New insights into nuclear physics and weak mixing angle using electroweak probes

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New insights into nuclear physics and weak mixing angle using electroweak probes



based on arXiv:2102.06153

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 Coherent elastic neutrino-nucleus scattering (CEvNS): a neutrino scatters off a nucleus via the exchange of a Z boson, and the nucleus recoils as a whole (coherently)

 $\nu_{\alpha} + (A, Z) \rightarrow \nu_{\alpha} + (A, Z)$

- Coherency condition: $q \cdot R \ll 1$
- Predicted in **1974** by Freedman
- Observed for the first time in **2017** by **the COHERENT Collaboration**
- Very challenging to detect due to **tiny nuclear recoils**
- Low-Energy Regime ($E_{\nu} \sim$ few tens MeV)
- Large cross section $(\sigma \propto N^2)$





Coherent elastic neutrino-nucleus scattering

keV

Interactions with nuclei and electrons, minimally disruptive of the nucleus

MeV

Interactions with nucleons inside nuclei, often disruptive, hadroproduction

TeV

GeV

1 MARCH 1974

VOLUME 9, NUMBER 5 Coherent effects of a weak neutral current

 $CE\nu NS$ process

Daniel Z. Freedman[†] National Accelerator Loboratory, Batavia, Illinois 60510 and Institute for Theoretical Physics, State University of New York, Stony Brook, New York 11790 (Received 15 October 1973; revised manuscript received 19 November 1973)

If there is a weak neutral current, then the elastic scattering process $\nu + A \rightarrow \nu + A$ should have a sharp coherent forward peak just as $\nu + A \rightarrow \nu + A$ does. Experiments to observe this peak can give important information on the isospin structure of the neutral ourrent. The experiments are very difficult, although the estimated cross sections (about 10⁻⁴⁸ cm² on a carbon) are favorable. The coherent cross sections (in contrast to incoherent) are almost energy-independent. Therefore, energies as 100 well ways be suitable. Quasi-coherent nuclear excitation processes $\nu + A \rightarrow \nu + A^{*}$ provide possible tests of the conservation of the weak neutral current. Because of strong coherent effects at very low energies, the nuclear elastic scattering process may be important in inhibiting cooling by neutrino emission in stellar collapse and neutron stars.

Deep Inelastic Scattering

PeV

An appropriate **source of neutrinos** is needed: high flux, well understood (low uncertainties), pulsed for background rejection, multiple flavors, etc.

COHERENT experiment



- COHERENT has observed for the first time CEνNS with a 14.6 kg CsI scintillating crystal (D. Akimov et al. Science 357.6356 (2017))
- New observation in 2020 with 24 kg LAr detector (upgrade to 750 kg), with >3σ CEvNS detection significance

 ^{Theoretical}
 ^{Experim}

5 10²

10 L

- In 2020 the COHERENT Collaboration presented the **updated results** on the CsI detector:
- Increased statistics. More than 2x!
- 2D Likelihood fit in numbers of photoelectrons and reconstructed time
- Result consistent with SM prediction at 1 σ
- Flux uncertainty now dominates the systematic
- Overall systematic uncertainty reduced: 28%→13%



$CE\nu NS$ cross section

• Let's go back to the cross section we used in our analysis, where we **distinguished** the contribution of the **proton and neutron form factors**



- The nuclear form factor, F(q), represents the Fourier transform of a spherically symmetric ground state mass distribution (both protons $\frac{de}{dE}$ and neutrons) normalized so that F(0)=1
- For a weak interaction like for CEvNS you deal with the weak form factor: the Fourier transform of the weak charge distribution (neutron + proton distribution weighted by the weak mixing angle)
- Most of the information we have on the nuclear size and nucleon's distribution inside the nuclei are related to the **electric charge**, and thus to the protons (informations extracted using **electron-nuclei scattering** data and **muonic x-ray** spectroscopy)

$$\frac{\sigma}{E_{r}} \cong \frac{G_{F}^{2} m_{N}}{4\pi} \left(1 - \frac{m_{N}E_{r}}{2E_{V}^{2}}\right) Q_{w}^{2} |F_{weak}(E_{r})|^{2}$$
Weak charge × weak form factor
Payne et al. Phys. Rev. C 100, 061304 (2019)
$$\left[g_{V}^{p}ZF_{Z}(E_{r}) + g_{V}^{n}NF_{N}(E_{r})\right]^{2}$$
Proton + Neutron from factor
$$\int_{p} \frac{\sigma}{\rho} \int_{p} \frac{\sigma}{\rho$$

From muonic X-rays data we have (for t fixed to 2.3 fm)

$$R_p^{\rm rms} = \sqrt{R_{ch}^2 - \left(\frac{N}{Z} \langle r_n^2 \rangle + \frac{3}{4M^2} + \langle r^2 \rangle_{SO}\right)}$$

 $R_p^{Cs} = 4.821 \pm 0.005$ fm (Cesium rms proton radius) $R_p^I = 4.766 \pm 0.008$ fm (lodine rms-proton radius) $R_{ch}^{Cs} = 4.804 \text{ fm}$ (Cesium charge rms radius) $R_{ch}^{I} = 4.749 \text{ fm}$ (lodine charge rms radius)

G. Fricke et al., Atom. Data Nucl. Data Tabl. 60, 177 (1995)

$$\frac{d\sigma}{dE_r} \cong \frac{G_F^2 m_N}{4\pi} \left(1 - \frac{m_N E_r}{2E_v^2}\right) \left[g_V^p Z F_Z\left(E_r, R_p^{CS/I}\right) + g_V^n N F_N(E_r, R_n^{CSI})\right]^2$$

 $R_p^{Cs/I}$ are very well known, so we fitted COHERENT CsI data looking for R_n^{CsI} ...

Since it is expected that also the neutron structures of Cs and I are similar and the current uncertainties of the COHERENT data do not allow to distinguish between them, we consider

$$F_{N,\mathbf{Cs}}(q^2) \simeq F_{N,\mathbf{I}}(q^2) \simeq F_N(q^2)$$



In order to get information on the neutron distribution of the CsI system we considered the following parametrizations of the neutron form factor

1. Two-parameters Fermi form factor

Neutron rms radius

$$R_n^2 = \frac{3}{5}c^2 + \frac{7}{5}(\pi a)^2.$$

We considered the same value of t=2.30 fm as for the proton form factor

2. Helm form factor

Neutron rms radius

$$R_n^2 = \frac{3}{5}R_0^2 + 3s^2$$

s is similar to the surface thickness. We considered the value s=0.9 fm which was determined for the proton form factor of similar nuclei.

With COHERENT new data and the new quenching factor, our fit of the average Csl neutron

radius gives

0

 $R_n^{CsI} = 5.55 \pm 0.44$ fm

Proton rms radius for Cs and I

 $R_p^{Cs} = 4.821 \text{ fm}$ and $R_p^{I} = 4.766 \text{ fm}$

are around 4.78 fm, with a difference of about 0.05 fm

The neutron skin

 $\Delta R_{np}^{CsI} = 0.76 \pm 0.44 \text{ fm}$

This result is compatible with all the nuclear mean field models.

Cadeddu et al., PRD 101, 033004 (2020), arXiv:1908.06045 Cadeddu et al., arXiv:2102.06153

... the central value tends to favour models that predict a larger value of R_n .

	^{127}I		^{133}Cs				
Model	$R_p^{\text{point}} R_p R_n^{\text{point}} R_n \Delta$	$\Delta R_{np}^{\text{point}} \Delta R_{np}$	$R_p^{\text{point}} R_p R_n^{\text{point}}$	$^{t} R_n \Delta R_{np}^{\text{point}} \Delta$	R_{np}		
SHF SkI3 81	4.68 4.75 4.85 4.92	0.17 0.17	4.74 4.81 4.91	4.98 0.18 0	.18		
SHF SkI4 81	4.67 4.74 4.81 4.88	0.14 0.14	$4.73\ 4.80\ 4.88$	4.95 0.15 0	.14		
SHF Sly4 82	4.71 4.78 4.84 4.91	0.13 0.13	$4.78 \ 4.85 \ 4.90$	4.98 0.13 0	.13		
SHF Sly5 82	4.70 4.77 4.83 4.90	0.13 0.13	$4.77\ 4.84\ 4.90$	4.97 0.13 0	.13		
SHF Sly6 82	4.70 4.77 4.83 4.90	0.13 0.13	$4.77 \ 4.84 \ 4.89$	4.97 0.13 0	.13		
SHF Sly4d 83	4.71 4.79 4.84 4.91	0.13 0.12	$4.78\ \ 4.85\ \ 4.90$	4.97 0.12 0	.12		
SHF SV-bas 84	4.68 4.76 4.80 4.88	0.12 0.12	4.74 4.82 4.87	4.94 0.13 0	.12		
SHF UNEDF0 85	4.69 4.76 4.83 4.91	0.14 0.14	4.76 4.83 4.92	4.99 0.16 0	.15		
SHF UNEDF1 86	4.68 4.76 4.83 4.91	0.15 0.15	4.76 4.83 4.90	4.98 0.15 0	.15		
SHF SkM [*] 87	4.71 4.78 4.84 4.91	0.13 0.13	4.76 4.84 4.90	4.97 0.13 0	.13		
SHF SkP 88	4.72 4.80 4.84 4.91	0.12 0.12	4.79 4.86 4.91	4.98 0.12 0	.12		
RMF DD-ME2 89	$4.67 \ 4.75 \ 4.82 \ 4.89$	0.15 0.15	4.74 4.81 4.89	4.96 0.15 0	.15		
RMF DD-PC1 90	4.68 4.75 4.83 4.90	0.15 0.15	4.74 4.82 4.90	4.97 0.16 0	.15		
RMF NL1 91	4.70 4.78 4.94 5.01	0.23 0.23	4.76 4.84 5.01	5.08 0.25 0	.24		
RMF NL3 92	4.69 4.77 4.89 4.96	0.20 0.19	4.75 4.82 4.95	5.03 0.21 0	.20		
RMF NL-Z2 93	4.73 4.80 4.94 5.01	0.21 0.21	4.79 4.86 5.01	5.08 0.22 0	.22		
RMF NL-SH 94	4.68 4.75 4.86 4.94	0.19 0.18	4.74 4.81 4.93	5.00 0.19 0	.19		

M. Cadeddu and F. Dordei, *Reinterpreting the weak mixing angle from atomic parity violation in view of the Cs neutron rms radius measurement from COHERENT*, PRD 99, 033010 (2019), arXiv:1808.10202





Interaction mediated by the photon and so mostly sensitive to the charge (proton) distribution Interaction mediated by the Z boson and so mostly sensitive to the weak (neutron) distribution.

- **Parity violation** in an atomic system can be obseved as an electric dipole transition amplitude between two atomic states with the same parity, such as the 6S and 7S states in cesium
 - Indeed, a transition between two atomic states with same parity (6S and 7S in Cs) is forbidden by the parity selection rule and cannot happen with the exchange of a photon
 - However, an electric dipole transition amplitude can be induced by a Z boson exchange between atomic electrons and nucleons-> Atomic Parity Violation (APV) or Parity Non Conserving (PNC)

The quantity that is measured in this transition is the nuclear weak charge:

 $Q_W^{SM} \approx Z (1 - 4 \sin^2 \theta_W^{SM}) - N$

APV

Weak Charge in the SM including radiative corrections

$$Q_W^{SM+r.c.} \equiv -2\left[Z\left(g_{AV}^{ep} + 0.00005\right) + N\left(g_{AV}^{en} + 0.00006\right)\right] \left(1 - \frac{\alpha}{2\pi}\right) \approx Z\left(1 - 4\sin^2\theta_W^{SM}\right) - N$$

Using SM prediction at low energy for the Weinberg angle $\sin^2 \hat{\theta}_W(0) = 0.23857(5)$, the theoretical value for the weak charge of Cesium is $Q_W^{SM} \begin{pmatrix} 133\\55}Cs \end{pmatrix} = -73.23(1)$



APV

$$Q_W = N \left(\frac{\operatorname{Im} E_{\text{PNC}}}{\beta}\right)_{\text{exp.}} \left(\frac{Q_W}{N \operatorname{Im} E_{\text{PNC}}}\right)_{\text{th.}} \beta_{\text{exp.+th.}}$$

Experimental value of electric dipole transition amplitude between 6S and 7S states in Cs

 $-\mathrm{Im}\left(\frac{\mathrm{E}_{\mathrm{PNC}}}{\beta}\right) = 1.5935(56) \,\mathrm{mV/cm}$

[C. S. Wood et al, Science **275**, 1759 (1997)]

Theoretical APV (or PNC) amplitude of the 6S-7S electric dipole transition

$$E_{\rm PNC} = \sum_{n} \left[\frac{\langle 6s | H_{\rm PNC} | np_{1/2} \rangle \langle np_{1/2} | d | 7s \rangle}{E_{6s} - E_{np_{1/2}}} + \frac{\langle 6s | d | np_{1/2} \rangle \langle np_{1/2} | H_{\rm PNC} | 7s \rangle}{E_{7s} - E_{np_{1/2}}} \right]$$

where **d** is the electric dipole operator, and $H_{\rm PNC} = -\frac{G_F}{2\sqrt{2}}Q_W\gamma_5\rho(\mathbf{r})$

is the nuclear spin independent Hamiltonian describing the *electron-nucleus weak interaction*

 $\rho(\mathbf{r}) = \rho_p(\mathbf{r}) = \rho_n(\mathbf{r}) \rightarrow neutron skin correction$ needed

β : tensor transition polarizability

It characterizes the size of the Stark mixing induced electric dipole amplitude (external electric field)

[Bennet and Wieman,PRL 82, 2484 (1999)] [A. Dzuba and V. Flambaum., PRA 62, 052101 (2000)]

 $\beta = 27.064(33) a_B^3$

PDG2020 average



Assuming to know the SM prediction at low-energy $\sin^2 \hat{\theta}_W(0) = 0.23857(5)$

The weak charge for APV with the neutron skin contribution reads $\widetilde{Q}_W \equiv Zq_p(1 - 4\sin^2\vartheta_W) - Nq_n$

This coupling depends on the integrals $q_{p,n} = 4\pi \int_0^\infty \rho_{p,n}(r)f(r)r^2 dr$ where $\mathbf{p}(\mathbf{r})$ are the **proton** and **neutron densities** in the nucleus and f(r) is the matrix element of the electron axial current between the atomic $\mathbf{s}_{1/2}$ and $\mathbf{p}_{1/2}$ wave functions inside the nucleus normalized to f(0)=1.

We performed the calculations considering charge, proton and neutron distribution densities that correspond to the form factors in **CEvNS** cross section using both Helm and 2pF parametrization.

COHERENT depends on both Cs and I, while APV only on Cs: we can **disentangle** the contributions

Results



$$\Delta R_{np}(^{133}Cs) = R_n - R_p = 0.45^{+0.33}_{-0.33} \text{ fm}$$

Contribution of Cs and I disentangled!!

Strong linear correlation between the neutron skin of Cs and Pb among different nuclear model predictions

PREX: parity-violating asymmetry APV in the elastic scattering of longitudinally polarized electrons on ²⁰⁸Pb Measurement of the lead neutron skin through an electroweak process

 $A_{
m PV} = rac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} pprox rac{G_F Q^2 |Q_W|}{4\sqrt{2} \pi lpha Z} rac{F_{
m W}(Q^2)}{F_{
m ch}(Q^2)}$

 $\Delta R_{np}(^{208}Pb) = 0.283 \pm 0.071 \text{ fm}$

R_w [fm]

adius 5.7

The neutron skin is a key parameter also for neutron stars properties

Results



Results

Both CEvNS data on CsI and APV on Cs **depend on** R_n and $sin^2(\vartheta_W)$: strong interplay between nuclear physics and weak interactions. Try to exploit **correlations** in both measurements!

The COHERENT only measurement is currently not competitive due to the suppression of the proton contribution $COHERENT \text{ only } \sin^2(\vartheta_W) = 0.220^{+0.028}_{-0.027}$



Data driven result!

CEvNS is helpful in combination with APV measurement on ¹³³Cs in order to provide experimental constrain on R_n and $sin^2(\vartheta_W)$ simultaneously

Here the value of R_n(¹³³Cs) was **extrapolated** using antriprotonic atoms, known to be affected by____ considerable **model dependencies**.

Waiting for future reduced uncertainties!

Future seems to be bright!

Maybe BSM physics or connection with g-2?!

PRD 104, L011701 (2021), 2104.03280



Thanks!

Do you have any questions?

Outline

)] CEvNS process Coherent elastic neutrinonucleus scattering 03 Nuclear Structure Electroweak neutron skin measurement

02 COHERENT experiment COHERENT latest results on cesium-iodide O4 APV Atomic Parity Violation experiment on Cesium

 $O5 \stackrel{Results}{\circ}$ Our results and conclusions

Coherency means that the nucleon wavefunctions in the target nucleus are in phase with each other: this is true at **low momentum transfer**.

Coherency condition: $q \cdot R \ll 1 \longrightarrow q \ll \frac{1}{R} \sim 0.2 \text{ fm}^{-1}$ Three-momentum transfer $q = \sqrt{2m_N E_r}$ (R~4 - 5 fm)

The interaction is coherent up to neutrino energies E_{ν} ~50 MeV for medium size nuclei, which translate to keV nuclear recoils

Despite the detection related challenges $\text{CE}\nu\text{NS}$ is characterized by a large cross section

$$\frac{d\sigma^{CE\nu NS}(E_{\nu}, E_{r})}{dE_{r}} \cong \frac{G_{F}^{2}}{4\pi} m_{N} \left(1 - \frac{m_{N}E_{r}}{2E_{\nu}^{2}}\right) Q_{w}^{2} \frac{|F(E_{r})|^{2}}{|V_{w}|^{2}}$$
Nuclear form factor

where $Q_w = N - (1 - 4 \sin^2 \theta_W) Z \cong N$.

 $\sin^2\theta_W$ is about ¼, the second term is close to zero so that the cross section scales with the neutron number squared $\sigma\propto N^2$

CEVNS process



An appropriate **source of neutrinos** is needed: high flux, well understood (low uncertainties), pulsed for background rejection, multiple flavors, etc.

Pulsed beam

PROTON BEAM

SHIELDING MONOLITH

CONCRETE AND GRAVE

Ge ARRAY

CEvNS process

Two types of neutrino sources are considered in experiments

Spallation neutron source: neutrinos produced from the decay of pions/muons

Spallation Neutron Source @Oak Ridge:

- 1 GeV protons hit liquid Hg target
- Reached 1.4 MW
- Pulsed @60Hz: measure steady-state bkg out of beam
- Pion-decay-at-rest neutrino source
- Multi-target program to measure N² dependence



Nuclear reactors: antineutrinos produced in beta decays



- COHERENT has observed for the first time CEvNS with a 14.6 kg CsI scintillating crystal
- 19.3 m from the source
- 134±22 CE ν NS events: 6.7 σ significance
- To be compared with prediction: 173±48 events





• New observation in 2020 with LAr detector

- In 2020 the COHERENT Collaboration presented the **updated results** on the CsI detector:
- Increased statistics. More than 2x!
- 2D Likelihood fit in numbers of photoelectrons and reconstructed time
- Result consistent with SM prediction at 1σ
- Flux uncertainty now dominates the systematic
- Overall systematic uncertainty reduced: 28%→13%

No-CEvNS rejection	11.6σ
SM CEvNS prediction	333±11(th)±42(ex)
Fit CEvNS events	306±20
Fit χ²/dof	82.4/98
CEvN cross section	$169^{+30}_{-26} \times 10^{-40} \mathrm{cm}^2$
SM cross section	$189 \pm 6 \times 10^{-40} \mathrm{cm}^2$



- 2020 results using 24 kg of atmosphering Ar (CENNS-10 detector)
- Test of the dependence on N^2 • $>3\sigma$ CEvNS detection significance (2021)14 COHERENT, PRL 126, 012002 - Analysis A 12 ---- Analysis B 10 2Δ(InL) 50 100 150 200 250 300 11 **CEvNS** Counts



Observed cross section consistent with the N^2 dependence

CENNS-10 is still taking data and an upgrade to a 750 kg detector



- The analogy with electron and x-ray diffraction is very close and it is merely necessary to replace the electron cloud of an atom by the proton cloud of a nucleus
- Born approximation: to obtain the actual scattering for a finite nucleus it is necessary to multiply the point charge scattering cross section by the square of the form factor
- Unfortunately for medium and heavy nuclei this procedure fails:
- As is well known, the first Born approximation is equivalent to consider both the incident and diffracted waves as a plane waves.
- The waves are distorted by the intese nuclear electromagnetic field, so that they can no longer be considered plane waves: DISTORTED WAVER BORN APPROXIMAPTON (DWBA)
- By considering the PWBA two principal types of errors are committed: the PWBA puts true zeros into the form factors, whereas the accurate calculations show minima rather than zeros; Radii determined from PWBA are generally larger than the exact calculations.

The charge radii of nuclei have been studied with muonic spectroscopy and the data were fitted with two-parameters Fermi (2pF) density distributions of the form

$$\rho_{2pF}(r,c,a) = \frac{\rho_0}{1 + e^{(r-c)/a}}$$



• The **half-density radius c** is related to the root-mean square (rms) radius

$$R_{rms} \equiv \sqrt{\langle r^2 \rangle} \equiv \sqrt{\frac{\int r^2 \rho(\mathbf{r}) \, d^3 r}{\int \rho(\mathbf{r}) \, d^3 r}} = \sqrt{\frac{\int r^2 \rho(\mathbf{r}) \, d^3 r}{Ze}} \rightarrow R_{rms}^{2pF} \equiv \sqrt{\langle r^2 \rangle} = \sqrt{\frac{3}{5} \, c^2 + \frac{7}{5} (\pi \, a)^2}$$

• The **a** parameter, called **diffuseness**, is related to the **surface thickness t**:

$t = 4 a \ln 3 \cong 4.40 a$

• In principle a three-parameters Fermi density distributions could be employed, adding the w parameter which allows for a **dip or a bump** in the central region

$$\rho_{3pF}(r,c,a,w) = \left(1 + w\frac{r^2}{c^2}\right)\rho_{2pF}$$

Charge radii of Cesium & Iodine: surface thickness fixed to t=2.3 fm (i.e. a=0.5234 fm)

TABLE IIIA. Muonic $2p \rightarrow 1s$ Transition Energies and Barrett Radii for Z < 60 and Z > 77See page 194 for Explanation of Tables

Isotope	E _{exp.} [keV]	<i>E_{theo.}</i> [keV]	NPol [keV]	c [fm]	$\langle r^2 \rangle_{model}^{1/2}$ [fm]	α [1/fm]	k	C, [am/keV]	R ^µ _{kα} [fm]	Ref.
¹³³ Cs Cesium	3840.702 39 3902.636 31	3840.670 3902.656	1.531 1.289	5.6710 1	4.804	0.1193 0.1182	2.2296 2.2274	-2.759 -2.710	6.1459 (1;13) 6.1464 (1;11)	[KI88]
¹²⁷ J lodine	3667.361 35 3723.742 33	3667.466 3723.650	0.532 1.454	5.5931 1	4.749	0.1166	2.2229 2.2209	-2.969 -2.919	6.0762 (1;5) 6.0768 (1;13)	[K188]

G. Fricke et al., Atom. Data Nucl. Data Tabl. 60, 177 (1995)

In a 2pF one can retrieve in a model-dependent way the rms charge radius

$$R_{ch}^{rms} \equiv \langle r^2 \rangle_{model}^{1/2} = \sqrt{\frac{3}{5} c^2 + \frac{7}{5} \left(\pi \frac{t_{fixed}}{4 \ln 3}\right)^2}$$

 $R_{ch}^{Cs} = 4.804 \text{ fm}$ (Cesium charge rms radius)

 $R_{ch}^{I} = 4.749 \text{ fm}$ (lodine charge rms radius)

Once the charge radius is determined, it is necessary to translate such quantity into the proton radius, taking into account **finite size** of both **protons** and **neutrons** plus **other corrections**

$$R_{ch}^{2} = \left[\begin{array}{c} R_{point}^{2} + \left\langle r_{p}^{2} \right\rangle \right] + \left[\begin{array}{c} \frac{N}{Z} \left\langle r_{n}^{2} \right\rangle \right] + \left[\left\langle r_{n}^{2} \right\rangle \right] + \left[$$

Assuming to know the SM prediction at low energy $\sin^2 \hat{\theta}_W(0) = 0.23857(5)$

The weak charge for APV with the neutron skin contribution reads $\widetilde{Q}_W \equiv Zq_p(1-4\sin^2\vartheta_W) - Nq_n$

This coupling depends on the integrals $q_{p,n} = 4\pi \int_0^\infty \rho_{p,n}(r) f(r) r^2 dr$

where $\mathbf{p}(\mathbf{r})$ are the proton and neutron densities in the nucleus and f(r) is the matrix element of the electron axial current between the atomic $\mathbf{s}_{1/2}$ and $\mathbf{p}_{1/2}$ wave functions inside the nucleus normalized to f(0)=1.

$$f(r) = 1 - 2\int_0^r \frac{V(r')}{r'^2} \int_0^{r'} V(r'')r''^2 dr'' dr' + \left(\frac{1}{r} \int_0^r V(r')r'^2 dr'\right)^2,$$

where V(r) represents the radial electric potential determined uniquely by the charge distributon $\rho_c(r)$ of the nucleus.

$$V(r) = 4\pi Z \alpha \left[\frac{1}{r} \int_0^r \rho_c(r') r'^2 \mathrm{d}r' + \int_r^\infty \rho_c(r') r' \mathrm{d}r' \right]$$

We performed the calculations considering charge, proton and neutron distribution densities that correspond to the form factors in **CEvNS** cross section using both Helm and 2pF parametrization.

Results



$$\Delta R_{np}(^{127}I) = R_n - R_p = 1.1^{+1.0}_{-0.9} \text{ fm}$$
$$\Delta R_{np}(^{133}Cs) = R_n - R_p = 0.45^{+0.33}_{-0.33} \text{ fm}$$

Contribution of Cs and I disentangled!!

Strong linear correlation between the neutron skin of Cs and Pb among different nuclear model predictions



 $A_{\rm PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \approx \frac{G_F Q^2 |Q_W|}{4\sqrt{2} \pi \alpha Z} \frac{F_{\rm W}(Q^2)}{F_{\rm ch}(Q^2)}$

PREX: parity-violating asymmetry APV in the elastic scattering of longitudinally polarized electrons on ²⁰⁸Pb Important complementarity of R_n with the astrophysical sector

- ΔR_{np} is the result of the competition between the Coulomb repulsion, the surface tension, that decreases when the excess neutrons are pushed to the surface, and the symmetry energy.
- The slope parameter, L, is the derivative of the symmetry energy wrt density at saturation
- Theoretical calculations show a strong linear correlation between ΔR_{np} and L, namely larger neutron skins translate into larger values of L

COHERENT and APV result L> 38.5 MeV



²⁰⁸Pb

PREX, PRL 126, 172502 (2021)

Given that L is proportional to the pressure of pure neutron $\stackrel{>}{\stackrel{>}{\xrightarrow{}}}$ matter at saturation density, larger values of ΔR_{np} imply a **larger size of neutron stars**

Results

Reed at al., PRL 126, 172503 (2021) Horowitz et al., PRL 86, 5647 (2001)





Results

Both CEvNS data on CsI and APV on Cs **depend on** R_n and $sin^2(\vartheta_W)$: strong interplay between nuclear physics and weak interactions. Try to exploit **correlations** in both measurements! The dependece of the weak charge on the Weinberg angle allows CEvNS to measure it



to the suppression of the proton contribution

CEvNS is helpful in combination with APV measurement on ¹³³Cs in order to provide experimental constrain on R_n and sin²(ϑ_W) simultaneously

Data driven result!

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Results

COHERENT+APV 1-Dmarginalization on $\sin^2(\vartheta_W)$ $\sin^2(\vartheta_W) = 0.2406^{+0.0035}_{-0.0035}$

Here the value of R_n(¹³³Cs) was **extrapolated** from hadronic experiments using antriprotonic atoms, known to be affected by considerable **model dependencies**.

