+m} \\ 0 \end{pmatrix} \quad P_R u_1 = \frac{1}{2} \sqrt{E+m} \begin{pmatrix} 1 + \frac{p}{E+m} \\ 0 \\ 1 + \frac{p}{E+m} \\ 0 \end{pmatrix}$$

$$u_1 = P_L u_1 + P_R u_1 = \frac{1}{2} \left(1 - \frac{p}{E+m}\right) \sqrt{E+m} \begin{pmatrix} 1 \\ 0 \\ -1 \\ 0 \end{pmatrix} + \frac{1}{2} \left(1 + \frac{p}{E+m}\right) \sqrt{E+m} \begin{pmatrix} 1 \\ 0 \\ 1 \\ 0 \end{pmatrix}$$

# Parity symmetry breaking



Aparté: what is the helicity? What is the chirality?

$$u_L = \sqrt{E + m} \begin{pmatrix} 1 \\ 0 \\ -1 \\ 0 \end{pmatrix} \quad u_R = \sqrt{E + m} \begin{pmatrix} 1 \\ 0 \\ 1 \\ 0 \end{pmatrix}$$

$$u_1 = P_L u_1 + P_R u_1 = \frac{1}{2} \left(1 - \frac{p}{E + m}\right) \sqrt{E + m} \begin{pmatrix} 1 \\ 0 \\ -1 \\ 0 \end{pmatrix} + \frac{1}{2} \left(1 + \frac{p}{E + m}\right) \sqrt{E + m} \begin{pmatrix} 1 \\ 0 \\ 1 \\ 0 \end{pmatrix}$$

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# Parity symmetry breaking



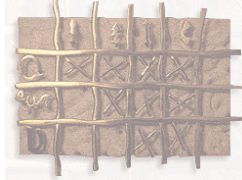
Aparté: what is helicity? What is chirality?

$$u_1 = P_L u_1 + P_R u_1 = \frac{1}{2} \left( 1 - \frac{p}{E + m} \right) u_L + \frac{1}{2} \left( 1 + \frac{p}{E + m} \right) u_R$$

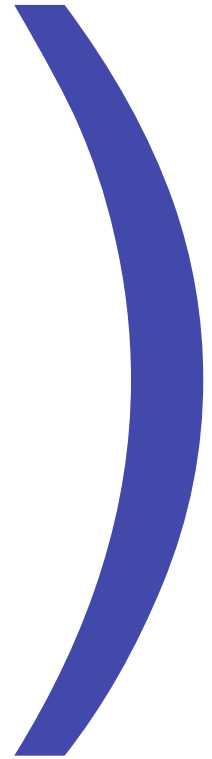
- For a massless particle, helicity IS chirality.
- For ultra-relativistic particles ( $E \gg m$ ), helicity IS chirality.
- The heavier is a particle, the larger is the mixing of chiral states for a given helicity.

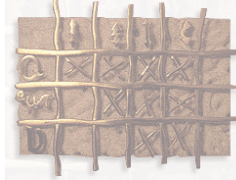
# Parity symmetry breaking

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Aparté: what is helicity? What is chirality?





## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

✓Quantum Field Theory: requirement of Lorentz Invariance (LI) of the matrix elements strongly constrains the form of the interaction vertices. We learnt QED and QCD to have vector currents. In general, 5 and only 5 combinations of 2 spinors and  $\gamma$ -matrices complies with Lorentz Invariance. They are called covariant bilinears:

Type	Expression	Components	Mediating Boson
Scalar	$\bar{\Psi}\Phi$	1	Spin 0
PseudoScalar	$\bar{\Psi}\gamma^5\Phi$	1	Spin 0
Vector	$\bar{\Psi}\gamma^\mu\Phi$	4	Spin 1
Axial Vector	$\bar{\Psi}\gamma^\mu\gamma^5\Phi$	4	Spin 1
Tensor	$\bar{\Psi}(\gamma^\mu\gamma^\nu - \gamma^\nu\gamma^\mu)\Phi$	6	Spin 2





## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

✓ WE, have to find which form or combination of forms would fit the experimental observation that parity symmetry is maximally violated in weak interaction and that left-handed helicity (=chirality) neutrinos seem to be the only authorized state in that scope.

✓ First a reminder on chirality states. Let's consider a half-spin particle:

$$(i\gamma^\mu \partial_\mu - m)\Psi = 0.$$

$$\Psi = \Psi_L + \Psi_R, \Psi_L = P_L \Psi, \Psi_R = P_R \Psi,$$

$$P_{L,R} = \frac{(1 \pm \gamma^5)}{2},$$

$$\gamma^5 = \begin{pmatrix} I & 0 \\ 0 & -I \end{pmatrix}.$$



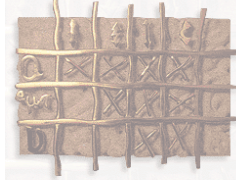
## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

✓ There are two vertex interaction forms compliant with our objectives: these are the Vector-AxisVector interaction:

$$\begin{aligned}\bar{\Psi}\gamma^\mu(1-\gamma^5)\Psi &= \bar{\Psi}(P_L + P_R)\gamma^\mu(1-\gamma^5)(P_L + P_R)\Psi \\ \bar{\Psi}\gamma^\mu(1-\gamma^5)\Psi &= 2\bar{\Psi}(P_L + P_R)\gamma^\mu(P_L^2 + P_LP_R)\Psi \\ \bar{\Psi}\gamma^\mu(1-\gamma^5)\Psi &= 2\bar{\Psi}_L\gamma^\mu\Psi_L\end{aligned}$$

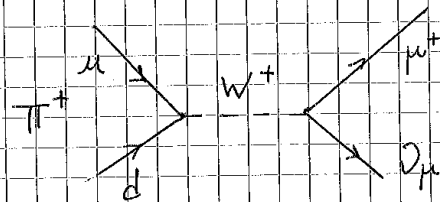
✓ **Selection of chirality states.** Only LL couplings allowed for particles. Maximal violation of the parity symmetry. **A natural candidate for the weak interaction.**

✓ *Homework 1: show that vectorial interactions selects democratically LL and RR interaction vertices. Show as well that  $[V+A]$  does the same as  $[V-A]$ .*



## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

$\pi$  Decay - Decay width and related matter  
Hands out



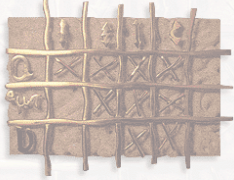
$$d\Gamma = \frac{1}{2E} \frac{1}{(2s_{\pi}+1)} \sum_{\text{spins}} |\overline{\mathcal{M}}|^2 dQ.$$

① HADRONIC MATRIX ELEMENT  $j_q^\mu = \bar{u}(u) \gamma^\mu (1 - \gamma^5) u(d)$   
Since quarks, cannot be calculated perturbatively for the strong interaction  $\rightarrow j_q^\mu = f_\pi p^\mu$ .  $p$  = momentum of  $\pi$ .

② LEPTONIC MATRIX ELEMENT AND  $\mathcal{M}$ .

$$j_\mu = \bar{u}(\mu^+) \gamma_\mu (1 - \gamma^5) u(\mu) \text{ and } \mathcal{M} = \frac{G_F}{\sqrt{2}} \left[ \bar{j}_q^\mu \right] \left[ j_\mu \right].$$

$$\rightarrow \mathcal{M} = \frac{G_F}{\sqrt{2}} f_\pi m_\mu \left[ \bar{u}(\mu^+) (1 - \gamma^5) u(\mu) \right]$$



## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

③ SUM OVER FINAL STATES SPINS

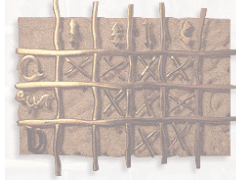
$$|\overline{\mathcal{M}}|^2 = \sum_{\text{spins}} \mathcal{M} \mathcal{M}^* = 4 G_F^2 f_\pi^2 m_\mu^2 F(q) \cdot F(q_\mu)$$

④ PHASE SPACE INTEGRATION

$$dQ = \frac{d^3 p(\mu)}{(2\pi)^3 \cdot 2E(\mu)} \cdot \frac{d^3 p(q_\mu)}{(2\pi)^3 \cdot 2E(q_\mu)} (2\pi)^4 \delta^{(4)}(p - p(\mu) - p(q_\mu))$$

⑤ BOTTOMLINE

$$\Gamma = \frac{G_F^2}{8\pi} f_\pi^2 \cdot \frac{m_\mu^2}{m_\pi^2} (m_\pi^2 - m_\mu^2)^2$$



## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

$$\Gamma(\pi^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2}{8\pi} \cdot f_\pi^2 \cdot m_\ell^2 \left( \frac{m_\pi^2 - m_\ell^2}{m_\pi^2} \right)^2$$

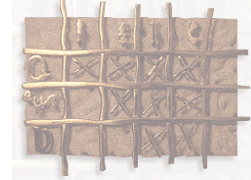
coupling constant

had. matrix element (LQCD)

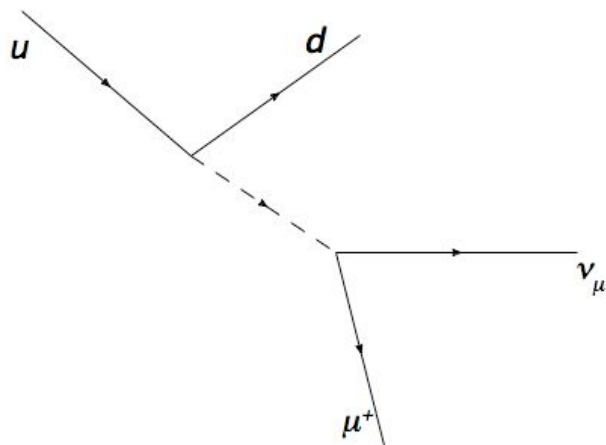
PARITY VIOLATION

PHASE SPACE CORRECTION

✓ Interpretation: you force the antilepton to be in its wrong helicity state (chirality is definitely right-handed). Electrons must hate you more than muons do (at least in the ratio of the squared masses).



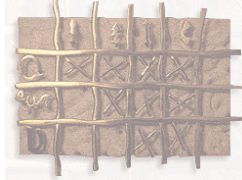
## Neutrinos are left-handed. Implications: the decay of the pion as an illustration



*To remove the QCD part of the decay width which is badly determined, it is relevant to consider a ratio of decay widths in leptons.*

*Again, we can compare the predictions with the different allowed Lorentz Invariant structures of the interaction to the measurement.*

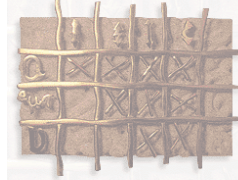
$$\begin{aligned}\frac{\Gamma(\pi^+ \rightarrow \mu^+ \nu_\mu)}{\Gamma(\pi^+ \rightarrow e^+ \nu_e)} &= (0.813 \pm 0.004) \cdot 10^4, \\ \frac{\Gamma(\pi^+ \rightarrow \mu^+ \nu_\mu)}{\Gamma(\pi^+ \rightarrow e^+ \nu_e)} &= 0.2 \text{ (S or P prediction),} \\ \frac{\Gamma(\pi^+ \rightarrow \mu^+ \nu_\mu)}{\Gamma(\pi^+ \rightarrow e^+ \nu_e)} &= 0.78 \cdot 10^4 \text{ (V - A prediction).}\end{aligned}$$



## Neutrinos are left-handed. Implications: the decay of the pion as an illustration

### ✓ Final notes on the subject:

- If the electron and muon decay widths differ a lot, lepton and antilepton decay widths are the same within experimental uncertainties, making  $CP$  a good symmetry of the weak interaction.
- In the actual calculation ( which I strongly encourage you to perform), you will observe a slight tension between the prediction and the measurement. Anticipating a bit the following elements of this lecture, this disagreement is related to the probability of the  $d \rightarrow u$  transition which is not amounting to unity.



## Modern parity violation experiments:LEP/SLD

### The Standard Model Tests (Part II)

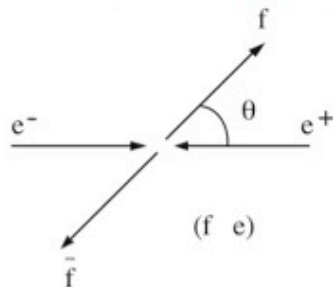


#### 3.3 The Parity-Violating forward-backward asymmetries in e+e-.

- Parity is maximally violated in weak interactions. This induces the fermion particle in the final state to be produced preferentially in the direction of the initial electron.

$$\frac{d\sigma^f}{d\cos\theta} = \sigma_{\text{tot}}^f \cdot \left[ \frac{3}{8}(1 + \cos^2\theta) + A_{\text{FB}}^{f\bar{f}} \cos\theta \right]$$

- The experimentalist's job is to identify the nature of the fermion and count how many times it is found forward (i.e. in the electron direction)

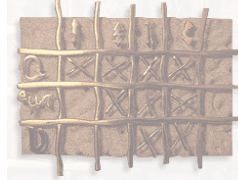


$$A_{\text{FB}}^{f\bar{f}} = \frac{N_F - N_B}{N_F + N_B} \text{ with } N_F = \int_0^1 \frac{d\sigma_{f\bar{f}}}{d\cos\theta} \cdot d\cos\theta$$

$$A_{\text{FB}}^{f\bar{f}} \propto A_e \cdot A_f \propto \frac{g_V^e g_A^e}{(g_V^e)^2 + (g_A^e)^2} \cdot \frac{g_V^f g_A^f}{(g_V^f)^2 + (g_A^f)^2}$$

Hence depends primarily to  $\sin^2\theta_{\text{eff}}$





## Modern parity violation experiments: SLD

### The Standard Model Tests (Part II)

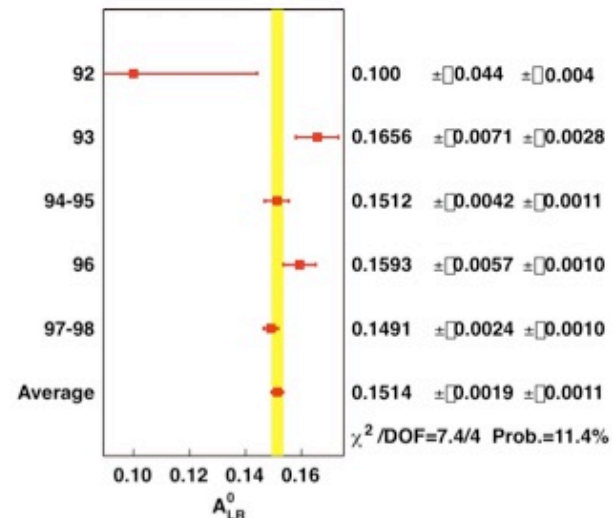


#### 3.4 The Parity-Violating Left-Right asymmetry from SLD

- We have seen in 3.3 that  $A_e$  was an excellent laboratory.
- SLC machine polarized the electron beam.
- Hence, knowing the polarization and just measuring the LL and RR production of Z boson yields  $A_e$  :

$$A_{LR} = \frac{N_L - N_R}{N_L + N_R} \cdot \frac{1}{\langle P_e \rangle}$$

$$\langle P_e \rangle_{1998} = 0.7292 \pm 0.0038$$



$$A_{LR}^0 = 0.1514 \pm 0.0022$$

$$\sin^2 \theta_{\text{eff}} = 0.23097 \pm 0.00027.$$



## Modern parity violation experiments: LEP

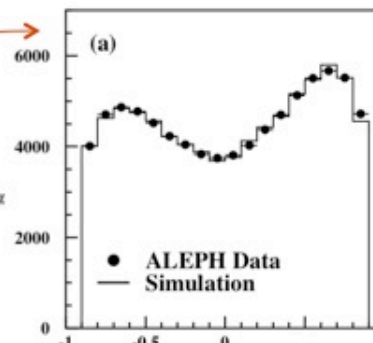
### The Standard Model Tests (Part II)



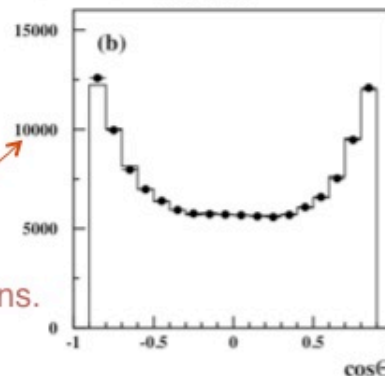
#### 3.3 The Parity-Violating forward-backward asymmetries in $e^+e^-$ .

- Then we fit the asymmetries to these data:

$$\begin{aligned}
 f_{ijkl} = & (F_{\ell,b}^{rs})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^b (1 - 2\chi_{ijkl}) x] dx \\
 & + (F_{\ell,b}^{ws})_{ijkl} \int_{-1}^1 [1+x^2 - \frac{8}{3} A_{FB}^b (1 - 2\chi_{ijkl}) x] dx \\
 & + (F_{bkg,b}^{asym})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^b (1 - 2\chi_{ijkl}) (2\eta_{ijk}^b - 1) x] dx \\
 & + (F_{\ell,c})_{ijkl} \int_{-1}^1 (1+x^2 - \frac{8}{3} A_{FB}^c x) dx \\
 & + (F_{c \rightarrow bkg}^{asym})_{ijkl} \int_{-1}^1 [1+x^2 - \frac{8}{3} A_{FB}^c (2\eta_{ijk}^c - 1) x] dx \\
 & + (F_{s \rightarrow bkg}^{asym})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^s (2\eta_{ijk}^s - 1) x] dx \\
 & + (F_{d \rightarrow bkg}^{asym})_{ijkl} \int_{-1}^1 [1+x^2 + \frac{8}{3} A_{FB}^d (2\eta_{ijk}^d - 1) x] dx \\
 & + (F_{u \rightarrow bkg}^{asym})_{ijkl} \int_{-1}^1 [1+x^2 - \frac{8}{3} A_{FB}^u (2\eta_{ijk}^u - 1) x] dx \\
 & + (F_{bkg}^{sym})_{ijkl} \int_{-1}^1 (1+x^2) dx,
 \end{aligned}$$



Parity violation even seen for charm.




Includes QED and QCD effects.

Measuring simultaneously the mixing parameter w/ leptons.

S.Monteil

TESchool of High Energy Physics

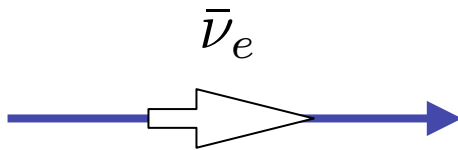
## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
  - ✓ One gets from experimental results so far the following picture:
- 
- The diagram illustrates parity violation in a weak interaction. It shows a particle decaying into two particles. A coordinate system is defined with the z-axis pointing upwards. The decay products are shown with their momenta and spins. The diagram demonstrates that the decay is not symmetric under parity transformation, which is a characteristic of weak interactions.
- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:

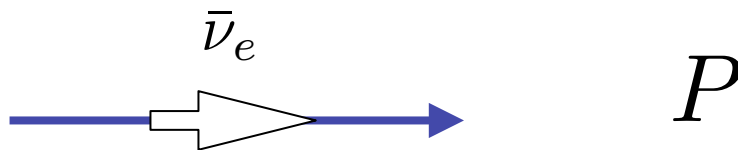


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:



- ✓ Any theory of the weak interaction shall include these properties.

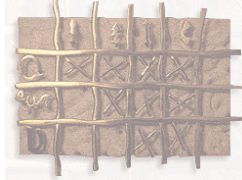


## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:

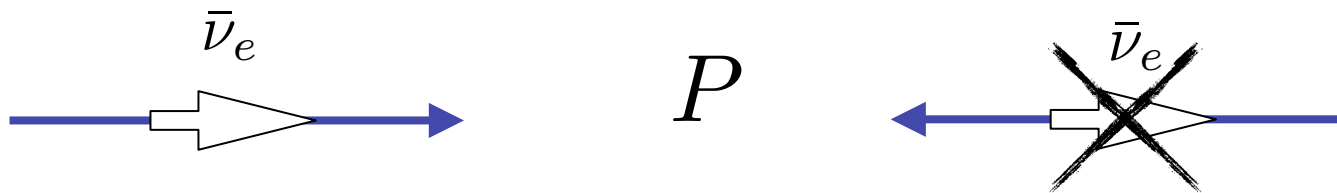


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:



- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:



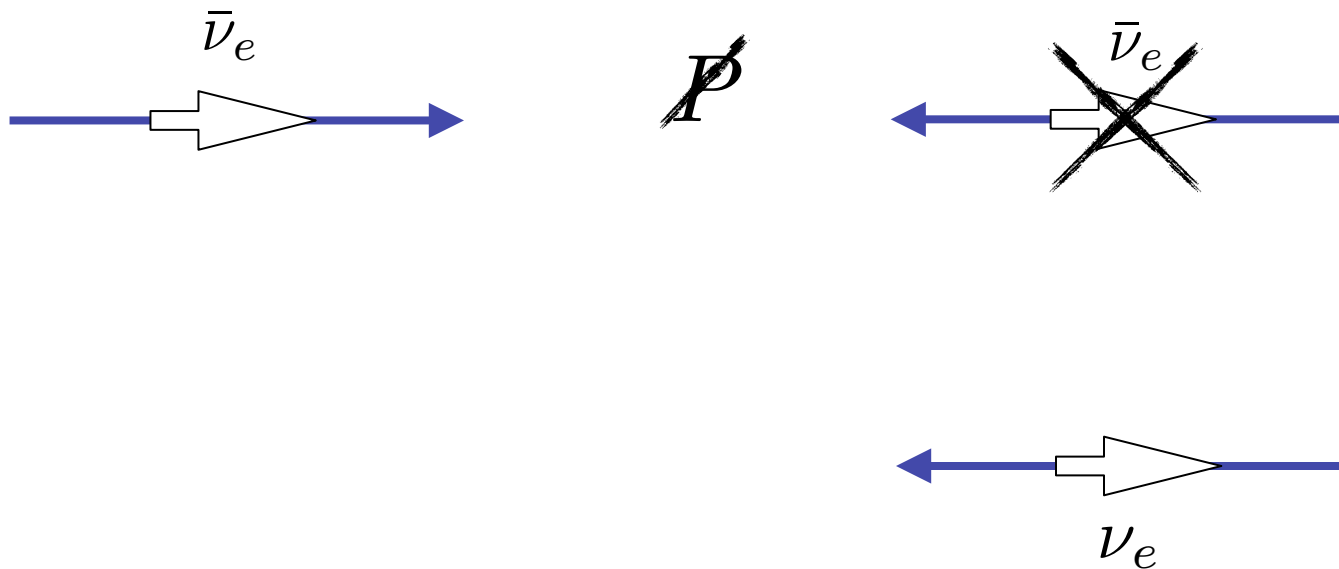
- ✓ Any theory of the weak interaction shall include these properties.



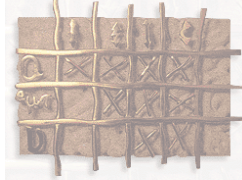


## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:

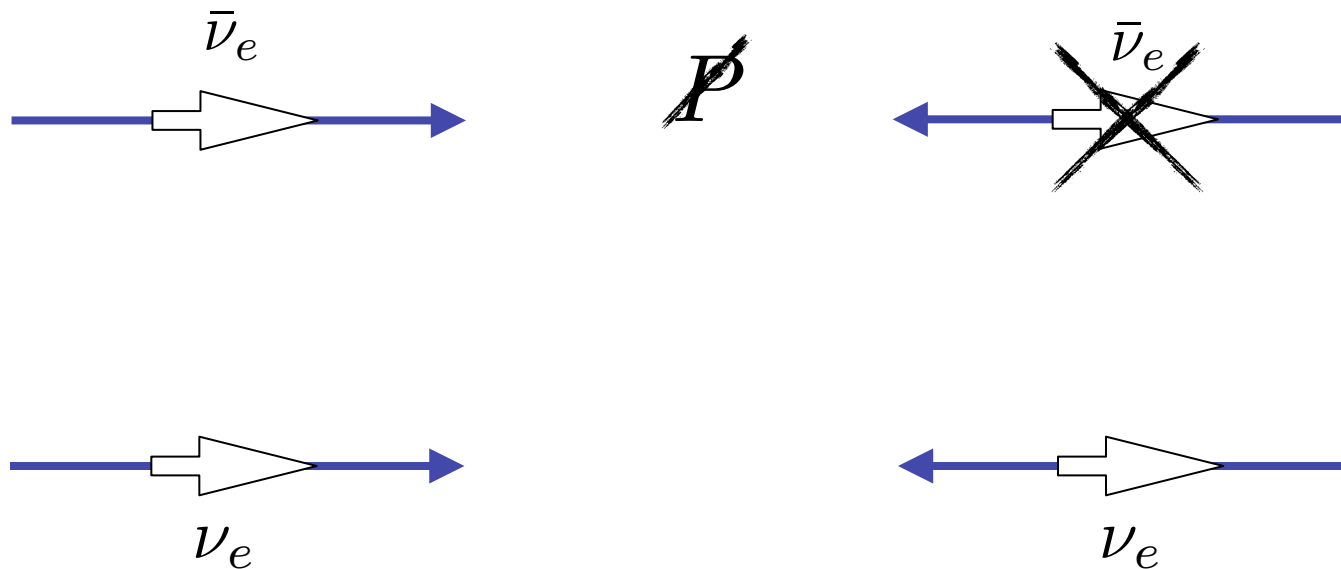


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:

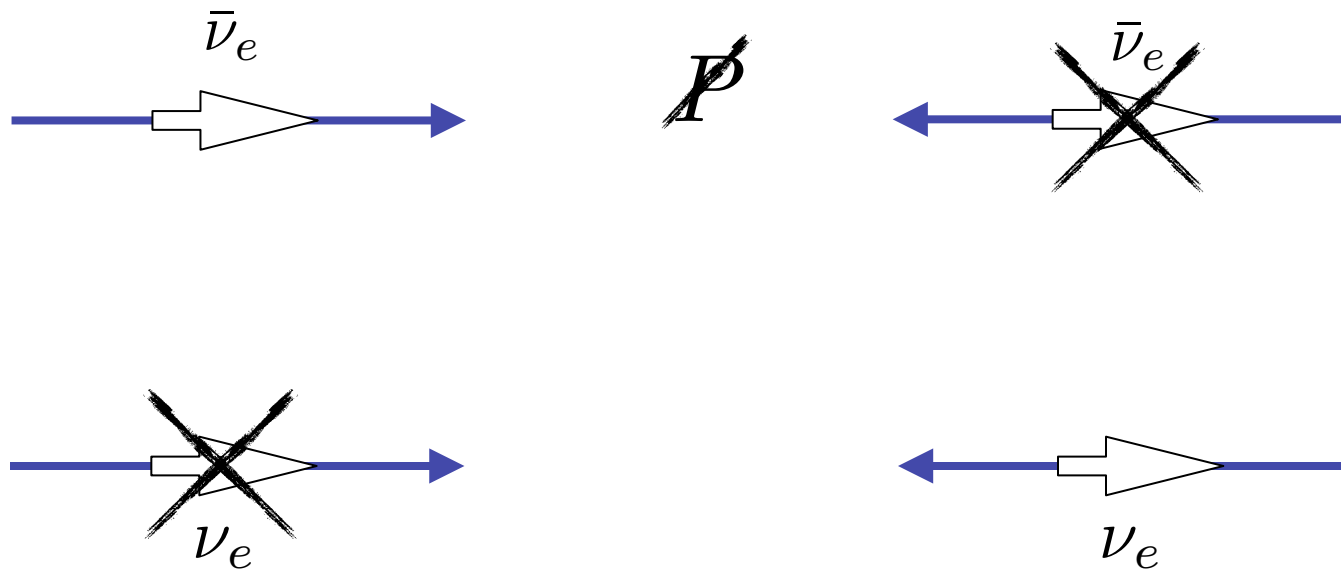


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:

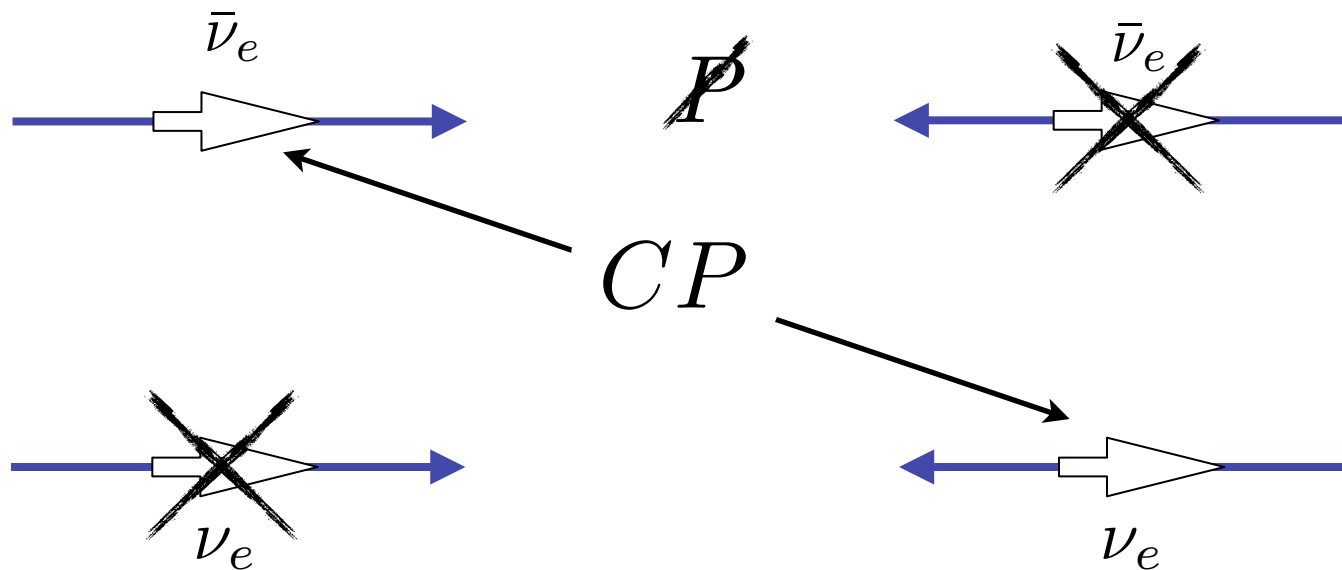


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity is violated in weak interaction.
- ✓ One gets from experimental results so far the following picture:

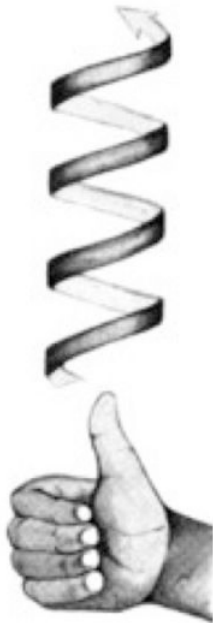


- ✓ Any theory of the weak interaction shall include these properties.



## An intermediate conclusion

- ✓ Parity violation do occur elsewhere

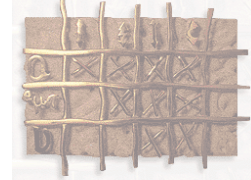


- ✓ But those are not of fundamental nature. The DNA molecule for instance can be synthesised.



**Question: OK, parity is violated in the weak interaction. But can't we restore the left-right symmetry by considering the product  $C \times P$ ? Seems a good symmetry at least in the pion decay.**

$$\Gamma(\pi^+ \rightarrow \ell^+ \nu_\ell) = \Gamma(\pi^- \rightarrow \ell^- \bar{\nu}_\ell)$$



## Discovery of $CP$ violation.

- With simple quantum mechanics, one can show that in absence of  $CP$  violation:

$$\begin{aligned} CP|K_1\rangle &= \frac{1}{\sqrt{2}}(CP|K^0\rangle + CP|\bar{K}^0\rangle) = \frac{1}{\sqrt{2}}(|K^0\rangle + |\bar{K}^0\rangle) = +|K_1\rangle \\ CP|K_2\rangle &= \frac{1}{\sqrt{2}}(CP|K^0\rangle - CP|\bar{K}^0\rangle) = \frac{1}{\sqrt{2}}(|\bar{K}^0\rangle - |K^0\rangle) = -|K_2\rangle \end{aligned}$$

- Final states  $CP$  eigenvalues are +1 ( $\pi\pi$ ) and -1 ( $\pi\pi\pi$ ). If  $CP$  is a conserved quantity, one then should have:

$$\begin{aligned} K_1 &\rightarrow \pi\pi \\ K_2 &\rightarrow \pi\pi\pi. \end{aligned}$$

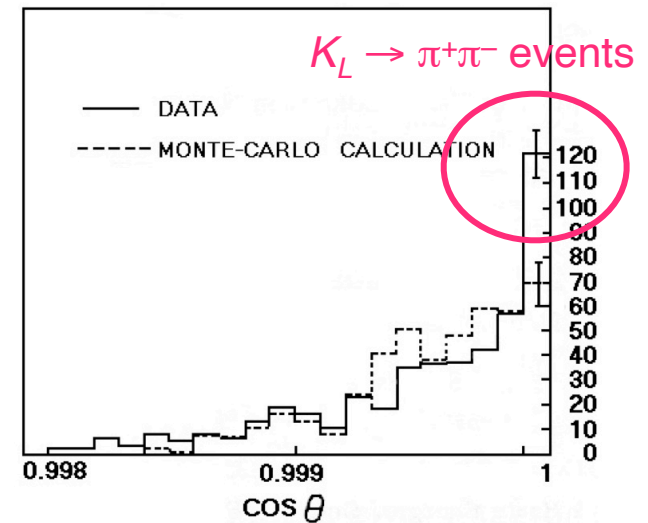
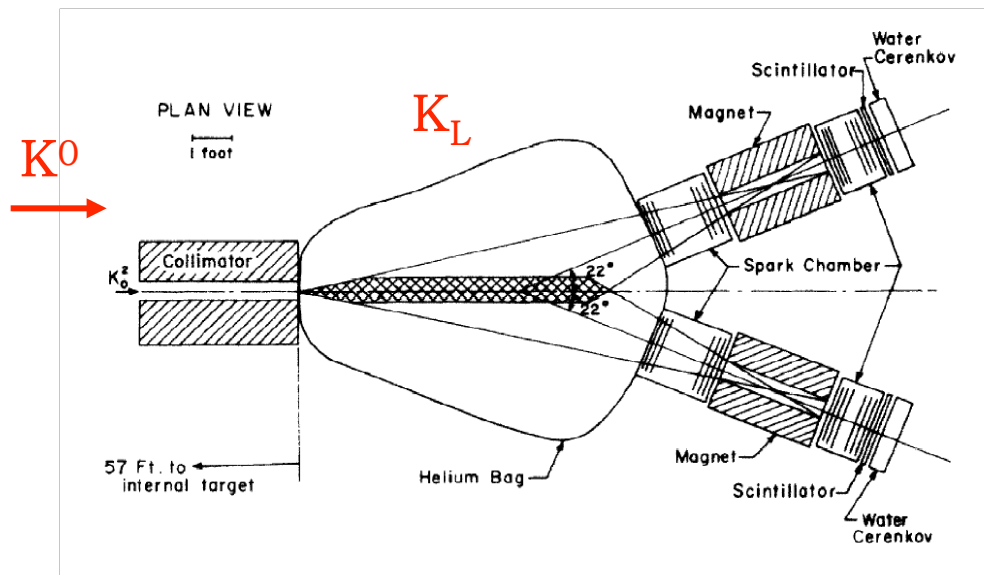
Which we'll identify as  $K_S^0$  and  $K_L^0$  respectively.

- measuring  $K_L^0$  decays into two pions ? Proof that  $CP$  symmetry is violated in weak interaction.



## Discovery of CP violation.

- The CP violation in kaon system: Christenson, Cronin, Fitch, Turlay. Phys. Rev. Lett. 13 (1964) 138.
- Far after the target, only the long species of  $K^0$  survive. They measured:

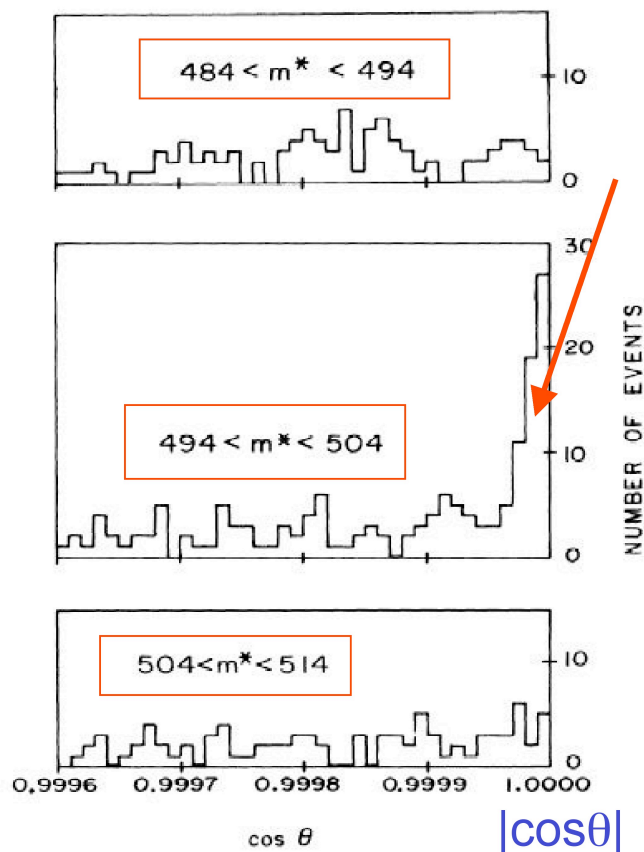


$$|\eta_{+-}| = \frac{A(K_L^0 \rightarrow \pi\pi)}{A(K_S^0 \rightarrow \pi\pi)}$$





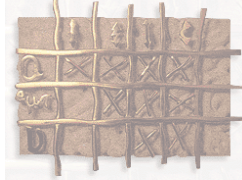
## Discovery of *CP* violation.



- Two-body decay : in the  $K^0$  center of mass system the two  $\pi$  are back to back :  $|\cos\theta|=1$ .

- Today's more precise measurement for the ratio of amplitudes:

$$|\eta_{+-}| = \frac{A(K_L^0 \rightarrow \pi\pi)}{A(K_S^0 \rightarrow \pi\pi)} = (2.271 \pm 0.017)10^{-3}.$$



## Discovery of *CP* violation.

Message Number 1:

The *CP* symmetry is violated in the mixing of neutral mesons, a pure electroweak phenomenon, e.g.

$$K^0 \longrightarrow \bar{K}^0 \neq \bar{K}^0 \longrightarrow K^0$$



## Discoveries of $CP$ violation

- At LHC, compare the decay rates of  $B^0_{d,s}$  and  $\text{anti}B^0_{d,s}$  into self-tagged final states  $K\pi$

$$A_{CP}(B^0 \rightarrow K\pi) = \frac{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) - \Gamma(B^0 \rightarrow K^+ \pi^-)}{\Gamma(\bar{B}^0 \rightarrow K^- \pi^+) + \Gamma(B^0 \rightarrow K^+ \pi^-)}$$
$$A_{CP}(B^0_s \rightarrow \pi K) = \frac{\Gamma(\bar{B}^0_s \rightarrow \pi^- K^+) - \Gamma(B^0_s \rightarrow \pi^+ K^-)}{\Gamma(\bar{B}^0_s \rightarrow \pi^- K^+) + \Gamma(B^0_s \rightarrow \pi^+ K^-)}.$$

- These raw asymmetries must be corrected from detection asymmetry and  $B$  production asymmetry:

$$A_{\Delta}(B^0_{(s)} \rightarrow K\pi) = \zeta_{d(s)} A_D(K\pi) + \kappa_{d(s)} A_P(B^0_{(s)} \rightarrow K\pi)$$

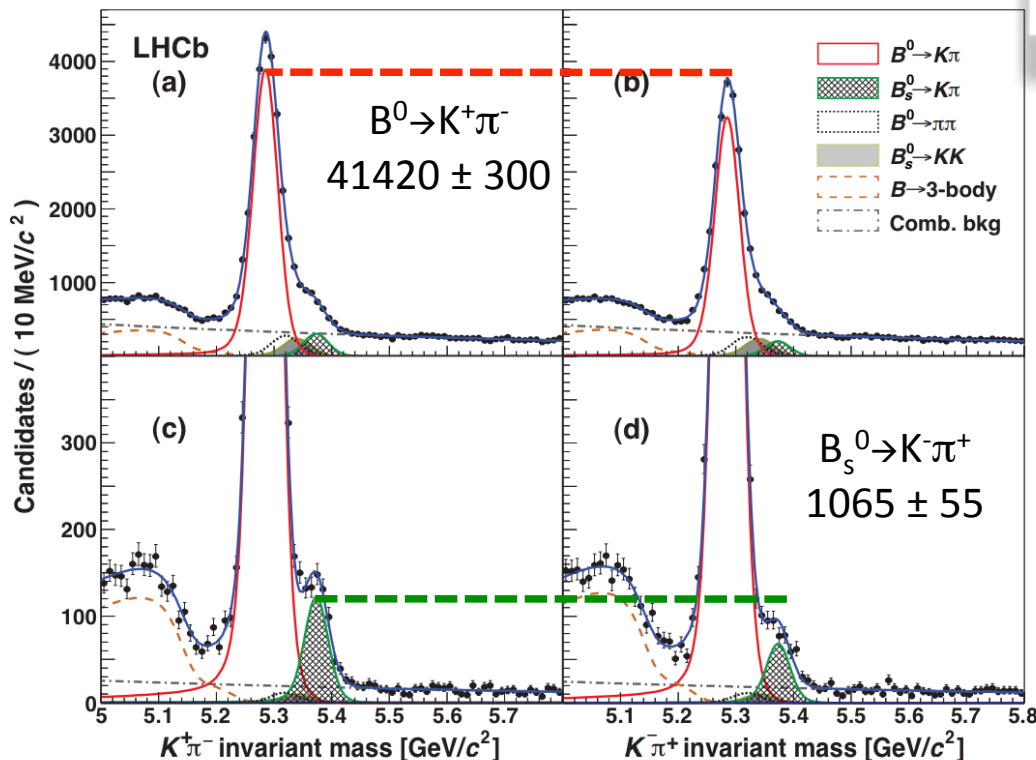
- Ingredients: these analyses are heavily relying on Particle Identification performance. It is also necessary to master the  $B$  production asymmetry and the differences of charged particle detection efficiencies (data-driven estimates).



## Other discoveries of CP violation.

- Compare the decay rates of self-tagged modes  $K\pi$

$$\mathcal{L} = (1/\text{fb} @ \sqrt{s} = 7 \text{ TeV})$$



$$A_{\text{raw}}(B^0 \rightarrow K^- \pi^+) = -0.091 \pm 0.006,$$

$$A_{\text{raw}}(B_s \rightarrow K^+ \pi^-) = 0.28 \pm 0.04,$$

- Data-driven control of PID efficiencies thanks to the self-tagged mode  $D^{*+} \rightarrow D^0 (K^- \pi^+) \pi^+$
- Raw asymmetries corrected from detection asymmetry (also  $D^{*+}$  control sample).
- $B$  production asymmetry simultaneously measured from decay time distribution.



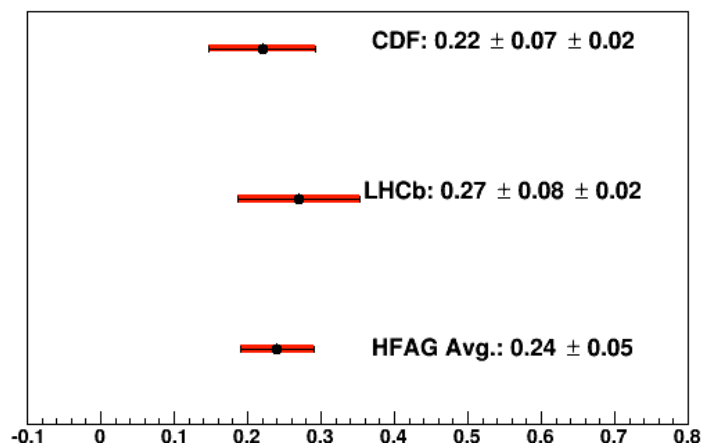
## Other discoveries of *CP* violation.

$$\begin{aligned} A_{\text{CP}}(B^0 \rightarrow K^- \pi^+) &= -0.080 \pm 0.007 \text{ (stat.)} \pm 0.003 \text{ (syst.)}, \\ A_{\text{CP}}(B_s \rightarrow K^+ \pi^-) &= 0.27 \pm 0.04 \text{ (stat.)} \pm 0.01 \text{ (syst.)}. \end{aligned}$$

- World best measurement for the  $B^0$

LHCB-PAPER-2013-018

- Former results for  $B_s$



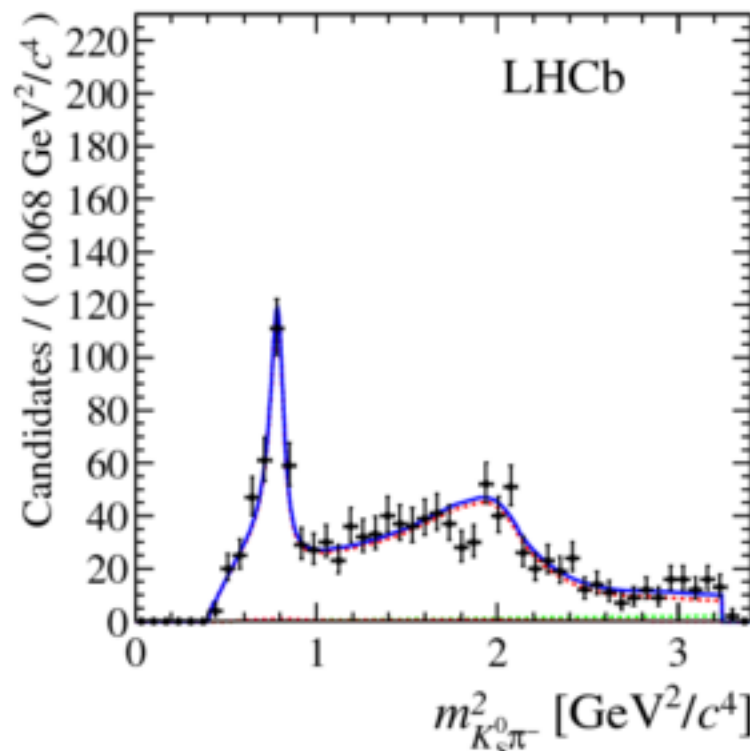
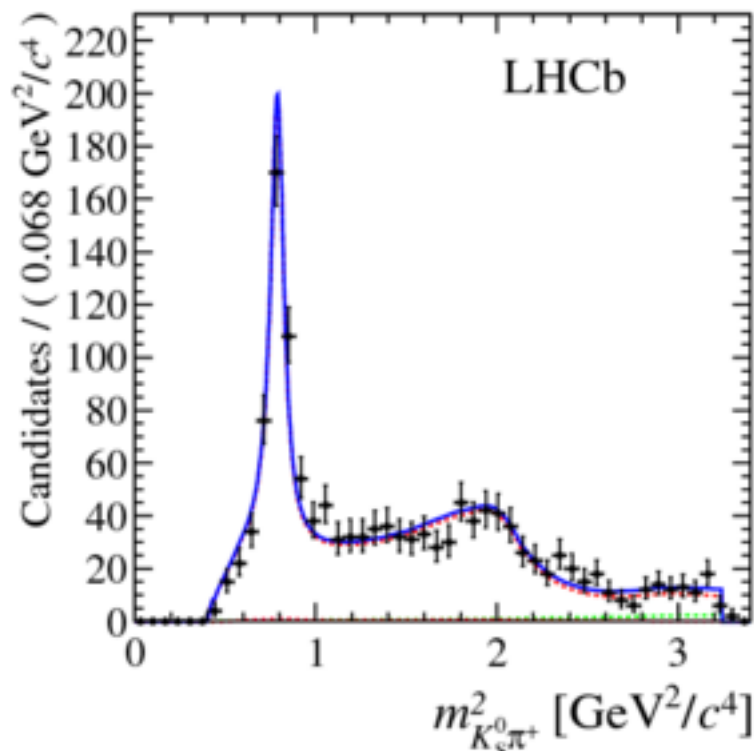
CDF-PUBLIC-10726

Phys. Rev. Lett. 108 (2012)

- First observation of *CPV* in the  $B_s$  system.

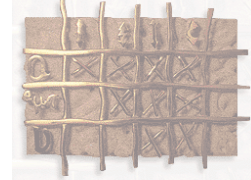


## Other discoveries of $CP$ violation.



[Phys. Rev. Lett. 120, 261801 \(2018\)](#)

$$A_{CP}(\overline{B}^0 \rightarrow K^*(892)^- \pi^+) = -0.30 \pm 0.06$$

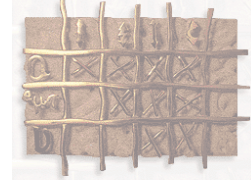


## Other discoveries of *CP* violation.

Message Number 2:

The *CP* symmetry is violated in the decay of beautiful particles, pure electroweak phenomenon, e.g.

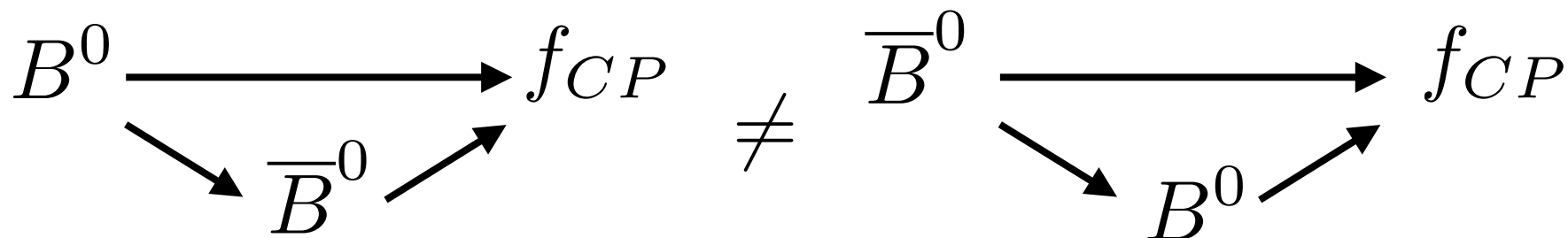
$$B^0 \longrightarrow K^+ \pi^- \neq \bar{B}^0 \longrightarrow K^- \pi^+$$



## Other discoveries of $CP$ violation.

Message Number 3:

The  $CP$  symmetry can be violated in the interplay (interference) of the two previous sources of  $CP$  violation, e.g.



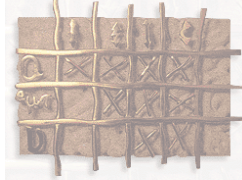




## Concluding this introduction

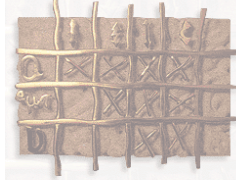
- $C$ ,  $P$  and  $CP$  are (so far) conserved in electromagnetic and strong interactions.
- $C$  and  $P$  symmetries are maximally violated by the weak interaction.
- $CP$  symmetry is slightly violated in the electroweak interaction.
- There are three ways of  $CP$  violation to manifest in the Nature so far:
  - 1) In the mixing of neutral particles (observed solely in neutral kaon mixing - 1964).
  - 2) In the decay of the beautiful and strange mesons ( $K$  and  $B_{d,s}$ , 2001 and 2004,2013 resp.).
  - 3) In the interference between decay and mixing of the beautiful particles (2001, see next chapters) .

And that's all.



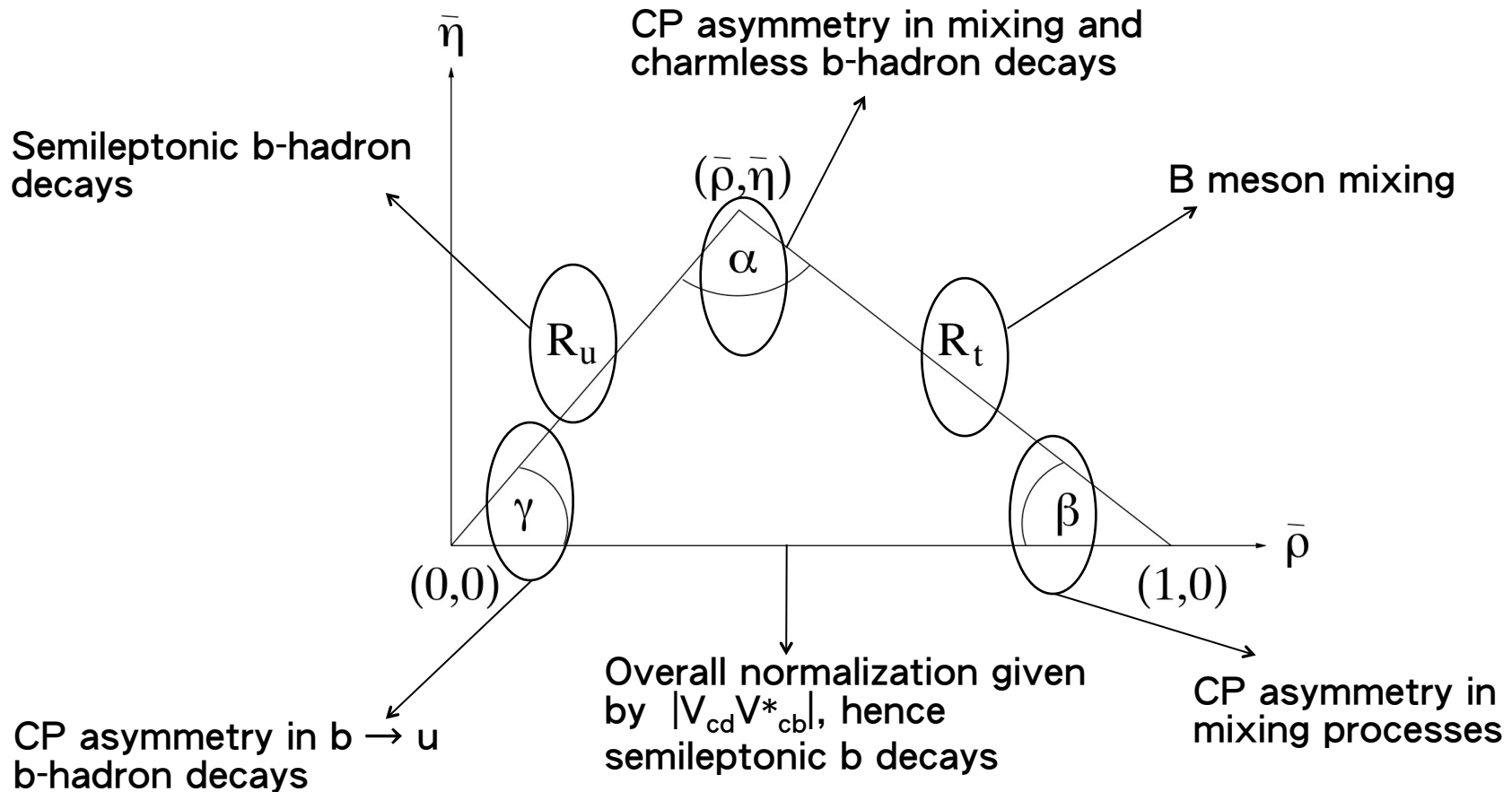
## A personal comment before going to Chapter II

- We do not have yet a (satisfactory) dynamical mechanism to explain these discrete symmetry breakings. And to my knowledge, no mathematical Physics way to do so.
- Still, what comes next is elegant.
- We'll try to make sense of the  $CP$  symmetry breaking phenomena.



## 2.4 Introduction: which measurements and where?

- B factories: all ! As far as UT is concerned.

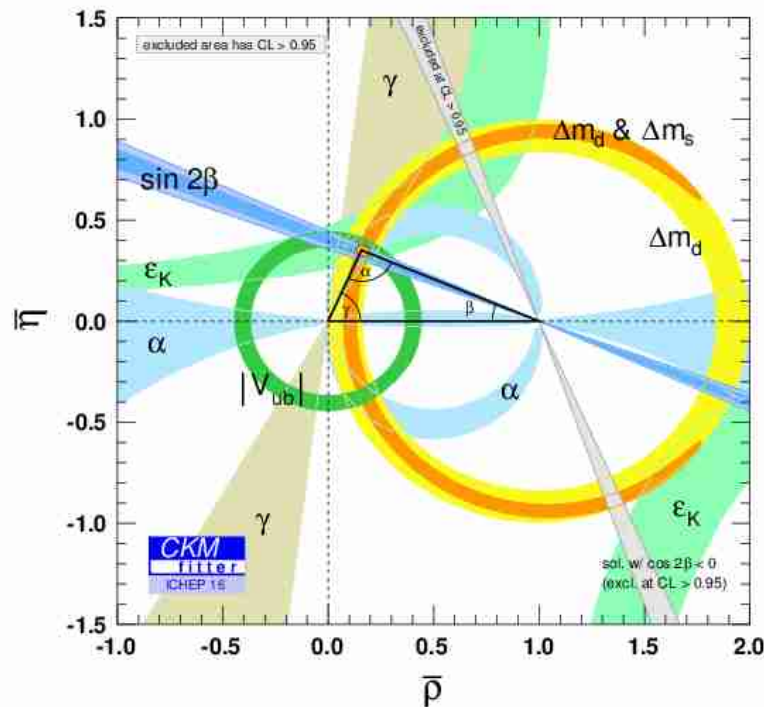


# Part II — Rare decays of heavy-flavoured particles



## Motivation

- In any HEP physics conference summary talk, you will find this plot, stating that (heavy) flavours and  $CP$  violation physics is a pillar of the Standard Model.



- One objective of this lecture is to undress this plot.