



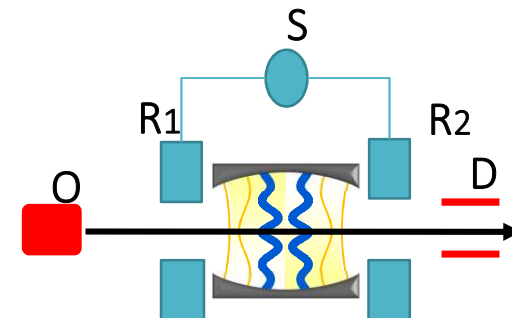
Universidade de Coimbra  
Departamento de Física

# Single-particle interference as a witnesses of Unruh effect

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# Event horizons

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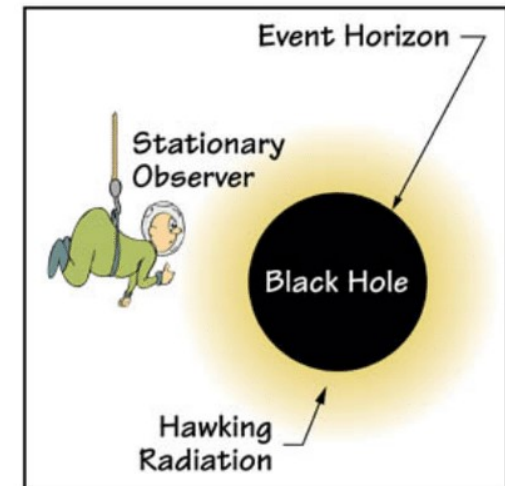
**THE HAWKING EFFECT** (1974) Black holes emit a black body radiation at a temperature inversely proportional to its mass.

$$T = \frac{\hbar c^3}{8\pi G M k_B}$$

For a one solar mass black hole, the peak Hawking radiation temperature is:

$$T_H = \frac{\hbar c^3}{8\pi G M_\odot k_B} = 6.170 \times 10^{-8} \text{ K.}$$

S. Hawking, *Nature*, **248**, 30 (1974).



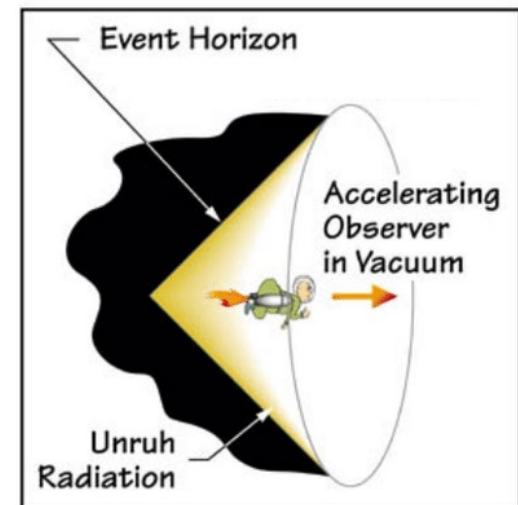
# Accelerating observers



**THE UNRUH EFFECT** (1976) observers uniformly accelerated through Minkowski spacetime registers a thermal radiation at a temperature proportional to its acceleration:

$$T = \frac{\hbar a}{2\pi c k_B}$$

**Vacuum** for inertial observer  $\longleftrightarrow$  **thermal state** for accelerating observer



W.G. Unruh, PRD 14, 870 (1976).

# Unruh Effect

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- Observer accelerating at the Earth's gravitational acceleration of  $g = 9.81 \text{ m}\cdot\text{s}^{-2}$

The temperature of the vacuum is only  $\approx 10^{-20} \text{ K}$ .

- For an experimental test of the Unruh effect it is planned to use accelerations:

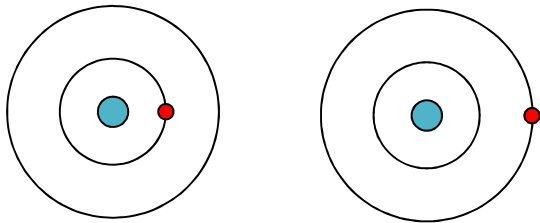
$$\approx 10^{20} \text{ m}\cdot\text{s}^{-2} \quad \longrightarrow \quad \approx 1 \text{ K}$$

# Detector model

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- Detector Unruh-Wald

Two-level system



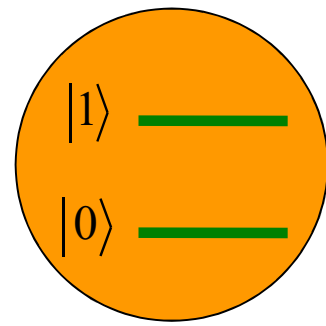
$|0\rangle$

$|1\rangle$

Environment

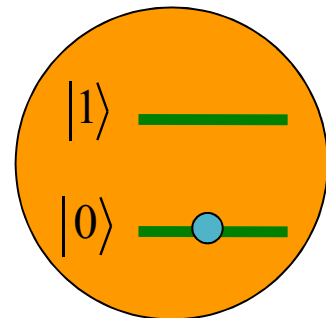
Scalar field  $\phi$

Detector

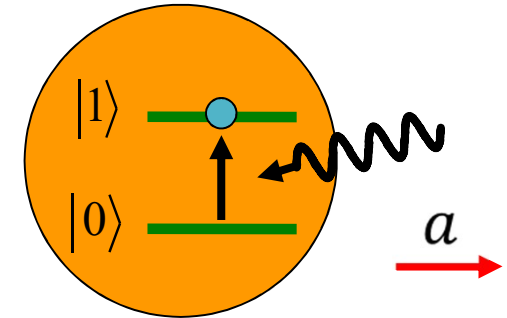


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Inertial  
 $a = 0$



Non-inertial  
 $a \neq 0$



## Using Berry's Phase to Detect the Unruh Effect at Lower Accelerations

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<sup>3</sup>*Department of Physics & Astronomy, University of Waterloo, Waterloo, Ontario N2L 3G1, Canada*

(Received 10 December 2010; published 19 September 2011)

We show that a detector acquires a Berry phase due to its motion in spacetime. The phase is different in the inertial and accelerated case as a direct consequence of the Unruh effect. We exploit this fact to design a novel method to measure the Unruh effect. Surprisingly, the effect is detectable for accelerations  $10^9$  times smaller than previous proposals sustained only for times of nanoseconds.

DOI: 10.1103/PhysRevLett.107.131301

PACS numbers: 04.70.Dy, 03.65.Ta, 04.62.+v, 42.50.Dv

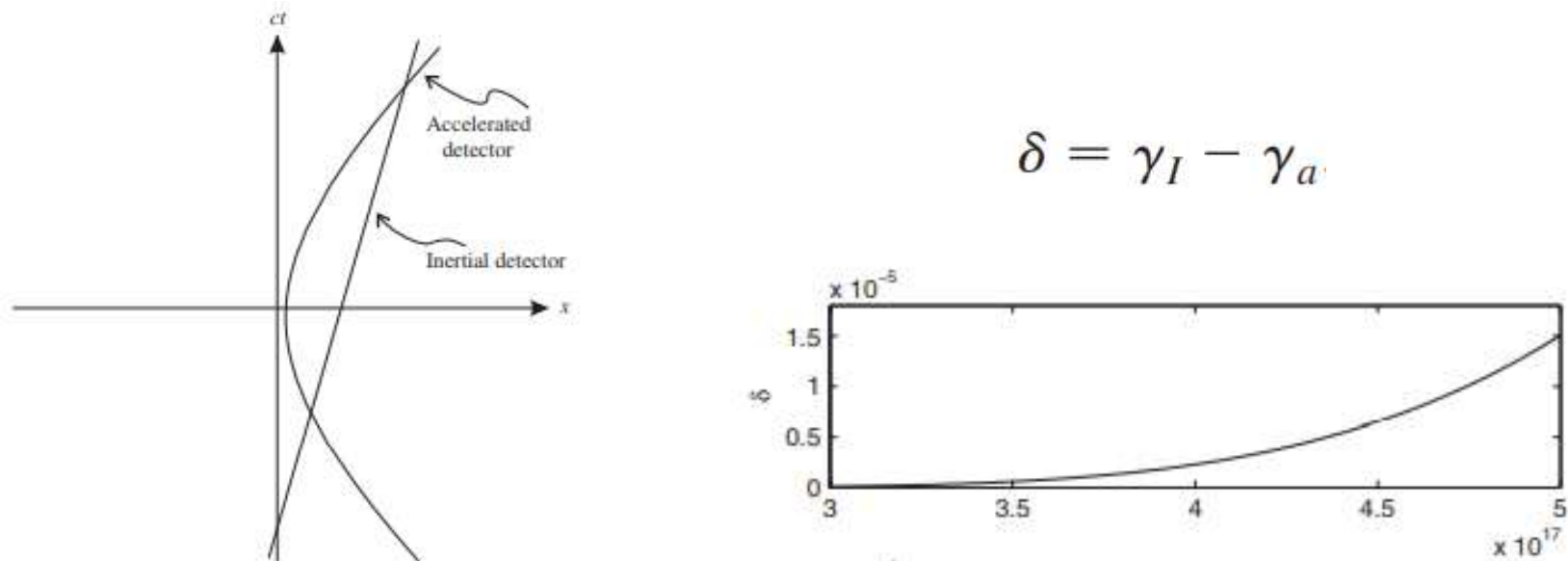
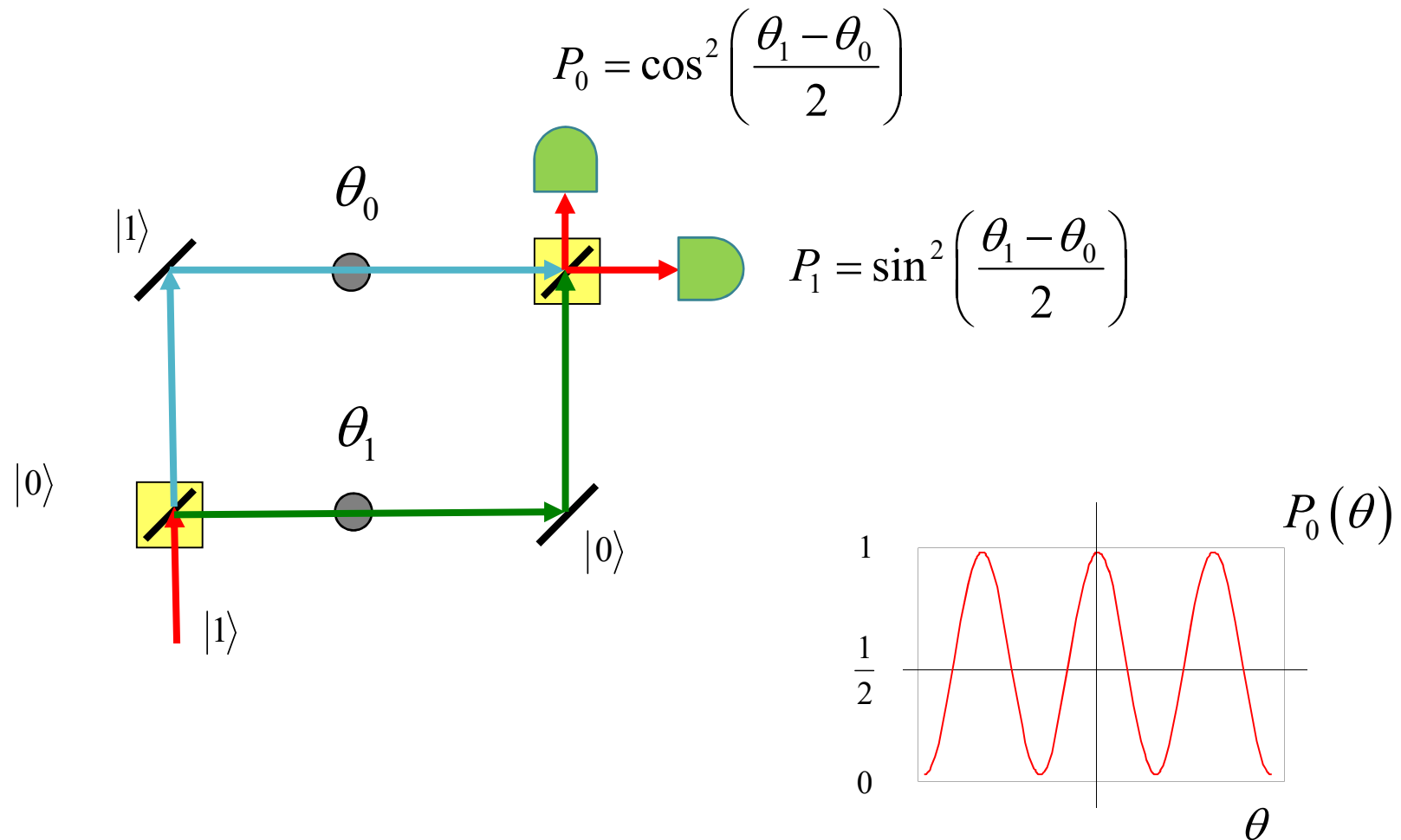


FIG. 1. Trajectories for an inertial and accelerated detector.

# Quantum interferometry

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# Quantum interferometry

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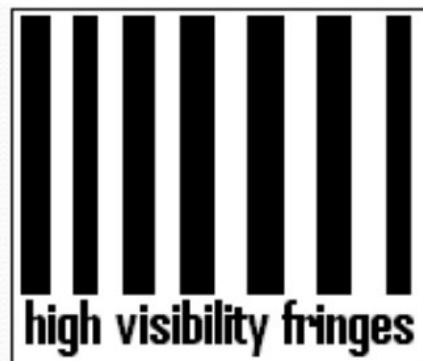
## Visibility of interference fringes

- It is defined as:

$$V = \frac{p^{max} - p^{min}}{p^{max} + p^{min}} \quad 0 \leq V \leq 1$$

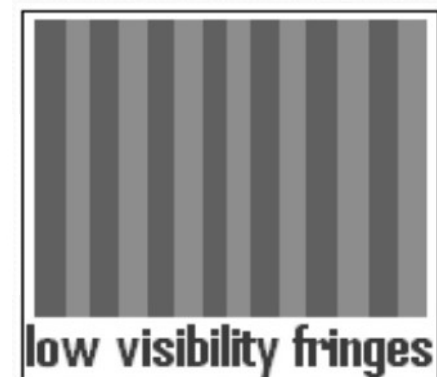
- High visibility:

$$p^{min} = 0, \\ V = 1.$$



- Low visibility:

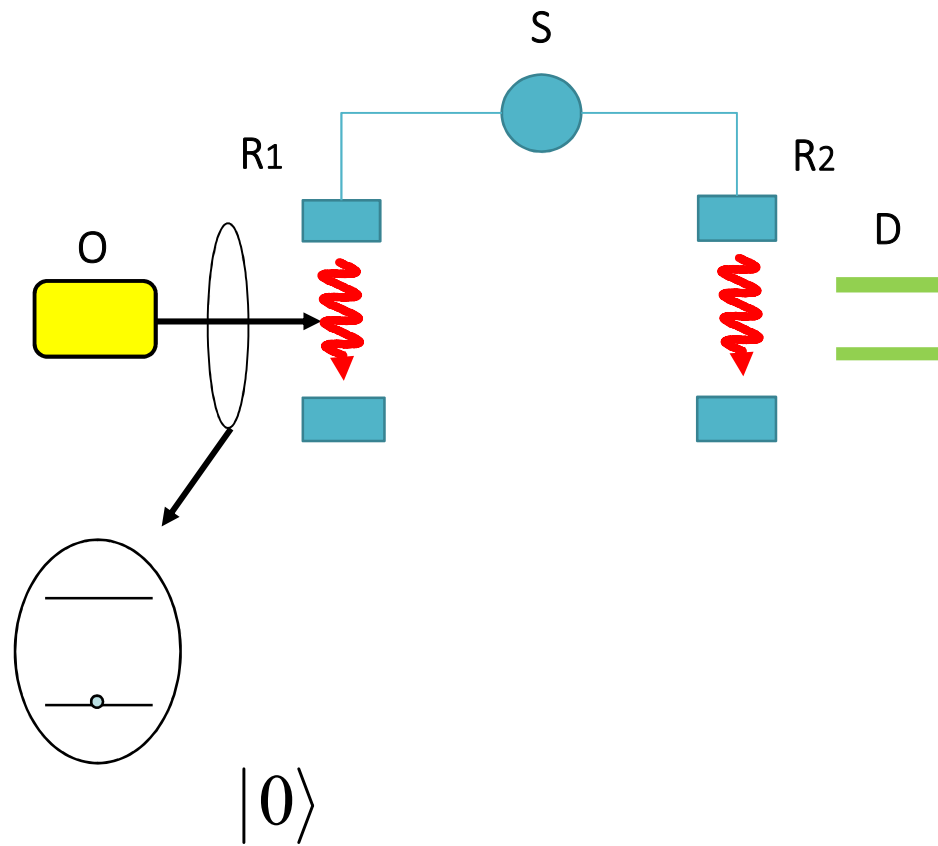
$$p^{min} = p^{max}, \\ V = 0.$$





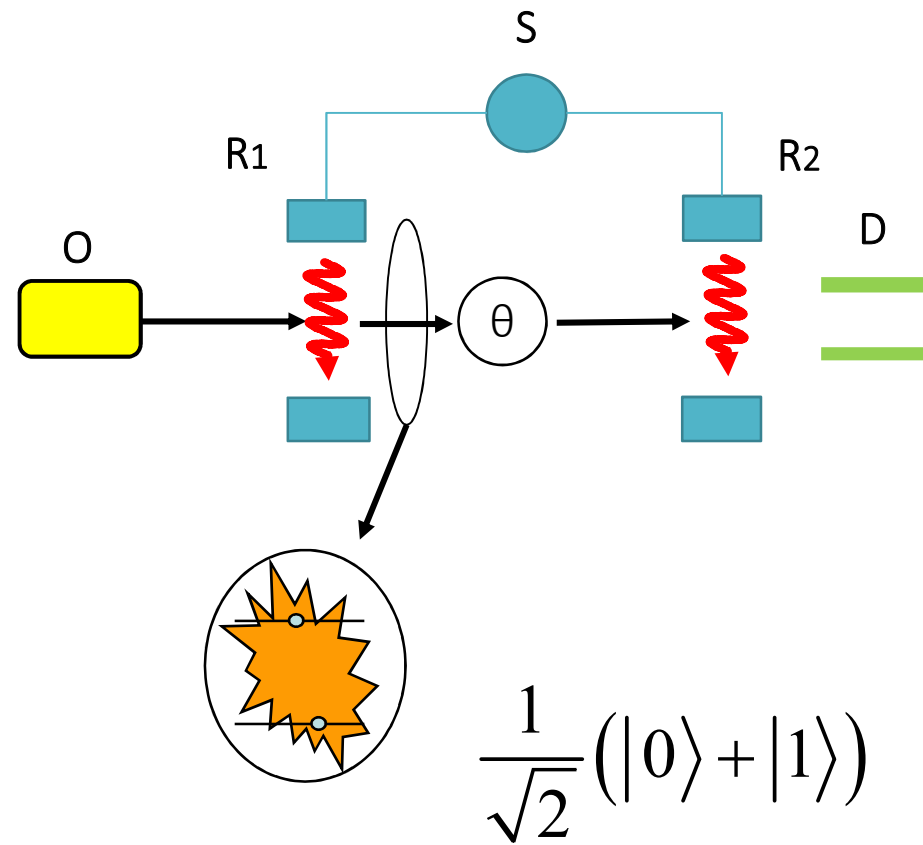
# Quantum interferometry

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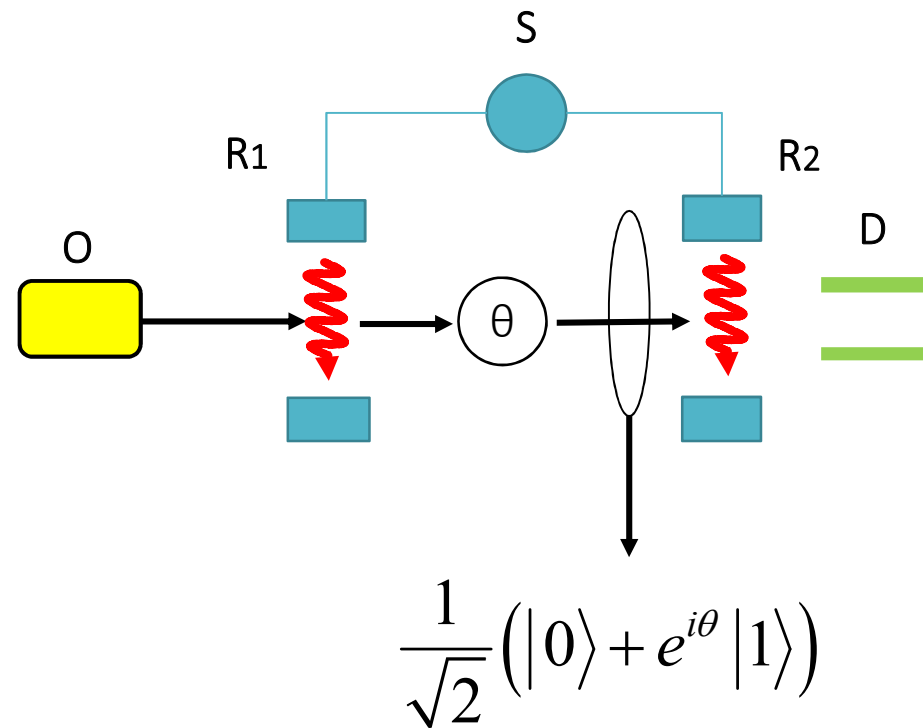
# Quantum interferometry

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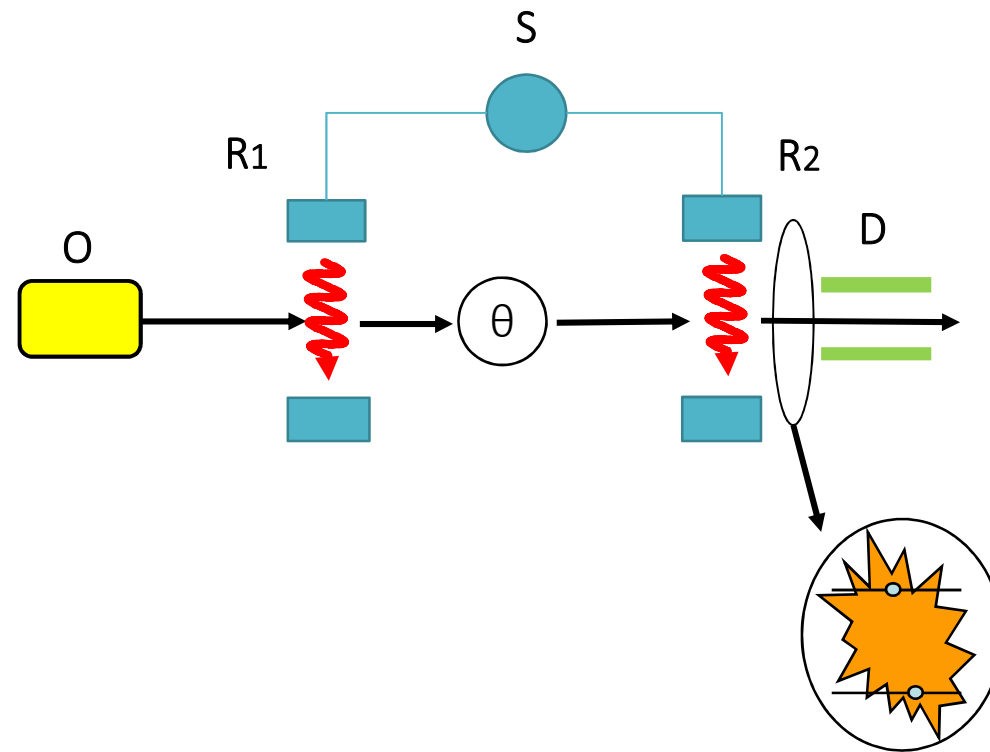
# Quantum interferometry

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# Quantum interferometry

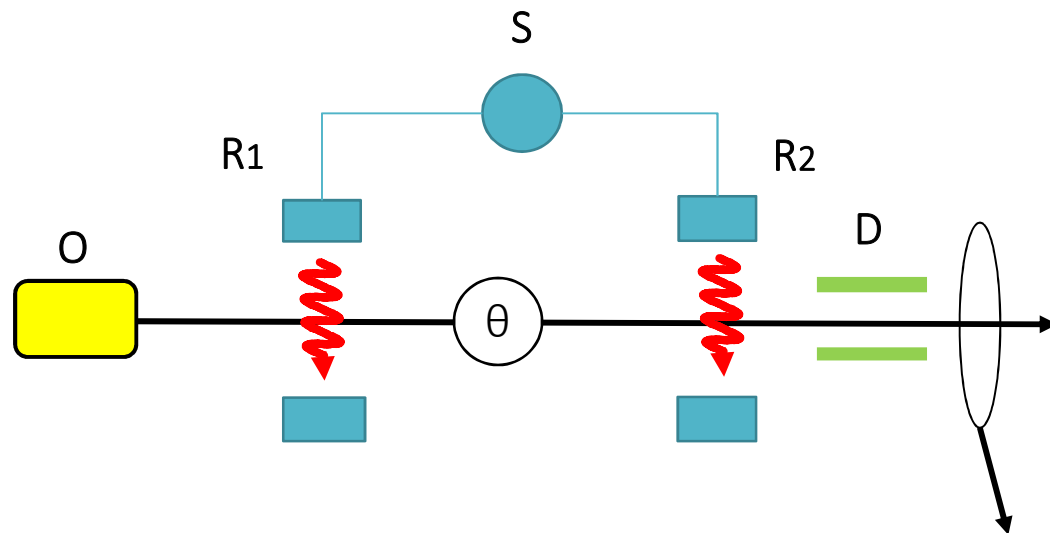
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$$\cos\left(\frac{\theta}{2}\right)|0\rangle - i \sin\left(\frac{\theta}{2}\right)|1\rangle$$

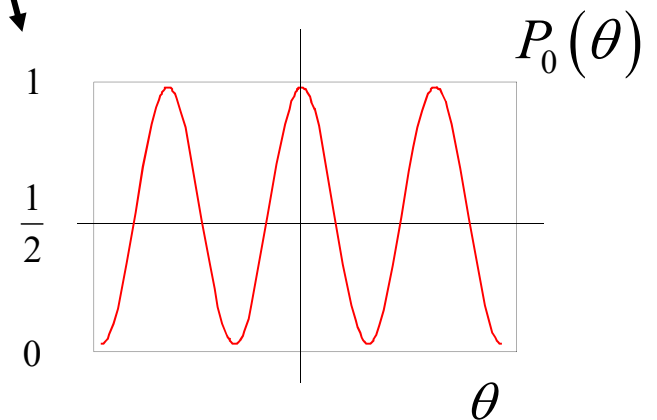
# Quantum interferometry

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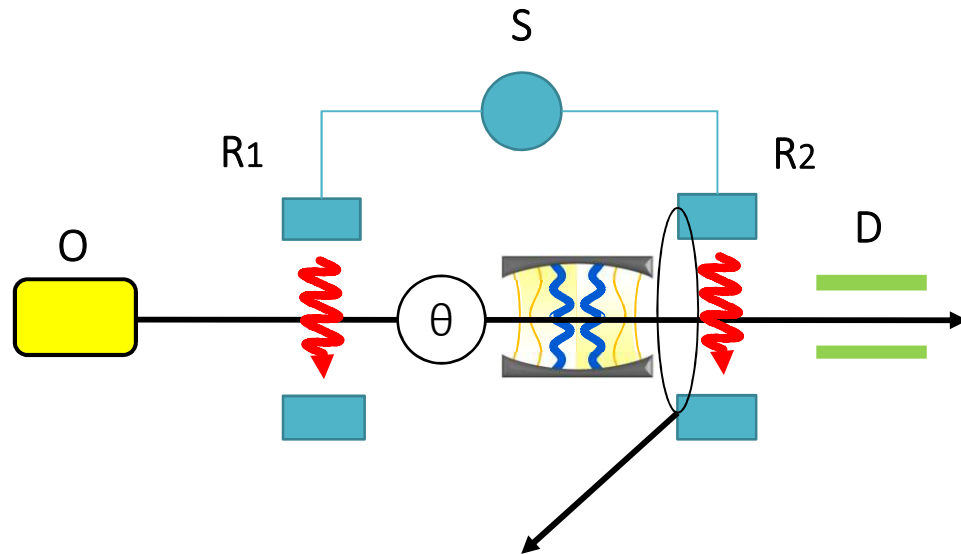


$$P_0 = \cos^2\left(\frac{\theta_1 - \theta_0}{2}\right)$$

$$P_1 = \sin^2\left(\frac{\theta_1 - \theta_0}{2}\right)$$



# Quantum interferometry + Environment



$$|0\rangle|e\rangle \rightarrow \frac{1}{\sqrt{2}} \left( |0\rangle|e_0\rangle + e^{i\theta} |1\rangle|e_1\rangle \right)$$

Entanglement between the atom and the environment (field)

**Inertial ( $a = 0$ )**

$$P_0 = \frac{1}{2} \left[ \cos^2 \left( \frac{\theta}{2} \right) + |\mu|^2 \right]$$

$$V = \frac{1}{1 + 2|\mu|^2} \approx 0.98 \text{ for } \mu = 0.1$$

**Non-inertial ( $a \neq 0$ )**

$$P_0 = \frac{1}{2} \left[ \cos^2 \left( \frac{\theta}{2} \right) + |\mu|^2 \coth \left( \frac{\pi\omega c}{a} \right) \right]$$

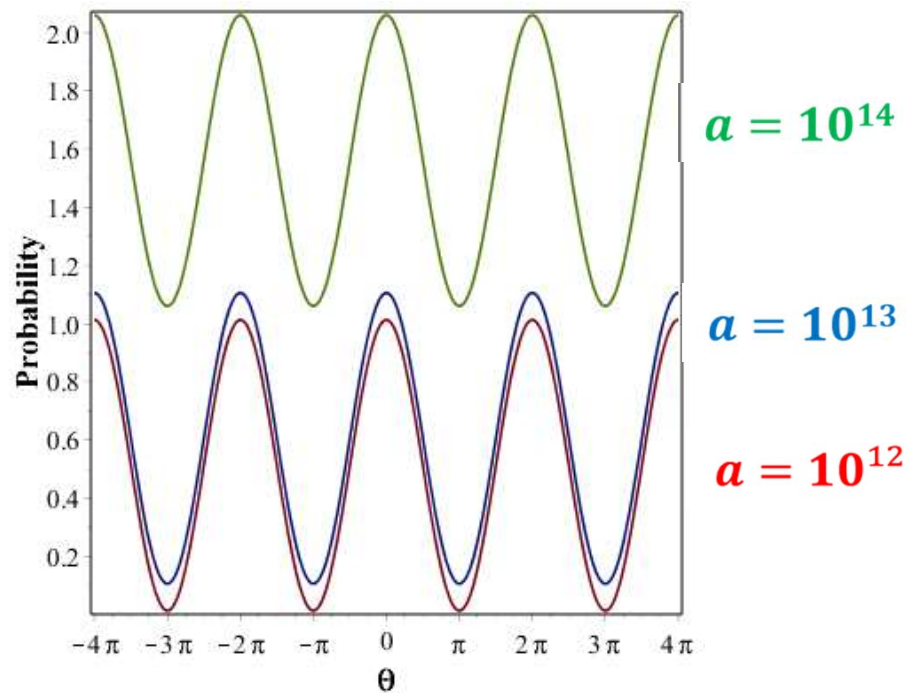
$$V = \frac{1}{1 + 2|\mu|^2 \coth \left( \frac{\pi\omega c}{a} \right)}$$

# Results

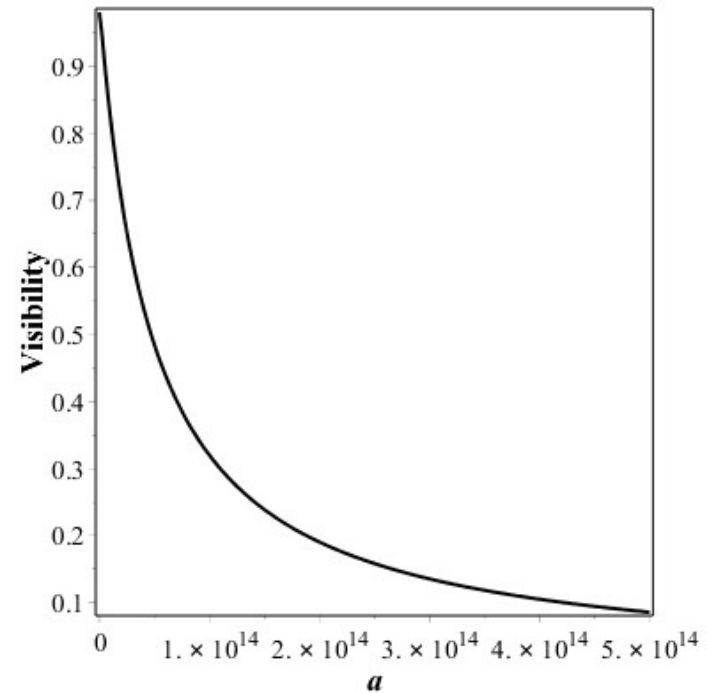
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## Non-inertial Case ( $a \neq 0$ )

### Probability ( $P_0$ )



### Visibility ( $V$ )



# Summary

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- ❑ The environment (scalar field) has an effect on the visibility of the interference fringes
- ❑ The visibility of the interference fringes are different for the inertial and accelerated case due to the Unruh effect
- ❑ This setup may provide a feasible way for the detection of the Unruh effect



**Obrigado!**