

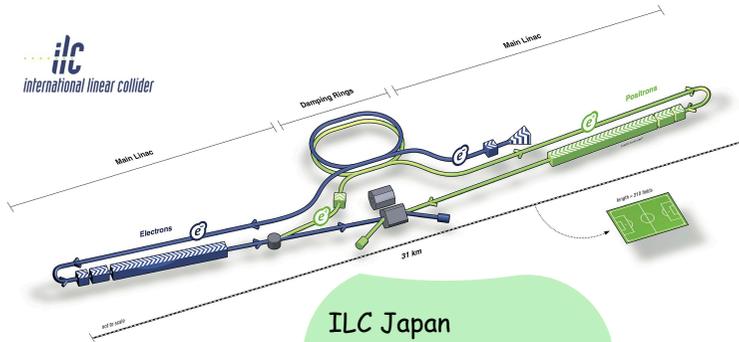
Portuguese Discussion on the European Strategy for Particle Physics

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LIP, Portugal

20 January 2025

Future e^+e^- Collider Projects

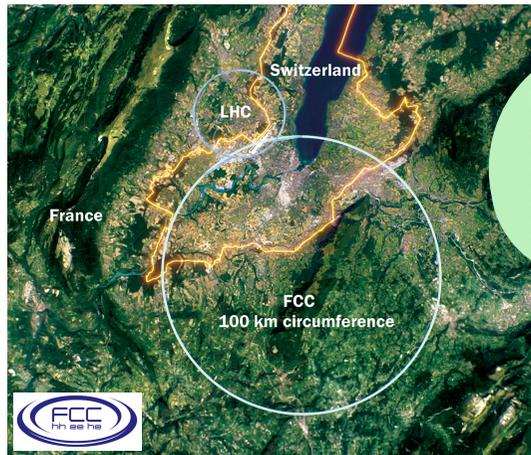
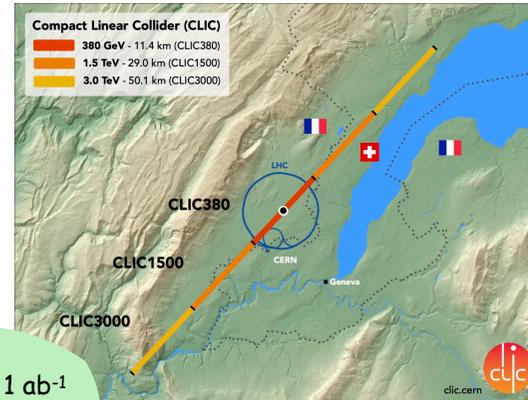


ILC Japan
 250 GeV, 11y \rightarrow 2 ab^{-1}
 500 GeV, 8.5y 4 ab^{-1}
 1000 GeV, 8.5y 8 ab^{-1}

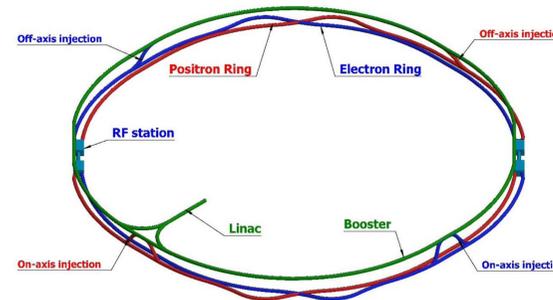


Cool Copper Collider
 250 GeV \rightarrow $1.3 \times 10^{34}/cm^2s$
 550 GeV \rightarrow $2.4 \times 10^{34}/cm^2s$

CLIC, CERN
 380 GeV, 8y \rightarrow 1 ab^{-1}
 1500 GeV, 7y 2.5 ab^{-1}
 3000 GeV, 8.5y 5 ab^{-1}



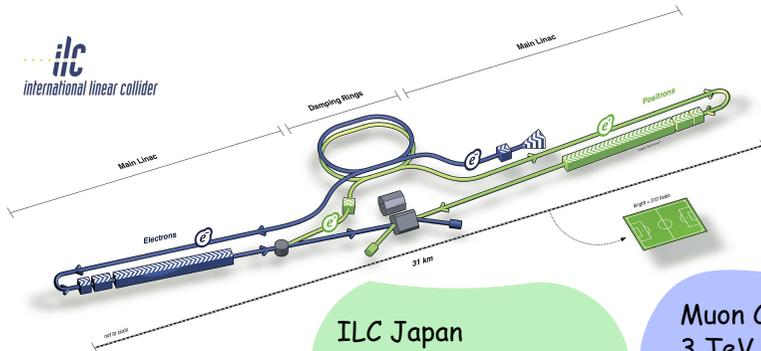
FCC-ee, CERN
 m_z , 4y \rightarrow 150 ab^{-1}
 2 m_w , 1-2y 10 ab^{-1}
 240 GeV, 3y 5 ab^{-1}
 2 m_{top} , 5y 1.5 ab^{-1}



CEPC, China
 m_z , 2y \rightarrow 16 ab^{-1}
 2 m_w , 1y 2.6 ab^{-1}
 240 GeV, 7y 5.6 ab^{-1}



Future Collider Projects

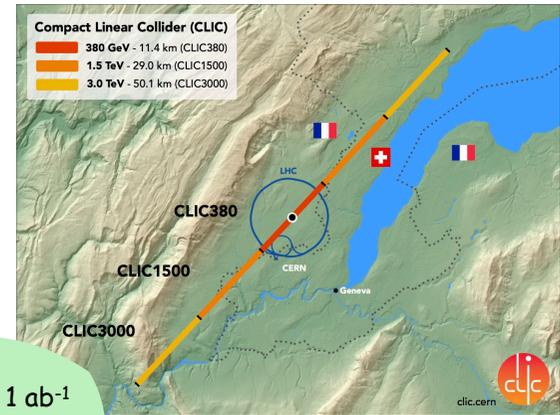


Cool Copper Collider
 250 GeV → $1.3 \times 10^{34} / \text{cm}^2 \text{s}$
 550 GeV → $2.4 \times 10^{34} / \text{cm}^2 \text{s}$

ILC Japan
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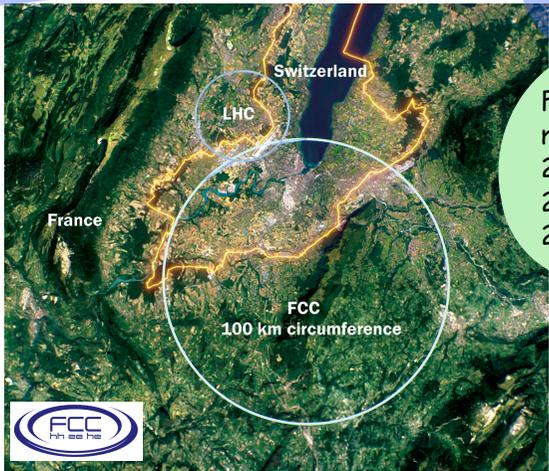
Muon Collider
 3 TeV → 1 ab^{-1}
 10 TeV → 10 ab^{-1}

CLIC, CERN
 380 GeV, 8y → 1 ab^{-1}
 1500 GeV, 7y → 2.5 ab^{-1}
 3000 GeV, 8.5y → 5 ab^{-1}



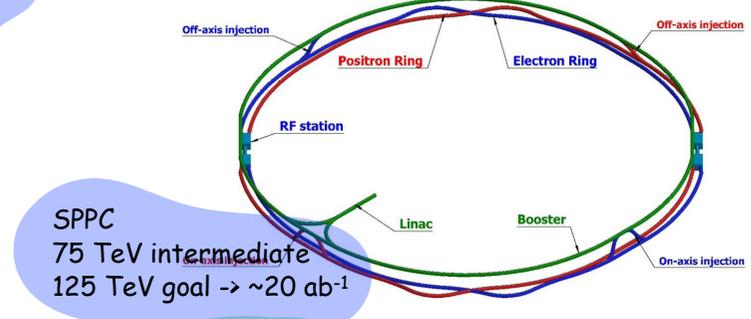
LHeC 0.2-1.3 TeV
 run together w/ HL-LHC
 (≈ Run 5) → 1 ab^{-1}

FCC-eh ($E_{e/p}=60 \text{ GeV}/50 \text{ TeV}$)
 3.5 TeV → 2 ab^{-1}
 run together w/ FCC-hh



FCC-ee, CERN
 mz, 4y → 150 ab^{-1}
 2 mw, 1-2y → 10 ab^{-1}
 240 GeV, 3y → 5 ab^{-1}
 2 m_{top}, 5y → 1.5 ab^{-1}

FCC-hh
 100 TeV → $\sim 20\text{-}25 \text{ ab}^{-1}$
 during 20-25y runtime

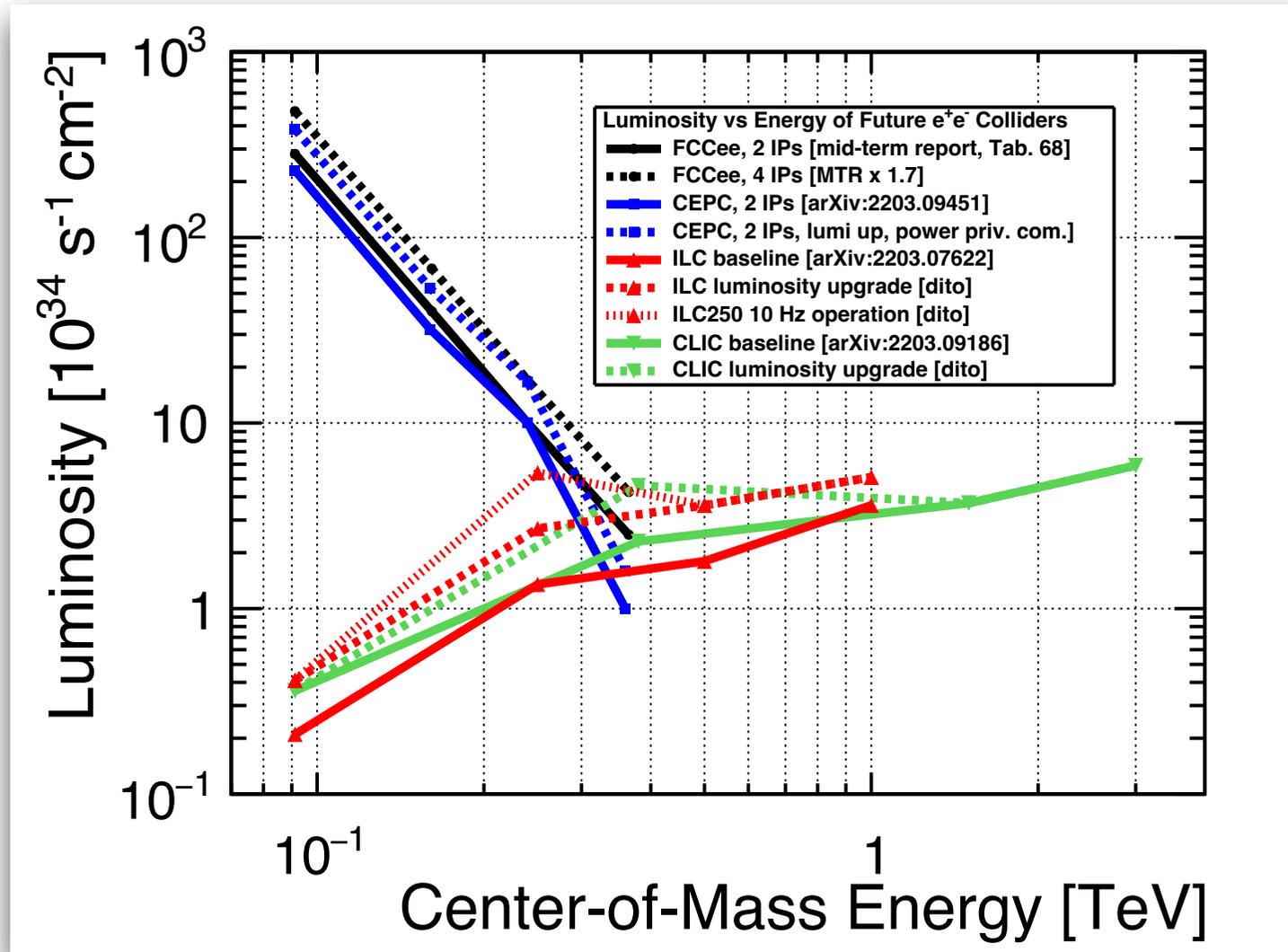


SPPC
 75 TeV intermediate
 125 TeV goal → $\sim 20 \text{ ab}^{-1}$

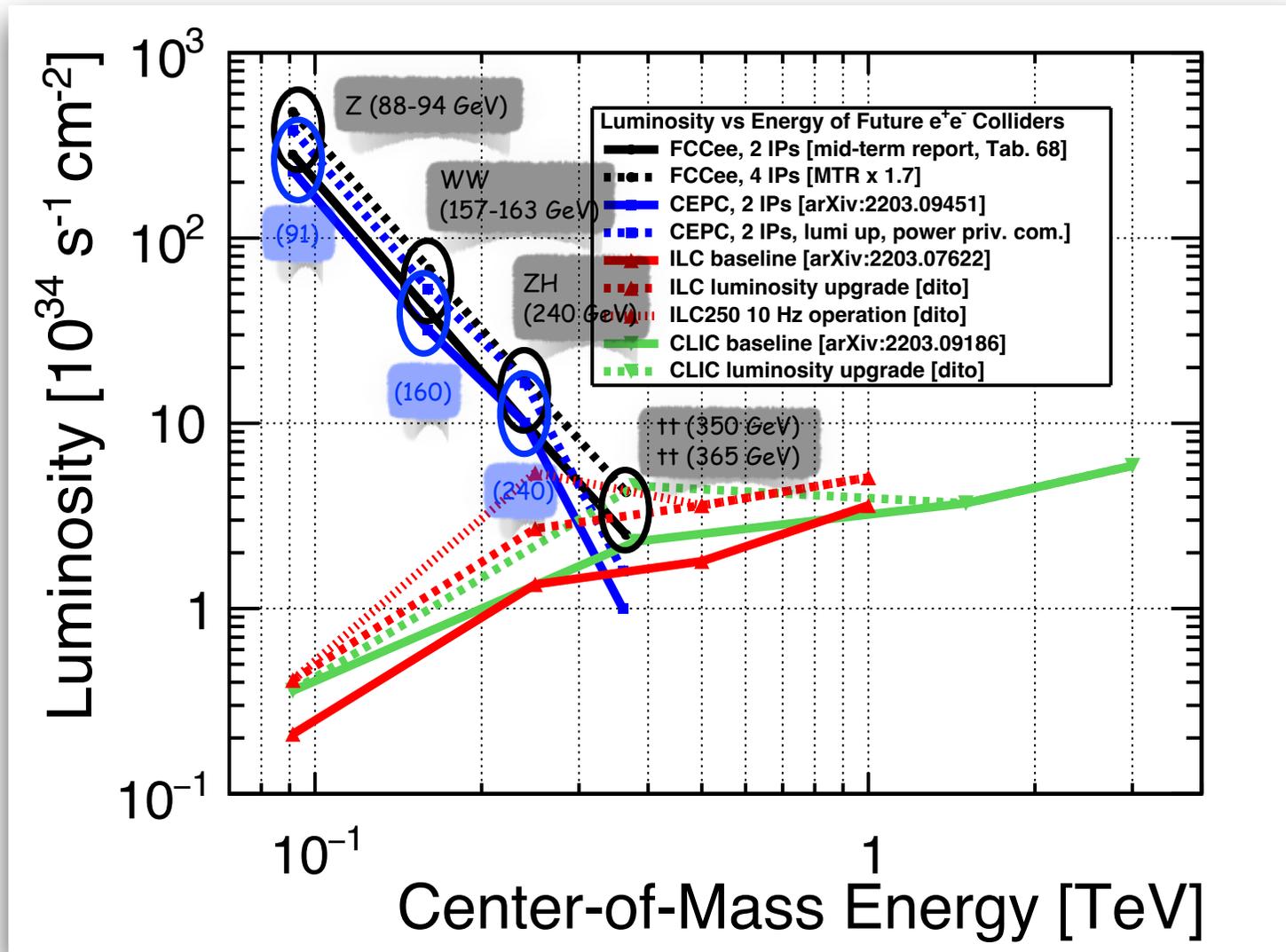
CEPC, China
 mz, 2y → 16 ab^{-1}
 2 mw, 1y → 2.6 ab^{-1}
 240 GeV, 7y → 5.6 ab^{-1}



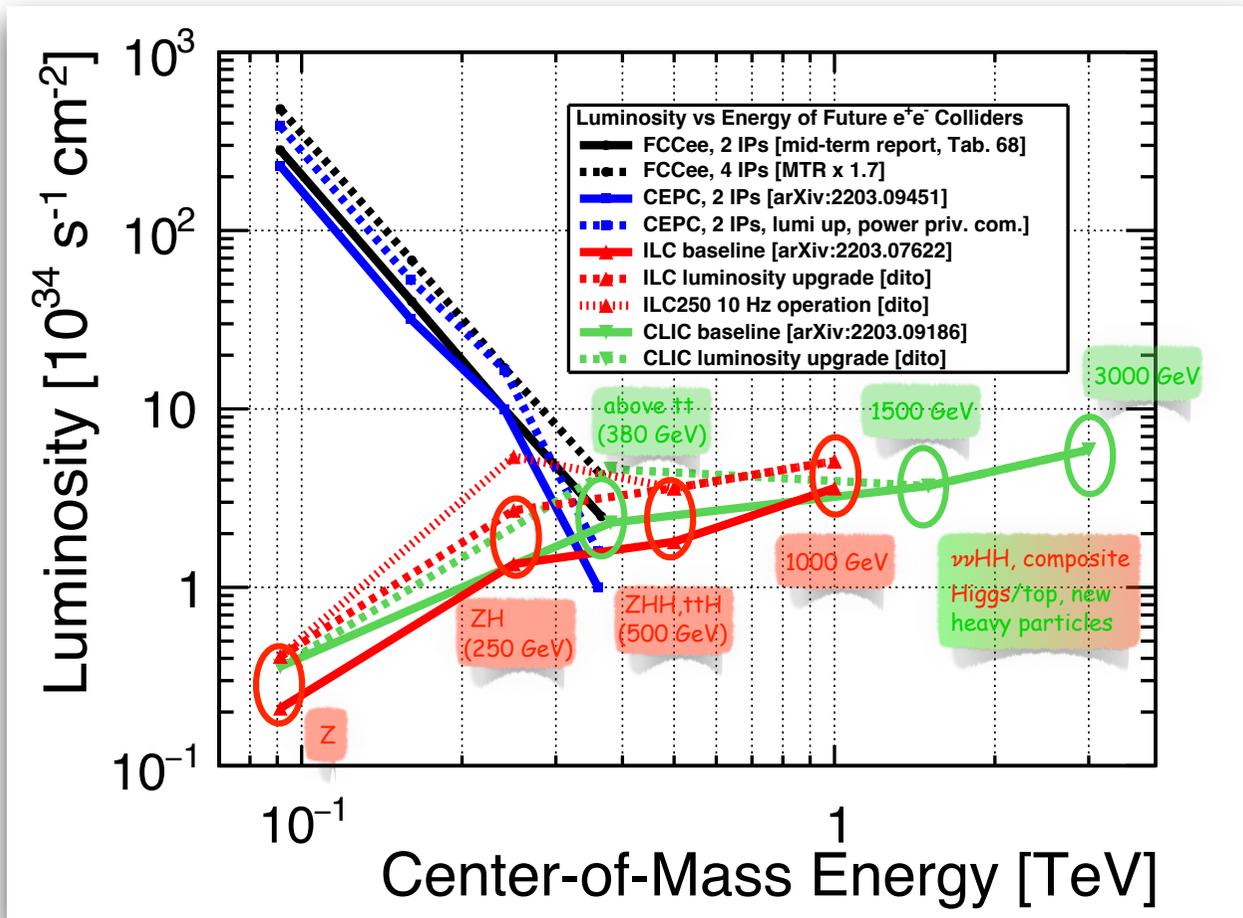
ee-Colliders Energy Range & Luminosity



ee-Colliders Energy Range & Luminosity



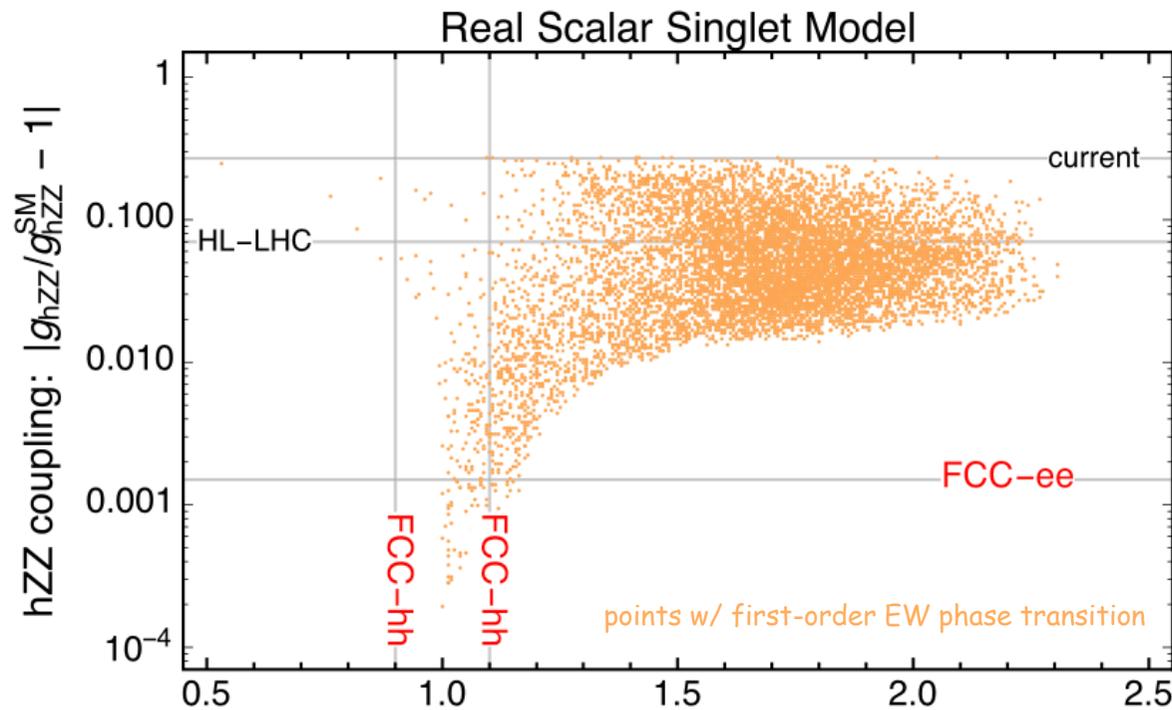
ee-Colliders Energy Range & Luminosity



Accelerator	\sqrt{s} (TeV)	Integrated luminosity (ab^{-1})
CLIC	1.5	2.5
CLIC	3	5
Muon Collider	3	1
Muon Collider	7	10
Muon Collider	14	20

Relation with Single Higgs Couplings

Real Scalar Singlet Model



Precise single Higgs coupling measurements at FCC-ee
constrain trilinear Higgs self-coupling values w/ FOPT

Summary Single Higgs

Higgs Factories

($e+e^-$ circ/lin, $\mu+\mu^-$)

- ◇ absolute coupling measur. ($\delta\Gamma_H = \mathcal{O}(1\%)$)
- ◇ perform similar (\mathcal{L} vs. polarisation)
- ◇ precision: % to ‰ level
- ◇ running at 2 energies: precision \uparrow
- ◇ less sensitive to rare decays

FCC-ee

- ◇ $\delta m_H = 4 \text{ MeV}$ ◇ $|\delta y_t| \sim 10\%$
- ◇ unique: H_{ee} -coupling measurement

mu-Collider

- ◇ lineshape: $\delta m_H = 0.21 \text{ MeV}$, $\delta\Gamma_H = 1.1\text{-}1.4\%$
- ◇ $|\delta y_t| \sim 3\%$ (\leftarrow high prec. Γ_H)

Linear $e+e^-$ Colliders

- ◇ $\delta m_H = 14 \text{ MeV}$
- ◇ $|\delta y_t|_{dir} \sim 3/1.5\%$ CLIC, ILC₅₀₀/ILC₁₀₀₀

(HE-)LHeC/FCC-eh

- ◇ precise measurement of pdf, α_S
- ◇ input for FCC-hh prec. measur.
- ◇ LHeC parallel to HL-LHC: synergy

FCC-hh

- ◇ optimal for rare decays & heavy states
- ◇ sub-percent on all major couplings
- ◇ precise measur. of diff. distributions

HE-LHC/FCC-hh_{<100TeV}

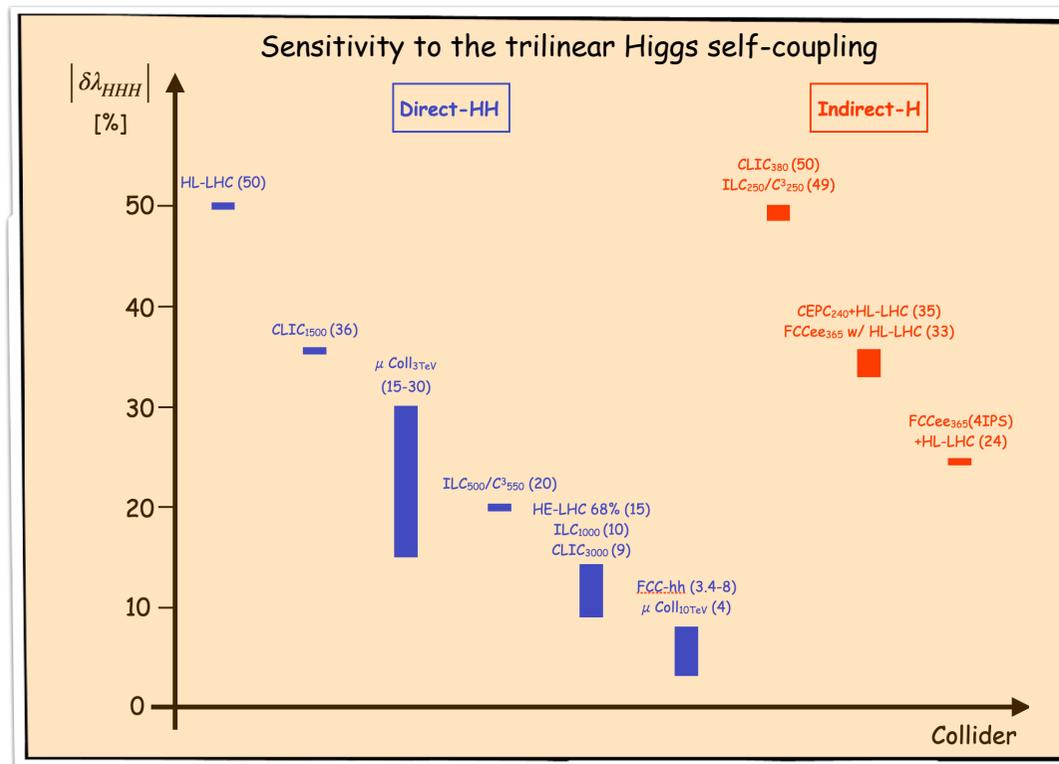
- ◇ precise measurements possible
- ◇ discovery & precision alternative

Summary Di-Higgs

Indirect Detection from Single Higgs

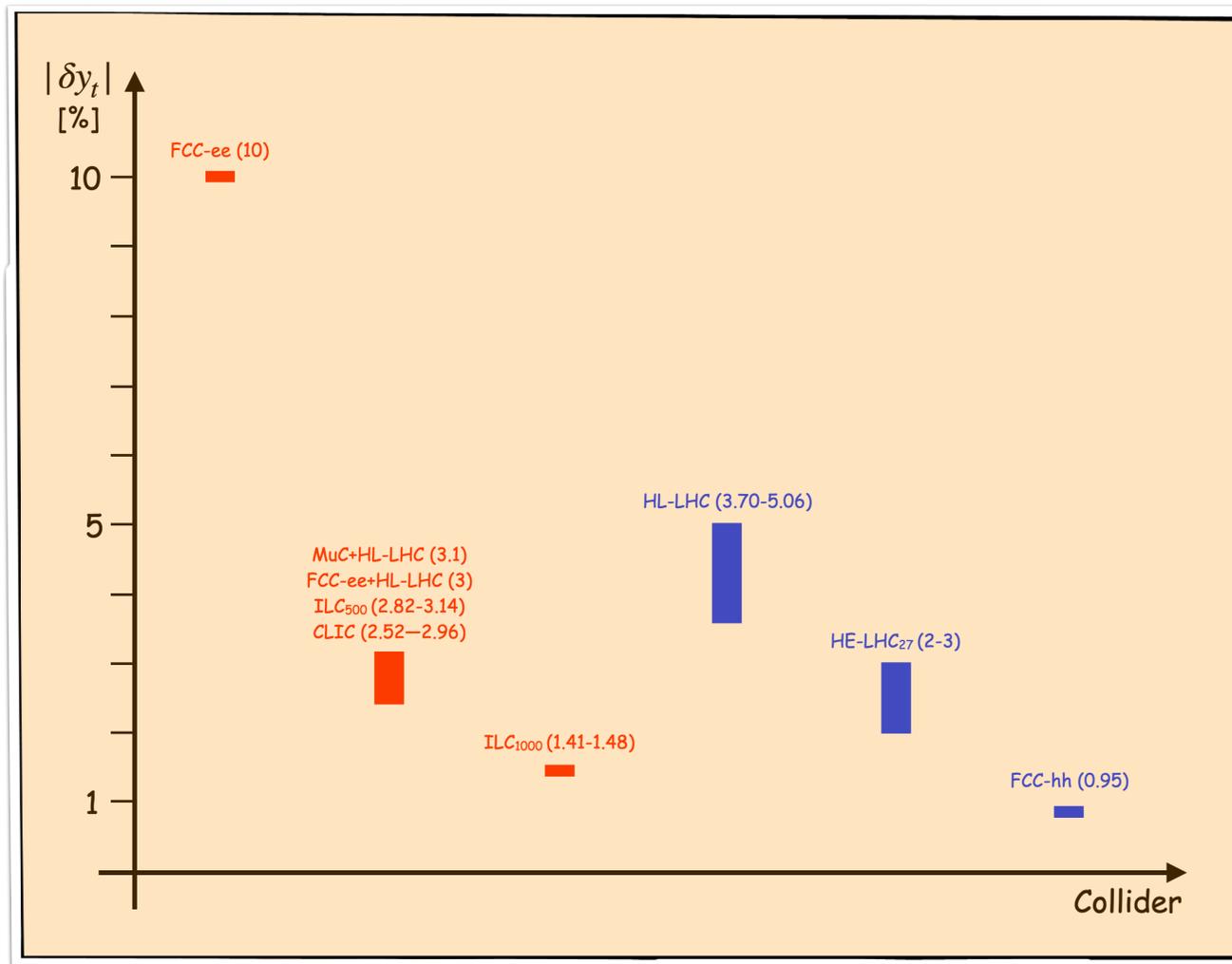
Direct Detection from Double Higgs

- ◇ Single/Di-Higgs: Sensitivity depends on New Physics Scenario
- ◇ Single Higgs: EFT analysis taking into account LO and NLO operators crucial
- ◇ Single/Di-Higgs: Challenge \rightsquigarrow determination of all input parameters as precisely as possible, exploit different energies, polarization



Note on λ_{HHHH} :
first studies show
sensitivity @ HL-LHC,
LC_{>1TeV}, FCC-hh

Comparison of various Collider Options



Higgs Mass Measurement

Higgs mass: comparison w/ other colliders

Today
~ 150 MeV

HL-LHC
~ 20 MeV

ILC₂₅₀
~ 14 MeV

FCC-ee
~ 4 MeV

muColl
~ 0.21 MeV

[HL-LHC: CMS-PAS-FTR-21-007, CERN-2019-007]

[ILC250: Yan, Watanuki, Fujii, Ishikawa, Jeans, Strube eal, Phys.Rev.D94(2016)113002 [1604.07524]]

[FCC-ee: Bernardi, Dewyspelaere, Eysermans, Li, FCC-Coll, ICHEP2024]

[muC: J. de Blas et al., arXiv:2203.04324 [hep-ph] from lineshape 0.21 MeV]

Precision on Trilinear Higgs Self-Coupling

Taken from: S. Dawson et al., arXiv:2209.07510 [hep-ph]

collider	Indirect- h	hh	combined
HL-LHC [78]	100-200%	50%	50%
ILC ₂₅₀ /C ³ -250 [51, 52]	49%	—	49%
ILC ₅₀₀ /C ³ -550 [51, 52]	38%	20%	20%
CLIC ₃₈₀ [54]	50%	—	50%
CLIC ₁₅₀₀ [54]	49%	36%	29%
CLIC ₃₀₀₀ [54]	49%	9%	9%
FCC-ee [55]	33%	—	33%
FCC-ee (4 IPs) [55]	24%	—	24%
FCC-hh [79]	-	3.4-7.8%	3.4-7.8%
μ (3 TeV) [64]	-	15-30%	15-30%
μ (10 TeV) [64]	-	4%	4%

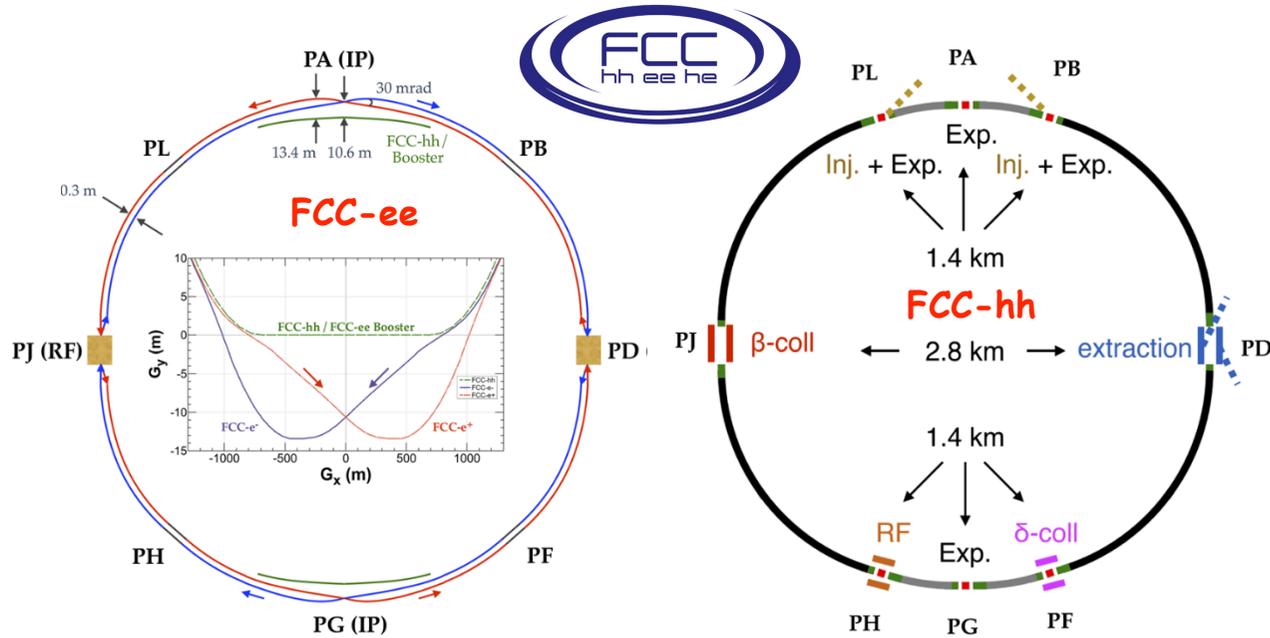
Sensitivity at 68% probability on λ_{hhh} . Values for indirect extraction from single Higgs below the first line are taken from [2]. The quoted values are combined with an independent determination of λ_{hhh} with 50% uncertainty from the HL-LHC. [2] J. de Blas et al., JHEP01 (2020) 139, arXiv:1905.03764 [hep-ph]

FCC Integrated Program

Stage1: Higgs, top, EW factory at highest luminosities (91→365 GeV)
Stage2: 100 TeV pp, energy frontier (in addition eh and ion options)

Higgs, top, EW&QCD precision
 model independence; flavor factory;
 weakly coupled new physics;
 prepare for hh

Higgs self-coupling
 Higgs-top Yukawa coupling
 Heavy new physics



2029-2041

2048-2063

2074-

Colliders and luminosity

SLIDE BY MAGGIE MÜHLEITNER

Collider Implications

Collider Observable	LHC	HL-LHC	FCC-ee ₃₆₅	CEPC	ILC	CLIC	Muon Collider	HE-LHC 27TeV, 15ab ⁻¹	FCC-hh
Single Higgs $ \delta_{VV} ^{exp}$	$\leq 7\%$ [1,2]	1.5% [5]	+HL-LHC 0.17% [55]	240/360+ HL-LHC 0.074/ 0.072% [83]	250/500/1000+ HL-LHC 0.22/0.17/ 0.16% [80]	380/500/1000+ HL-LHC 0.44/0.40 /0.39% [7]	3/10TeV+ HL-LHC 0.89/ 0.33% [69]	1.3% [5]	+FCCee/eh 0.12% [80]
$ \delta_{h^3} ^{theor}$	x40	x9	100 %	40 %	130-100%	260-230%	530-200%	x8	72%
Single Higgs $ \delta_{h^3}^{exp} $			FCC-ee w/HL-LHC 33% [55] FCCee _{4IP} w/HL-LHC 24% [55]	CEPC ₂₄₀ + HL-LHC 35% [82]	ILC ₂₅₀ / C ³ ₂₅₀ 49% [51,52]	CLIC ₃₈₀ 50% [54]			
Di- Higgs $ \delta_{h^3}^{exp} $	-1.4-7.5 [3,4]	50% [5,6]			ILC ₅₀₀ /C ³ ₅₅₀ 20% [10,51,52] ILC ₁₀₀₀ 10% [7]	CLIC ₁₅₀₀ 36% [54] CLIC ₃₀₀₀ ~9% [9,54]	Muon _{3TeV} 15-30% [64] Muon _{10TeV} 4% [64]	95%CL ~30% [11] 68%CL ~15% [11]	30 ab ⁻¹ 3.4-7.8% [79]

Do we actually have a saying?

🗣️ Is the FCC-ee decided? (If so we have a generation of precision physics waiting).

What can we do to help to approve the FCC-ee?

🗣️ Will China build their circular collider? (Decision by end 2025/ beginning 2026).

What is the alternative for CERN? Or others? (muon collider?)

🗣️ Build a physics case for a linear collider? (that compares the different possibilities).

What motivates the different energies and luminosities?

CP-violation and a Model

CP-violation and a Model, the C2HDM

$$g_{2HDM}^{hVV} = \sin(\beta - \alpha) g_{SM}^{hVV}$$

CP-VIOLATING 2HDM

"PSEUDOSCALAR" COMPONENT (DOUBLET)

$$g_{C2HDM}^{hVV} = \cos \alpha_2 g_{2HDM}^{hVV}$$

$$|s_2| = 0 \Rightarrow h_1 \text{ is a pure scalar,}$$

$$|s_2| = 1 \Rightarrow h_1 \text{ is a pure pseudoscalar}$$

Type I

$$\kappa_U' = \kappa_D' = \kappa_L' = \frac{\cos \alpha}{\sin \beta}$$

h_{125} couplings

Type II

$$\kappa_U'' = \frac{\cos \alpha}{\sin \beta}$$

$$\kappa_D'' = \kappa_L'' = -\frac{\sin \alpha}{\cos \beta}$$

$$Y_{C2HDM} = \cos \alpha_2 Y_{2HDM} \pm i\gamma_5 \sin \alpha_2 \tan \beta (1/\tan \beta)$$

Type F(Y)

$$\kappa_U^F = \kappa_L^F = \frac{\cos \alpha}{\sin \beta}$$

$$\kappa_D^F = -\frac{\sin \alpha}{\cos \beta}$$

Type LS(X)

$$\kappa_U^{LS} = \kappa_D^{LS} = \frac{\cos \alpha}{\sin \beta}$$

$$\kappa_L^{LS} = -\frac{\sin \alpha}{\cos \beta}$$

THREE NEUTRAL STATES MIX

CP-VIOLATING 2HDM

$$[h_i]_{mass} = [R_{ij}][h_j]_{gauge}$$

$$[R_{ij}] = \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix}$$

There are many other combinations if one moves away from the alignment limit

$$h_1 \rightarrow ZZ(+) \quad h_2 \rightarrow ZZ(+) \quad h_2 \rightarrow h_1 Z$$

Combinations of three decays

Forbidden in the exact alignment limit

$$h_1 \rightarrow ZZ \Leftrightarrow CP(h_1) = 1 \quad h_2 \rightarrow ZZ \quad CP(h_2) = 1 \quad h_2 \rightarrow h_1 Z \quad CP(h_2) = -CP(h_1)$$

$$h_3 h_2 Z \quad CP(h_3) = -CP(h_2) \quad h_3 h_1 Z \quad CP(h_3) = -CP(h_1) \quad h_2 h_1 Z \quad CP(h_2) = -CP(h_1)$$

$$h_3 \rightarrow h_2 h_1 \Rightarrow CP(h_3) = CP(h_2)$$

CP-violation and a Model, the C2HDM

If the world is too SM-like we need to go to the general C2HDM to find signs of CP-violation. And we need more energy.

Let us go the general 2HDM in the alignment limit (h_1 is SM like). In this case only if we find other particles a search for CP-violation makes sense.

In this limit the vertices that are CP-violating

$$h_3h_3h_3; \quad h_3h_2h_2; \quad h_3H^+H^-; \quad h_3h_3h_3h_1; \quad h_3h_2h_2h_1; \quad h_3h_1H^+H^-;$$

A different choice of the parameters of the potential would interchange h_2 and h_3 .

A combination of 3 decays signals CP-violation

$$h_2H^+H^-; \quad h_3H^+H^-; \quad Zh_2h_3$$

$$h_2h_kh_k; \quad h_3H^+H^-; \quad Zh_2h_3; \quad (k = 2, 3) \quad (2 \leftrightarrow 3)$$

$$h_2h_kh_k; \quad h_3h_lh_l; \quad Zh_2h_3; \quad (k, l = 2, 3)$$

CP-violation with a lot of energy

CP-violation with a lot of energy

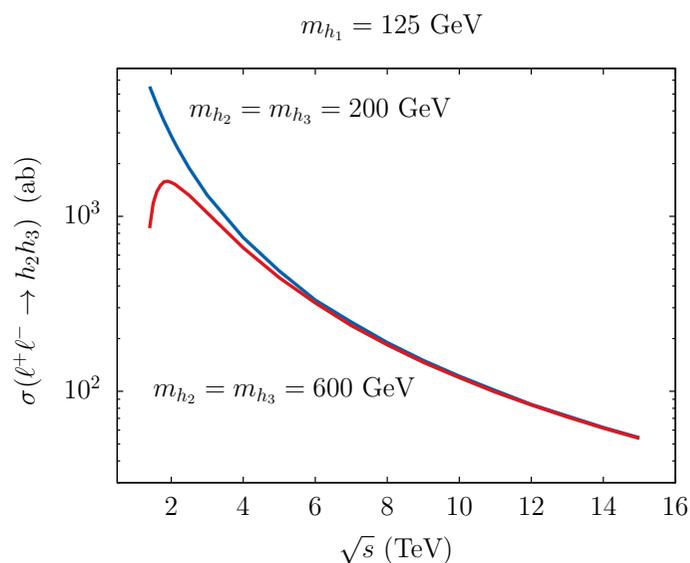
It could happen that at the end of the last LHC run we just move closer and closer to the alignment limit and to a very CP-even 125 GeV Higgs. Considering a few future lepton colliders

Accelerator	\sqrt{s} (TeV)	Integrated luminosity (ab^{-1})
CLIC	1.5	2.5
CLIC	3	5
Muon Collider	3	1
Muon Collider	7	10
Muon Collider	14	20

$$h_2 H^+ H^-; \quad h_3 H^+ H^-; \quad Zh_2 h_3$$

$$h_2 h_k h_k; \quad h_3 H^+ H^-; \quad Zh_2 h_3; \quad (k = 2, 3) \quad (2 \leftrightarrow 3)$$

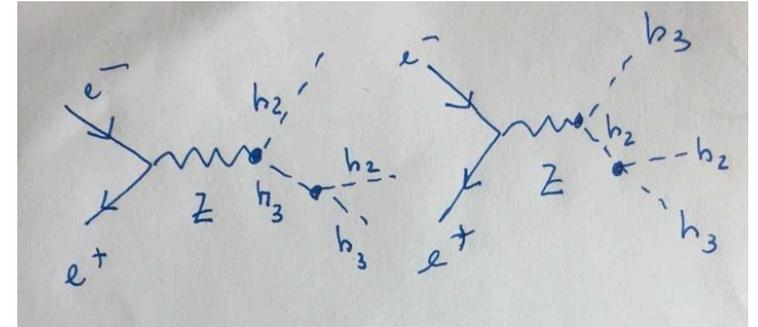
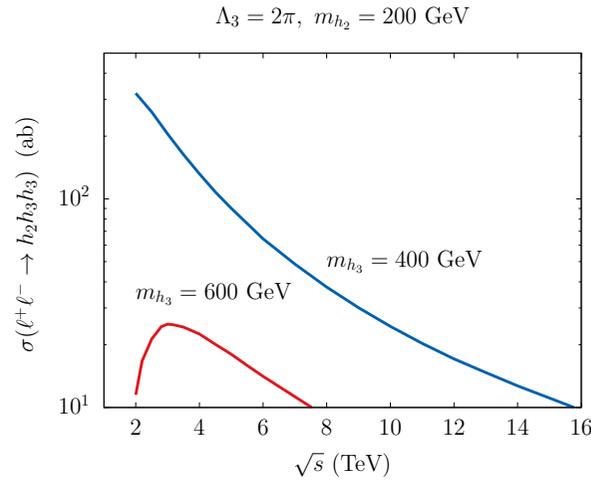
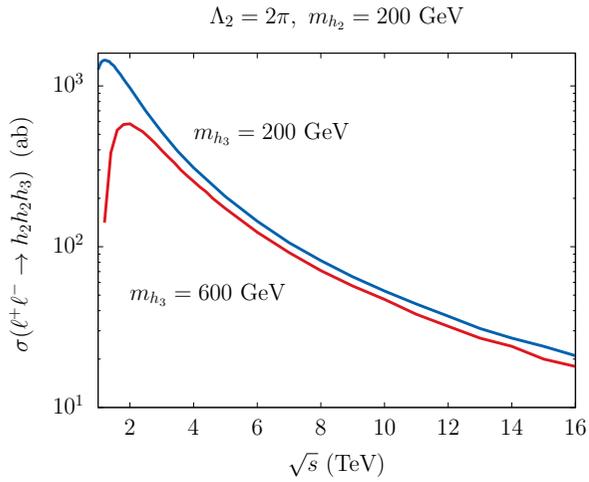
$$h_2 h_k h_k; \quad h_3 h_l h_l; \quad Zh_2 h_3; \quad (k, l = 2, 3)$$



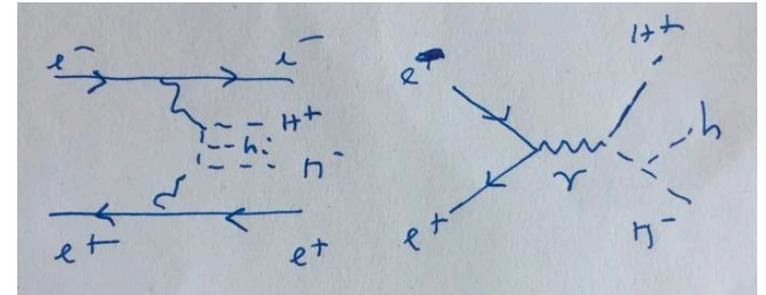
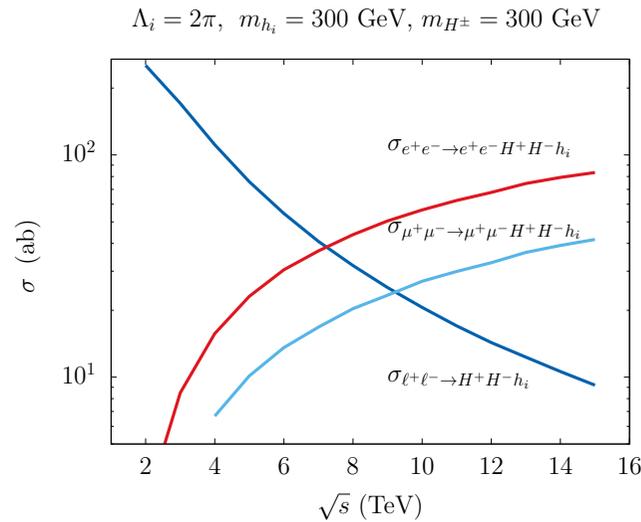
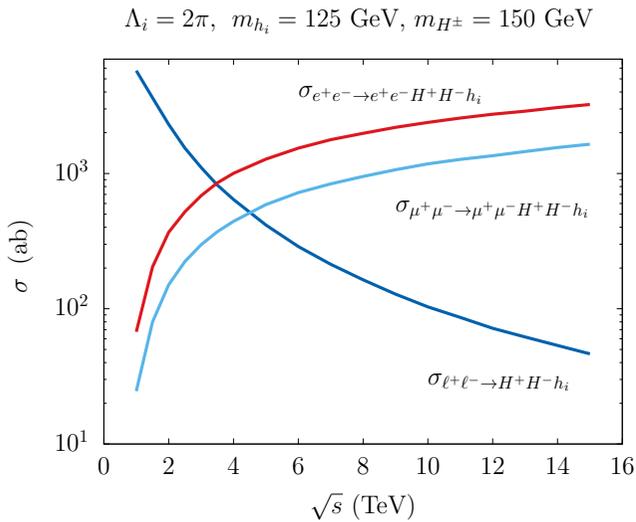
This is an s-channel process with a Z exchange and therefore a gauge coupling. We still need to detect the 2 scalars.

CP-violation with a lot of energy

If the new particles are heavier we will need more energy. Still it will be a hard task.

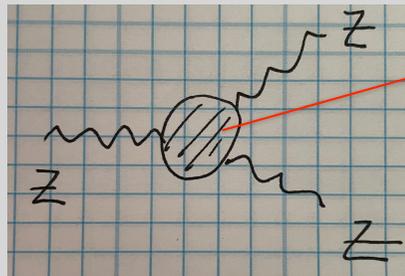


$h_2 h_3 h_3; h_3 h_2 h_2; Zh_2 h_3$



$h_2 H^+ H^-; h_3 H^+ H^-; Zh_2 h_3$

CP-violation with not so much energy



CP-VIOLATION IS HIDDEN INSIDE THE BLOB!

NOTE THAT THESE ARE DIMENSION SIX OPERATORS, THEY APPEAR AT ONE-LOOP IN RENORMALISABLE MODELS. THEY LEAD TO A FINITE RESULT WITH NO NEED FOR RENORMALISATION.

IN THE SM $f_4^Y = 0$ AT ONE-LOOP.

CP-violation with not so much energy (ZZZ)

Low energy means to go quantum - look inside loops. Remember CP-violation could be seen via the combination:

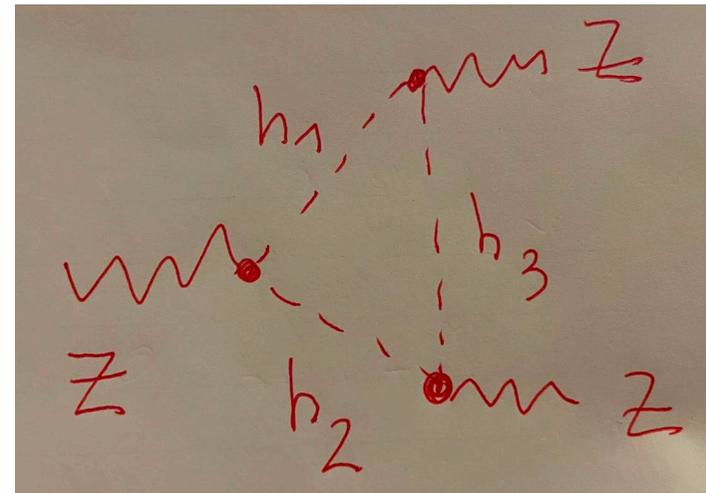
$$h_2 \rightarrow h_1 Z \quad CP(h_2) = - CP(h_1)$$

$$h_3 \rightarrow h_1 Z \quad CP(h_3) = - CP(h_1)$$

$$h_3 \rightarrow h_2 Z \quad CP(h_3) = - CP(h_2)$$

And see if it is possible to extract information from the measurement of the triple ZZZ anomalous coupling.

If we don't have access to the decays we can build a nice Feynman diagram with the same vertices.



Can we build such a model? Dark versions in the 3HDM and 2HDM+singlet and also in the C2HDM

3HDM - CORDERO-CID, HERNÁNDEZ-SÁNCHEZ, KEUS, KING, MORETTI, ROJAS, SOKOŁOWSKA, JHEP 12 (2016) 014

2HDM+SINGLET - AZEVEDO, FERREIRA, MÜHLLEITNER, PATEL, RS, WITTBRODT, JHEP 1811 (2018) 091

CP-violation with not so much energy (ZZZ)

The most general form of the vertex includes a P-even CP-violating term of the form

$$i\Gamma_{\mu\alpha\beta} = -e \frac{p_1^2 - m_Z^2}{m_Z^2} f_4^Z (g_{\mu\alpha} p_{2,\beta} + g_{\mu\beta} p_{3,\alpha}) + \dots$$

GAEMERS, GOUNARIS, ZPC 1 (1979) 259; HAGIWARA, PECCEI, ZEPPENFELD, HIKASA, NPB282 (1987) 253; GRZADKOWSKI, OGREID, OSLAND, JHEP 05 (2016) 025

CMS COLLABORATION, EPJC78 (2018) 165.

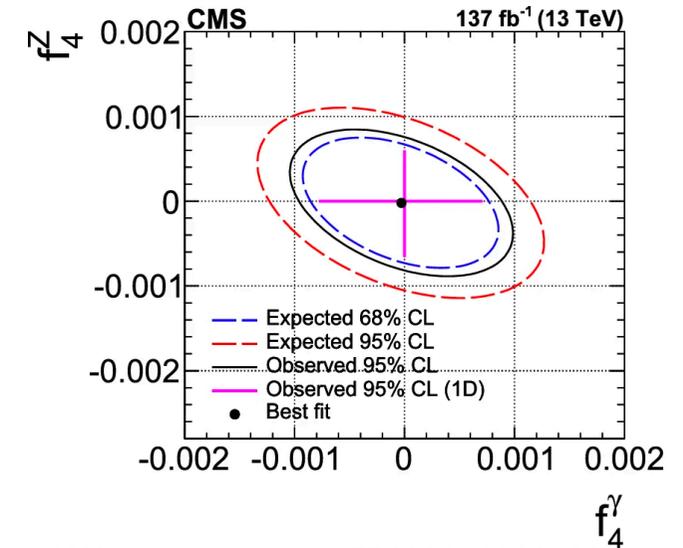
$$-1.2 \times 10^{-3} < f_4^Z < 1.0 \times 10^{-3}$$

ATLAS COLLABORATION, PRD97 (2018) 032005.

$$-1.5 \times 10^{-3} < f_4^Z < 1.5 \times 10^{-3}$$

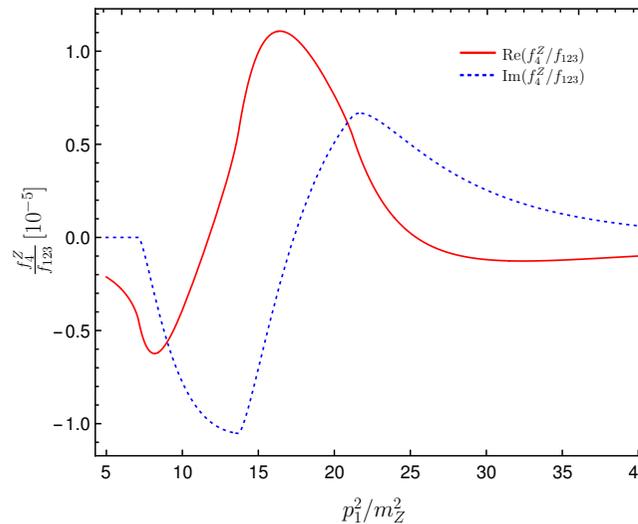
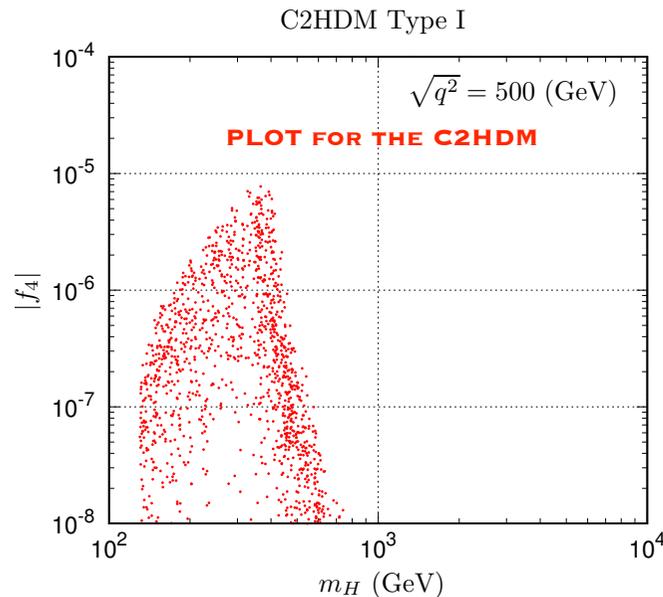
BÉLUSCA-MAÍTO, FALKOWSKI, FONTES, ROMÃO, SILVA, JHEP 04 (2018) 002

PLOT FOR CP IN THE DARK



CMS COLLABORATION, EPJC81 (2021) 81.

AZEVEDO, FERREIRA, MÜHLLEITNER, PATEL, RS, WITTBRODT, JHEP 1811 (2018) 091



The typical maximal value for f_4 seems to be below 10^{-4} .

No studies for future colliders

CP-violation with not so much energy (hWW)

More CP-violation inside loops

$$\mathcal{L}_{hZZ} = \kappa \frac{m_Z^2}{v} h Z_\mu Z^\mu + \frac{\alpha}{v} h Z_\mu \partial_\alpha \partial^\alpha Z^\mu + \frac{\beta}{v} h Z_{\mu\nu} Z^{\mu\nu} + \frac{\gamma}{v} h Z_{\mu\nu} \tilde{Z}^{\mu\nu}$$

ONLY TERM IN THE C2HDM (AND SM) AT TREE-LEVEL

$$i\Gamma_{hWW}^{\mu\nu} = i(g_2 m_w) \left[g^{\mu\nu} \left(1 + a_W - \frac{b_{W1}}{m_W^2} (k_1 \cdot k_2) \right) + \frac{b_{W2}}{m_W^2} k_1^\nu k_2^\mu + \frac{c_W}{m_W^2} \epsilon^{\mu\nu\rho\sigma} k_{1\rho} \cdot k_{2\sigma} \right]$$

P-VIOLATING, CP VIOLATION

$$\mathcal{M}(hW^+W^-) \sim a_1^{W^+W^-} m_W^2 \epsilon_{W^+}^* \epsilon_{W^-}^* + a_3^{W^+W^-} f_{\mu\nu}^* \tilde{f}^{*- \mu\nu}$$

CP-violation with not so much energy (hWW)

In this case we start with the most general WWh vertex

$$\mathcal{M}(hW^+W^-) \sim a_1^{W^+W^-} m_W^2 \epsilon_{W^+}^* \epsilon_{W^-}^* + a_3^{W^+W^-} f_{\mu\nu}^{*+} \tilde{f}^{*- \mu\nu}$$

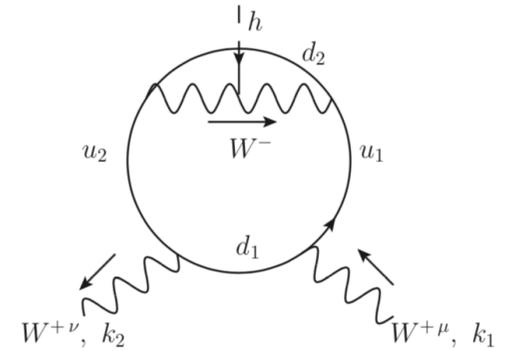
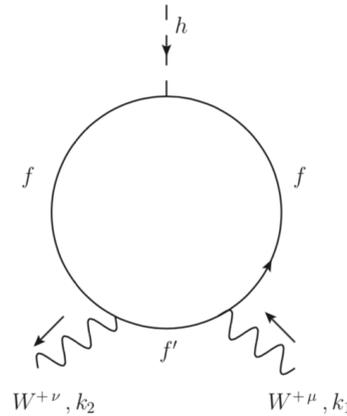
TERM IN THE SM AT TREE-LEVEL
BUT ALSO IN MODELS WITH CP-VIOLATION

TERM COMING FROM A CPV OPERATOR.

- CONTRIBUTION FROM THE SM AT 2-LOOP
- CONTRIBUTION FROM C2HDM AT 1-LOOP

$$c_{\text{CPV}}^{\text{C2HDM}} \simeq 6.6 \times 10^{-4} \sim \mathcal{O}(10^{-3})$$

$$C_{\text{CPV}} = 2 \frac{a_3^{W^+W^-}}{a_1^{W^+W^-}} \quad \frac{a_3^{W^+W^-}}{a_1^{W^+W^-}} \in [-0.81, 0.31]$$



HUANG, MORAIS, RS, JHEP 01 (2021) 168

EXPERIMENTAL BOUND FROM ATLAS AND CMS

CMS COLLABORATION, PRD100 (2019) 112002.

ATLAS COLLABORATION, EPJC 76 (2016) 658.

Parameter	Observed/(10 ⁻³)		Expected/(10 ⁻³)	
	68% C.L.	95% C.L.	68% C.L.	95% C.L.
$f_{a3} \cos(\phi_{a3})$	0.00 ± 0.27	[-92, 14]	0.00 ± 0.23	[-1.2, 1.2]

Parameter	Observed/(10 ⁻³)		Expected/(10 ⁻³)	
	68% CL	95% CL	68% CL	95% CL
f_{a3}	0.20 ^{+0.26} _{-0.16}	[-0.01, 0.88]	0.00 ± 0.05	[-0.21, 0.21]

CMS COLLABORATION, ARXIV:2205.05120V1.

THE BOUND HAS IMPROVED AT LEAST TWO ORDERS OF MAGNITUDE

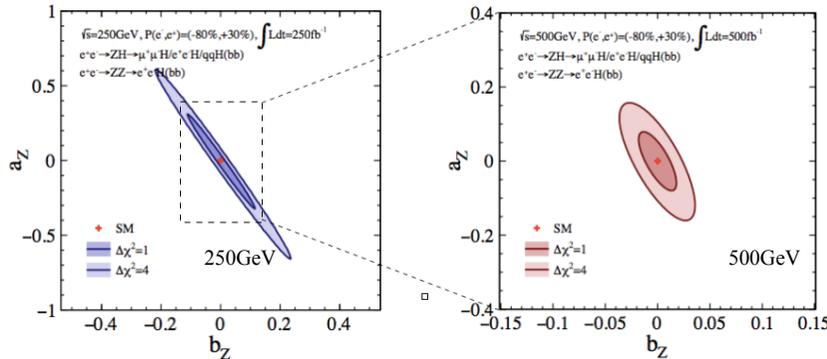
CP-violation with not so much energy (hZZ)

Anomalous ZZH/γZH couplings



3-parameter fit

$$\mathcal{L}_{ZZH} = M_Z^2 \left(\frac{1}{v} + \frac{a_Z}{\Lambda} \right) Z_\mu Z^\mu H + \frac{b_Z}{2\Lambda} \hat{Z}_{\mu\nu} \hat{Z}^{\mu\nu} H + \frac{\tilde{b}_Z}{2\Lambda} \hat{Z}_{\mu\nu} \tilde{Z}^{\mu\nu} H \quad (\Lambda=1\text{TeV})$$



SLIDE FROM KEISUKE FUJII'S
PRESENTATION AT HIGGS COUPLINGS
2018, TOKYO

SITIVITY PROJECTIONS FOR FUTURE COLLIDERS

5-parameter fit

1σ bounds
including 500 GeV operation

**ZZH / γZH structures
can be measured to ~0.5%**

ZH + ZZ at 250 + 500 GeV with H20

<https://arxiv.org/abs/1506.07830>

$$\left\{ \begin{array}{l} a_Z = \pm 0.0223 \quad (\eta_Z = \pm 0.5\%) \\ \zeta_{ZZ} = \pm 0.0067 \\ \zeta_{AZ} = \pm 0.0024 \\ \tilde{\zeta}_{ZZ} = \pm 0.0109 \end{array} \right., \quad \rho = \begin{pmatrix} 1 & -.837 & -.134 & -.009 & -.010 \\ - & 1 & .040 & .008 & .013 \\ - & - & 1 & .006 & -.0012 \\ - & - & - & 1 & .600 \\ - & - & - & - & 1 \end{pmatrix}$$

The most comprehensive study for futures colliders so far was performed for the ILC. The work presents results are for polarised beams $P(e^-, e^+) = (-80\%, 30\%)$ and two COM energies 250 GeV (and an integrated luminosity of 250 fb⁻¹) and 500 GeV (and an integrated luminosity 500fb⁻¹). Limits obtained for an energy of 250 GeV were $c_{CPV}^W \in [-0.321, 0.323]$ and $c_{CPV}^Z \in [-0.016, 0.016]$. For 500 GeV we get $c_{CPV}^W \in [-0.063, 0.062]$ and $c_{CPV}^Z \in [-0.0057, 0.0057]$.

OGAWA, PHD THESIS (2018)

THEREFORE MODELS SUCH AS THE C2HDM MAY BE WITHIN THE REACH OF THESE MACHINES. CAN BE USED TO CONSTRAINT THE C2HDM AT LOOP-LEVEL

Thank you!



CP violation from C violation - still observable at the LHC

♦ Example C2HDM T1: H_1 =SM-like Higgs CP-even, $m_{H_3} = 267$ GeV

m_{H_1} [GeV]	m_{H_2} [GeV]	m_{H^\pm} [GeV]	α_1	α_2	α_3	$\tan \beta$	$\text{Re}(m_{12}^2)$ [GeV ²]
125.09	265	236	1.419	0.004	-0.731	5.474	9929

$\sigma_{H_1 H_1}^{\text{NLO}}$ [fb]	K -factor	$\Gamma_{H_1}^{\text{tot}}$ [GeV]	$\Gamma_{H_2}^{\text{tot}}$ [GeV]	$\Gamma_{H_3}^{\text{tot}}$ [GeV]	$\Gamma_{H^\pm}^{\text{tot}}$ [GeV]
387	2.06	4.106×10^{-3}	3.625×10^{-3}	4.880×10^{-3}	0.127
$\lambda_{3H_1}/\lambda_{3H}$	$y_{t,H_1}^e/y_{t,H}$	$\sigma_{H_1}^{\text{NNLO}}$ [pb]	$\sigma_{H_2}^{\text{NNLO}}$ [pb]	$\sigma_{H_3}^{\text{NNLO}}$ [pb]	
0.995	1.005	49.75	0.76	0.84	

$\sigma(H_2) \times \text{BR}(H_2 \rightarrow H_1 H_1) = 191$ fb ,	$\sigma(H_2) \times \text{BR}(H_2 \rightarrow WW) = 254$ fb
$\sigma(H_2) \times \text{BR}(H_2 \rightarrow ZZ) = 109$ fb ,	$\sigma(H_2) \times \text{BR}(H_2 \rightarrow ZH_1) = 122$ fb
$\sigma(H_3) \times \text{BR}(H_3 \rightarrow H_1 H_1) = 235$ fb ,	$\sigma(H_3) \times \text{BR}(H_3 \rightarrow WW) = 315$ fb
$\sigma(H_3) \times \text{BR}(H_3 \rightarrow ZZ) = 136$ fb ,	$\sigma(H_3) \times \text{BR}(H_3 \rightarrow ZH_1) = 76$ fb .

CP-even

CP-odd

CP violation from C violation - still observable at the LHC

♦ Example C2HDM T1: H_1 =SM-like Higgs CP-even, $m_{H_3} = 267$ GeV

m_{H_1} [GeV]	m_{H_2} [GeV]	m_{H^\pm} [GeV]	α_1	α_2	α_3	$\tan \beta$	$\text{Re}(m_{12}^2)$ [GeV ²]
125.09	265	236	1.419	0.004	-0.731	5.474	9929

$\sigma_{H_1 H_1}^{\text{NLO}}$ [fb]	K-factor	$\Gamma_{H_1}^{\text{tot}}$ [GeV]	$\Gamma_{H_2}^{\text{tot}}$ [GeV]	$\Gamma_{H_3}^{\text{tot}}$ [GeV]	$\Gamma_{H^\pm}^{\text{tot}}$ [GeV]
387	2.06	4.106×10^{-3}	3.625×10^{-3}	4.880×10^{-3}	0.127

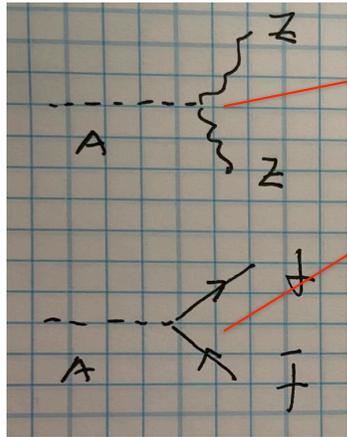
$\lambda_{3H_1}/\lambda_{3H}$	$y_{t,H_1}^e/y_{t,H}$	$\sigma_{H_1}^{\text{NNLO}}$ [pb]	$\sigma_{H_2}^{\text{NNLO}}$ [pb]	$\sigma_{H_3}^{\text{NNLO}}$ [pb]	
0.995	1.005	49.75	0.76	0.84	

$$\begin{aligned}
 \sigma(H_2) \times \text{BR}(H_2 \rightarrow H_1 H_1) &= 191 \text{ fb}, & \sigma(H_2) \times \text{BR}(H_2 \rightarrow WW) &= 254 \text{ fb} \\
 \sigma(H_2) \times \text{BR}(H_2 \rightarrow ZZ) &= 109 \text{ fb}, & \sigma(H_2) \times \text{BR}(H_2 \rightarrow ZH_1) &= 122 \text{ fb} \\
 \sigma(H_3) \times \text{BR}(H_3 \rightarrow H_1 H_1) &= 235 \text{ fb}, & \sigma(H_3) \times \text{BR}(H_3 \rightarrow WW) &= 315 \text{ fb} \\
 \sigma(H_3) \times \text{BR}(H_3 \rightarrow ZZ) &= 136 \text{ fb}, & \sigma(H_3) \times \text{BR}(H_3 \rightarrow ZH_1) &= 76 \text{ fb}.
 \end{aligned}$$

CP-even

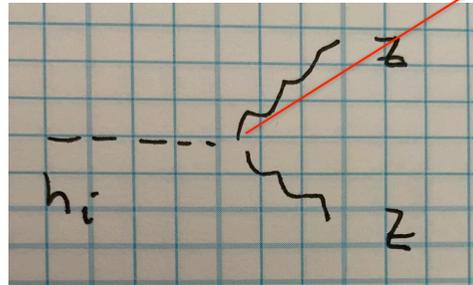
CP-odd

However...

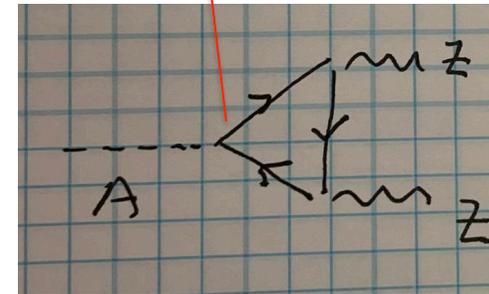


Disallowed in a CP conserving model. A is a pseudoscalar

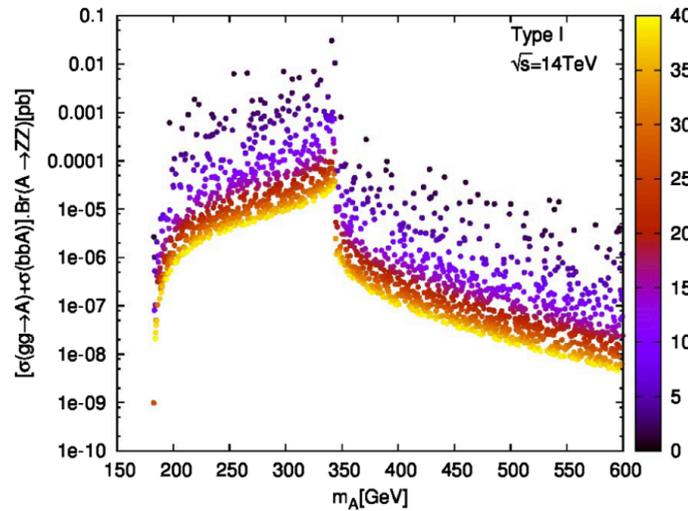
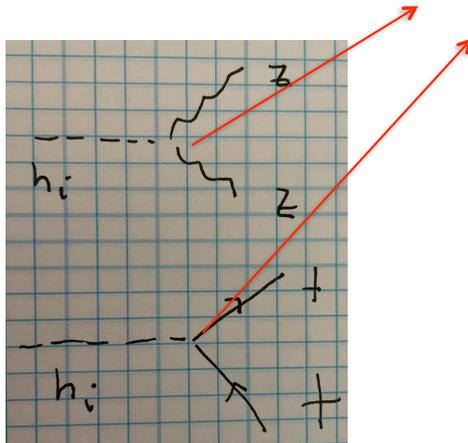
Allowed in a CP-conserving model.



If this tree-level coupling is very small (of the order of the loop process below) it is not possible to distinguish the models.



Both allowed in a CP-violating model.

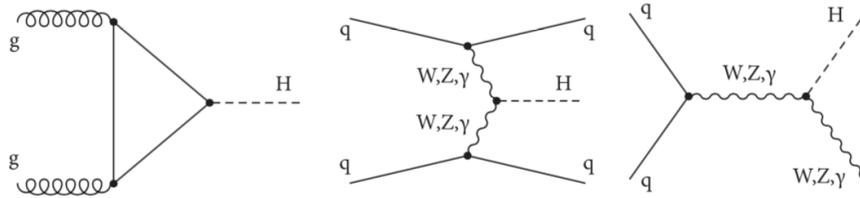


To unambiguously identify CP-violation combine as many CP-sensitive measurements as possible

CP-violation with not so much energy (hWW)

$$A(\text{HVV}) \sim \left[a_1^{\text{VV}} + \frac{\kappa_1^{\text{VV}} q_1^2 + \kappa_2^{\text{VV}} q_2^2}{(\Lambda_1^{\text{VV}})^2} \right] m_{\text{V}1}^2 \epsilon_{\text{V}1}^* \epsilon_{\text{V}2}^* + a_2^{\text{VV}} f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + a_3^{\text{VV}} f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

EFFECTIVE LAGRANGIAN (CMS NOTATION)



CMS COLLABORATION, PRD100 (2019) 112002.

FIG. 1. Examples of leading-order Feynman diagrams for H boson production via the gluon fusion (left), vector boson fusion (middle), and associated production with a vector boson (right). The HWW and HZZ couplings may appear at tree level, as the SM predicts. Additionally, HWW , HZZ , $HZ\gamma$, $H\gamma\gamma$, and Hgg couplings may be generated by loops of SM or unknown particles, as indicated in the left diagram but not shown explicitly in the middle and right diagrams.

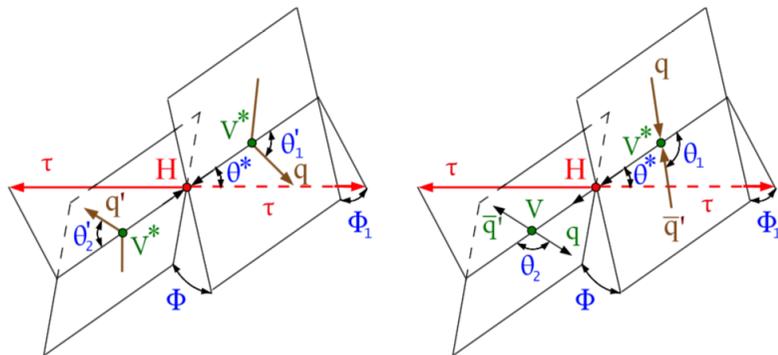


FIG. 2. Illustrations of H boson production in $qq' \rightarrow gg(qq') \rightarrow H(qq') \rightarrow \tau\tau(qq')$ or VBF $qq' \rightarrow V^*V^*(qq') \rightarrow H(qq') \rightarrow \tau\tau(qq')$ (left) and in associated production $qq' \rightarrow V^* \rightarrow VH \rightarrow q\bar{q}'\tau\tau$ (right). The $H \rightarrow \tau\tau$ decay is shown without further illustrating the τ decay chain. Angles and invariant masses fully characterize the orientation of the production and two-body decay chain and are defined in suitable rest frames of the V and H bosons, except in the VBF case, where only the H boson rest frame is used [26,28].

$$f_{a3} = \frac{|a_3|^2 \sigma_3}{|a_1|^2 \sigma_1 + |a_2|^2 \sigma_2 + |a_3|^2 \sigma_3 + \tilde{\sigma}_{\Lambda 1} / (\Lambda_1)^4 + \dots}, \quad \phi_{a3} = \arg\left(\frac{a_3}{a_1}\right),$$

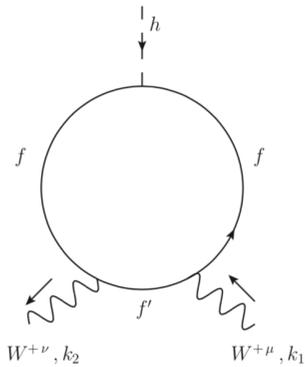
$$f_{a2} = \frac{|a_2|^2 \sigma_2}{|a_1|^2 \sigma_1 + |a_2|^2 \sigma_2 + |a_3|^2 \sigma_3 + \tilde{\sigma}_{\Lambda 1} / (\Lambda_1)^4 + \dots}, \quad \phi_{a2} = \arg\left(\frac{a_2}{a_1}\right),$$

$$f_{\Lambda 1} = \frac{\tilde{\sigma}_{\Lambda 1} / (\Lambda_1)^4}{|a_1|^2 \sigma_1 + |a_2|^2 \sigma_2 + |a_3|^2 \sigma_3 + \tilde{\sigma}_{\Lambda 1} / (\Lambda_1)^4 + \dots}, \quad \phi_{\Lambda 1},$$

$$f_{\Lambda 1}^{Z\gamma} = \frac{\tilde{\sigma}_{\Lambda 1}^{Z\gamma} / (\Lambda_1^{Z\gamma})^4}{|a_1|^2 \sigma_1 + \tilde{\sigma}_{\Lambda 1}^{Z\gamma} / (\Lambda_1^{Z\gamma})^4 + \dots}, \quad \phi_{\Lambda 1}^{Z\gamma},$$

CP-violation with not so much energy (hWW)

THE C2HDM



Starting with $f=t$ and $f'=b$

Is it worth it?

$$i\mathcal{M}_{tb}^{\text{C2HDM}} \sim \frac{ig^2 N_c c_t^o}{16\pi^2 v} \frac{m_t^2}{m_W^2} |V_{tb}|^2 \epsilon_{\mu\nu\rho\sigma} k_1^\rho k_2^\sigma \mathcal{I}_1 \left(\frac{m_t^2}{m_W^2}, \frac{m_b^2}{m_W^2} \right)$$

$$\mathcal{I}_1(x, y) \equiv \int_0^1 d\alpha \frac{\alpha^2}{\alpha x + (1-\alpha)y - \alpha(1-\alpha)}$$

And because $f=b$ and $f'=t$ can also contribute, the final result is

$$c_{\text{CPV}}^{\text{C2HDM}} = \frac{N_c g^2}{32\pi^2} |V_{tb}|^2 \left[\frac{c_t^o m_t^2}{m_W^2} \mathcal{I}_1 \left(\frac{m_t^2}{m_W^2}, \frac{m_b^2}{m_W^2} \right) + \frac{c_b^o m_b^2}{m_W^2} \mathcal{I}_1 \left(\frac{m_b^2}{m_W^2}, \frac{m_t^2}{m_W^2} \right) \right]$$

$$C_{\text{CPV}} = 2 \frac{a_3^{W^+W^-}}{a_1^{W^+W^-}}$$

$$c_{\text{CPV}}^{\text{C2HDM}} \simeq 6.6 \times 10^{-4} \sim \mathcal{O}(10^{-3})$$

USING ALL EXPERIMENTAL (AND THEORETICAL) BOUNDS