Prospects for the measurement of b-quark mass at the ILC

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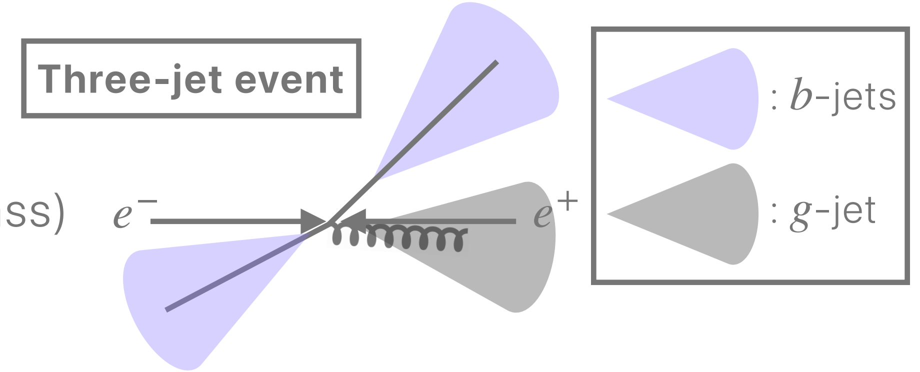
1. Running b-quark mass



- Quarks can not be observed
  → "Single" quark masses are not observables,
  and they are observed as running parameters(running mass)
- Running mass is described by RGE:

$$\mu^2 \frac{\partial m_q(\mu)}{\partial \mu^2} = -\gamma\left(\alpha_s(\mu)\right) m_q(\mu)$$

μ : renormalization scale
$\gamma\left(\alpha_s(\mu)\right)$: Perturbative function

2. Inferring of running b-quark mass

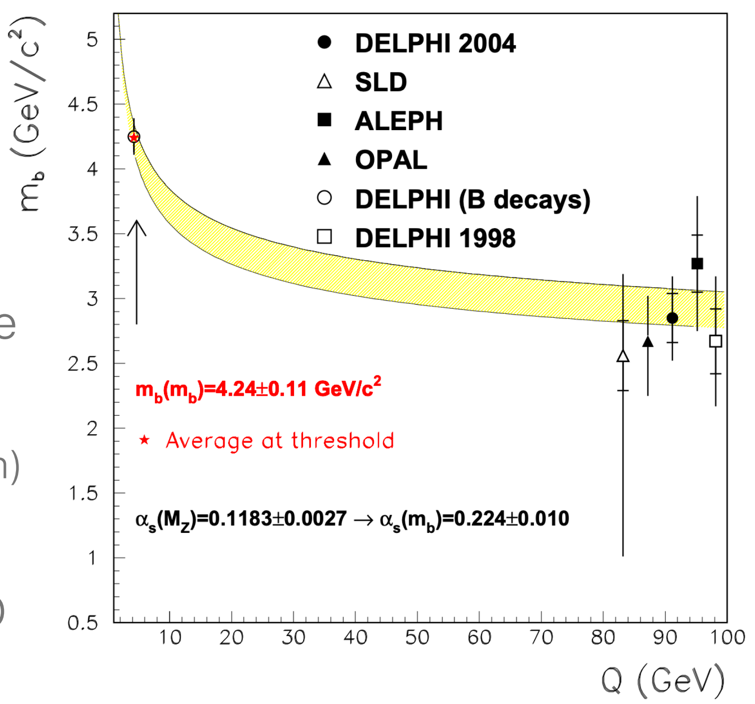
- Quarks and gluons appear as jets
  →running quark masses are obtained from hadronic observables
  Exclusive observables(e.g. three jet rates) have better sensitivity(by a factor of 10 @Z-pole) of quark mass
- Jet should be defined so that avoid infrared(soft/collinear) divergence
  →Jet-Clustering algorithm (JADE, DURHAM, CAMBRIDGE…)

$$R_3^f = \frac{\Gamma_{3j}^f(y_c)}{\Gamma^f}$$

$\Gamma_{3j}^f(y_c)$: $e^+e^- \to f\bar{f}g \to$ 3-jet xsect (y_c : resolution parameter from algorithm)
Γ^f : Total width for $e^+e^- \to f\bar{f}$

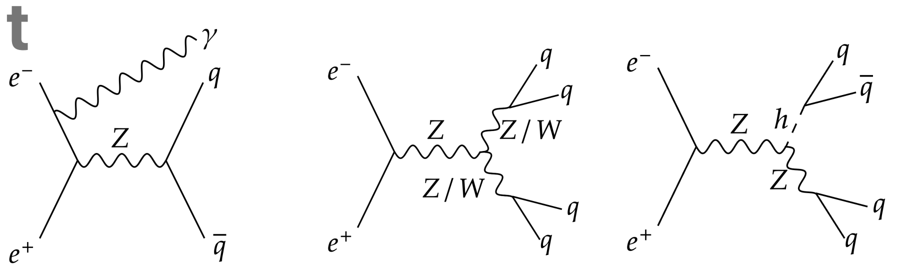
- The b-quark mass at Z-pole has been measured precisely at LEP/SLD
  →**b-quark mass at higher energies at the ILC?**
  Estimate dominant systematic errors at 250GeV ILC and Giga-Z ILC

b-quark mass evolution



(arXiv:hep-ex/0603046)

5. Environment of 250GeV measurement



Radiative return
Di-boson events

- ■Signal event: $e^+e^- \to q\bar{q}$ $(q = u, d, s, b)$
- ■BKG events:
  1. Radiative return (w/ <50 GeV ISR γ)
  2. Di-boson events
- ■Luminosity: 2ab^{-1} with two polarizations $(P_{e^-}, P_{e^+}) = (-0.8, +0.3)$ and $(+0.8, -0.3)$
- Used old DBD sample → event generated by LO for massless quarks in WHIZARD
  Mass effects are only implemented in PYTHIA(PS+Hadronization)
- Situation is completely different from LEP's Z-pole measurement

6. Event selection

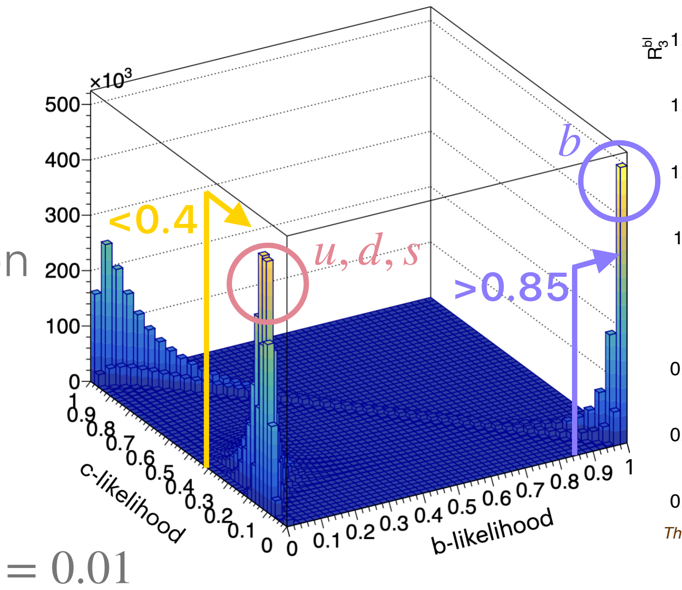
- ■Radiative return cut
  Construct ISR energy from 2-jets kinematically and remove invisible γs

$$K_{reco} = \frac{250\ \text{GeV} \sin\psi_{acol}}{\sin\psi_{acol} + \sin\theta_1 + \sin\theta_2}$$

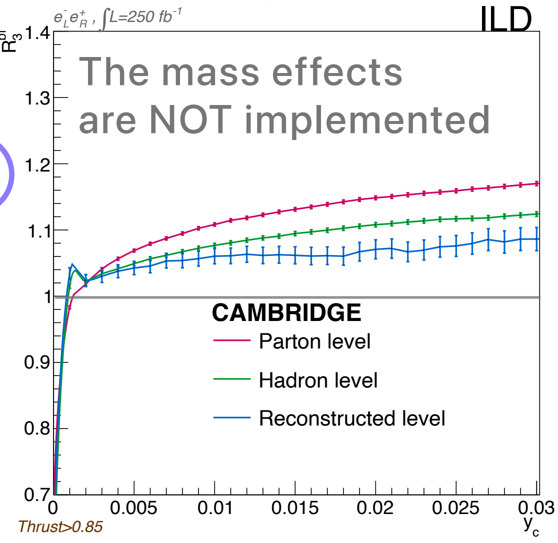
ψ_{acol} : angle of btw 2 jets
θ_i : polar angle of each jet

  Visible γs are removed by neutral PFO information
- ■Di-boson events cut: use Thrust>0.85
- ■Flavor-tagging
  Efficiency: 80%(for b), 58%(for uds)
  Purity: 98.7%(for b), 96.1%(for uds)
- ■Jet-reconstruction: CAMBRIDGE algorithm w/ $y_c = 0.01$

Flavor-tagging likelihoods



Measured R_3^{bl} for each level



The mass effects are NOT implemented

3. Definition of the Observable

- Consider double-ratio R_3^{bl} as the observable
  Cancel or reduce EW corrections and systematic uncertainties (hadronization effect)

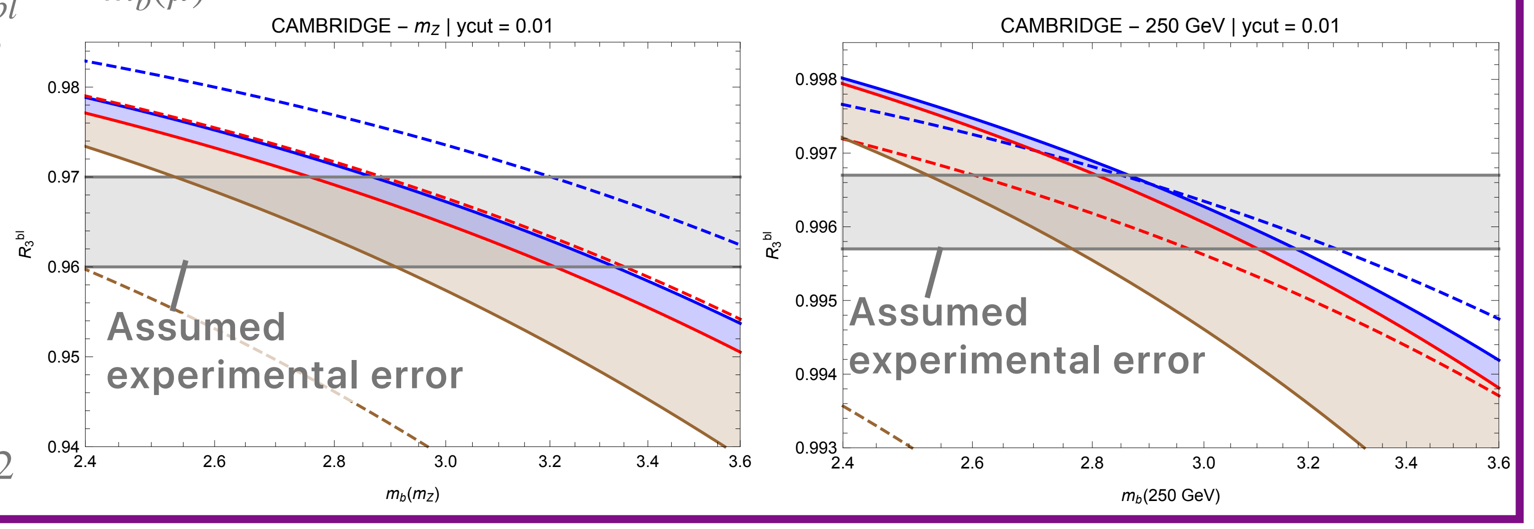
$$R_3^{bl} = \frac{\Gamma_{3j}^b(y_c)/\Gamma^b}{\Gamma_{3j}^l(y_c)/\Gamma^l} = 1 + \underbrace{\frac{\alpha_s(\mu)}{\pi} a_0(y_c)}_{\text{massless correction}} + \bar{r}_b(\mu)\left(\underbrace{b_0(\bar{r}_b, y_c)}_{\text{massive LO correction}} + \underbrace{\frac{\alpha_s(\mu)}{\pi} b_1(\bar{r}_b, y_c, \mu)}_{\text{massive NLO correction}}\right)$$

$(l = u, d, s)$

$$\bar{r}_b(\mu) = m_b^2(\mu)/s$$
$$\bar{b}_1 = b_1 + 2b_0\left(4/3 - \log\bar{r}_b + \log\left(\mu^2/s\right)\right)$$

4. Sensitivity of b-quark mass at high energies

- Sensitivity of b-quark mass for R_3^{bl} is given by $\Delta R_3^{bl} \sim \frac{2\left(1 - R_3^{bl}\right)}{m_b(\mu)} \Delta m_b(\mu)$ (e.g. CAMBRIDGE predictions are given below)
  If we want $\Delta m_b = 0.4$ GeV, we need to measure R_3^{bl} with a precision of 1% (for Z-pole) and 0.1% (for 250 GeV)
  →**The sensitivity at 250 GeV is ~5 times deteriorated**



LO calculation
----- NLO calculation
Pole mass, $\mu = \sqrt{s}$
Running mass, $\mu = 2\sqrt{s}$
Running mass, $\mu = \sqrt{s}/2$

7. Assessment of uncertainties

- The mass effects are not implemented in the current MC, but corrections between different levels are worthful:

$$R_3^{bl}\Big|_{parton} = C_{had} \times C_{det} \times R_3^{bl}\Big|_{reco}$$

Hadronization correction
$$C_{had} = \frac{R_3^{bl}\Big|_{parton}}{R_3^{bl}\Big|_{hadron}}$$

Detector correction
$$C_{det} = \frac{R_3^{bl}\Big|_{hadron}}{R_3^{bl}\Big|_{reco}}$$

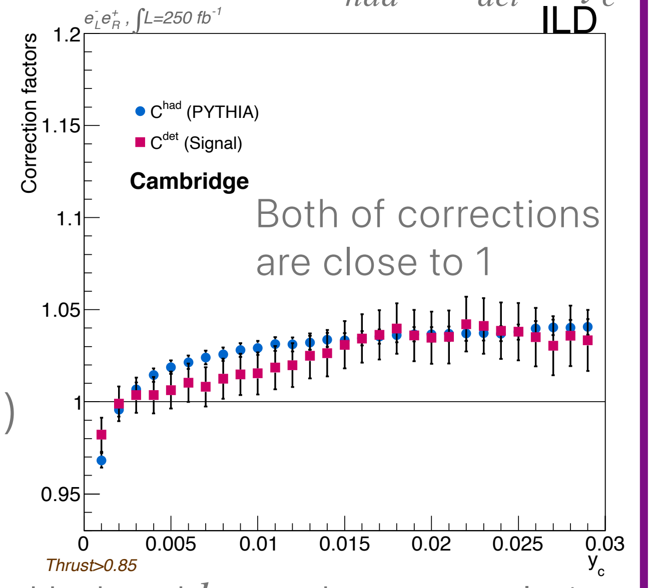
- Estimate systematic uncertainties from these corrections:
  - ■Hadronization model
    LEP's time: 0.2% uncertainty on C_{had} (Compare different hadronization models and tunes)
    → assumed its half thanks for higher energy B-hadrons and more data
  - ■Detector
    Propagated flavor-tagging efficiency(0.1-0.5%) and BKG contaminations(O(1%)) to C_{det} through Toy-MC
- Statistical uncertainty is estimated at 2ab^{-1} H20 scenario
- b-quark mass precision for $R_3^{bl} = 0.996$, $m_b = 2.75$ GeV:

$$\Delta m_b(250) = 0.76(stat.) \pm 0.59(exp.) \pm 0.34(had.) \pm 0.07(theo.)\ \text{GeV}$$

- Giga-Z ILC gives better precision thanks for 100times larger statistics, superior flavor-tagging :

DELPHI: $\Delta m_b(m_Z) = 0.18(stat.) \pm 0.13(exp.) \pm 0.19(had.) \pm 0.12(theo.)$ GeV
ILD: $\Delta m_b(m_Z) = 0.02(stat.) \pm 0.02(exp.) \pm 0.09(had.) \pm 0.06(theo.)$ GeV

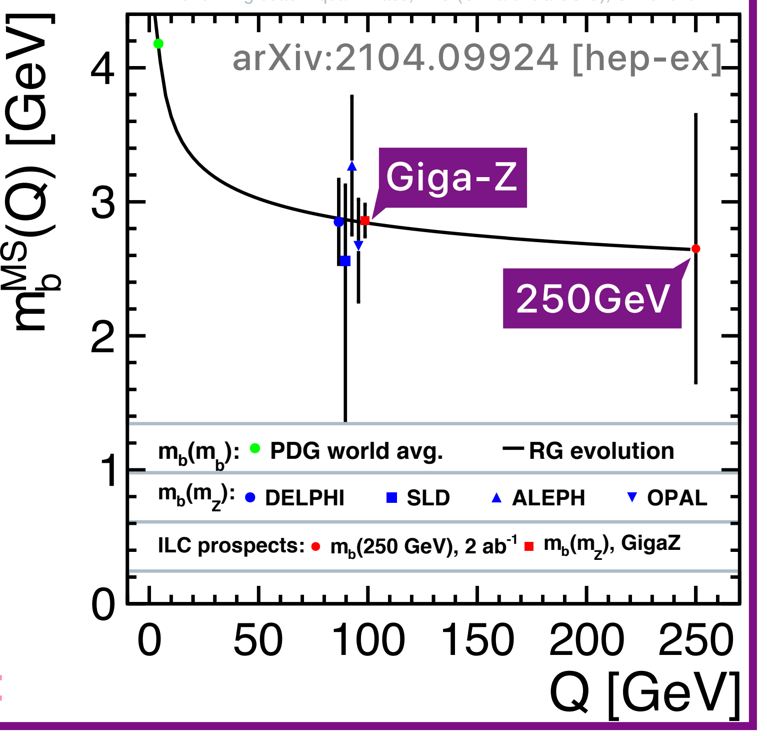
Correction factors C_{had} & C_{det} vs y_c



Both of corrections are close to 1

Updated b-quark mass evolution

The running bottom quark mass, IFIC (U. Valencia/CSIC), U. Tohoku



8. Conclusion and Prospects

- **ILC 250GeV measurement has limited b-quark mass sensitivity, but it will add a new point at never proved energies**
- **Giga-Z ILC will provide superior result at Z-pole than LEP and better QCD test**