

The phi meson in nuclear matter in a transport approach

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Talk at the “Particles and Nuclei International Conference (PANIC 2021)”,
online
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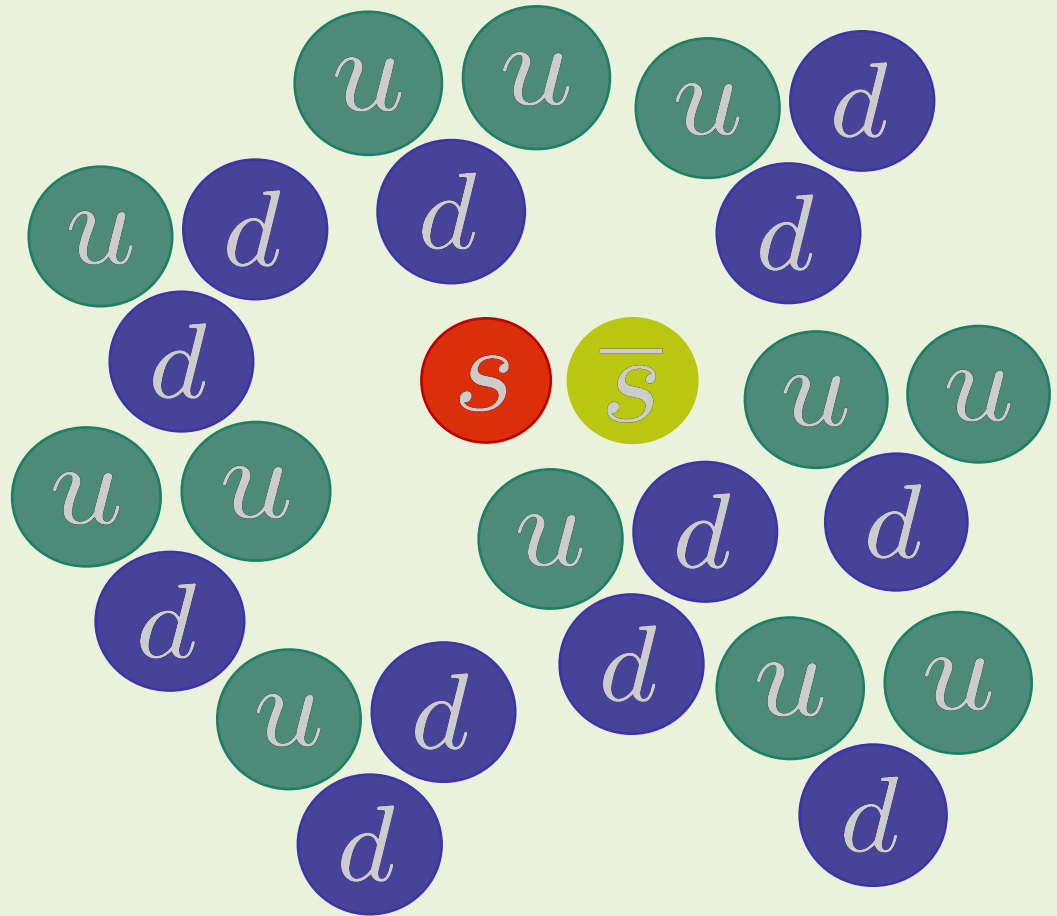
Work done in collaboration with
Elena Bratkovskaya (Frankfurt U./GSI)

ϕ meson



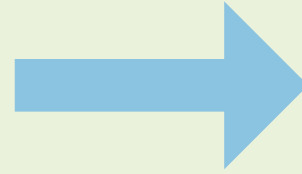
$$m_{\phi} = 1019 \text{ MeV}$$

$$\Gamma_{\phi} = 4.3 \text{ MeV}$$



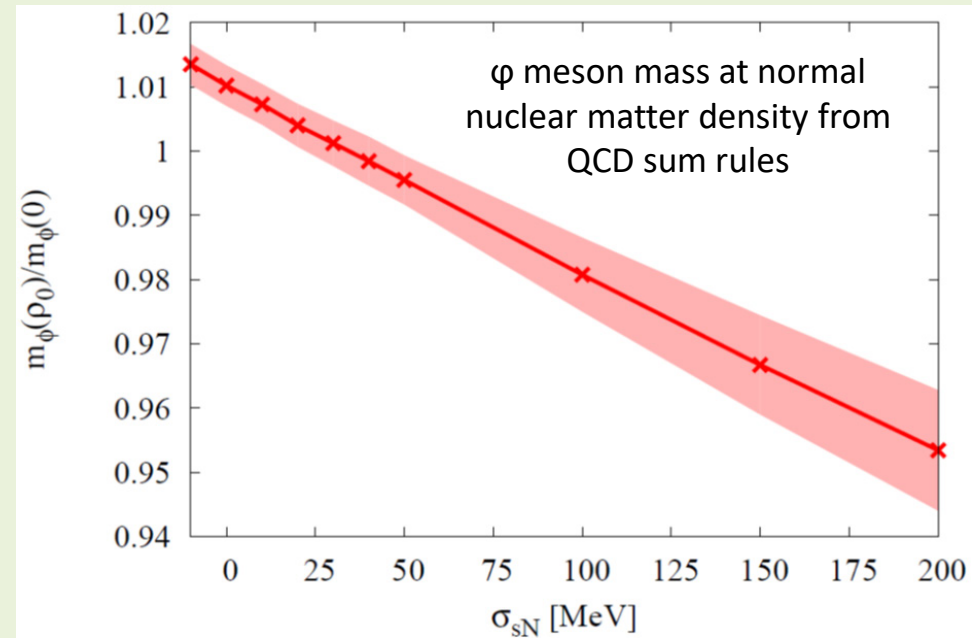
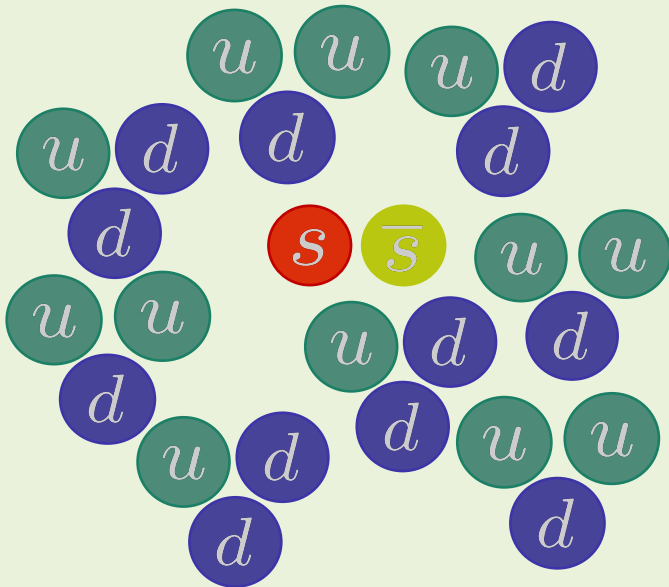
Motivation: clarify the relation between hadron masses and chiral symmetry

$$\begin{aligned} \langle 0 | \bar{u}u | 0 \rangle & \searrow \\ \langle 0 | \bar{d}d | 0 \rangle & \searrow \\ \langle 0 | \bar{s}s | 0 \rangle & \searrow \end{aligned}$$



$$m_\phi \searrow ?$$

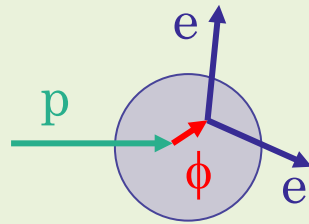
P. Gubler and K. Ohtani, Phys. Rev. D **90**, 094002 (2014).



$$|\langle \bar{s}s \rangle_\rho| = |\langle \bar{s}s \rangle_0| - \frac{\rho}{m_s} \sigma_{sN} + \dots$$

Previous experimental results

KEK
E325



12 GeV
pA-reaction

slow φ s

Pole mass:

$$\frac{m_\phi(\rho)}{m_\phi(0)} = 1 - k_1 \frac{\rho}{\rho_0}$$

0.034 ± 0.007

intermediate
 φ s

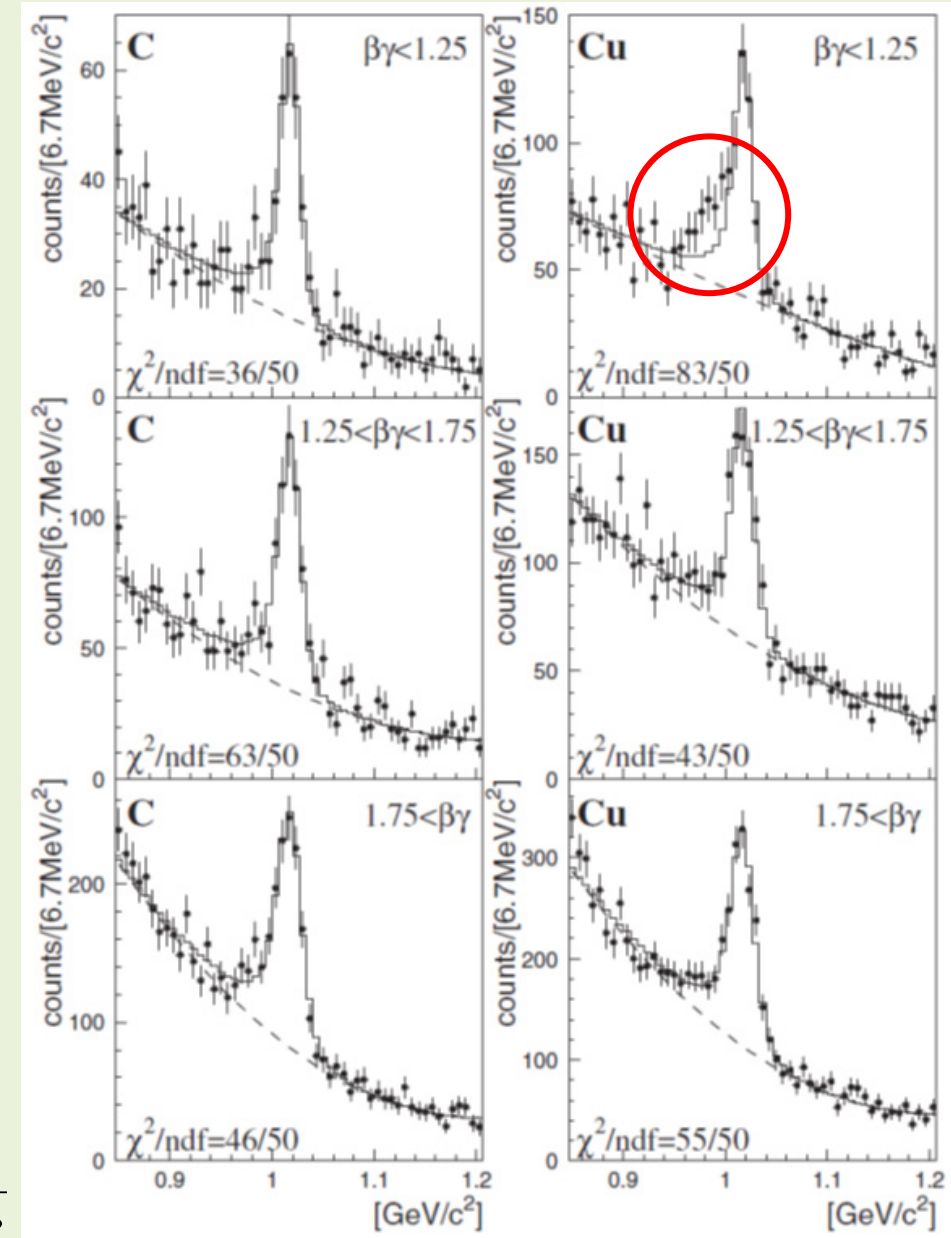
Pole width:

$$\frac{\Gamma_\phi(\rho)}{\Gamma_\phi(0)} = 1 + k_2 \frac{\rho}{\rho_0}$$

2.6 ± 1.5

fast φ s

$$\beta\gamma = \frac{|\vec{p}|}{m_\phi}$$




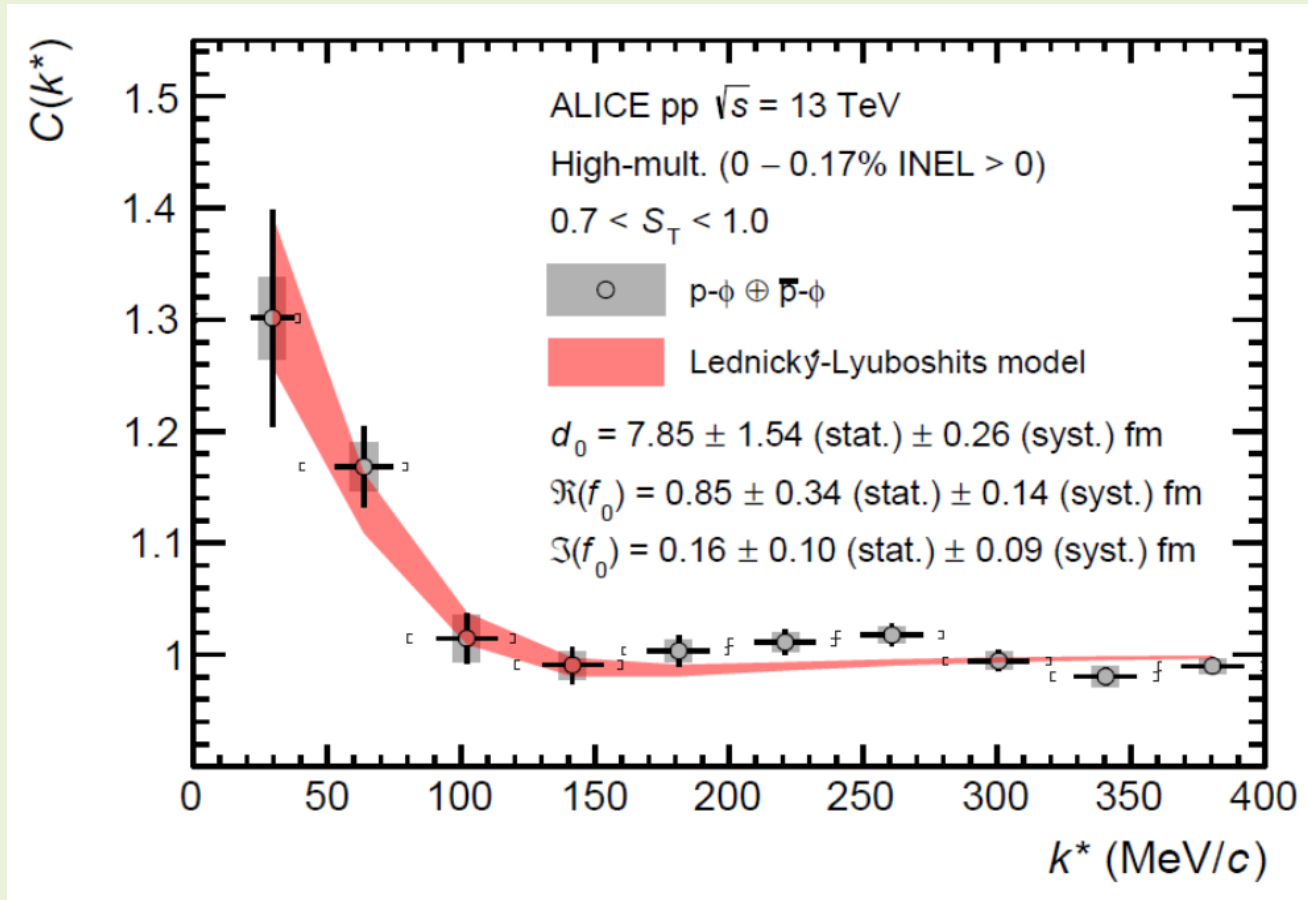
Is currently measured again at the J-PARC E16
experiment with 100x increased statistics

New experimental results

ALICE

Measurement of ϕ N correlation

Attraction!




Extracted ϕ N scattering length

Real part:

$$\Re(f_0) = 0.85 \pm 0.34(\text{stat.}) \pm 0.14(\text{syst.}) \text{ fm}$$



Attractive

Imaginary part:

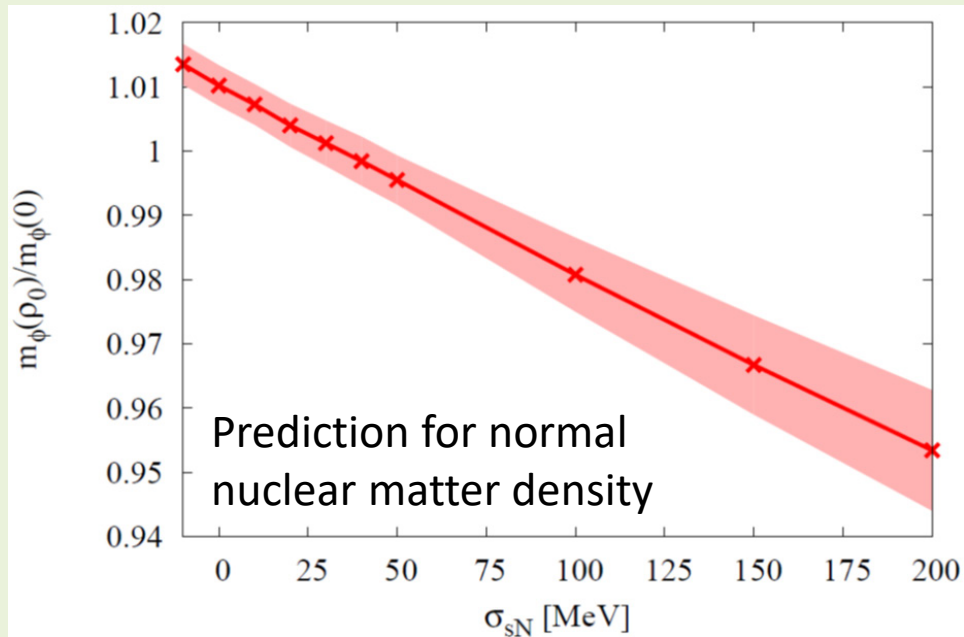
$$\Im(f_0) = 0.16 \pm 0.10(\text{stat.}) \pm 0.09(\text{syst.}) \text{ fm}$$



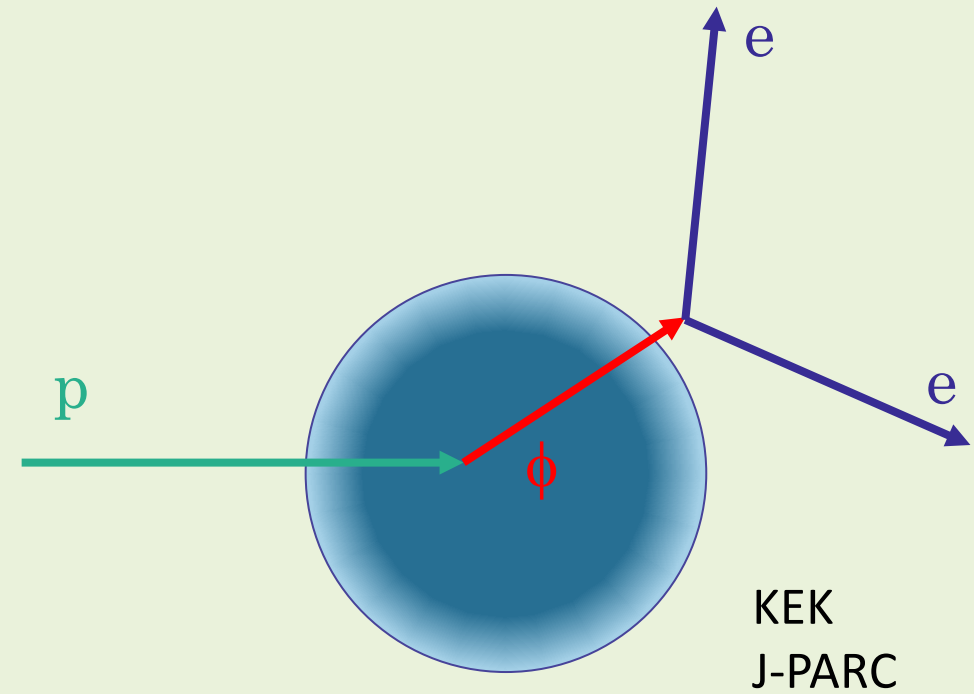
Small
absorption/broadening ?

How compare theory with the KEK E325 experiment?

Theory



Experiment



Realistic simulation of pA reaction is needed!

Our tool: a transport approach

PHSD (Parton Hadron String Dynamics)

E.L. Bratkovskaya and W. Cassing, Nucl. Phys. A **807**, 214 (2008).

W. Cassing and E.L. Bratkovskaya, Phys. Rev. C **78**, 034919 (2008).

Off-shell dynamics of vector mesons is included
 (dynamical modification of the vector meson spectral
 function during the simulated reaction)

off-shell terms

Testparticle approach:

$$\frac{d\vec{X}_i}{dt} = \frac{1}{1 - C_{(i)}} \frac{1}{2\varepsilon_i} \left[2\vec{P}_i + \vec{\nabla}_{P_i} \operatorname{Re} \Sigma_{(i)}^{\text{ret}} + \frac{\varepsilon_i^2 - \vec{P}_i^2 - M_0^2 - \operatorname{Re} \Sigma_{(i)}^{\text{ret}}}{\tilde{\Gamma}_{(i)}} \vec{\nabla}_{P_i} \tilde{\Gamma}_{(i)} \right],$$

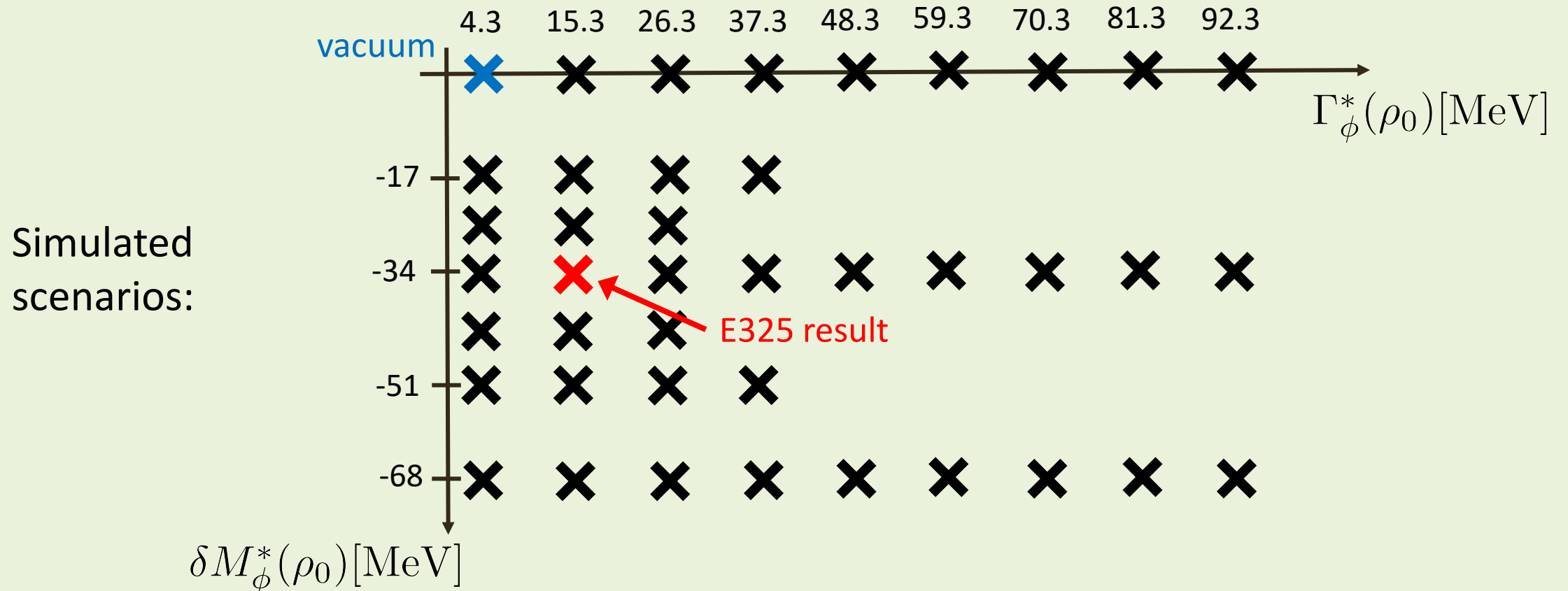
$$\frac{d\vec{P}_i}{dt} = -\frac{1}{1 - C_{(i)}} \frac{1}{2\varepsilon_i} \left[\vec{\nabla}_{X_i} \operatorname{Re} \Sigma_{(i)}^{\text{ret}} + \frac{\varepsilon_i^2 - \vec{P}_i^2 - M_0^2 - \operatorname{Re} \Sigma_{(i)}^{\text{ret}}}{\tilde{\Gamma}_{(i)}} \vec{\nabla}_{X_i} \tilde{\Gamma}_{(i)} \right],$$

$$\frac{d\varepsilon_i}{dt} = \frac{1}{1 - C_{(i)}} \frac{1}{2\varepsilon_i} \left[\frac{\partial \operatorname{Re} \Sigma_{(i)}^{\text{ret}}}{\partial t} + \frac{\varepsilon_i^2 - \vec{P}_i^2 - M_0^2 - \operatorname{Re} \Sigma_{(i)}^{\text{ret}}}{\tilde{\Gamma}_{(i)}} \frac{\partial \tilde{\Gamma}_{(i)}}{\partial t} \right],$$

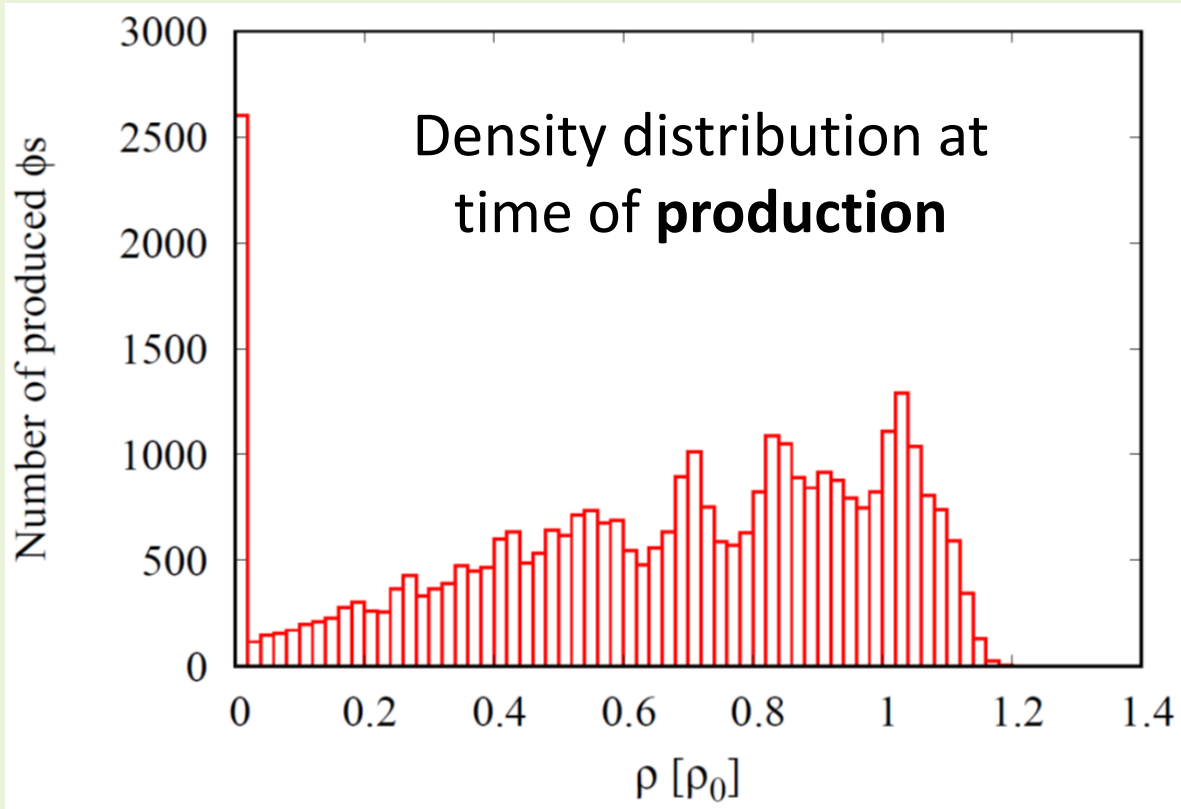
Advantage: vector meson spectra can be chosen freely

Our choice: a Breit-Wigner with density dependent mass and width

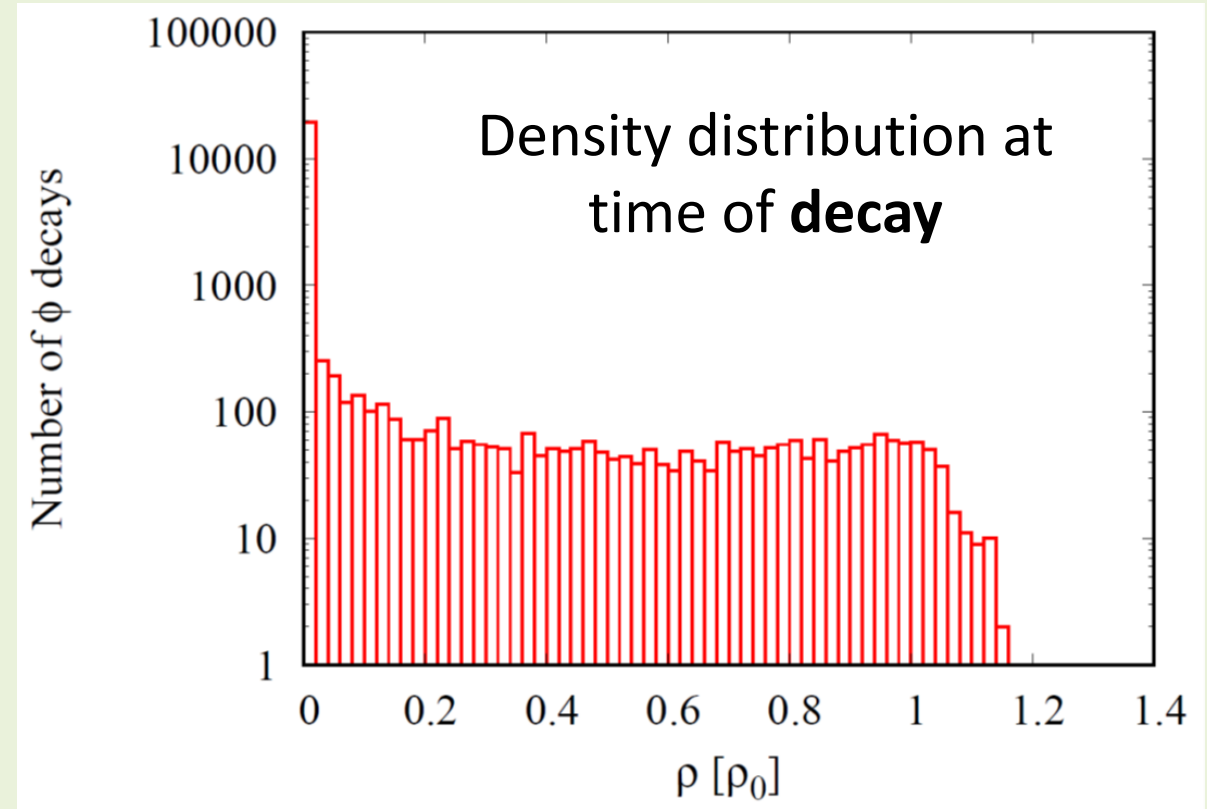
$$A_\phi(M, \rho) = C \frac{2}{\pi} \frac{M^2 \Gamma_\phi^*(M, \rho)}{[M^2 - M_\phi^{*2}(\rho)]^2 + M^2 \Gamma_\phi^{*2}(M, \rho)} \quad \text{with} \quad \begin{cases} M_\phi^*(\rho) = M_\phi^{\text{vac}} \left(1 - \alpha^\phi \frac{\rho}{\rho_0}\right), \\ \Gamma_\phi^*(M, \rho) = \Gamma_\phi^{\text{vac}} + \alpha_{\text{coll}}^\phi \frac{\rho}{\rho_0} \end{cases}$$



What density does the ϕ feel in the reaction (p+Cu at 12 GeV)?

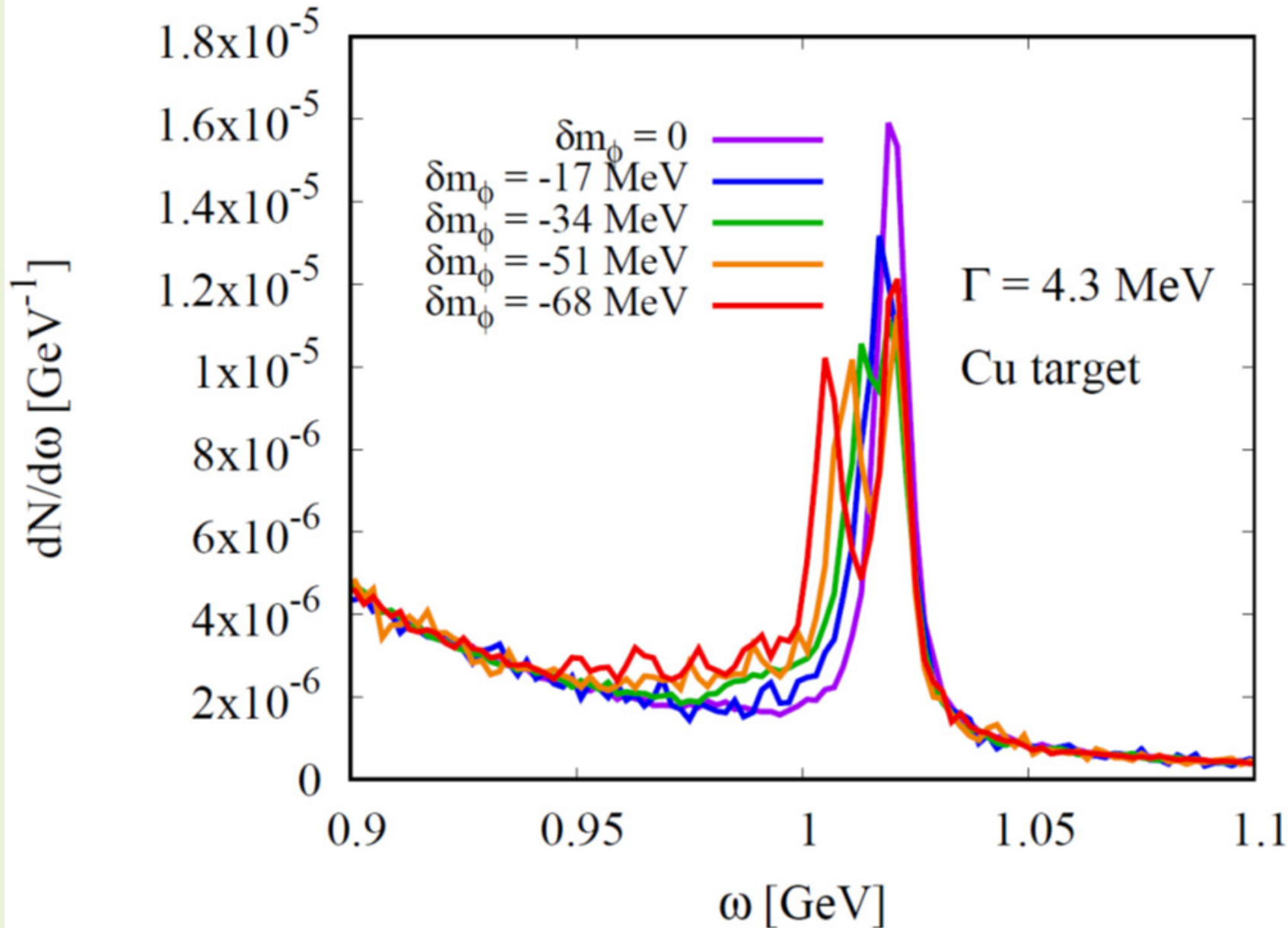


Majority of ϕ mesons are produced at densities around ρ_0



Majority of ϕ mesons decay in free space (note the log-scale!)

The dilepton spectrum in the ϕ meson region



p + Cu at 12 GeV

No acceptance
corrections!

No finite
resolution effects!

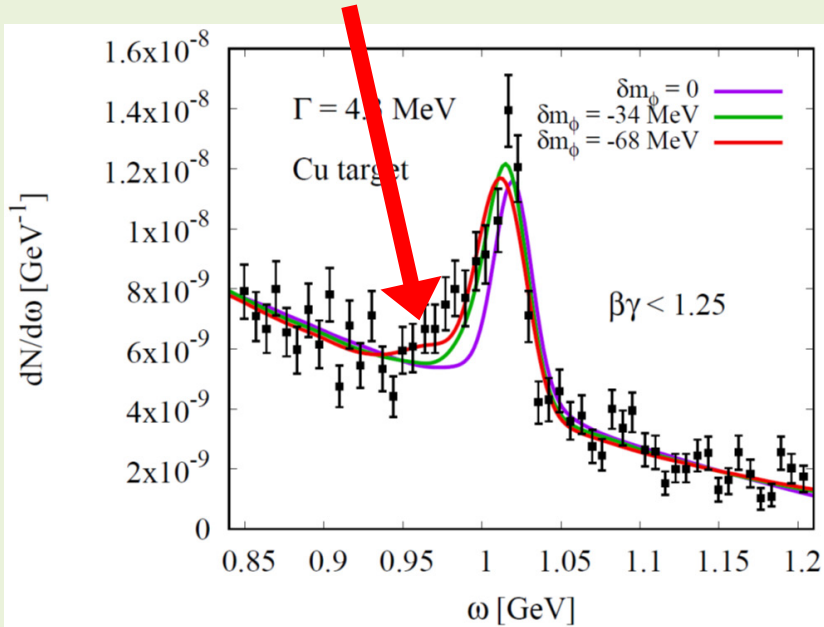
Fits to experimental Copper target data (E325)

As expected, a significant negative mass shift is needed to reproduce the slow φ data

Surprisingly large effect for fast φ s with a large mass shift



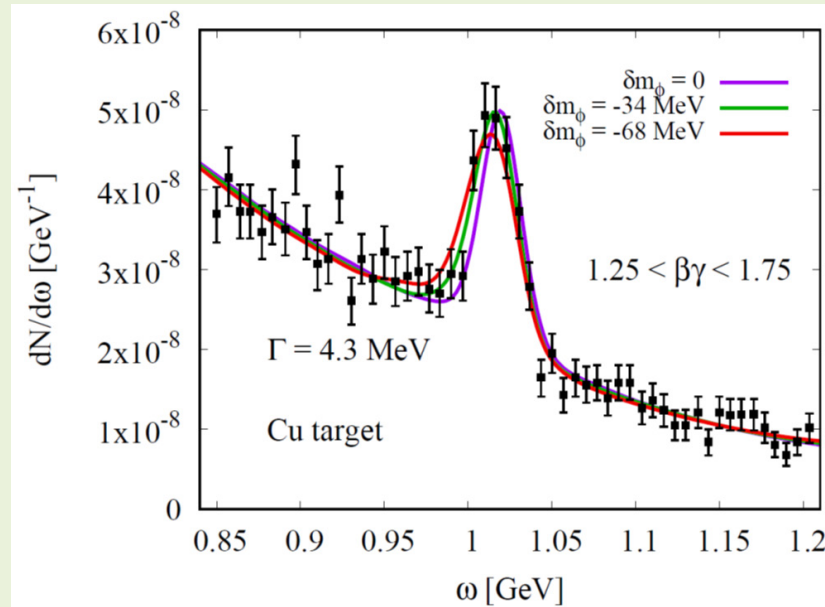
Related to initial stage of the collision



slow φ s



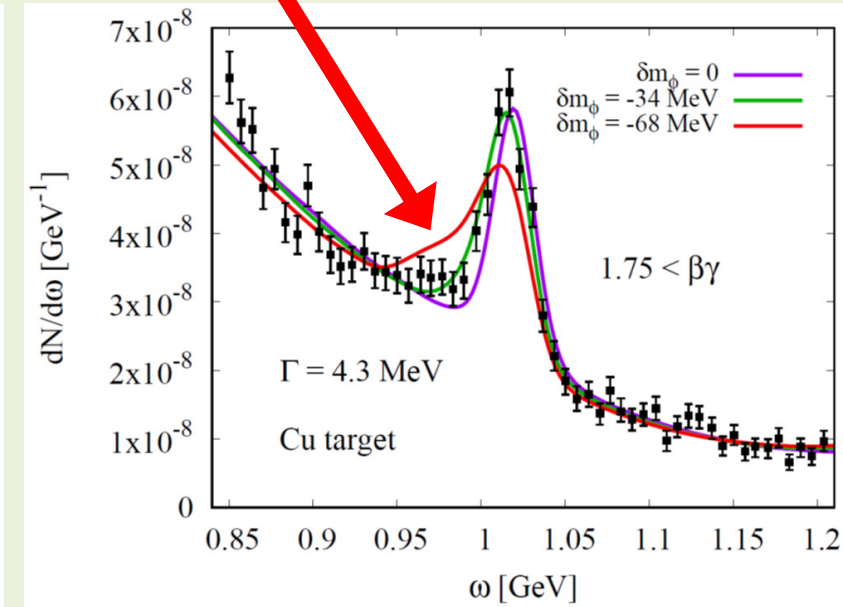
Favors relatively large negative mass shift



intermediate φ s



No strong constraints for any modification scenario



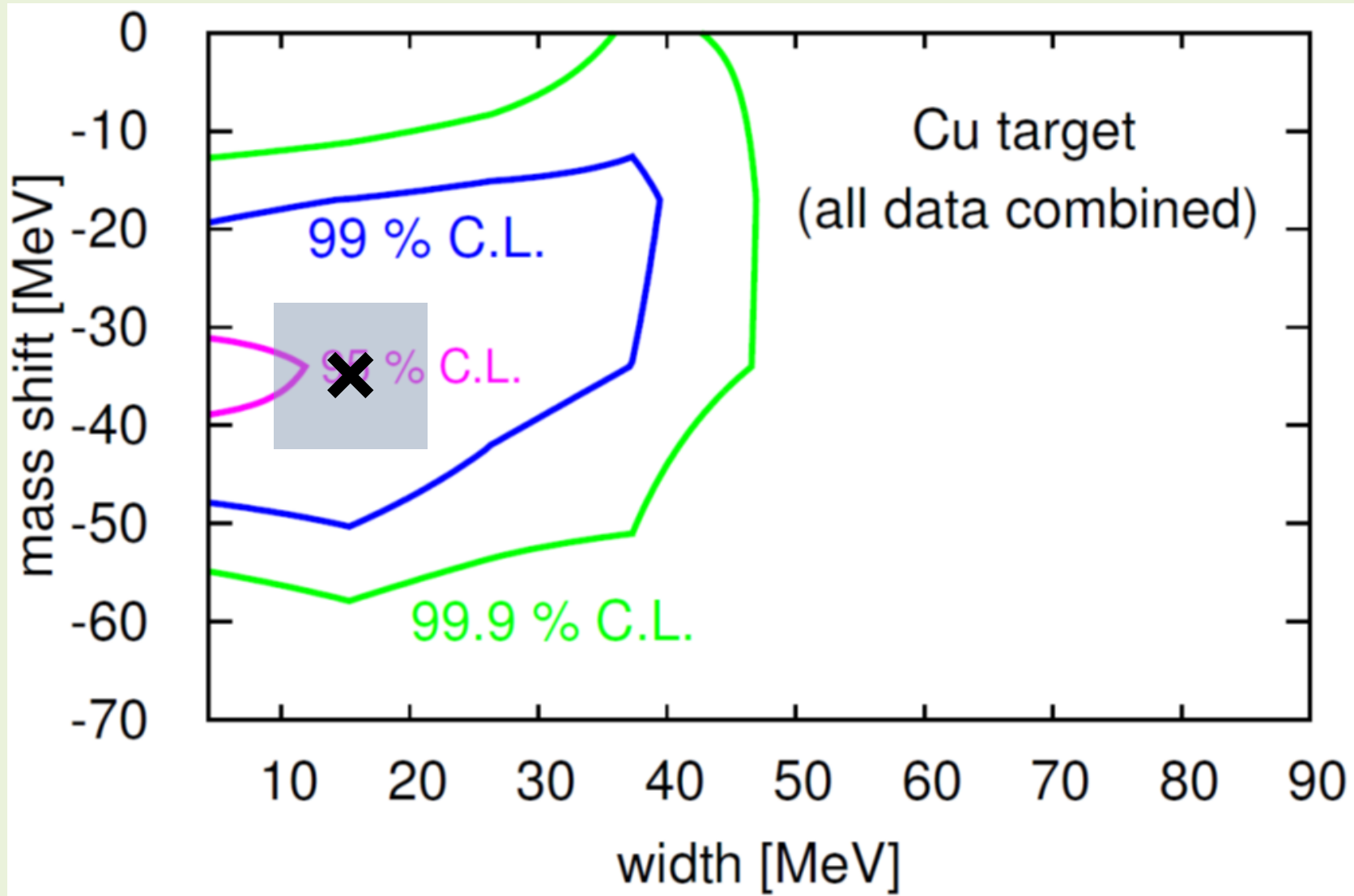
fast φ s



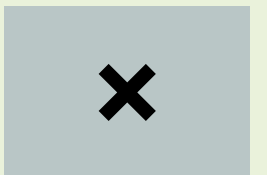
Favors small mass shift

Fits to experimental Copper target data (E325)

Confidence levels of combined Copper data



Conclusion of the
E325 Collaboration

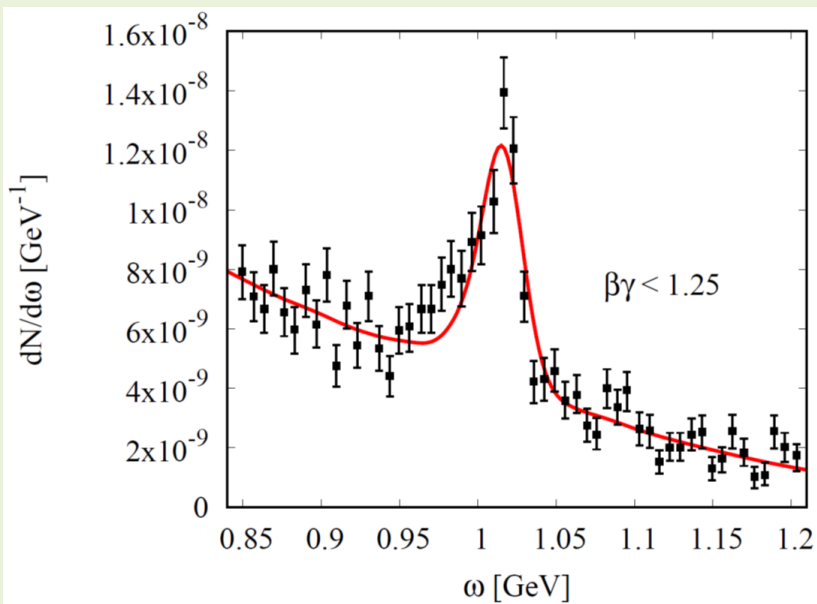


Best fit to E325 data (p + Cu at 12 GeV)

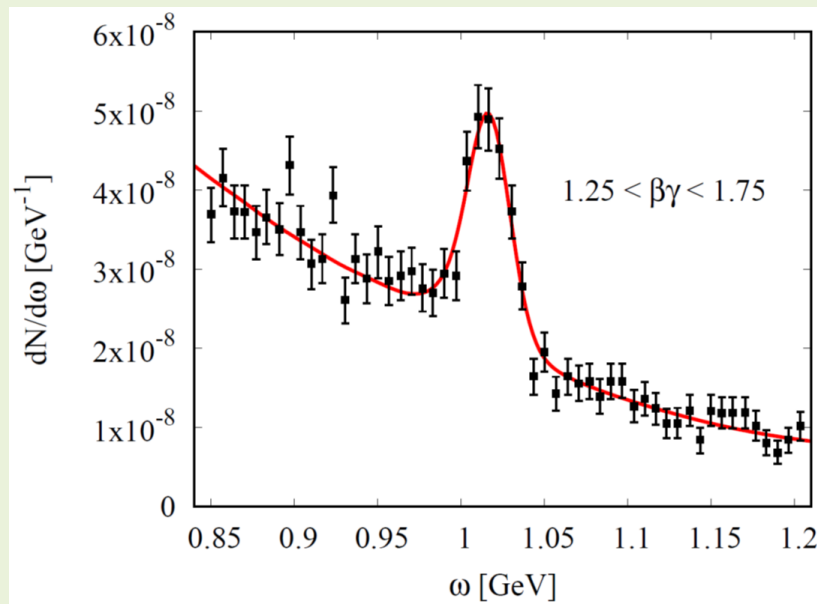
$$\delta m_\phi(\rho_0) = -34 \text{ MeV}$$

$$\Gamma(\rho_0) = 4.3 \text{ MeV}$$

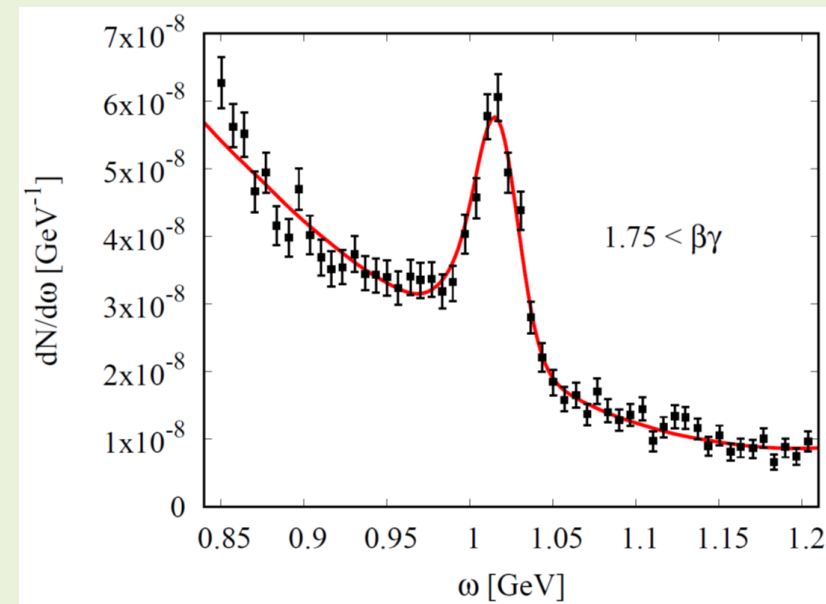
vacuum value



slow ϕ s



intermediate ϕ s



fast ϕ s

Summary and Conclusions

- ★ A lot of new experimental information about the φ N interaction is becoming available (LHC, J-PARC, HADES)
- ★ Studying the modification of the φ meson spectral function experimentally at finite density is non-trivial. A good understanding of the underlying reactions is needed!
- ★ We conducted numerical simulations of the pA reactions measured at the E325 experiment at KEK, using the PHSD transport code

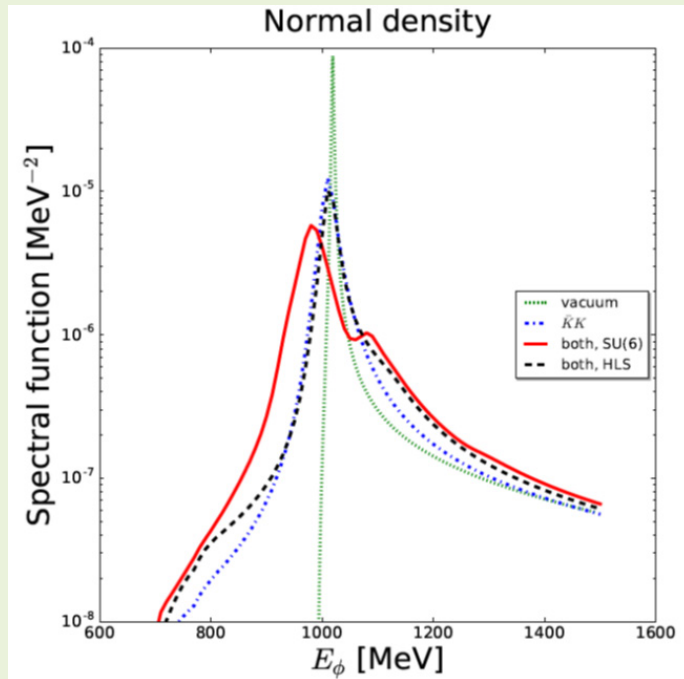


Our results indicate that the experimental data favor a **negative mass shift with zero or only small broadening!**

Backup slides

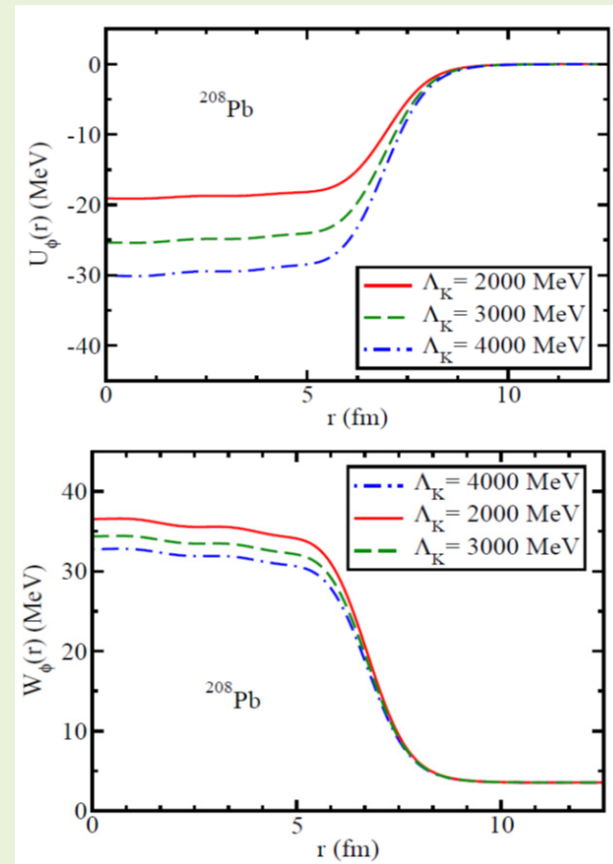
Many theoretical works about the ϕ meson at finite density in recent years

Spectral functions from hadronic models



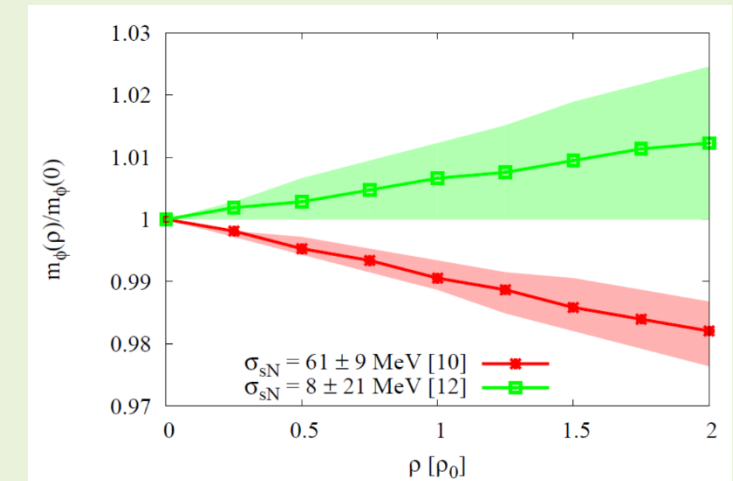
- P. Gubler and W. Weise, Phys. Lett. B **751**, 396 (2015).
P. Gubler and W. Weise, Nucl. Phys. A **954**, 125 (2016).
D. Cabrera *et al.*, Phys. Rev. C **95**, 015201 (2017).
D. Cabrera *et al.*, Phys. Rev. C **96**, 034618 (2017).

Possibility of ϕ -nucleus bound state



- J.J. Cobos-Martinez *et al.*, Phys. Lett. B **771**, 113 (2017).
J.J. Cobos-Martinez *et al.*, Phys. Rev. C **96**, 035201 (2017).


Mass shift in nuclear matter from QCD sum rules



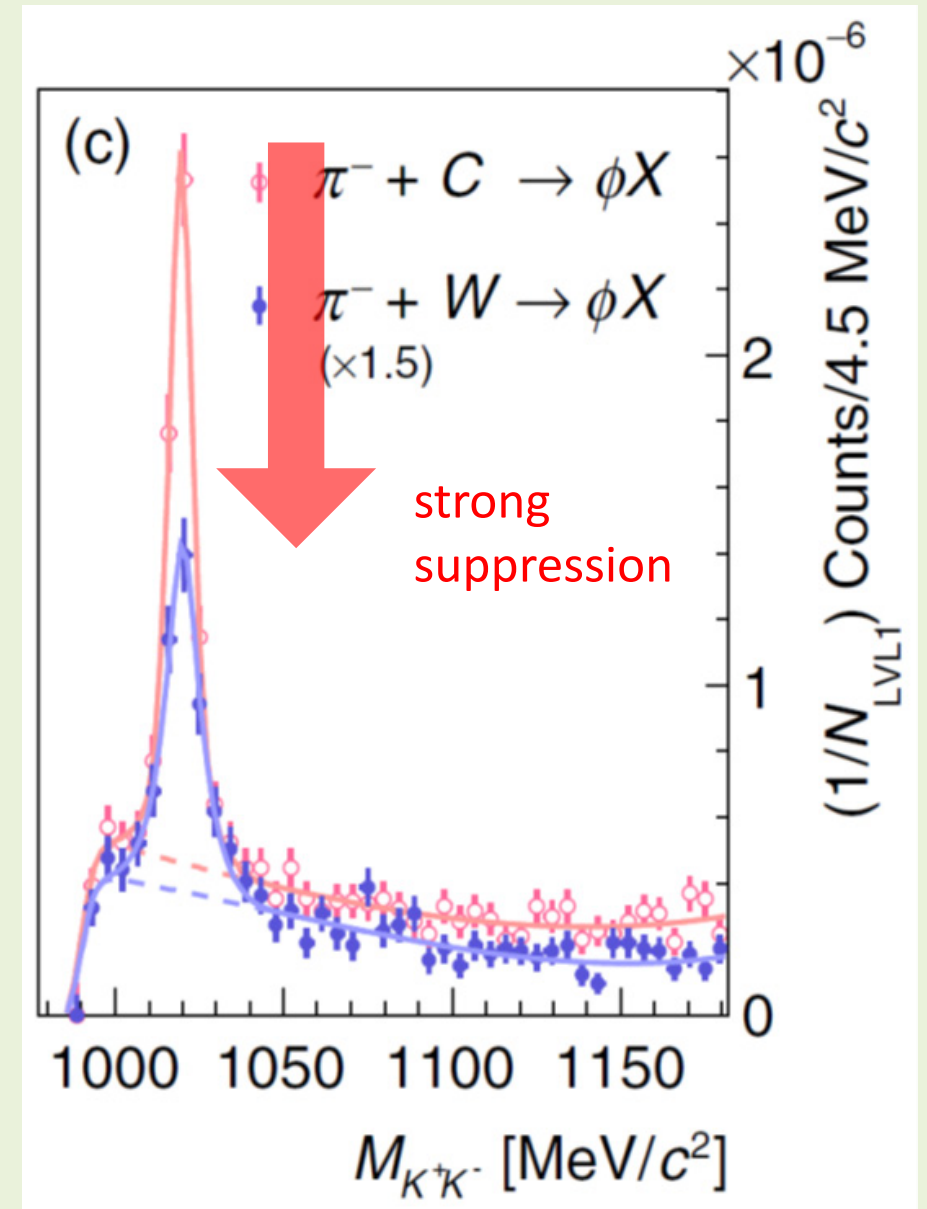
- P. Gubler and K. Ohtani, Phys. Rev. D **90**, 094002 (2014).
H.J. Kim *et al.*, Phys. Lett. B **772**, 194 (2017).
H.J. Kim and P. Gubler, Phys. Lett. B **805**, 135412 (2020).

Recent experimental results

HADES: 1.7 GeV π^- -A-reaction

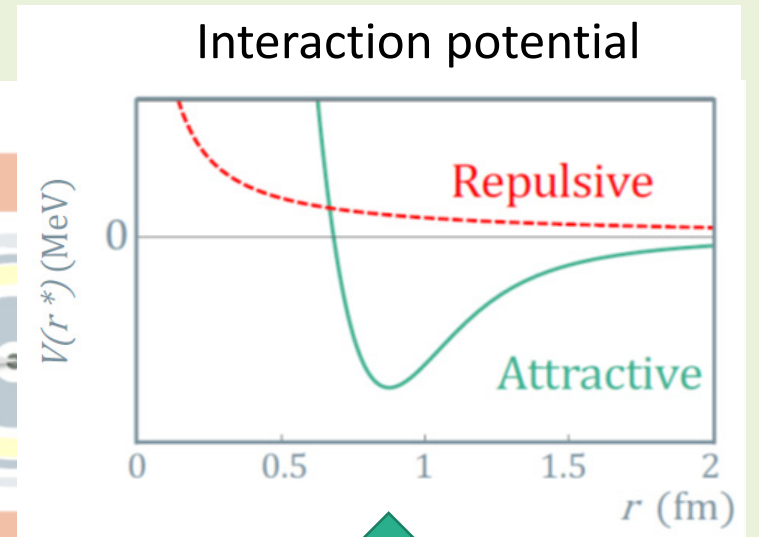
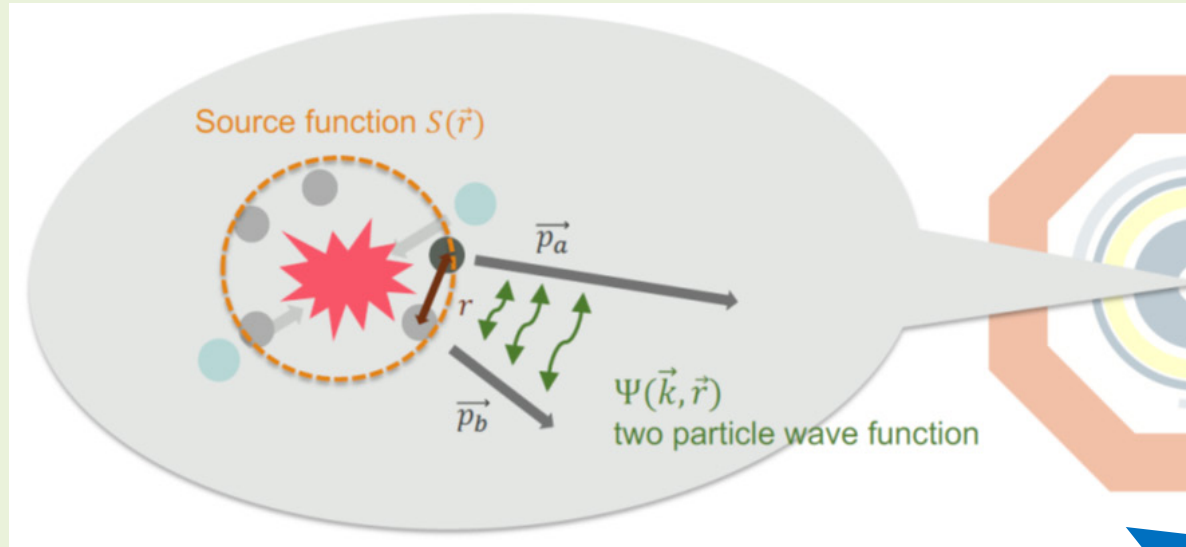
- ★ Larger suppression of K^- in the Tungsten target compared to the Carbon target
 - ★ K^-/ϕ ratio is similar for both Tungsten and Carbon targets
- 
- ★ Observation of large suppression (broadening?) of the ϕ meson in large nuclei

K^+K^- - invariant mass spectrum

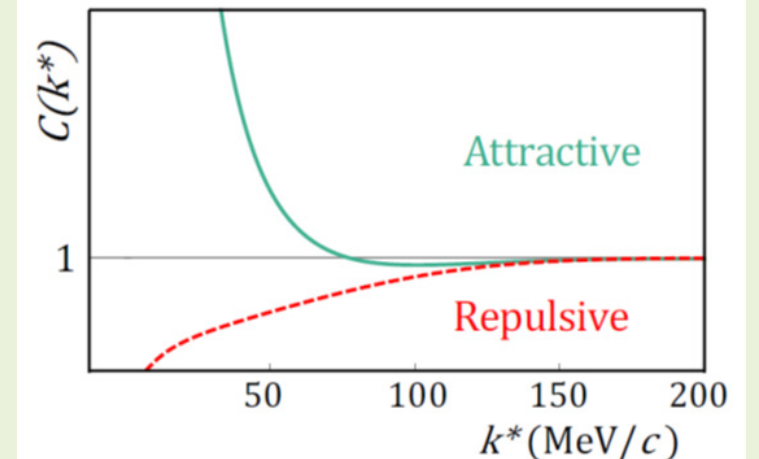


New experimental results

ALICE (Femtoscscopy)



Correlation function



The observable to be measured: the correlation function:

$$C(k) = \mathcal{N} \frac{N_{\text{Same}}}{N_{\text{Mixed}}} = \int S(\vec{r}) |\Psi(\vec{k}, \vec{r})|^2 d^3\vec{r}$$

Emission source (Gaussian)

Relative momentum of the particle pair

Results for the ϕ meson mass at rest (from QCD sum rules)

Most important parameter, that determines the behavior of the ϕ meson mass at finite density:

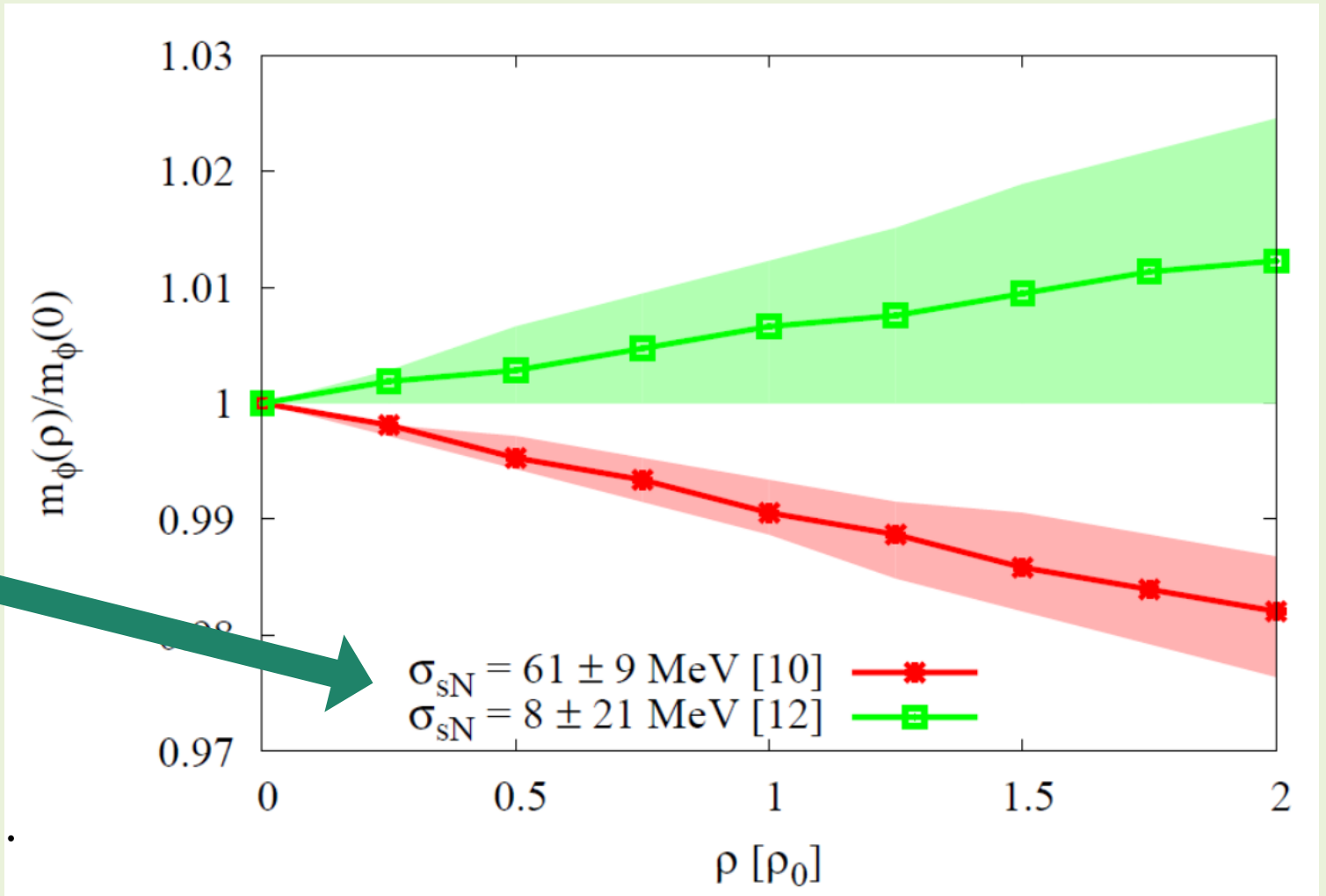
Strangeness content of the nucleon



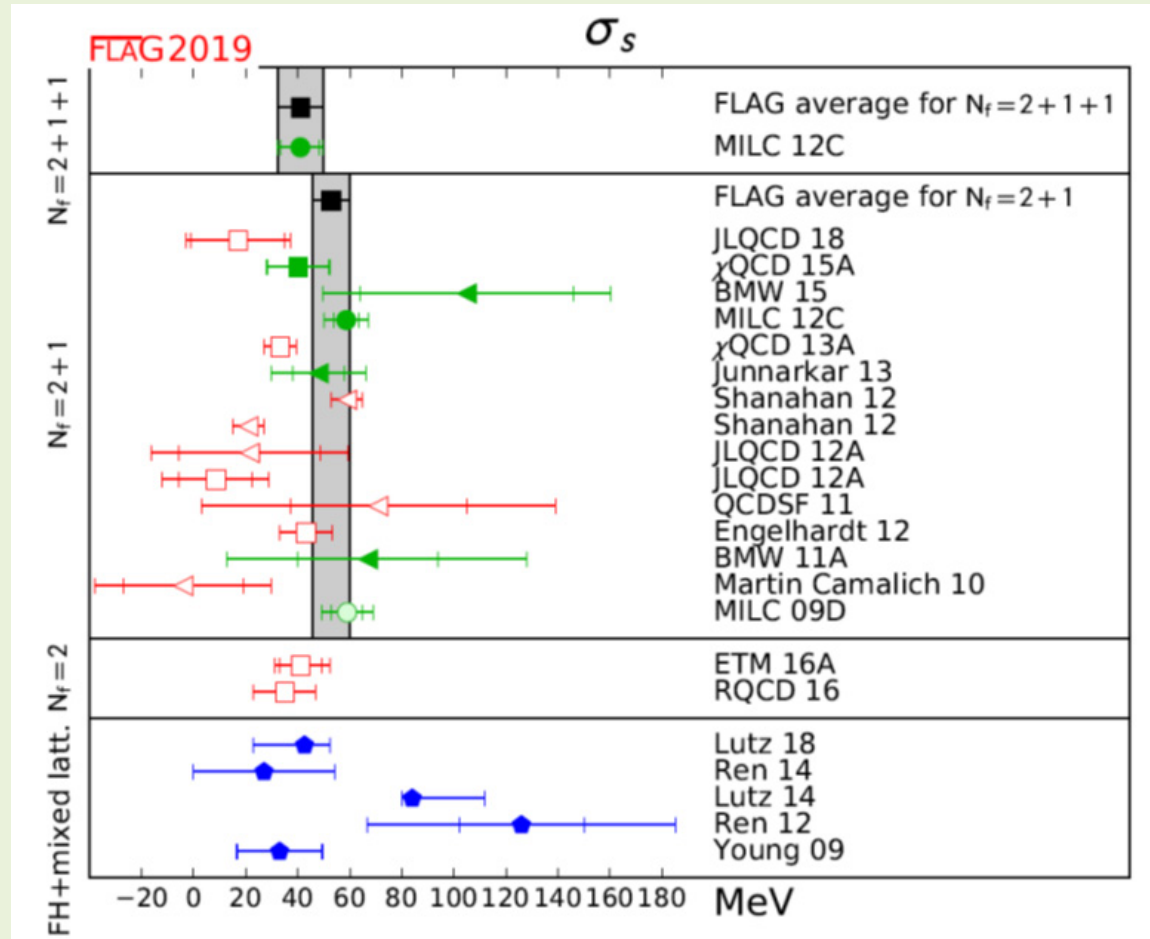
$$\sigma_{sN} = m_s \langle N | \bar{s}s | N \rangle$$



$$\langle \bar{s}s \rangle_\rho = \langle \bar{s}s \rangle_0 + \langle N | \bar{s}s | N \rangle \rho + \dots$$



What does lattice QCD say about σ_s ?



<http://flag.unibe.ch/2019/>

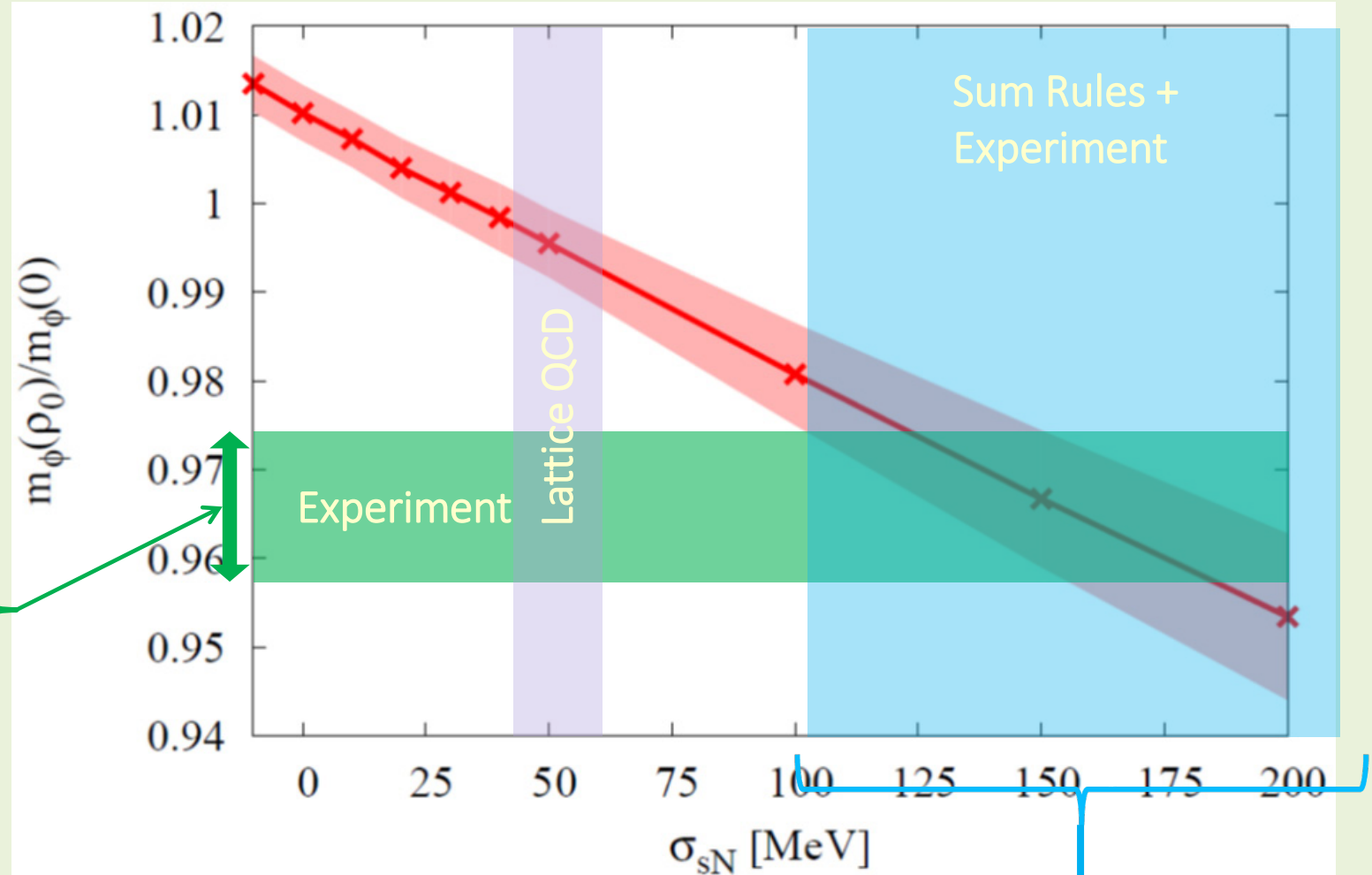
See also the most recent results of the BMW collaboration: Sz. Borsanyi et al., arXiv:2007.03319 [hep-lat].

Compare Theory with Experiment

Not consistent?

Will be measured again with better statistics at the E16 experiment at J-PARC!

$$\frac{m_\phi(\rho)}{m_\phi(0)} = 0.966 \pm 0.007$$

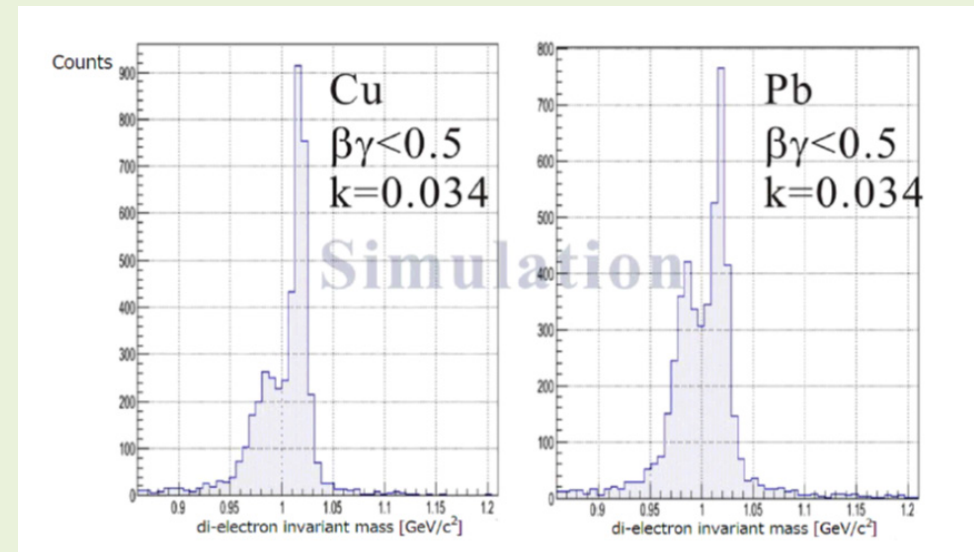
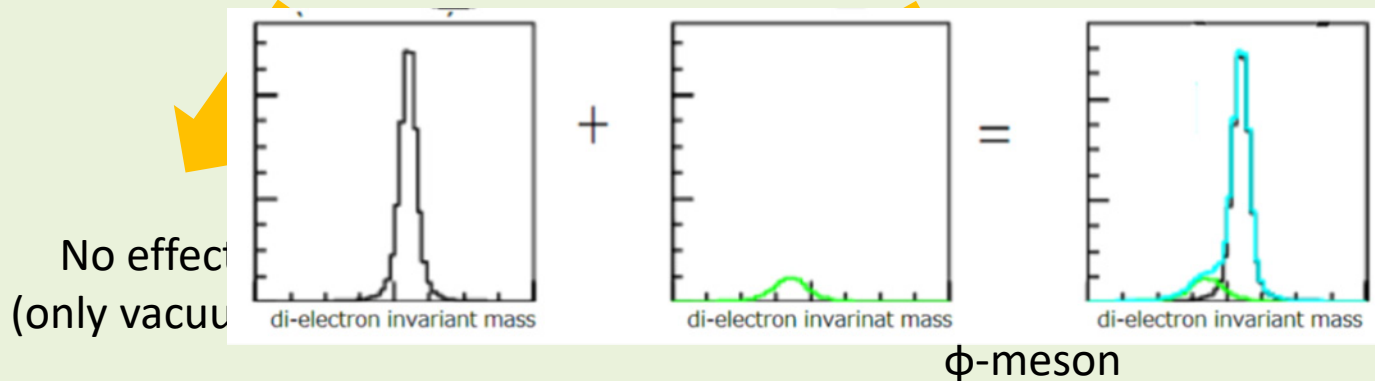
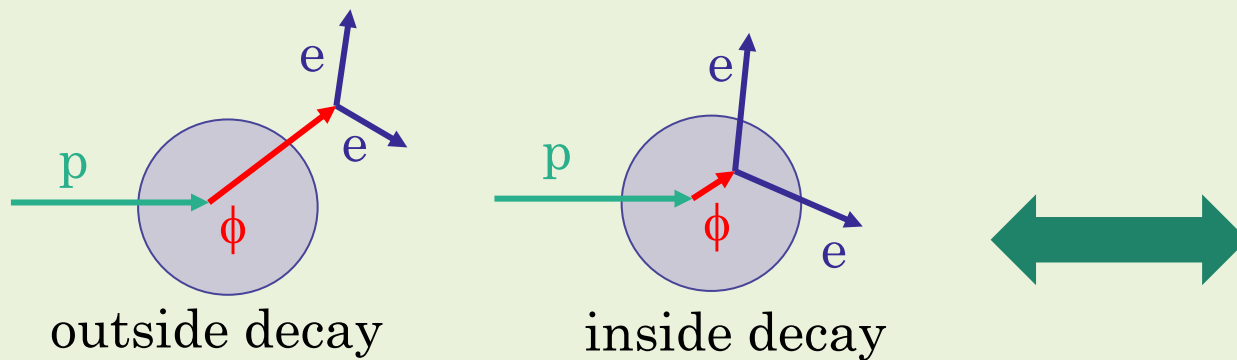


$$\sigma_{sN} \sim 160 \pm 50 \text{ MeV}$$

The experimental situation

The E325 Experiment (KEK)

Slowly moving ϕ mesons are produced in 12 GeV $p+A$ reactions and are measured through di-leptons.



Y. Morino et. al. (J-PARC E16 Collaboration),
JPS Conf. Proc. 8, 022009 (2015).

Our tool: a transport code

PHSD (Parton Hadron String Dynamics)

W. Cassing and E. Bratkovskaya, Phys. Rev. C **78**, 034919 (2008).

Example:

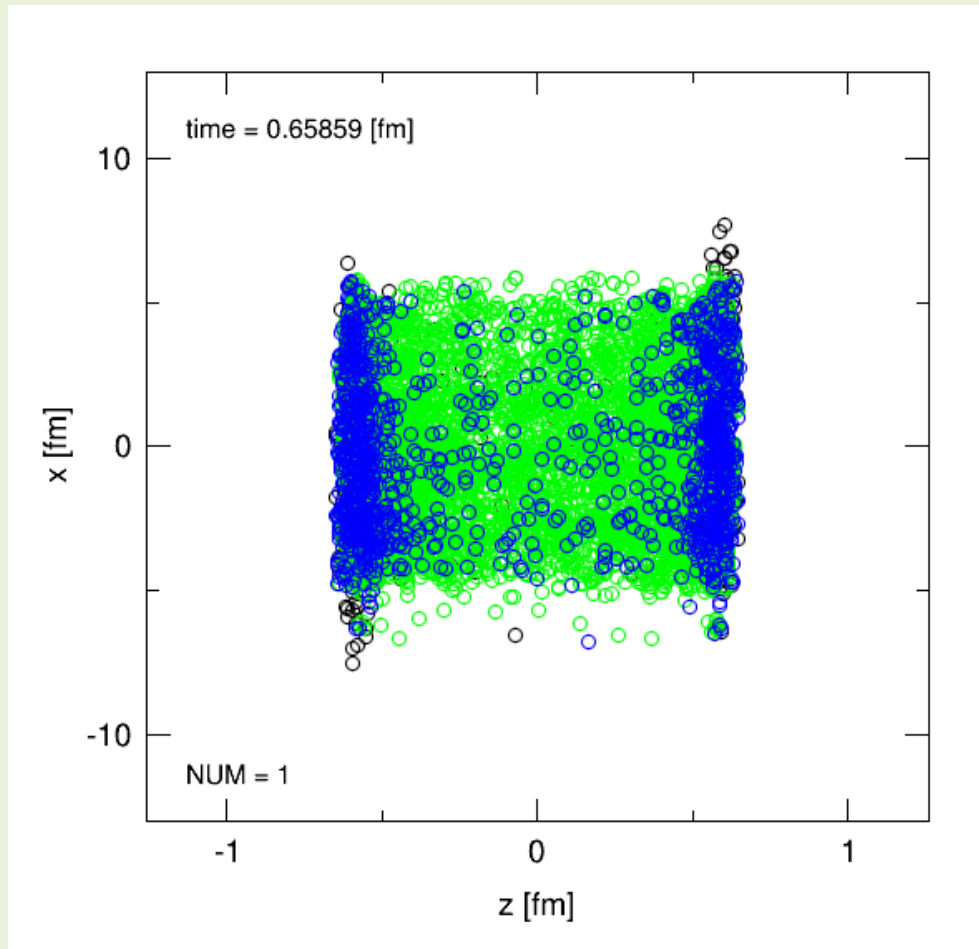
Au+Au collision at 200 GeV

$b = 2$ fm

nucleons

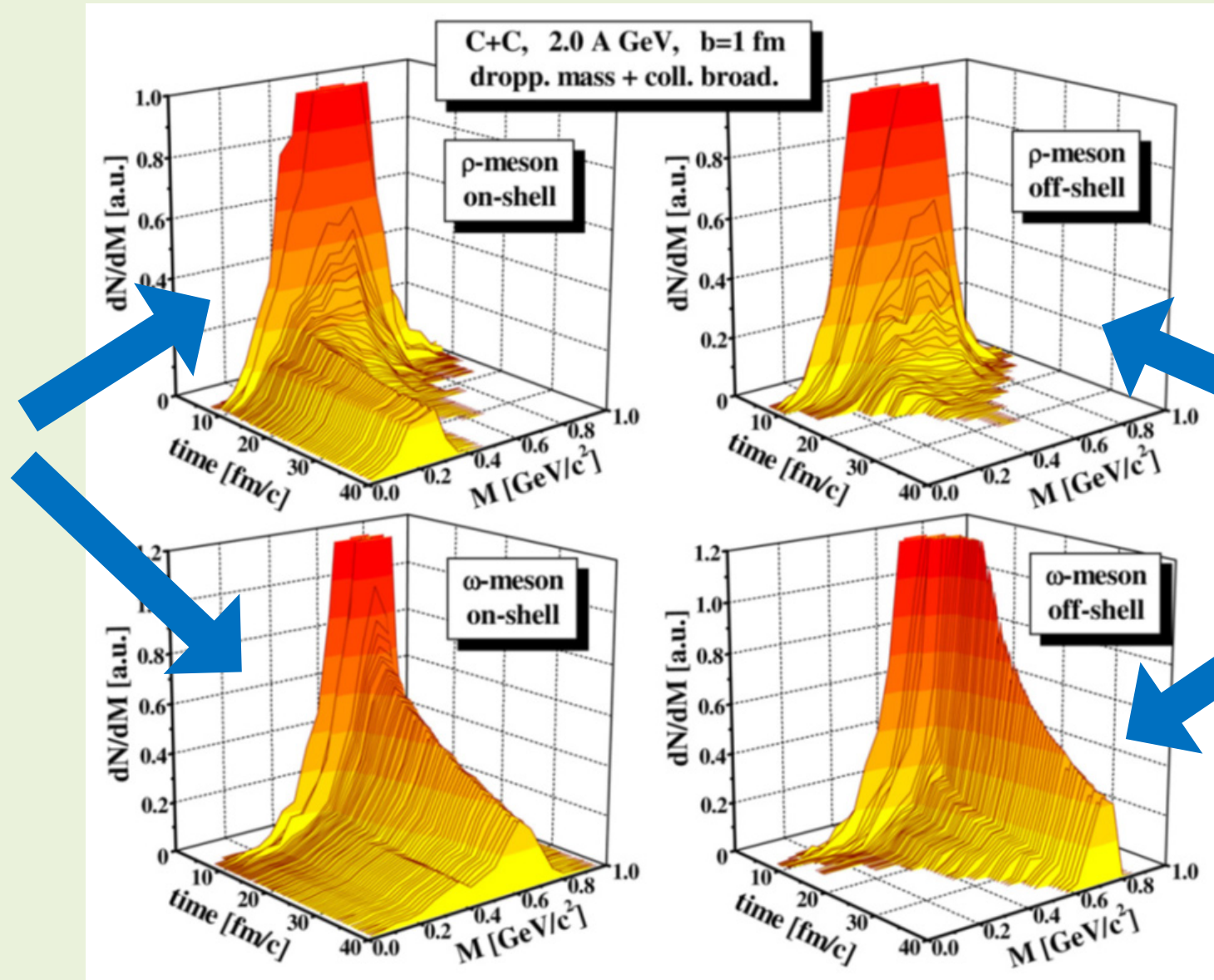
quarks

gluons



The importance of off-shell contributions

Only on-shell contributions:
Vacuum spectral function
are not recovered at late
time of the reaction



Off-shell
contributions
included:
correct behavior

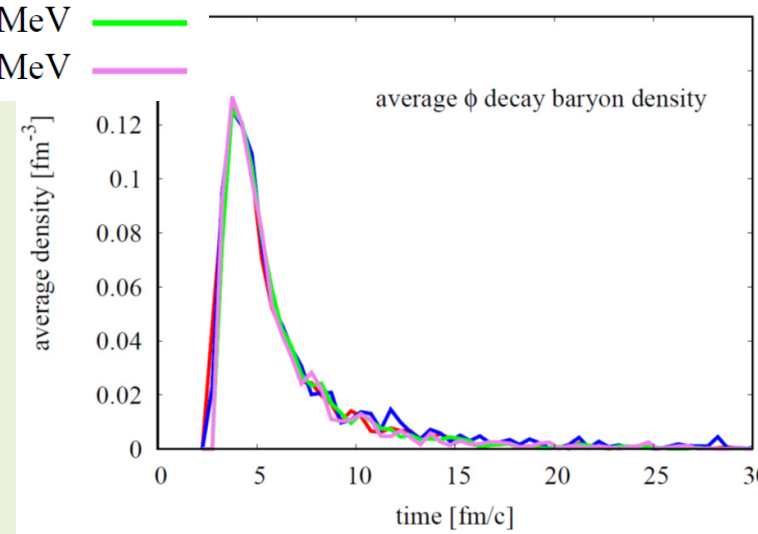
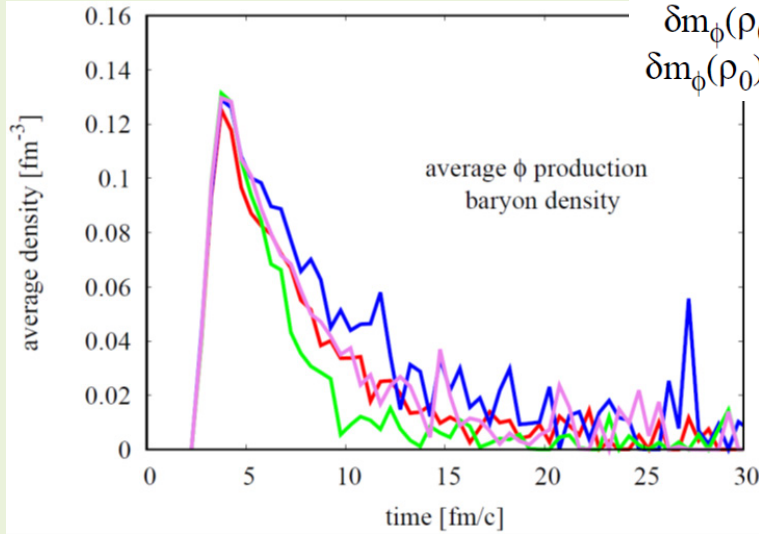
What density does the ϕ feel in the reaction (p+Cu/C at 12 GeV)?

Production

Decay

- $\delta m_\phi(\rho_0) = 0, \Gamma(\rho_0) = 4.3 \text{ MeV}$ — (red line)
- $\delta m_\phi(\rho_0) = 0, \Gamma(\rho_0) = 59.3 \text{ MeV}$ — (blue line)
- $\delta m_\phi(\rho_0) = -68 \text{ MeV}, \Gamma(\rho_0) = 4.3 \text{ MeV}$ — (green line)
- $\delta m_\phi(\rho_0) = -68 \text{ MeV}, \Gamma(\rho_0) = 59.3 \text{ MeV}$ — (magenta line)

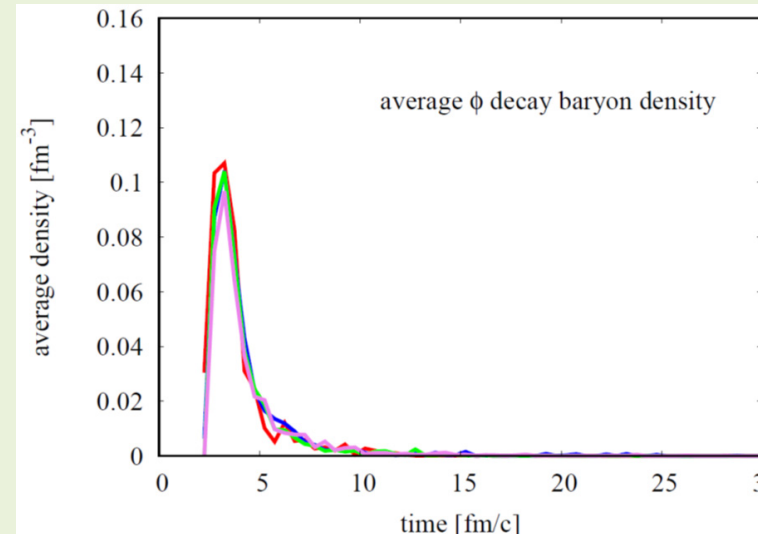
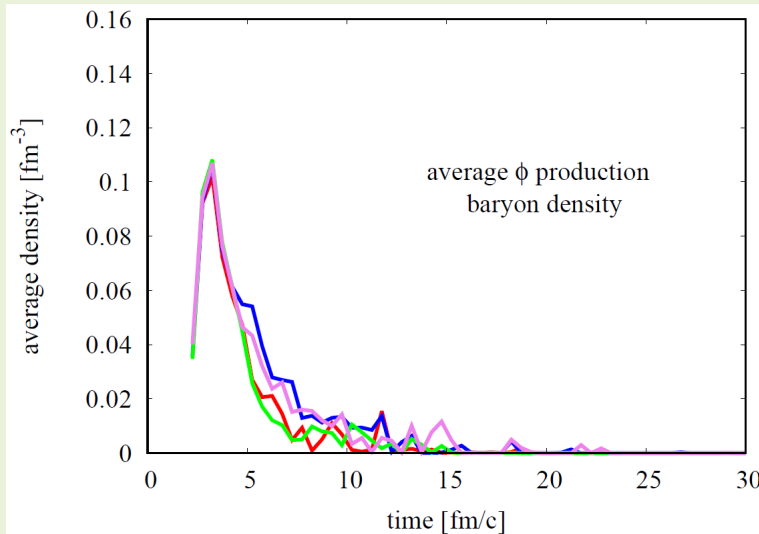
Cu
target



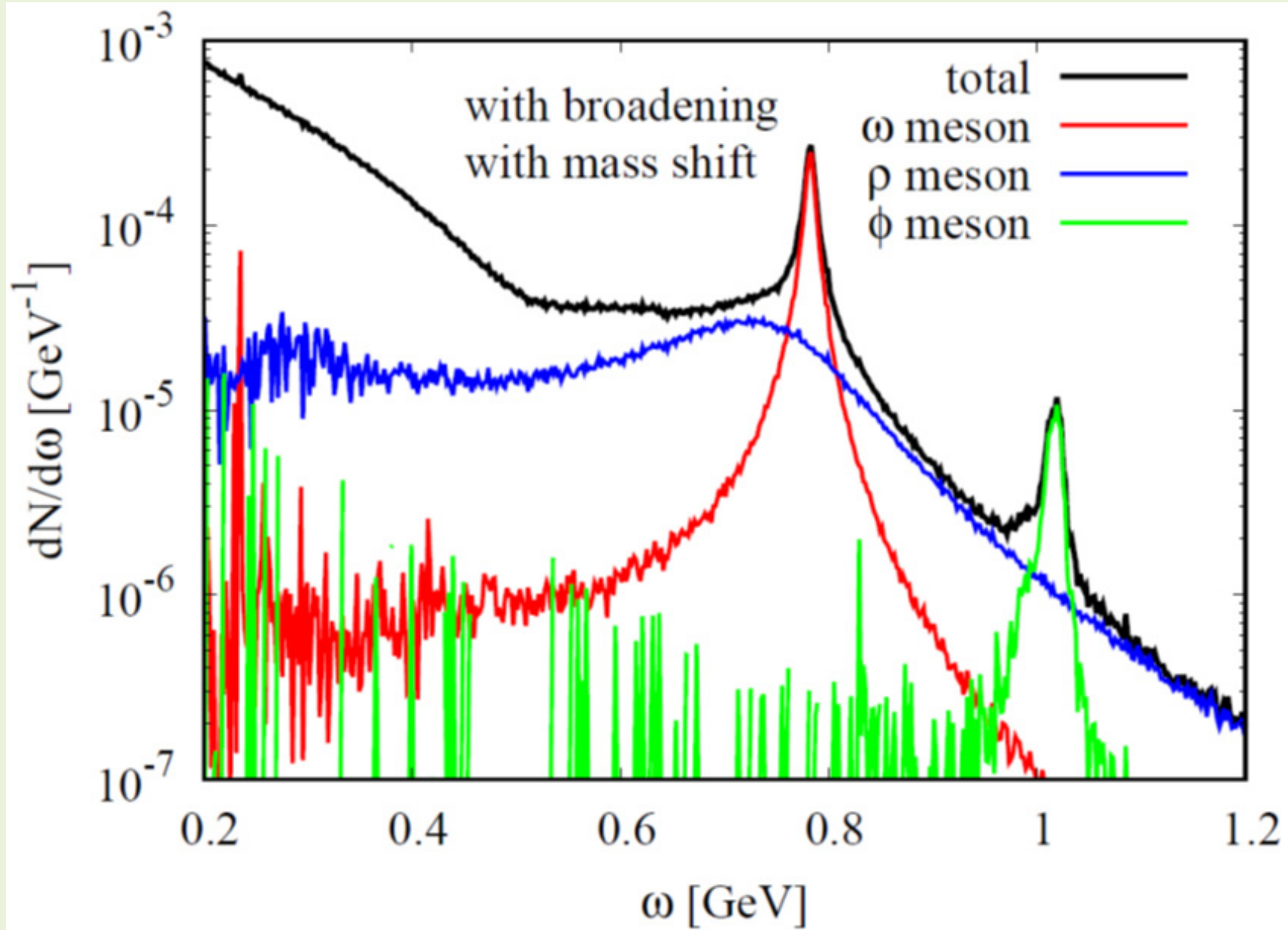
ϕ mesons are on average created at a density significantly below ρ_0

ϕ mesons on average decay at a density significantly below ρ_0

C
target



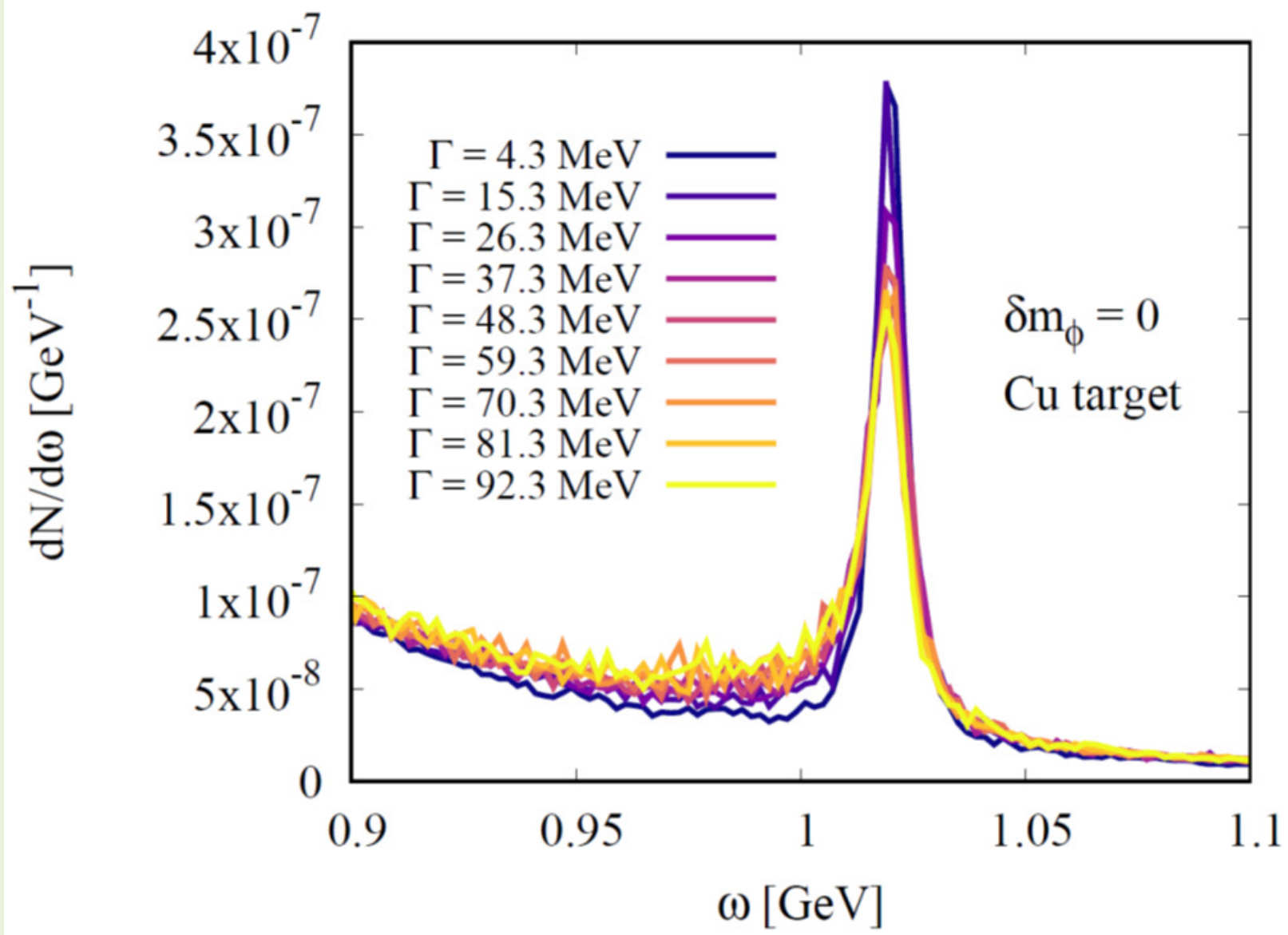
The dilepton spectrum



p+Cu at 12 GeV

The ϕ meson peak is clearly visible.

The dilepton spectrum in the ϕ meson region



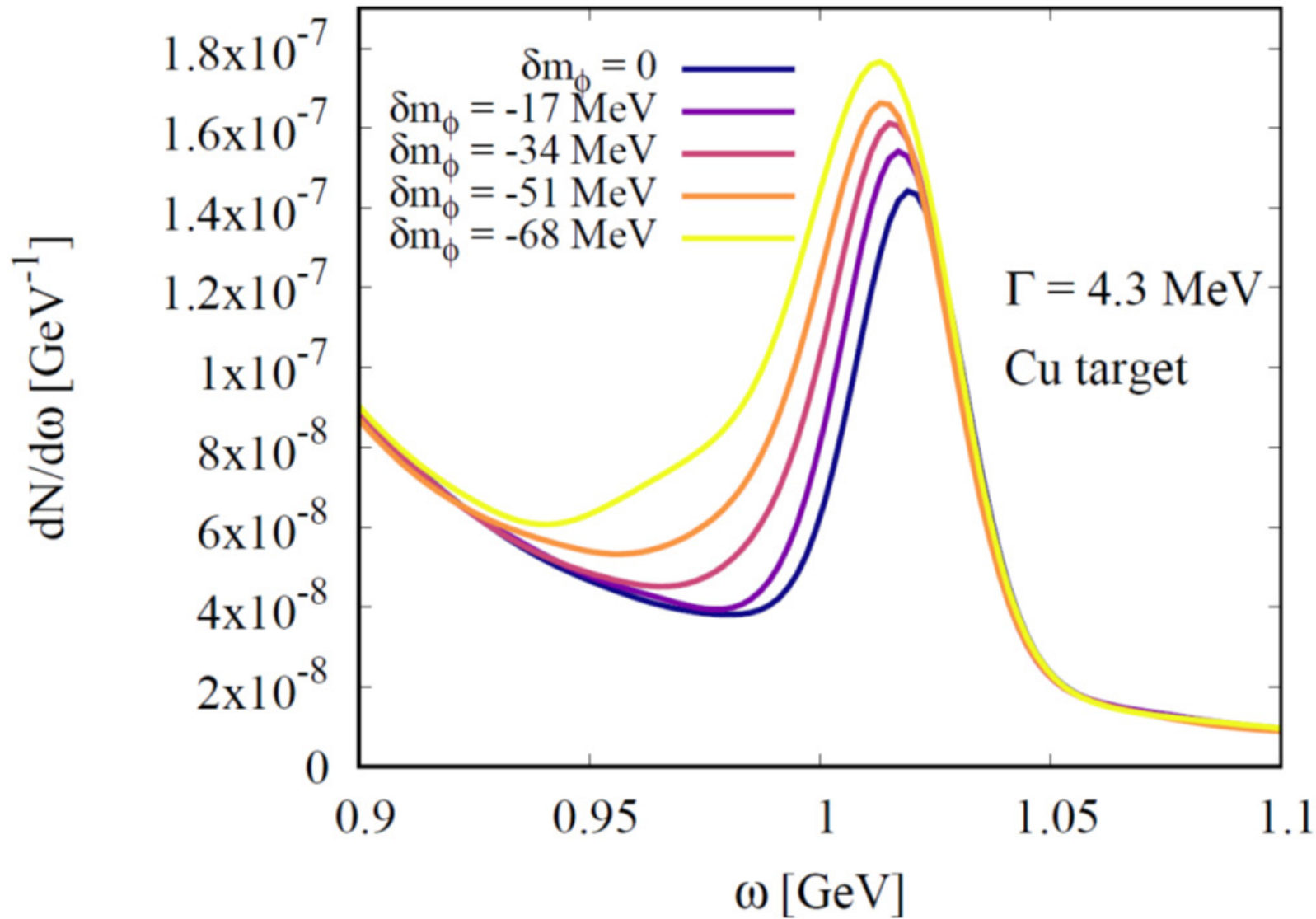
p + Cu at 12 GeV

No acceptance
corrections!

No finite
resolution effects!

Preliminary

The dilepton spectrum in the ϕ meson region

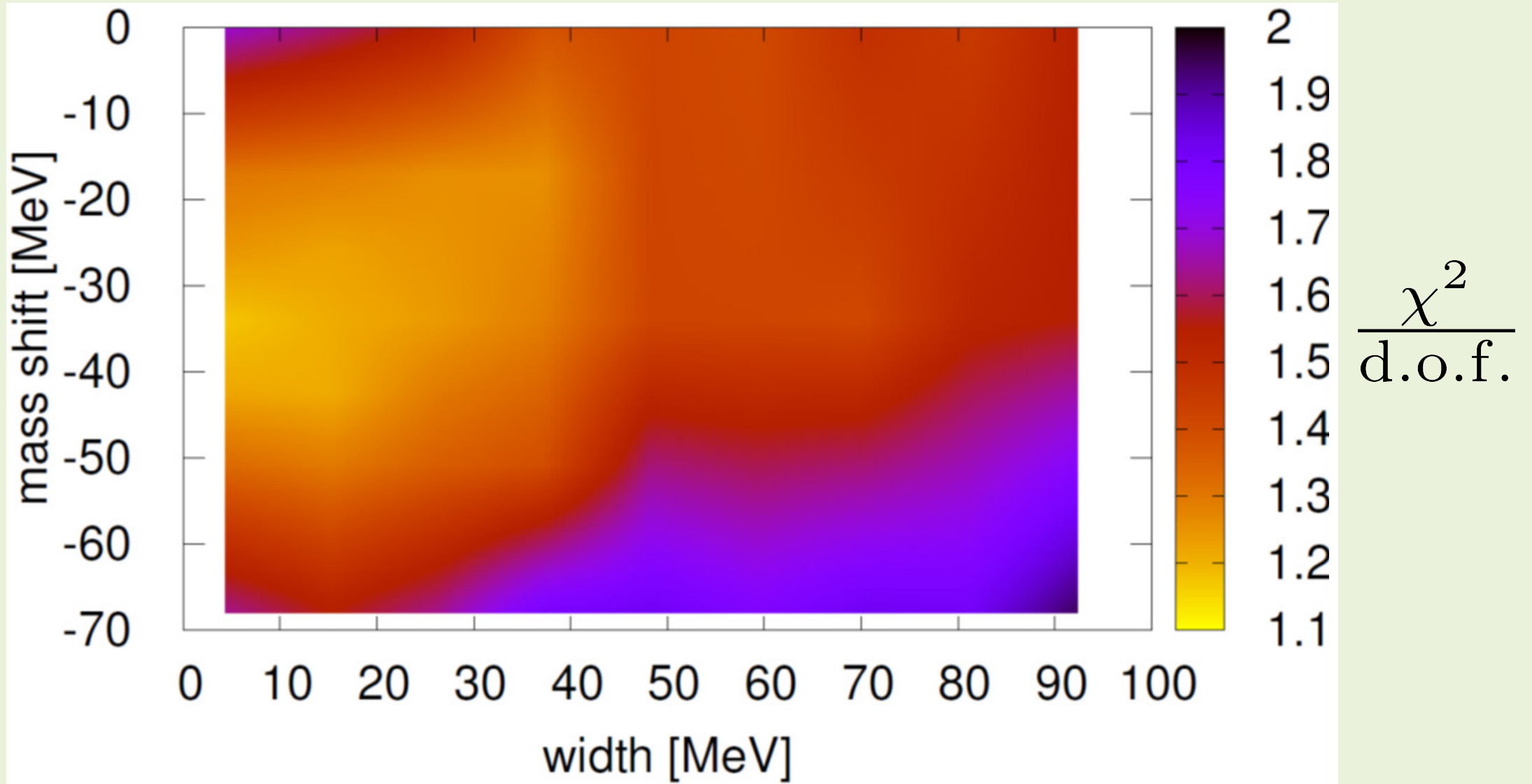


p + Cu at 12 GeV

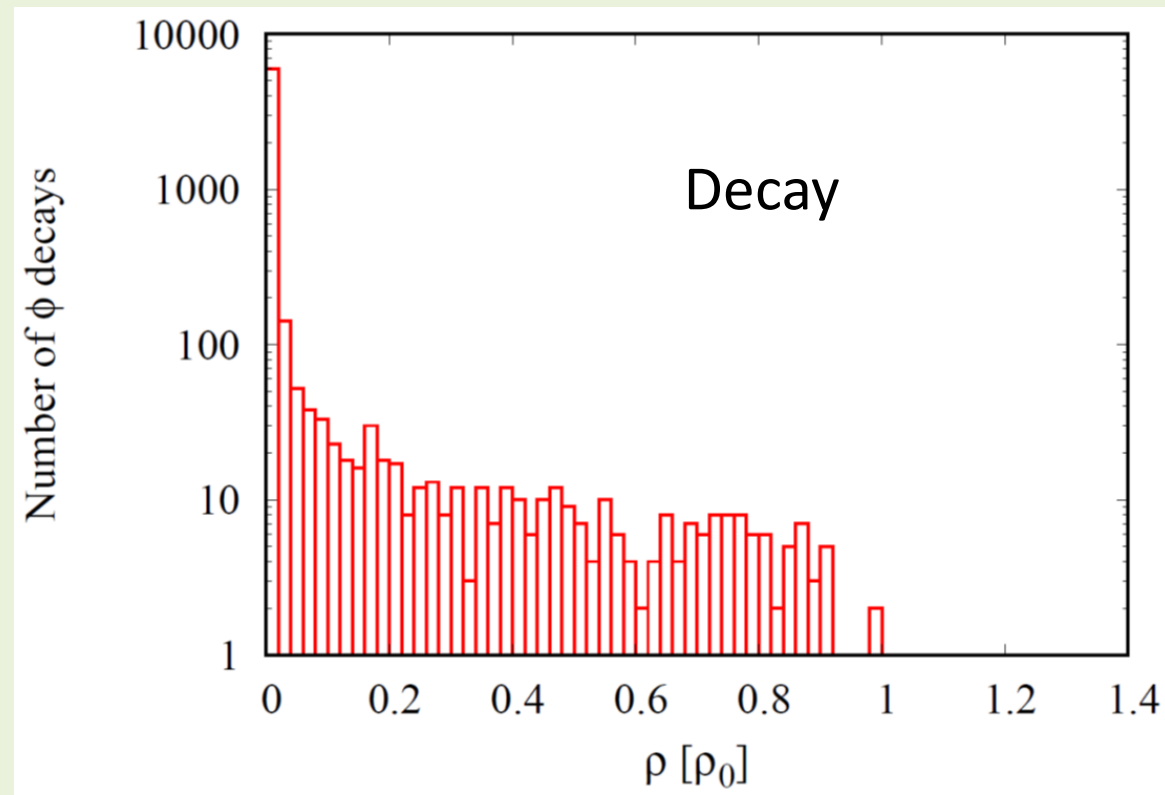
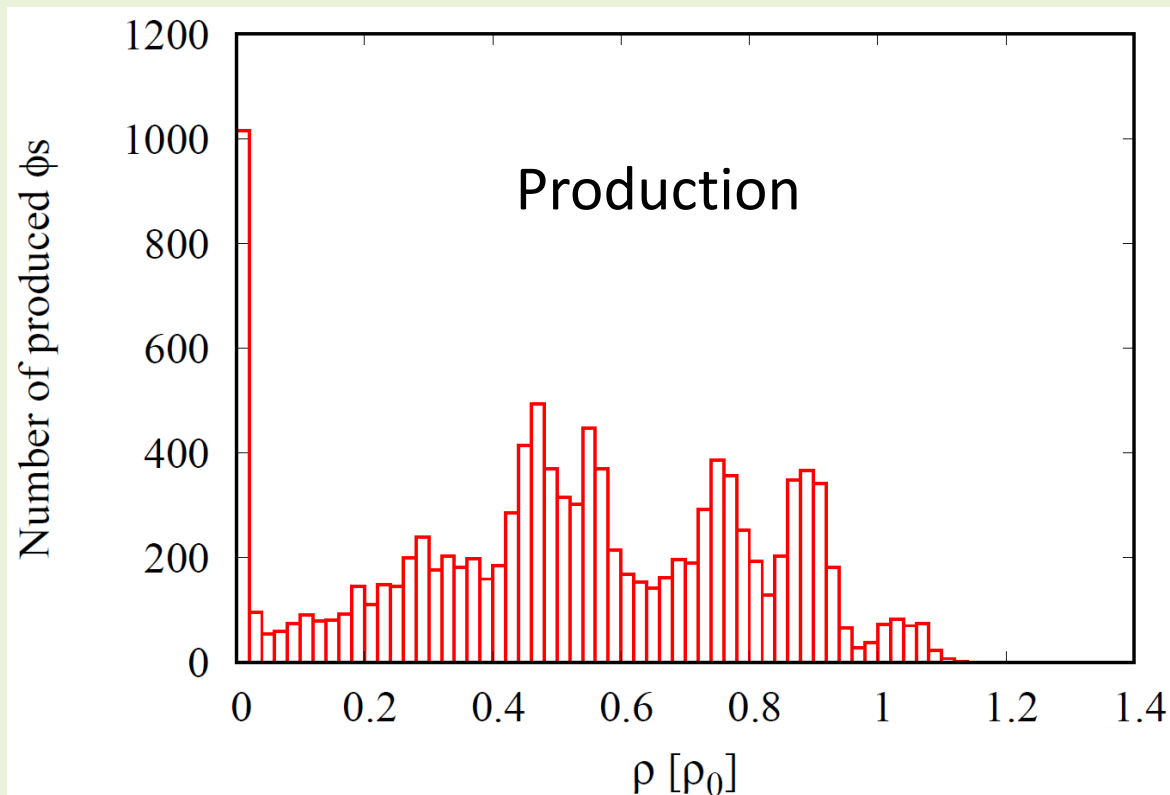
With acceptance corrections!

With finite resolution effects!

All Copper data combined

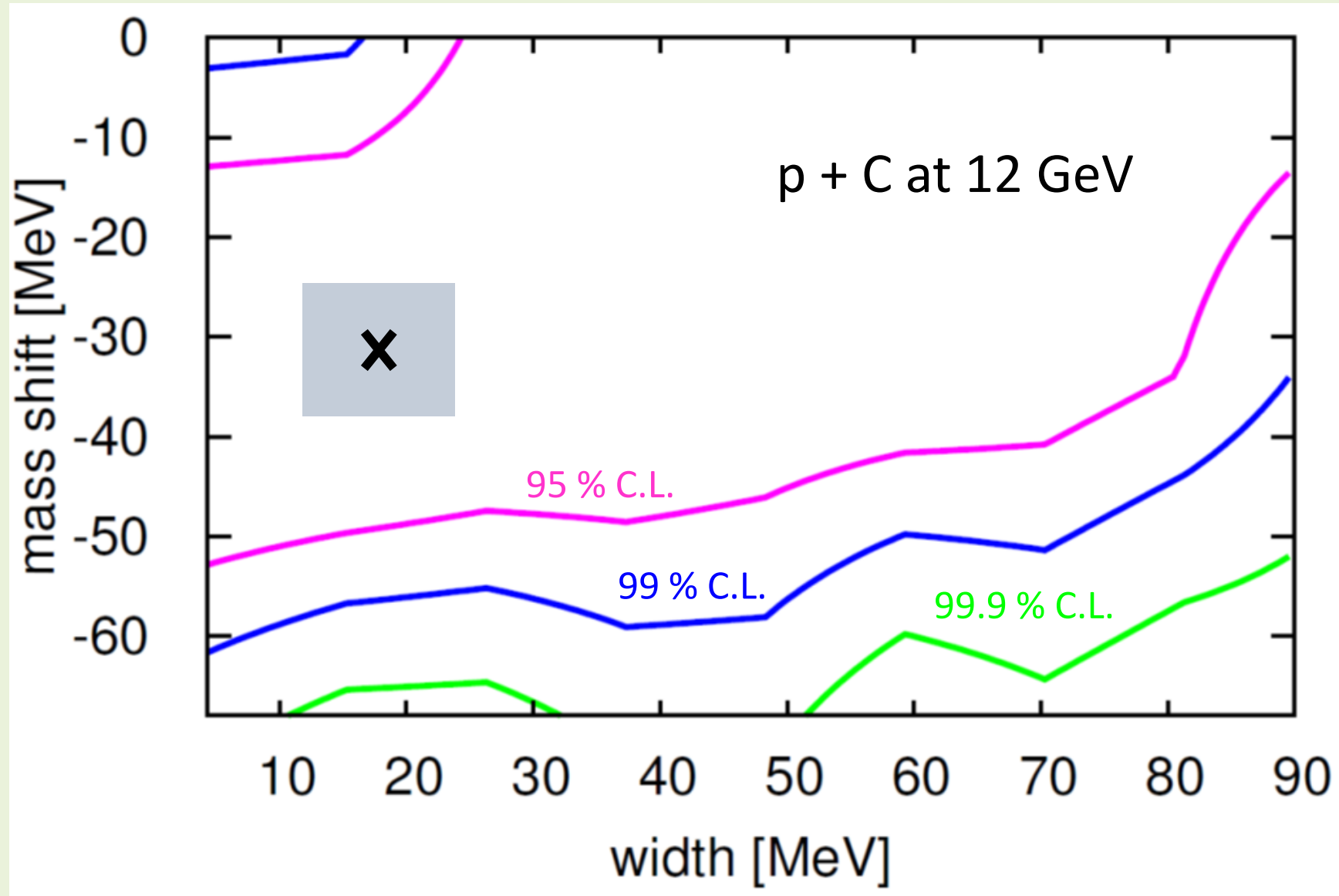


What density does the ϕ feel in the reaction (p+C at 12 GeV)?

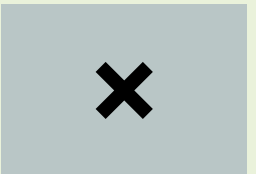


Fits to experimental Carbon target data (E325)

Confidence levels of combined Carbon data



Conclusion of the E325 Collaboration



Final step: comparison to experimental data

- Potential issues:
- ★ Experimental background is not included in the simulation
 - ★ Normalization of the experimental dilepton spectrum is not given



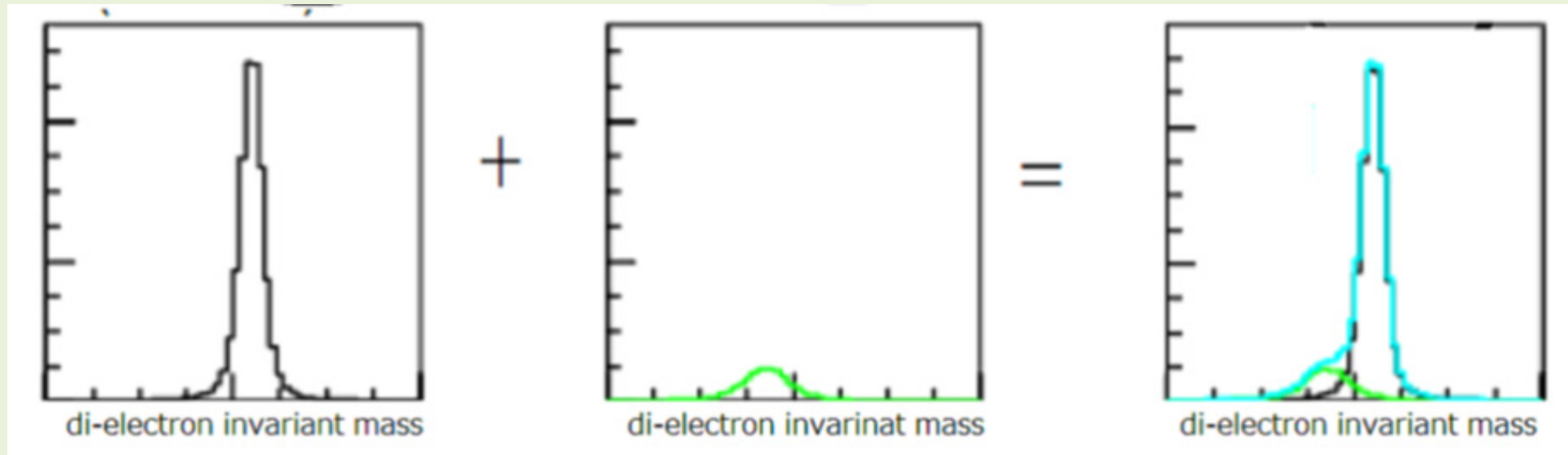
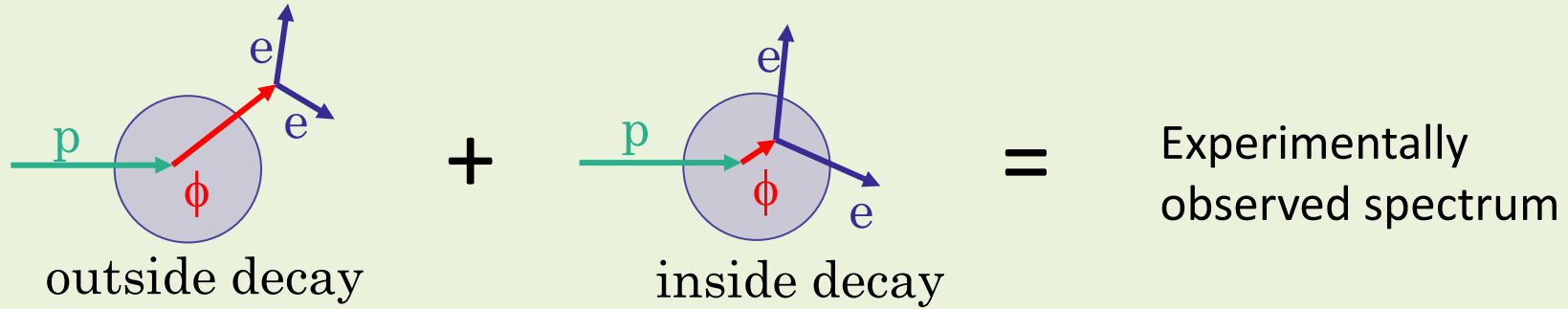
Fit to experimental data is necessary!

Dilepton spectrum:

$$\rho(\omega) = \underbrace{a\omega^2 + b\omega + c}_{\text{Background}} + \underbrace{A\rho_{\phi, \text{PHSD}}(\omega)}_{\phi \text{ meson signal}}$$

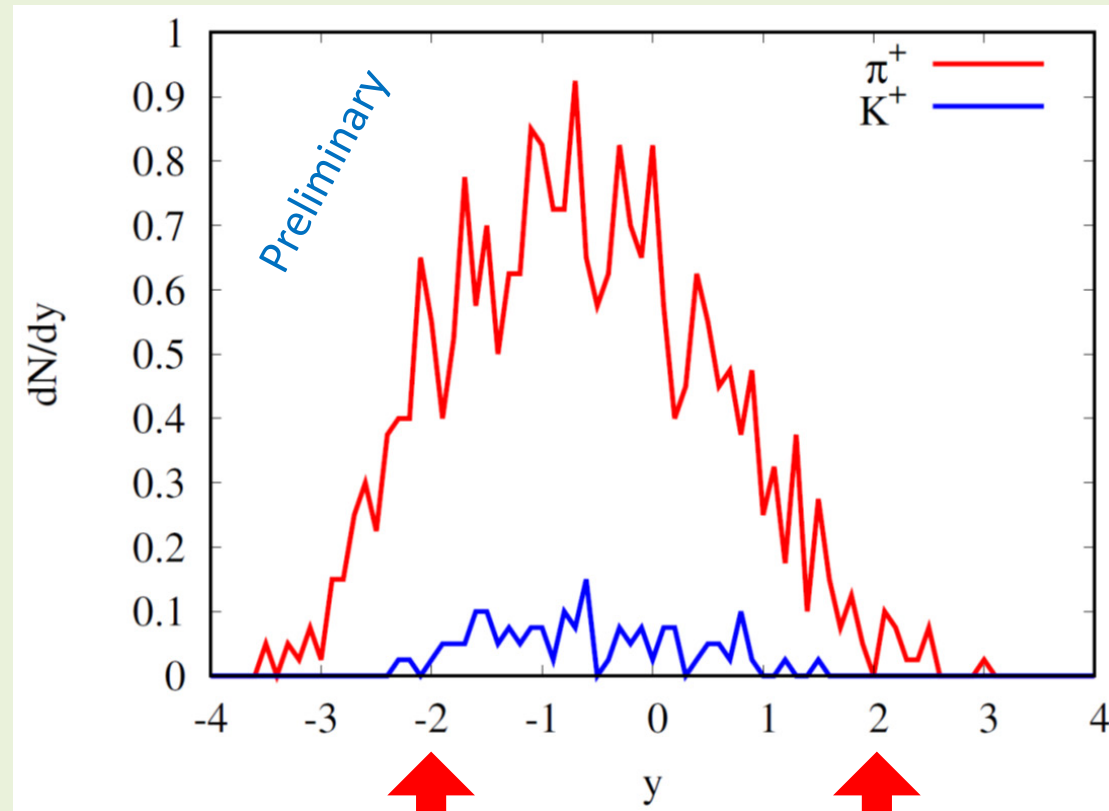
Fitted to the experimental dilepton spectrum
independently for each $\beta\gamma$ -region

Experimental di-lepton spectrum



A first look at a reaction to be probed at J-PARC: pA collisions with initial proton energy of 30 GeV

A first look at the reaction:
Rapidity distribution of
protons/mesons



Due to the large collision
energy, the incoming
proton passes through the
target nucleus

nucleon target
after collision

projectile proton
after collision

Our tool: a transport code

PHSD (Parton Hadron String Dynamics)

W. Cassing and E. Bratkovskaya, Phys. Rev. C **78**, 034919 (2008).

W. Cassing and E. Bratkovskaya, Phys. Rept. **308**, 65 (1999).

W. Cassing, V. Metag, U. Mosel and K. Niita, Phys. Rept. **188**, 363 (1990).

Basic Ingredient 1: Solve a Vlasov-Uehling-Uhlenbeck type equation for each particle type

$$\left(\frac{\partial}{\partial t} + \frac{\mathbf{p}_1}{m} \cdot \frac{\partial}{\partial \mathbf{r}} - \frac{\partial}{\partial \mathbf{r}} U_{\text{BHF}}(\mathbf{r}; t) \cdot \frac{\partial}{\partial \mathbf{p}_1} \right) f(\mathbf{r}, \mathbf{p}_1; t) = \left(\frac{\partial f}{\partial t} \right)_{\text{coll}}$$

mean field
(tuned to reproduce
nuclear matter properties)

particle distribution
function

Basic Ingredient 2: „Testparticle“ approach



$$f_h(\mathbf{r}, \mathbf{p}; t) = \frac{1}{N_{\text{test}}} \sum_i^{N_h(t) \times N_{\text{test}}} \delta(\mathbf{r} - \mathbf{r}_i(t)) \delta(\mathbf{p} - \mathbf{p}_i(t))$$

Structure of QCD sum rules for the phi meson

$$\frac{1}{M^2} \int_0^\infty ds e^{-\frac{s}{M^2}} \rho(s) = c_0(\rho) + \frac{c_2(\rho)}{M^2} + \frac{c_4(\rho)}{M^4} + \frac{c_6(\rho)}{M^6} + \dots$$

In Vacuum

$$\text{Dim. 0: } c_0(0) = 1 + \frac{\alpha_s}{\pi}$$

$$\text{Dim. 2: } c_2(0) = -6m_s^2$$

$$\text{Dim. 4: } c_4(0) = \frac{\pi^2}{3} \langle \frac{\alpha_s}{\pi} G^2 \rangle + 8\pi^2 m_s \langle \bar{s}s \rangle$$

$$\text{Dim. 6: } c_6(0) = -\frac{448}{81} \kappa \pi^3 \alpha_s \langle \bar{s}s \rangle^2$$

Structure of QCD sum rules for the phi meson

$$\frac{1}{M^2} \int_0^\infty ds e^{-\frac{s}{M^2}} \rho(s) = c_0(\rho) + \frac{c_2(\rho)}{M^2} + \frac{c_4(\rho)}{M^4} + \frac{c_6(\rho)}{M^6} + \dots$$

In Nuclear Matter

Dim. 0: $c_0(\rho) = c_0(0)$

$$\langle \bar{s}s \rangle_\rho = \langle \bar{s}s \rangle_0 + \langle N | \bar{s}s | N \rangle \rho + \dots$$

Dim. 2: $c_2(\rho) = c_2(0)$

Dim. 4: $c_4(\rho) = c_4(0) + \rho \left[-\frac{2}{27} M_N + \frac{56}{27} m_s \langle N | \bar{s}s | N \rangle \right. \\ \left. + \frac{4}{27} m_q \langle N | \bar{q}q | N \rangle + A_2^s M_N - \frac{7}{12} \frac{\alpha_s}{\pi} A_2^g M_N \right]$

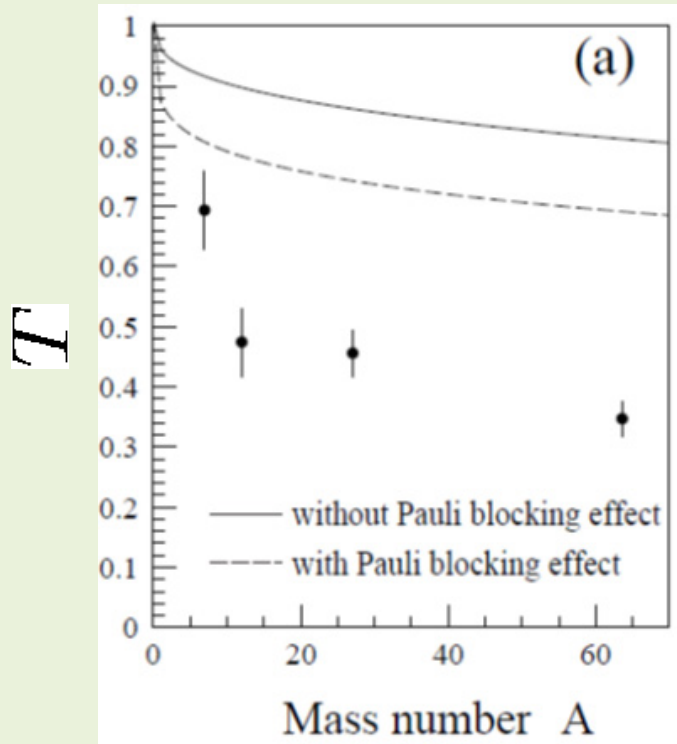
Dim. 6: $c_6(\rho) = c_6(0) + \rho \left[-\frac{896}{81} \kappa_N \pi^3 \alpha_s \langle \bar{s}s \rangle \langle N | \bar{s}s | N \rangle - \frac{5}{6} A_4^s M_N^3 \right]$

Other experimental results

There are some more experimental results on the ϕ -meson width in nuclear matter, based on the measurement of the transparency ratio T :

$$T = \frac{\sigma_{\gamma A \rightarrow \phi X}}{A \sigma_{\gamma N \rightarrow \phi X}}$$

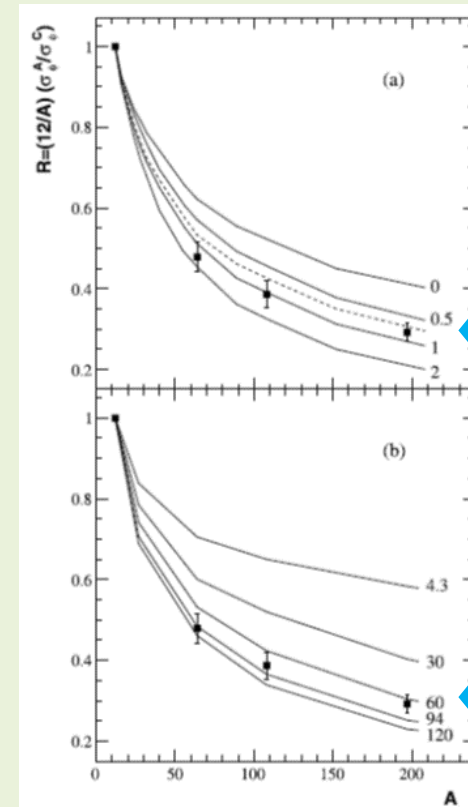
Measured at SPring-8 (LEPS)



$\Gamma_{\phi}(\rho_0) \simeq 30 \text{ MeV}$

Theoretical calculation:
D. Cabrera, L. Roca, E. Oset,
H. Toki and M.J. Vicente Vacas,
Nucl. Phys. **A733**, 130 (2004).

Measured at COSY-ANKE



Theoretical calculation:
V.K. Magas, L. Roca and E. Oset,
Phys. Rev. C **71**, 065202 (2005).

$\Gamma_{\phi}(\rho_0) \simeq 27 \text{ MeV}$

Theoretical calculation:
E. Ya. Paryev,
J. Phys. G **36**, 015103 (2009).

$\Gamma_{\phi}(\rho_0) \simeq 73 \text{ MeV}$