



13th IDPASC SCHOOL

PALERMO, 17-27 SEPTEMBER, 2024

STANDARD MODEL COSMOLOGY & DARK MATTER

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- By the end of the 20th century ...
**we have a comprehensive,
fundamental theory of all
observed forces of nature which
has been tested and might be
valid from the Planck length
scale [10^{-33} cm.] to the edge of
the universe [10^{+28} cm.]**

D. Gross 2007

In this last decade → the triumph of the STANDARD

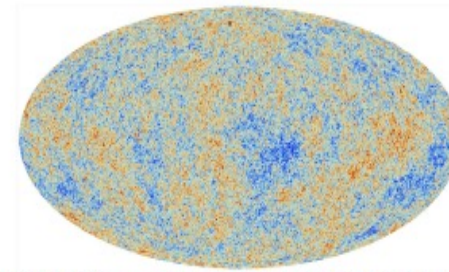
- PARTICLE STANDARD MODEL
- COSMOLOGY STANDARD MODEL

Three Generations of Matter (Fermions) spin 1/2

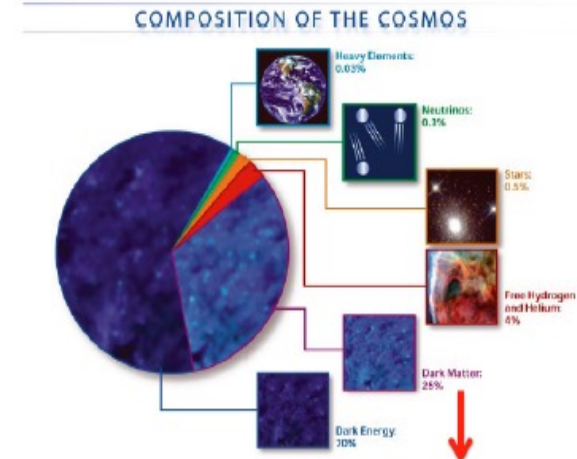
	I	II	III	
mass ~	2.4 MeV	1.27 GeV	173.2 GeV	
charge ~	2/3	2/3	2/3	
name ~	u up	c charm	t top	g gluon
	Left Right	Left Right	Left Right	
Quarks	d down	s strange	b bottom	γ photon
	Left Right	Left Right	Left Right	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z ⁰ weak force
	Left Right	Left Right	Left Right	
Leptons	e electron	μ muon	τ tau	W [±] weak force
	Left Right	Left Right	Left Right	

Bosons (Force s) spin 1

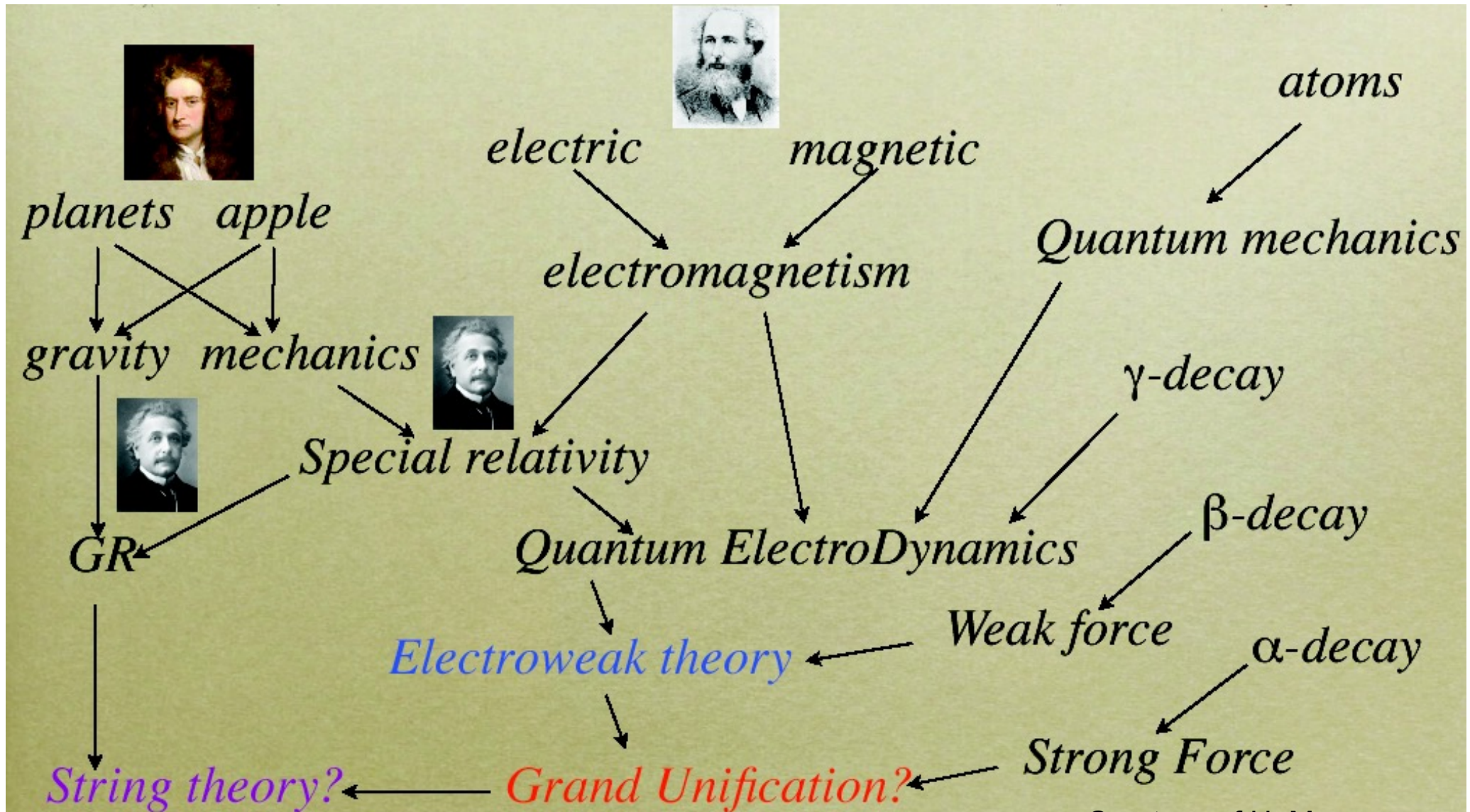
126 GeV	Higgs boson	spin 0
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Λ CDM + "SIMPLE" INFLATION

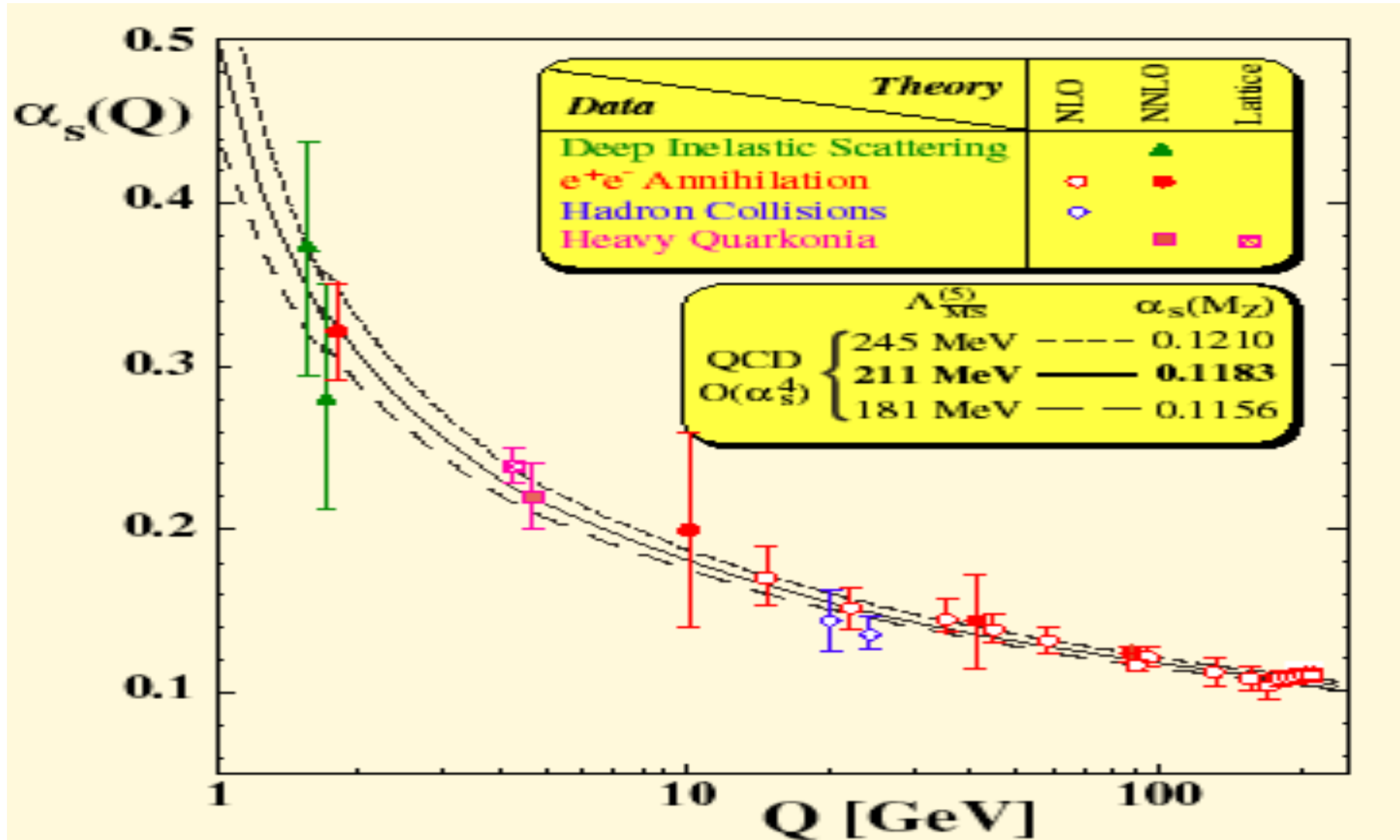


UNIFICATION of FUNDAMENTAL INTERACTIONS

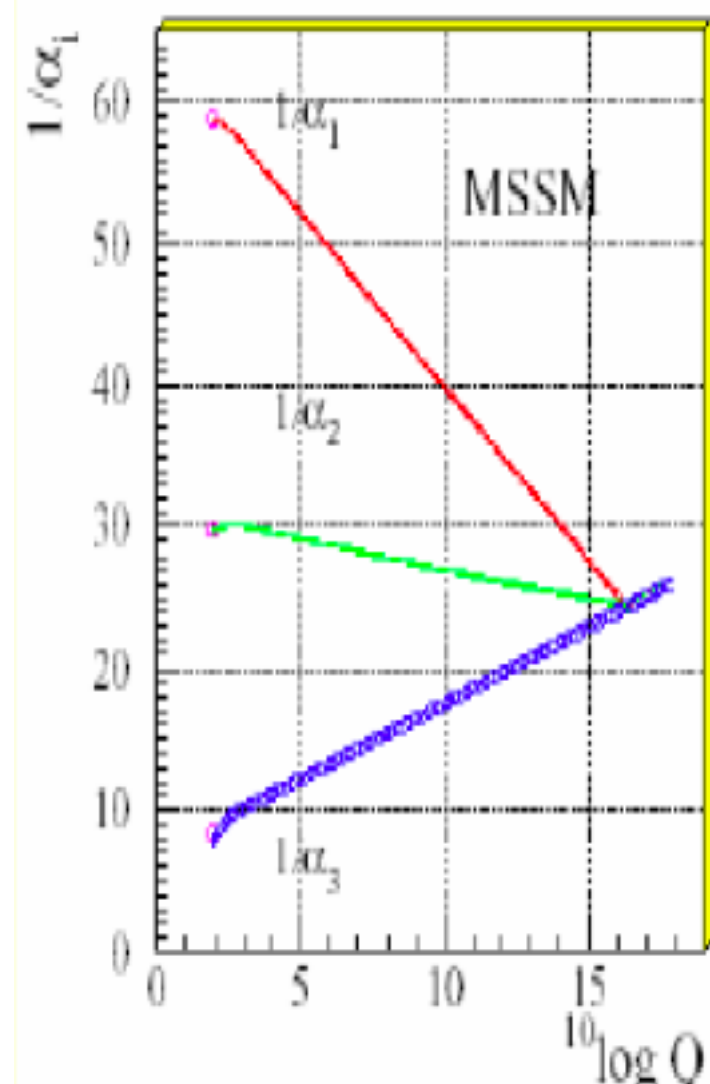
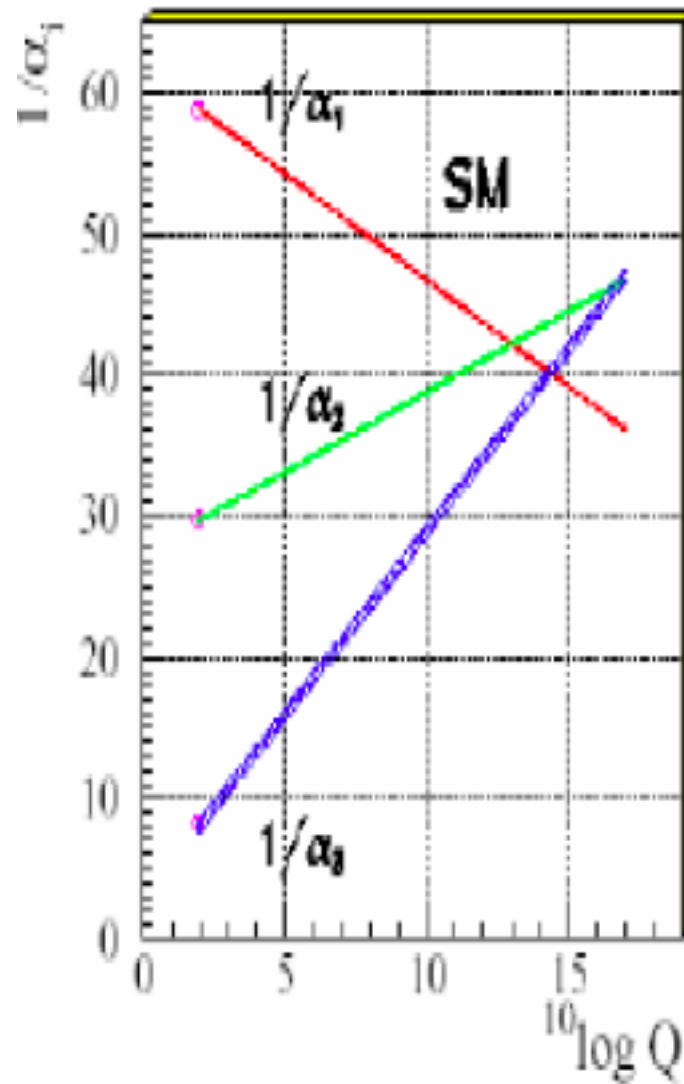


The **COUPLING CONSTANTS** of fundamental interactions are **NOT** constant, but

RUNNING COUPLING CONSTANTS



Only one fundamental interaction?



Symmetry Breaking/Restoration

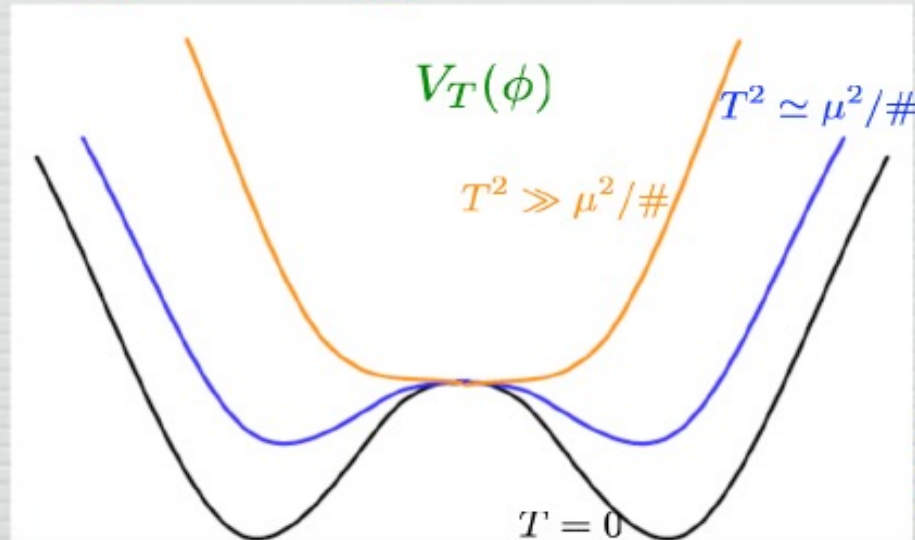
$$-i\lambda \int \frac{d^3p}{(2\pi)^3} \frac{1}{2E} f(p) \propto -i\lambda T^2$$

$$\text{p} \quad \text{p} \quad + \quad \text{p} \begin{array}{c} T \quad T \\ \diagdown \quad \diagup \end{array} \text{p} \quad + \quad \text{p} \begin{array}{c} T \quad T \quad T \quad T \\ \diagdown \quad \diagup \quad \diagdown \quad \diagup \end{array} \text{p} \quad + \dots$$

forward scattering

$$\frac{i}{p^2 - m^2} + \left(\frac{i}{p^2 - m^2} \right)^2 (-i\lambda T^2) + \left(\frac{i}{p^2 - m^2} \right)^3 (-i\lambda T^2)^2 + \dots = \frac{i}{p^2 - m^2 - \lambda T^2} \leftarrow \text{thermal mass}$$

$$V(\phi) = -\frac{1}{2}\mu^2\phi^2 + \frac{1}{4!}\lambda\phi^4 \xrightarrow{T \gg \mu} \frac{1}{2}(-\mu^2 + \#T^2)\phi^2 + \frac{1}{4!}\lambda\phi^4$$

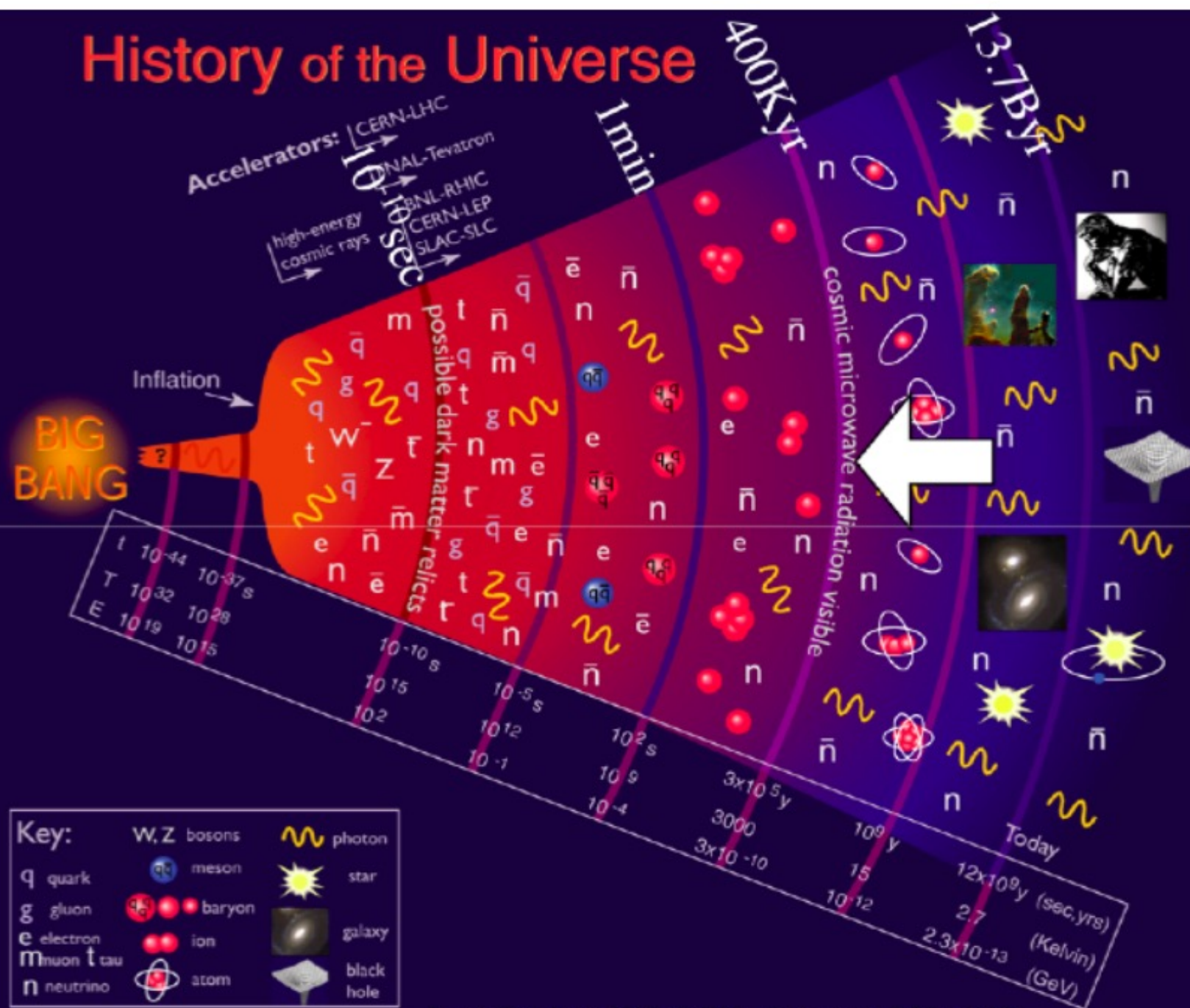


positive contributions from all relativistic particles coupled to ϕ

M. Pietroni, ISAPP – Padova, 2024

symmetry breaking phase transitions in the early Universe!

History of the Universe



HISTORY OF THE UNIVERSE

Big Bang

Inflation

$t = 10^{-36} s$
 $E = 10^{16} GeV$

Accelerators

LHC protons

RHIC & LHC heavy ions

Size of visible universe

Structure formation

Cosmic Microwave Background radiation is visible

Dark energy accelerated expansion

TODAY

opaque

transparent

Key

quark	neutrino	ion	star
gluon	bosons	atom	galaxy
electron	meson	photon	black hole
muon	baryon		
tau			

Timeline Labels:

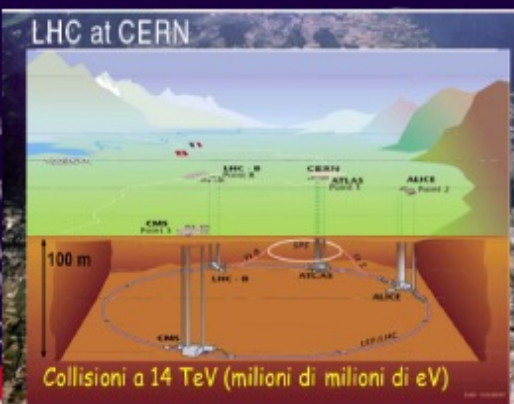
- $t = 10^{-10} s$, $E = 10^2 GeV$
- $t = 10^{-4} s$, $E = 10^{-1} GeV$
- $t = 10^2 s$, $E = 10^{-4} GeV$
- $t = 3 \times 10^5 y$, $E = 3 \times 10^{-10} GeV$
- $t = 10^9 y$, $E = 10^{-12} GeV$
- $t = 3.8 \times 10^9 y$, $E = 2.3 \times 10^{-13} GeV$

Particle Data Group, LBNL © 2014 Supported by DOE

Supported by DOE

History of the

Accelerators: CERN-LHC
high-energy cosmic rays



BIG BANG

Inflation

t 10^{-44} 10^{-37} s
 T 10^{32} 10^{28}
 E 10^{19} 10^{15}





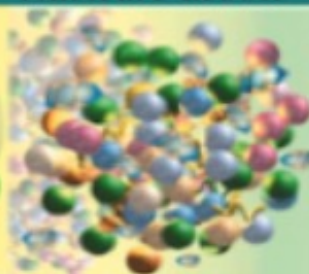

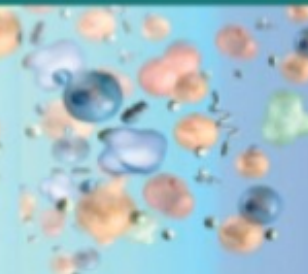

CMS

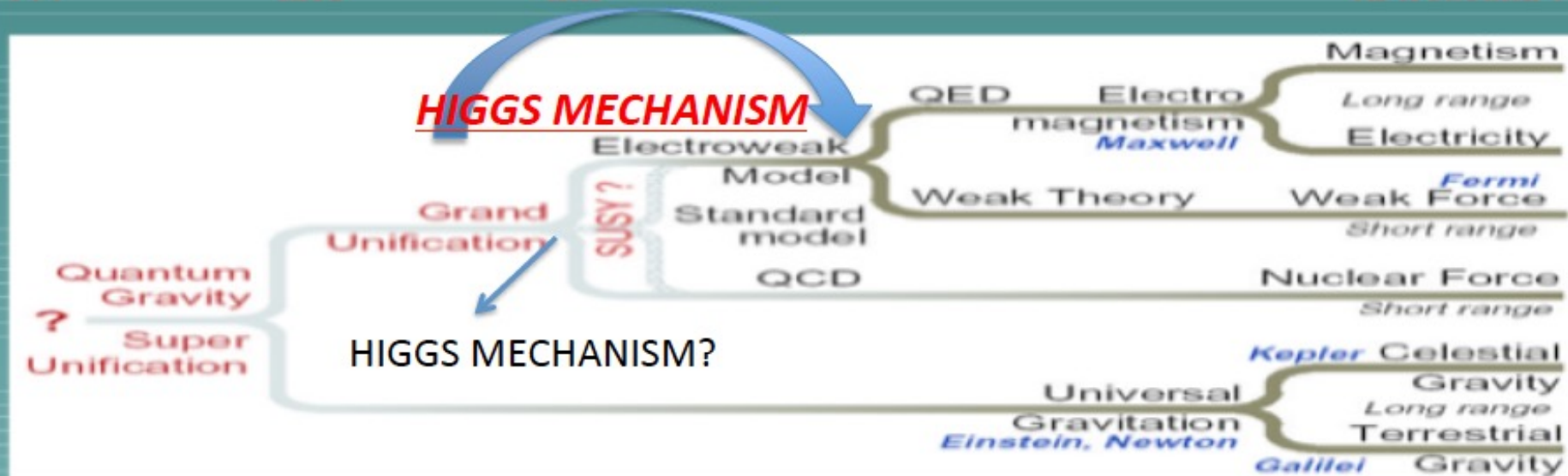
Key:

q quark	W, Z bosons	meson	photon	star
g gluon		baryon		galaxy
e electron		ion		black hole
μ muon		atom		
ν neutrino				

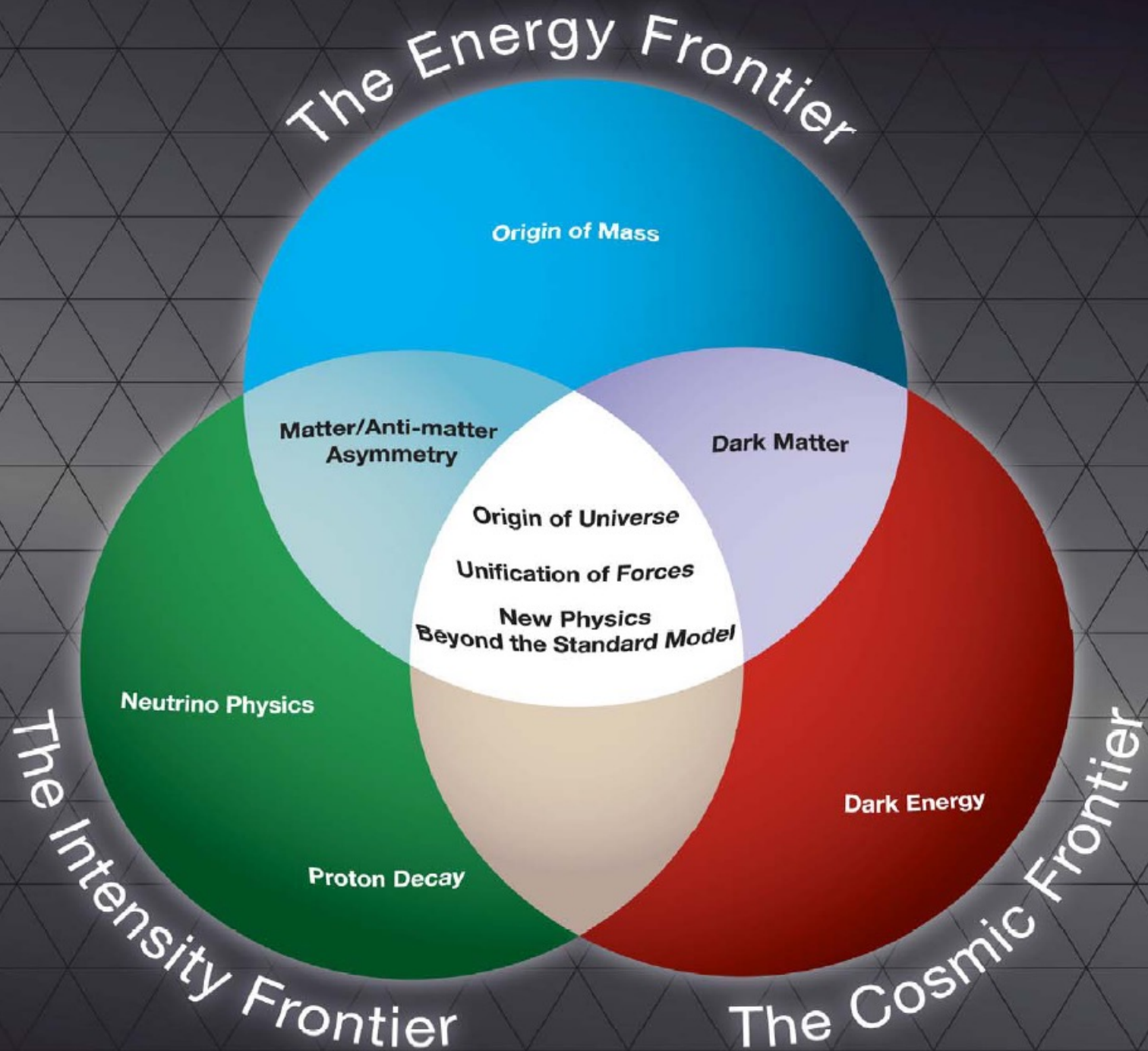
Today

12×10^9 y (sec.yrs)
2.7 (Kelvin)
 2.3×10^{-13} (GeV)

Big Bang	Quark-Gluon Plasma		Protoni e neutroni	Protoni e Nuclei leggeri	Atomi →Galassie →Molecole→DNA
<i>Gravità</i>	<i>Nucleare forte</i>	<i>Nucleare debole</i>			
					
10^{-43} sec	10^{-32} sec	10^{-10} sec	10^{-4} sec	100 sec	300KY → 15GY
10^{-35} m	10^{-32} m	10^{-18} m	10^{-16} m	10^{-15} m	10^{-10} m
10^{19} GeV	10^{16} GeV	10^2 GeV	1 GeV	1 MeV	10 eV
???	LHC	LEP			As tronomia→



Theories:		
STRINGS?	RELATIVISTIC/QUANTUM	CLASSICAL

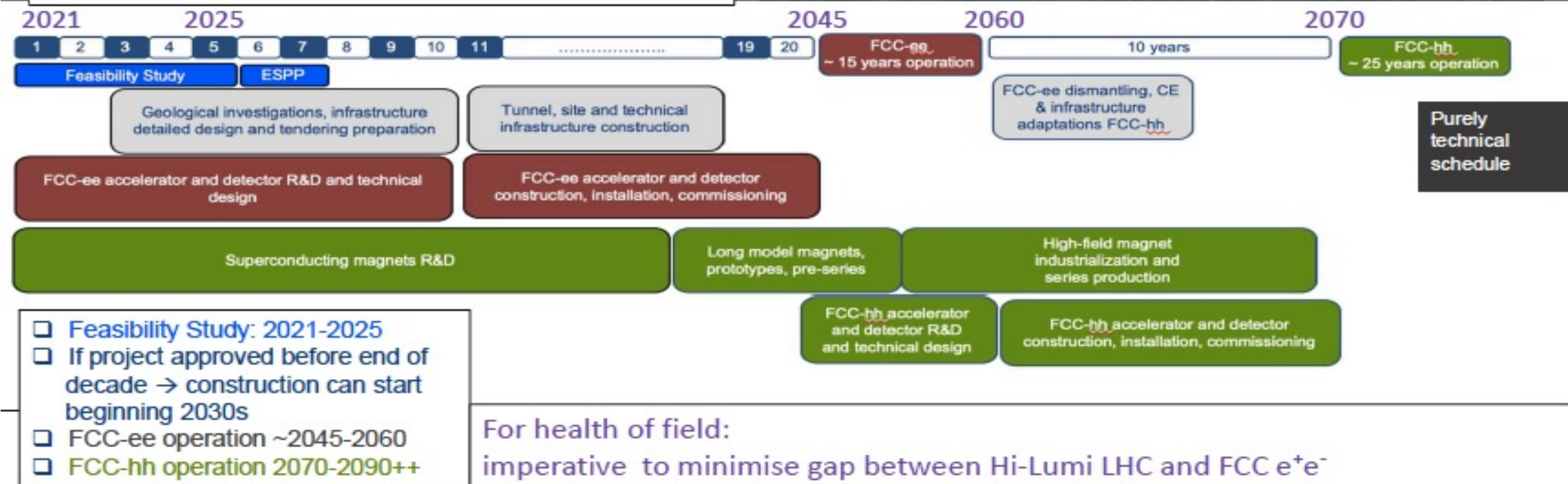
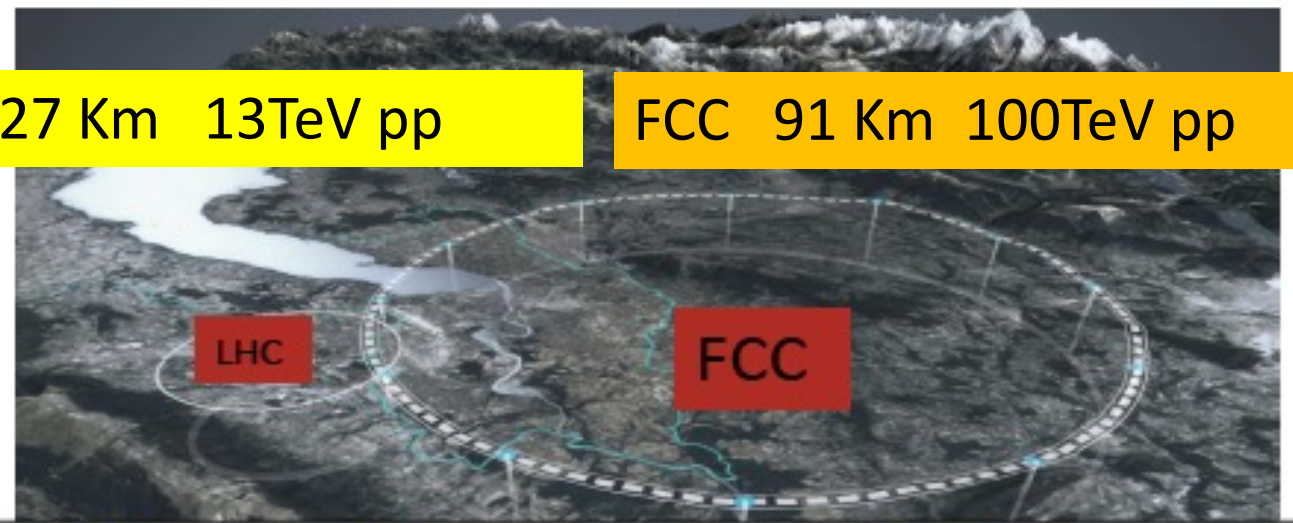


This leaves us with
the Future Circular Collider (e^+e^-
followed by pp) – at CERN
or maybe a similar facility in China

Reference <https://indico.cern.ch/event/1202105/timetable/>
I have drawn particularly on discussions with and slides
provided by Fabiola Gianotti and Gavin Salam

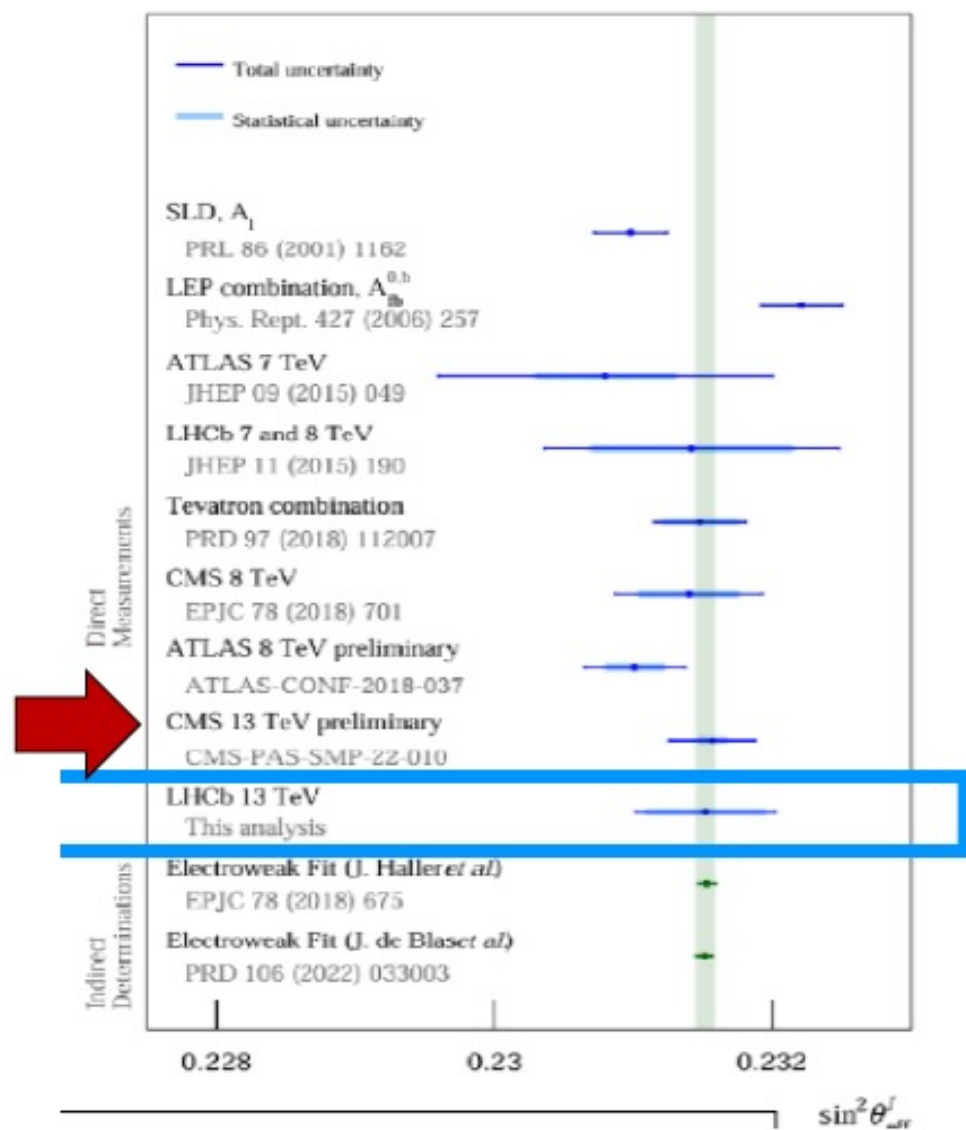
LHC 27 Km 13TeV pp

FCC 91 Km 100TeV pp

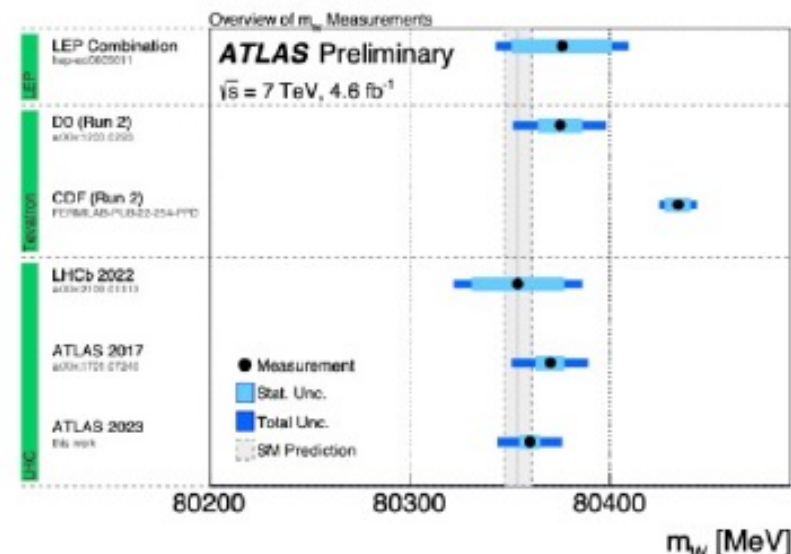


Testing the GAUGE part of the SM

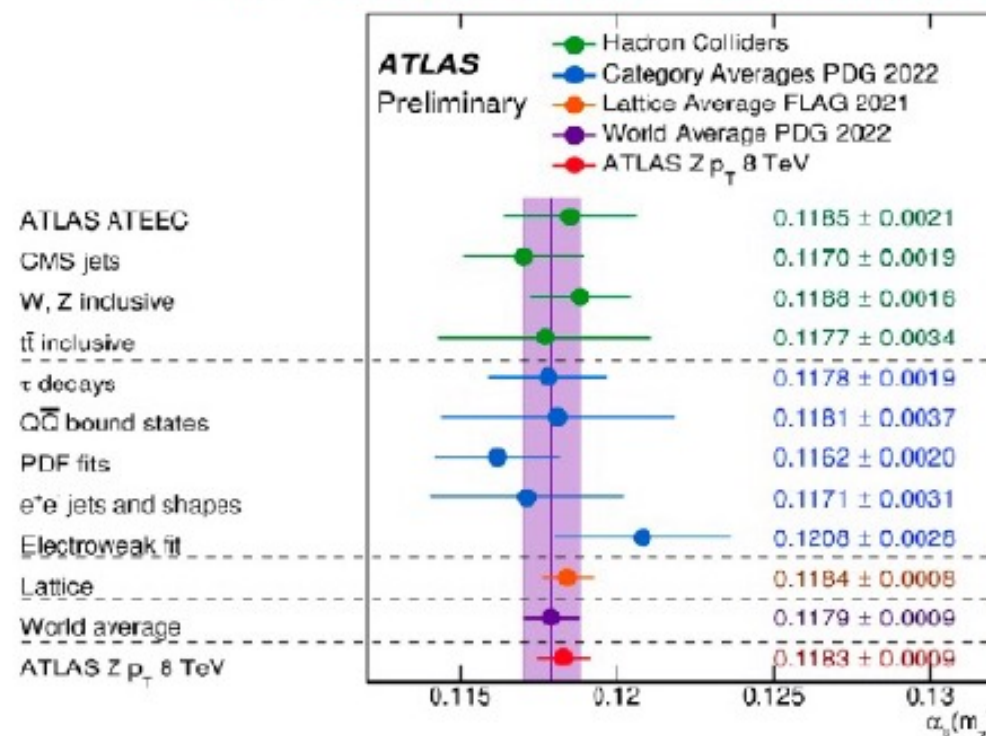
LHC: from **DISCOVERY** to **PRECISION** physics machine



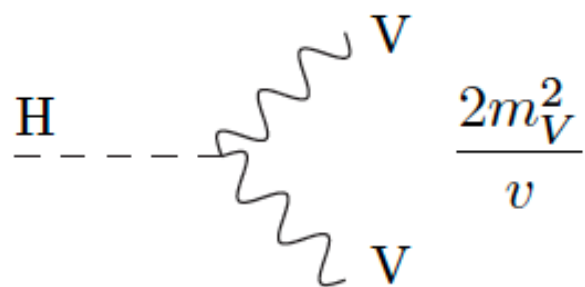
$$\sin^2 \theta_{eff}^l = 0.23152 \pm 0.00044 \pm 0.00005 \pm 0.00022$$



$$m_W = 80360 \pm 5_{(\text{stat.})} \pm 15_{(\text{syst.})} = 80360 \pm 16 \text{ MeV}$$



Testing the HIGGS part of the SM: present and future



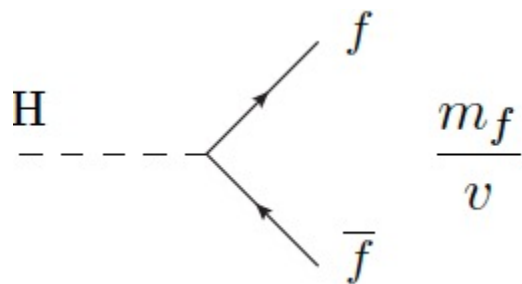
$$|\partial_\mu \phi|^2$$

$\kappa_{W,Z}$

Current
6%

HL-LHC
1.5%, 1.7 %

FCC (ee)
0.4%, 0.2 %



$$\bar{\Psi}_i y_{ij} \Psi_j \phi + h.c.$$

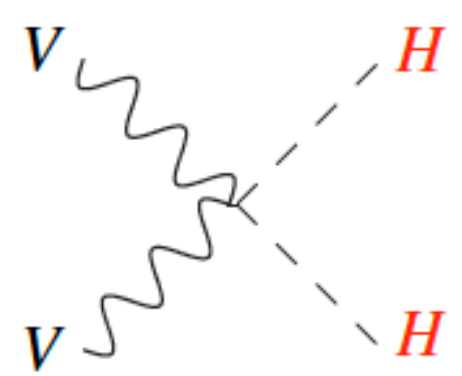
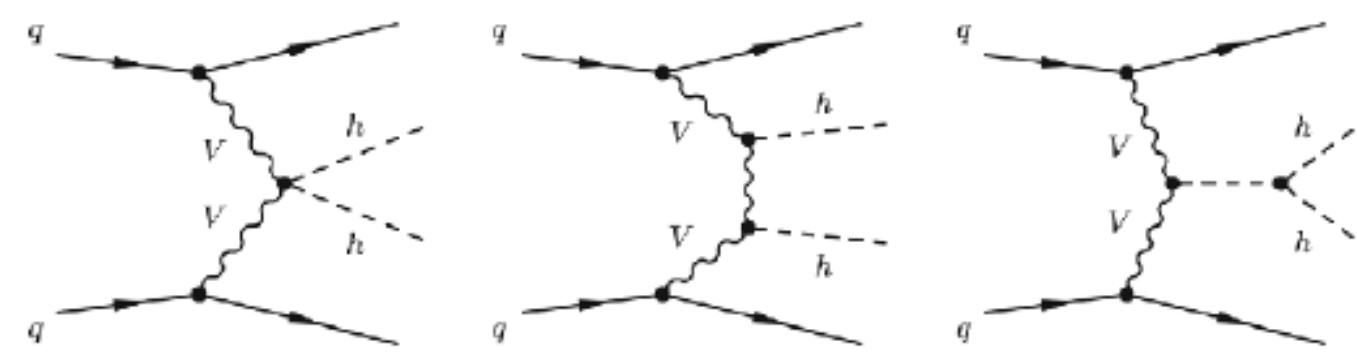
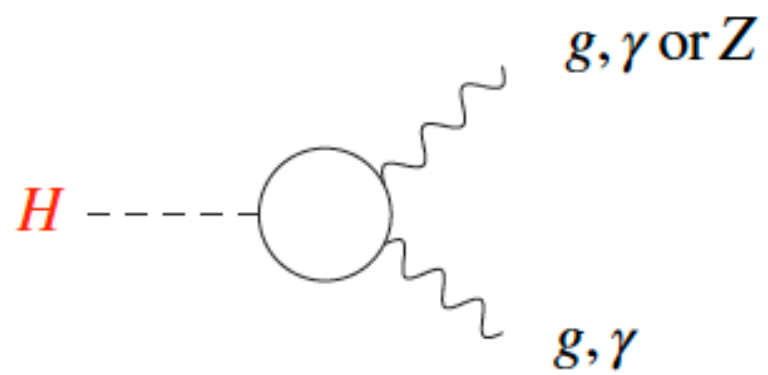
κ_t
 κ_b
 κ_τ
 κ_μ

Current
11%
11%
8%
20%

HL-LHC
3.4%
3.7%
1.9%
4.3%

FCC (ee)
-
0.7%
0.7%
8.9%*

FCC (hh)
1%

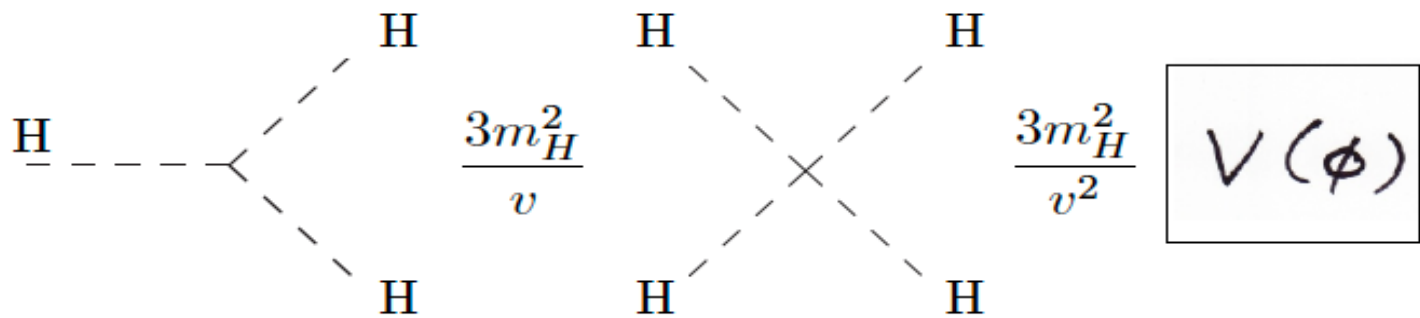


$$g_{HHVV} \sim \frac{2M_V^2}{v^2}$$

$$\kappa_{2V} \in [0.67, 1.38]$$

CMS result (ATLAS similar)

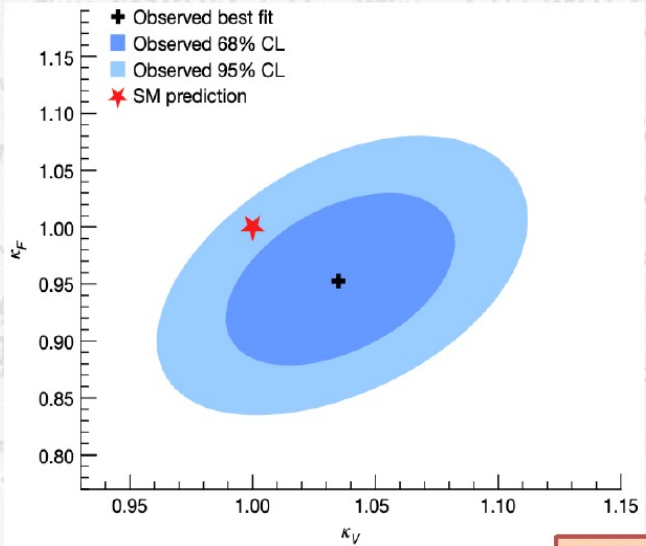
	Current	HL-LHC	FCC (ee)
κ_γ	6%	1.8%	3.9%
κ_g	7%	2.5%	1%
$\kappa_{Z\gamma}$	30%	9.8%	



Large trilinear deviations are possible while deviations of the Higgs to Z coupling remain small

Status of Higgs Couplings

What are experimental limits on modifications of couplings relative to Standard Model prediction?



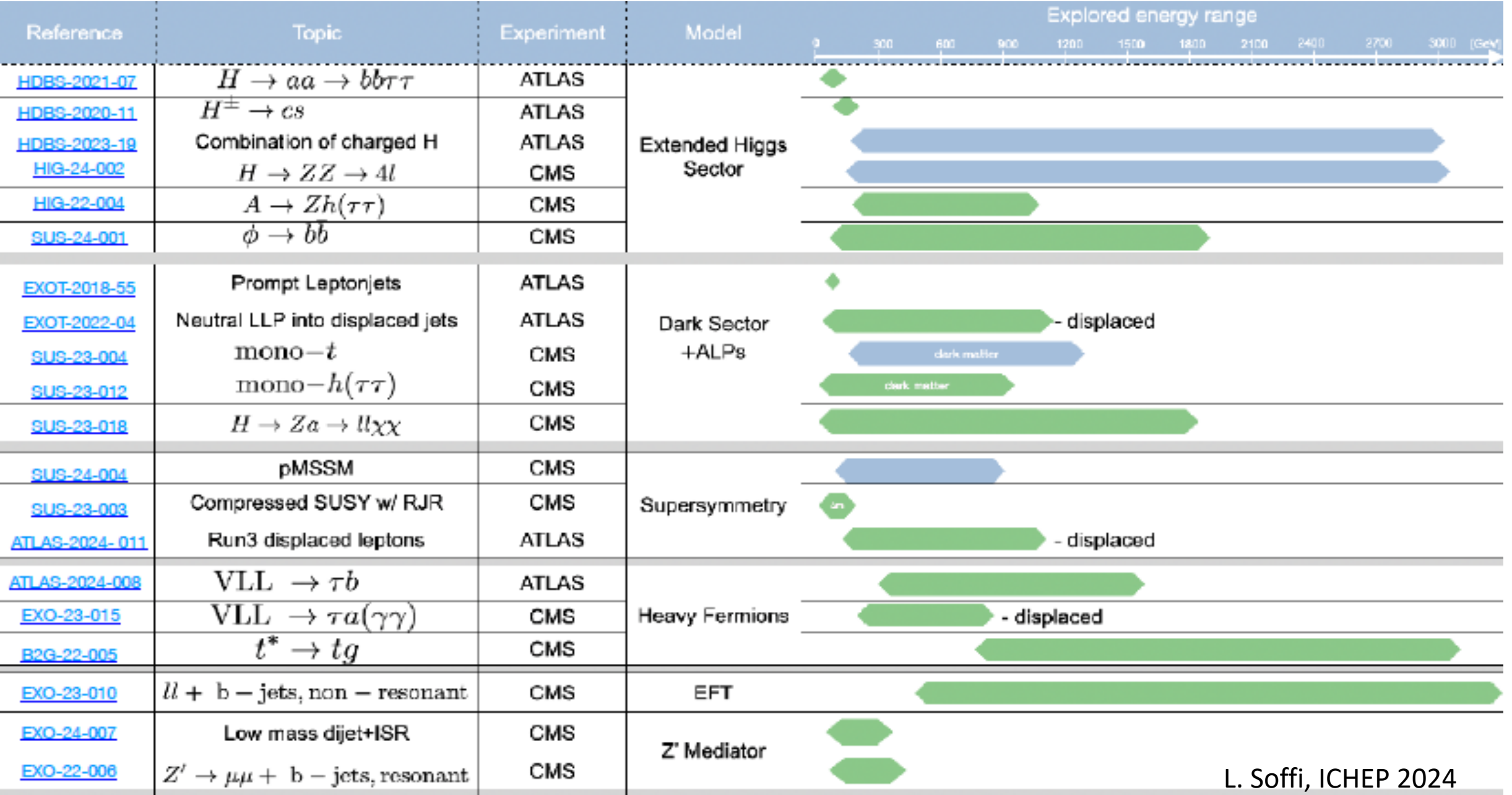
ATLAS, Nature, 2022

Higgs physics is still in its nascence. Pions were discovered in the early 1940's. Their fundamental origin, QCD, was developed theoretically in the early 1970's and only experimentally established in the late 1970's.

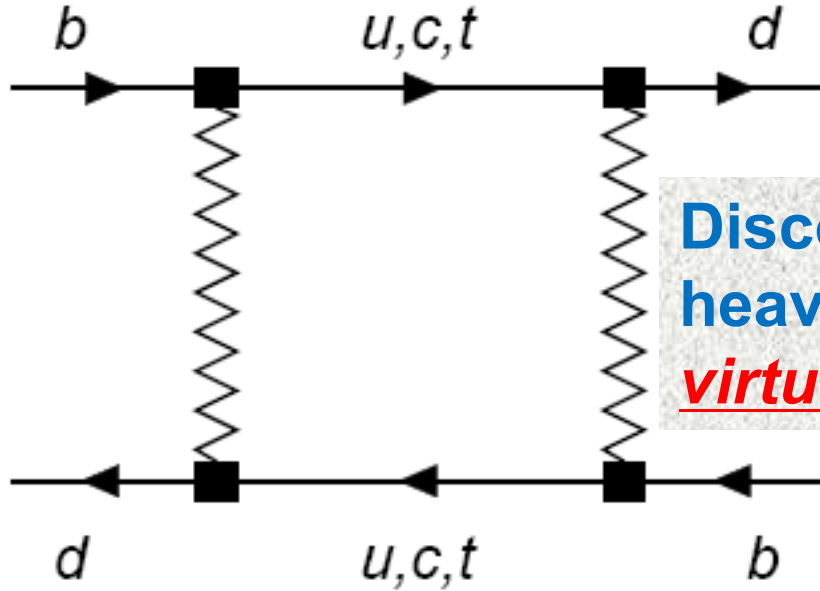
Twelve years since discovery of the Higgs boson.

As it stands, we don't know how it interacts with itself, or if it is composite; with far-reaching implications.

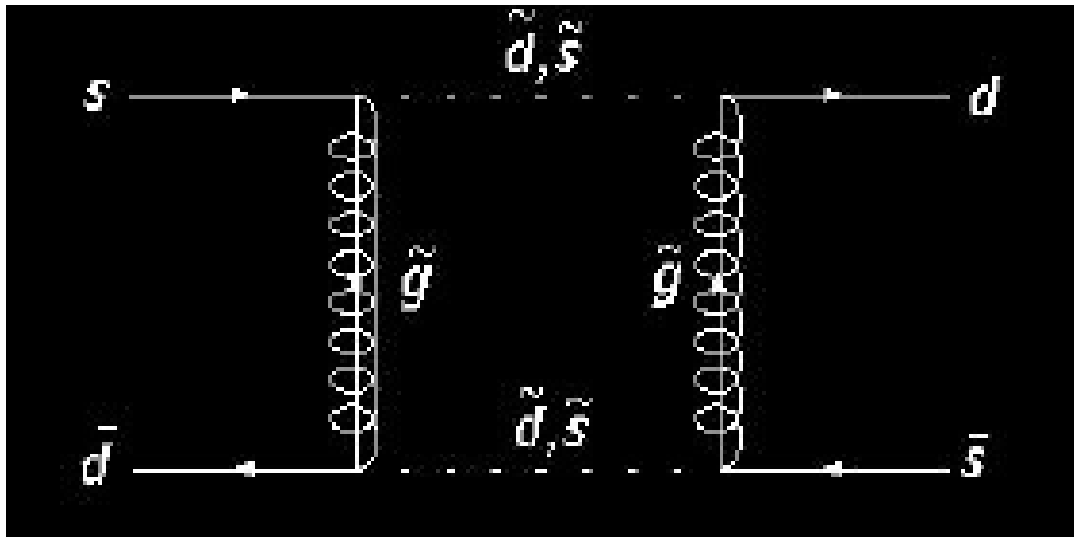
(Desperately) seeking SUSY particles or many other kinds of new particles beyond the SM particle spectrum



THE HIGH-INTENSITY ROAD



Discovering the presence of the heavy up-type quarks through their virtual effects on physical processes

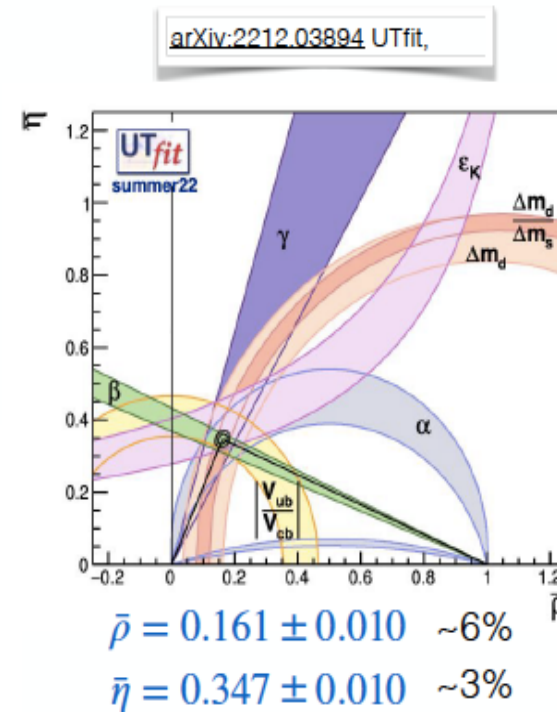
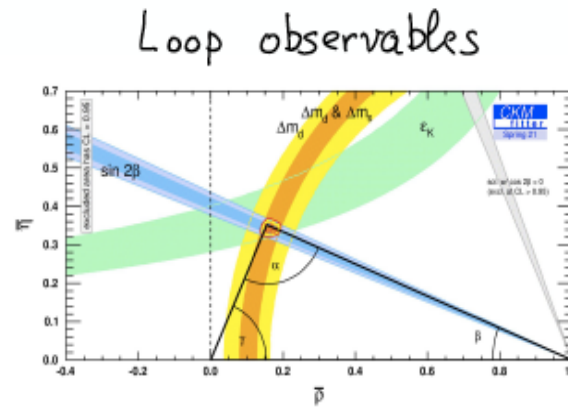
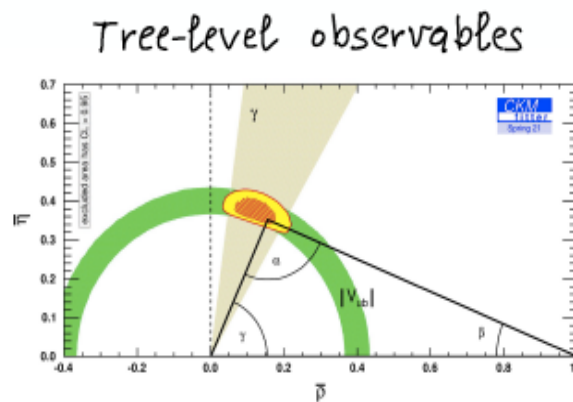


Looking for **NEW PARTICLES** through their virtual effects → **discrepancies** w.r.t. the **SM predictions**

Mixings and CP Violation in the SM quark sector (hadronic flavour physics): the SM brilliantly passes unscathed all the extremely demanding flavour tests!

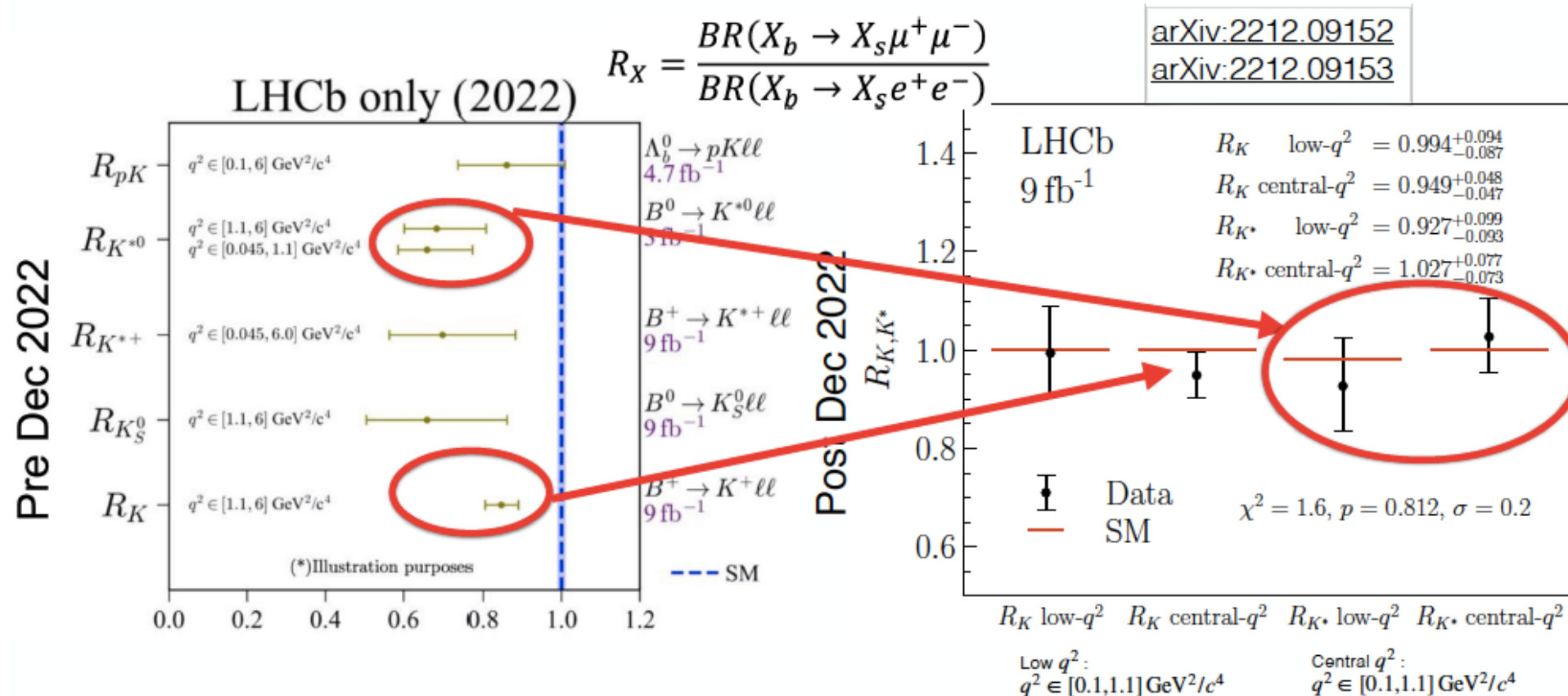
Consistency tests of the CKM matrix

- At the current level of precision ($\sim\%$), all measurements are consistent and intersect in the apex of the UT
- What is particularly noteworthy is the consistency of the tree-level determinations of CKM elements, with those obtained from meson-anti meson mixing



- New Physics effects (if there) are small!
- But... past examples show that it is unwise to think that few % is good enough

Tests of Lepton Flavour Universality



First Belle II RD* measurement!

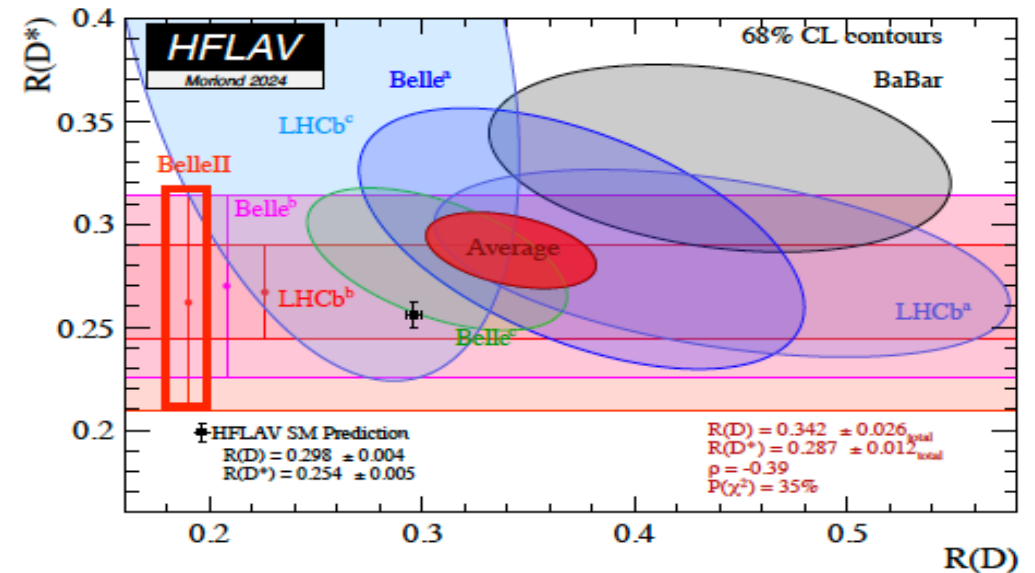
Both TH and EXP clean!

$$\mathcal{R}(D^{(*)}) = \frac{\mathcal{B}(B^0 \rightarrow D^{(*)} - \tau^+ \nu_\tau)}{\mathcal{B}(B^0 \rightarrow D^{(*)} - \mu^+ \nu_\mu)}$$

A remaining flavor puzzle in B physics?

A puzzling result
in tree-level $b \rightarrow c$ transitions

$\sim 3\sigma$ tension



$$R_D^* = 0.26 \pm 0.04^{+0.04}_{-0.03}$$

In conclusion, **NO** firm hints for any **discrepancy** between **SM** expectations and experimental results in the many and accurate tests in **FLAVOR PHYSICS** (FCNC, lepton flavor universality in K,D, B semileptonic decays, etc.)

Complementary (*not* ALTERNATIVE!) approach → **HIGH-PRECISION EXPS. in SMALL/MID-SCALE RIs**

Low-energy high-precision expts. can exploit :

- many recent *advances in experimental techniques and technologies* + (experimental as well as theoretical) *synergies* with adjacent areas of particle physics (atomic, molecular, optical, nuclear, particle physics)
- the relevant impact of *quantum mechanical virtual effects* on physical phenomena → access to the exploration of BSM new physics areas (large energy scales, very feebly coupled new particles, hidden sectors, etc.)
difficult to be probed by traditional HE particle physics

SYNERGY between small/mid-scale & large-scale experiments → casting a wider and tighter net for possible effects of BSM physics

Community Planning Exercise: **Snowmass 2021** Blum, Winter et al. arXiv:2209.08041v2

→ **2023 P5** (Particle Physics Project Prioritization Panel) **Report**

Electric and Magnetic Dipole Moments of a fermion

Interaction of a fermion f with the photon field A_μ , $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

$$\begin{aligned} -d_f \frac{\vec{S}}{|\vec{S}|} \cdot \vec{E} &\rightarrow d_f \frac{i}{2} (\bar{f} \sigma_{\mu\nu} \gamma_5 f) F^{\mu\nu} \\ -\mu_f \frac{\vec{S}}{|\vec{S}|} \cdot \vec{B} &\rightarrow e (\bar{f} \gamma_\mu f) A^\mu + a_f \frac{e}{4m_f} (\bar{f} \sigma_{\mu\nu} f) F^{\mu\nu} \end{aligned}$$

the usual **minimal coupling** of fermions with the photon give rise to a magnetic moment with **gyromagnetic factor** $g = 2$

the **dimension 5 operators** induce an **electric dipole moment** d_f and an **anomalous magnetic moment** a_f

$$\mu_f = g_f \frac{e}{2m_f} \quad , \quad (g_f - 2) = 2a_f$$

$$\vec{\mu}_\ell = \frac{e}{2m} \vec{\ell}$$

$$\vec{\mu}_s = g \frac{e}{2m} \vec{s}$$

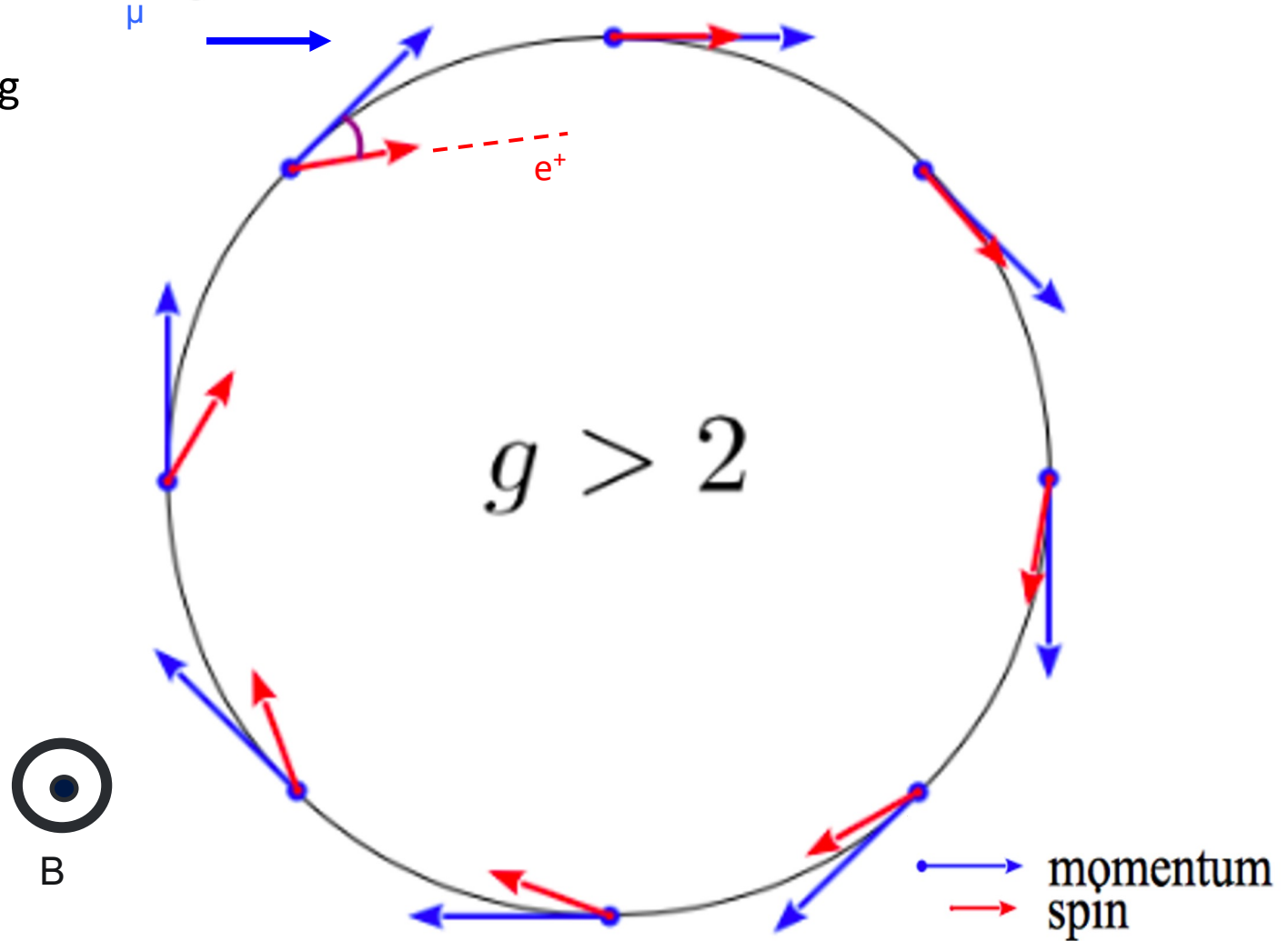
Put a beam of polarized muons into a storage ring

Both the muon spin and momentum precess

Because g is slightly greater than 2 the spin precesses faster than the momentum

$$a = (g-2)/2$$

$$a_\mu = \omega_a \frac{eB}{mc}$$

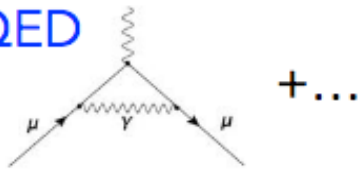


The 4 classes of SM contributions to the muon g-2

uncertainty largely dominated by the **hadronic contributions in Vacuum Polarization (HVP)**

$$a_\mu(\text{SM}) = a_\mu(\text{QED}) + a_\mu(\text{Weak}) + a_\mu(\text{Hadronic})$$

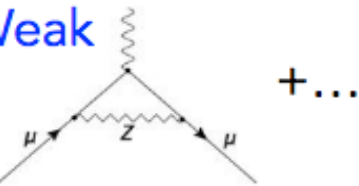
QED



$$116\,584\,718.9(1) \times 10^{-11}$$

0.001 ppm

Weak

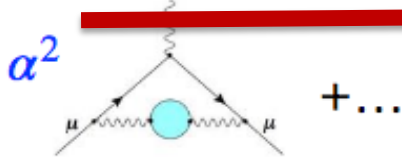


$$153.6(1.0) \times 10^{-11}$$

0.01 ppm

Hadronic...

...Vacuum Polarization (HVP)

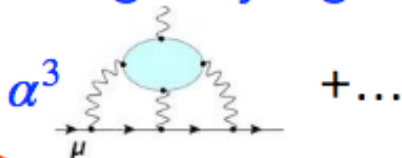


$$6845(40) \times 10^{-11}$$

[0.6%]

0.37 ppm

...Light-by-Light (HLbL)

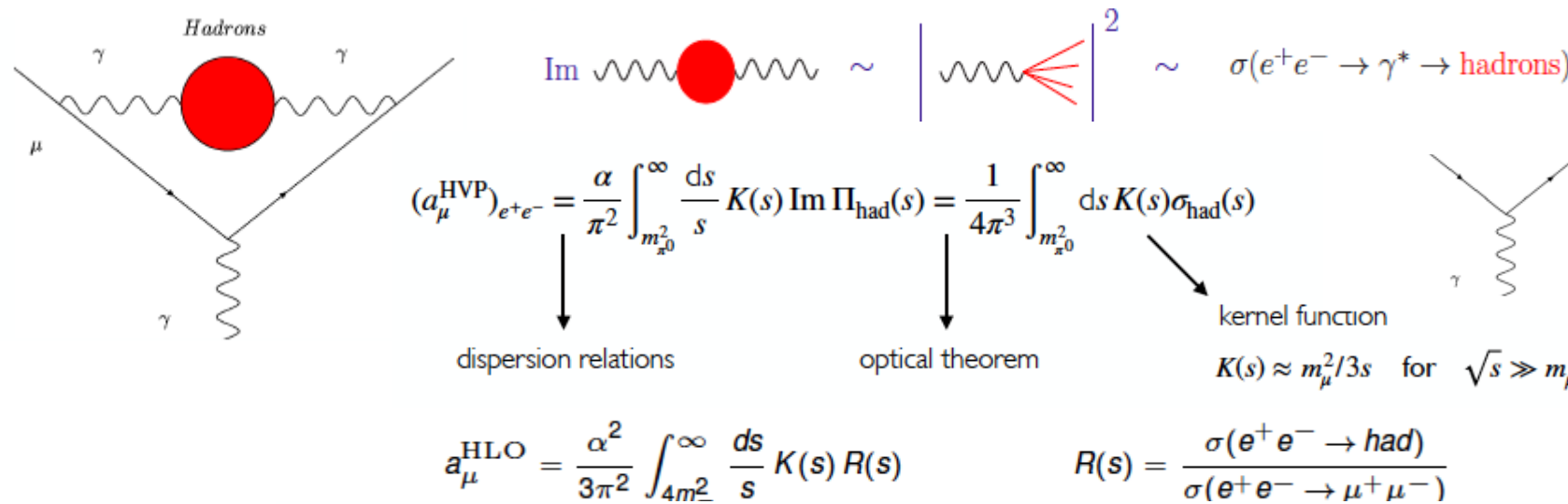


$$92(18) \times 10^{-11}$$

[20%]

0.15 ppm

Hadronic Vacuum Polarization (HVP) contribution



$$a_\mu^{\text{HLO}} = 6895 (33) \times 10^{-11}$$

F. Jegerlehner, arXiv:1711.06089

$$= 6939 (40) \times 10^{-11}$$

Davier, Hoecker, Malaescu, Zhang, arXiv:1908.00921

$$= 6928 (24) \times 10^{-11}$$

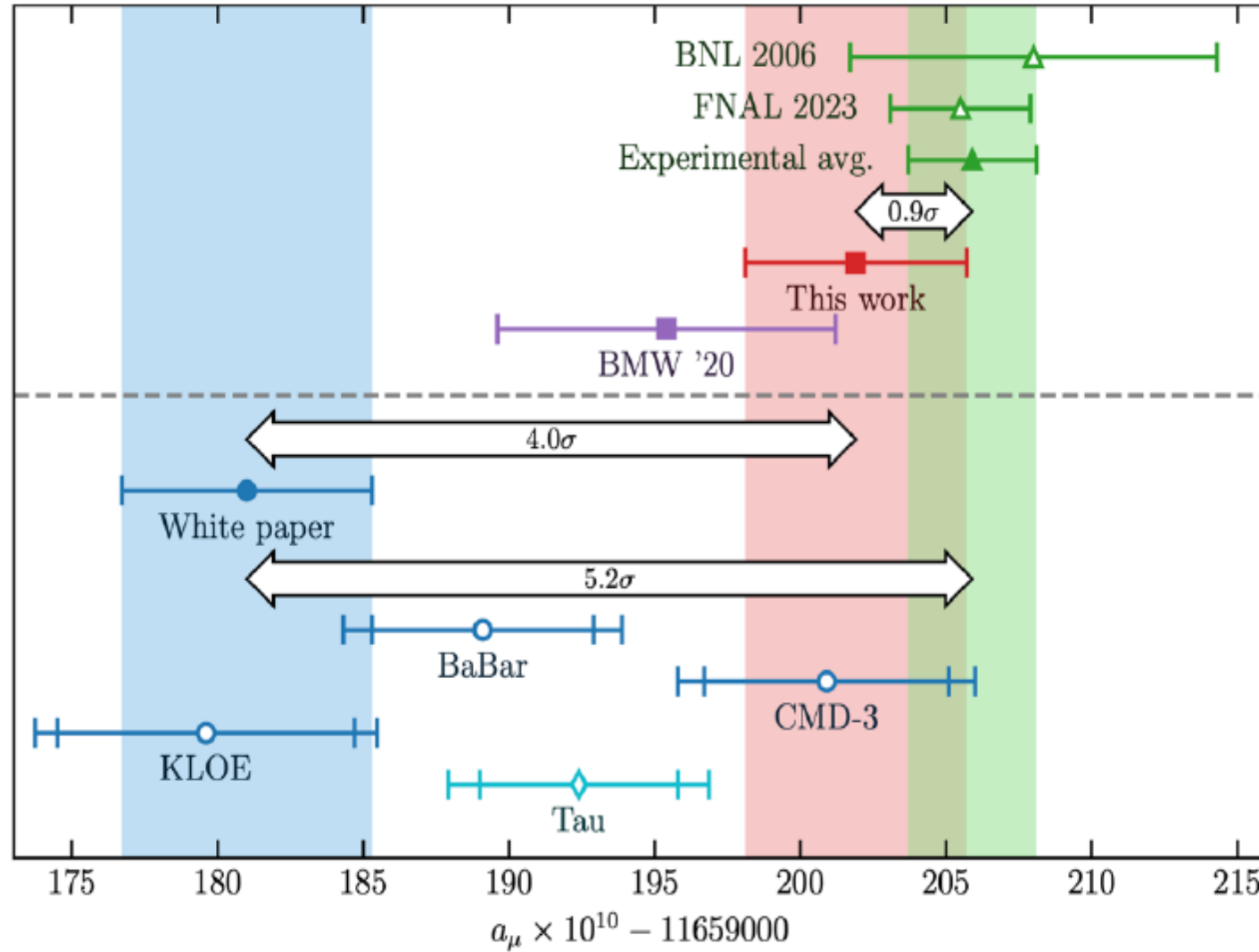
Keshavarzi, Nomura, Teubner, arXiv:1911.00367

$$= 6931 (40) \times 10^{-11} (0.6\%)$$

WP20 value

WP20 = White Paper of the Muon g-2 Theory Initiative: arXiv:2006.04822

Several important news from the front of $(g_\mu - 2)$ predictions from BaBar and Lattice in conjunction with data!



Scanning $e^+e^- \rightarrow \pi^+ \pi^-$ – ECM = 0.32-2 GeV

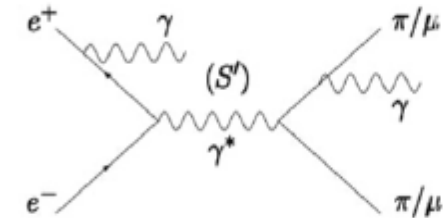
CMD-3 at VEPP-2000 e^+e^- collider

Better detector performance Larger statistics (x30 CMD-2)

New BMW result including finer lattice and long distance effects from e^+e^- data!

New BaBar studies of higher order radiation and impact on the vacuum polarisation predictions of $(g-2)$!

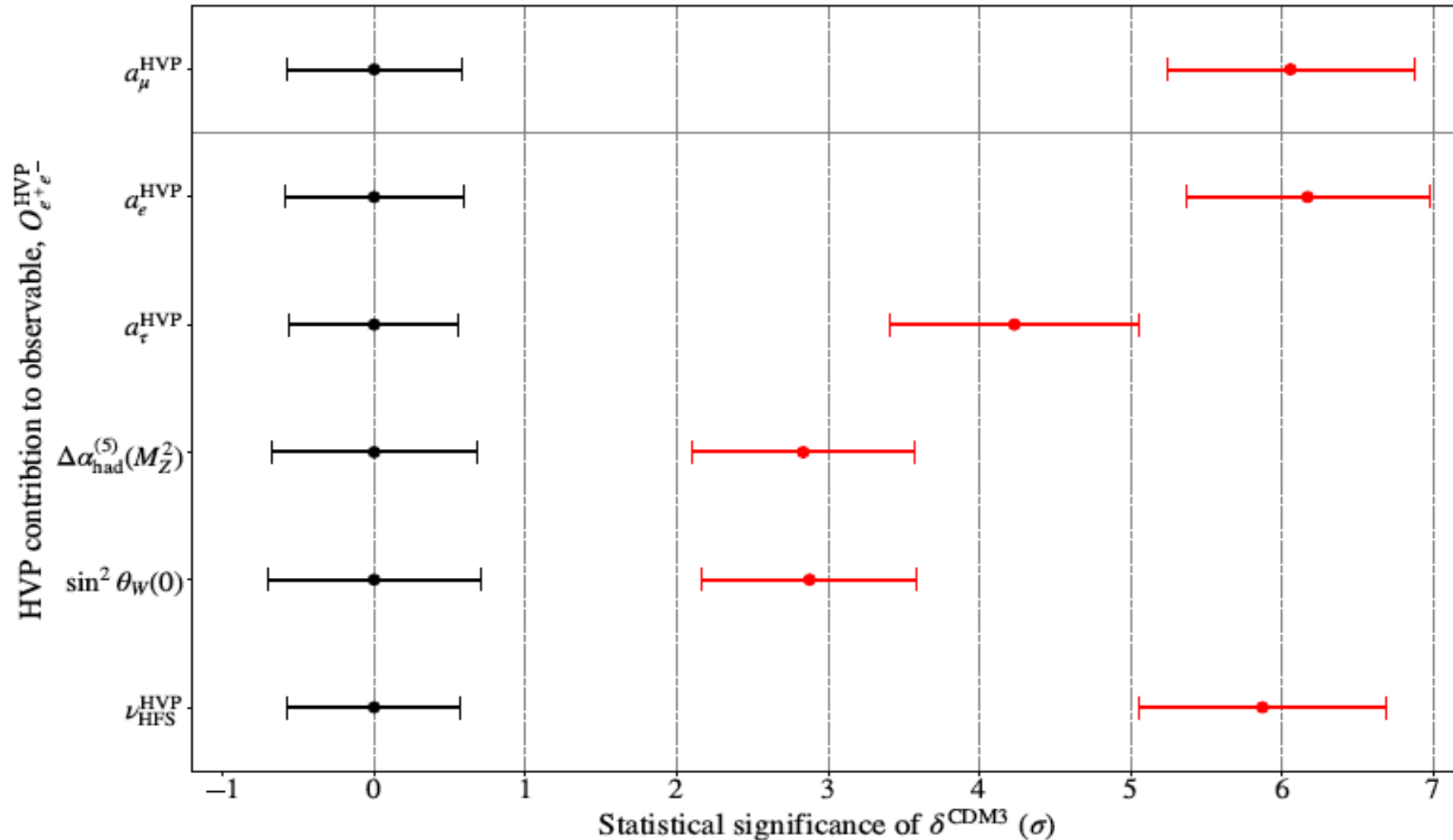
NNLO Radiative corrections need to be better understood and accounted in analyses!



Model independent tests of the HVP contribution to the muon g-2

New Observables providing independent tests of the current tensions observed in the muon g-2:

- i) the **electron g-2**;
- ii) the **tau g-2**;
- iii) the **running of the QED coupling constant α** ;
- iv) the low-energy weak mixing angle **$\sin^2\theta_W(0)$** ;
- v) the **Muonium hyperfine splitting (HFS)**



L. Di Luzio, A. Keshavarzi, A.M.,
P. Paradisi arXiv:2408.01123

Measurement of the Electron Magnetic Moment

X. Fan,^{1,2,*} T. G. Myers,² B. A. D. Sukra,² and G. Gabrielse^{2,†}

¹*Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA*

²*Center for Fundamental Physics, Department of Physics and Astronomy,
Northwestern University, Evanston, Illinois 60208, USA*

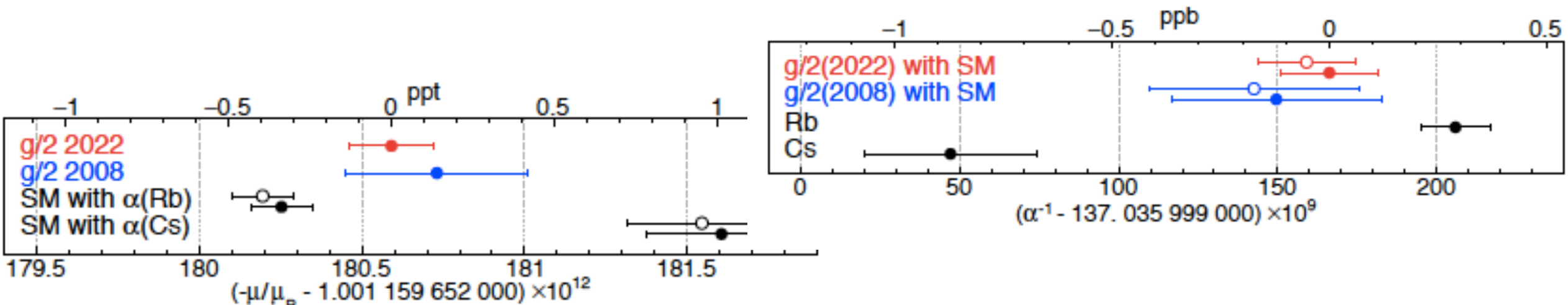
(Dated: December 8, 2022)

The electron magnetic moment, $-\mu/\mu_B = g/2 = 1.001\,159\,652\,180\,59(13)$ [0.13 ppt], is determined 2.2 times more accurately than the value that stood for 14 years. The most precisely determined property of an elementary particle tests the most precise prediction of the Standard Model (SM) to 1 part in 10^{12} . The test would improve an order of magnitude if the uncertainty from discrepant measurements of the fine structure constant α is eliminated since the SM prediction is a function of α . The new measurement and SM theory together predict $\alpha^{-1} = 137.035\,999\,166(15)$ [0.11 ppb] with an uncertainty ten times smaller than the current disagreement between measured α values.

$$a_e^{\text{EXP}} = 0.00115965218059(13)$$

$$\delta a_e^{\text{EXP}} = 1.3 \times 10^{-13}$$

In **2008** Gabrielse et al. had obtained $\delta a_e^{\text{EXP}} = 2.8 \times 10^{-13}$



ν peculiarity: in the SM
ONLY LEFT-HANDED ν



- i) **V–A** structure of the charged weak currents (i.e. the W boson couples only to the **LEFT-HANDED** fermions) ;
- ii) ν doesn't couple to photons (no neutral currents observed at the time the SM was proposed);
- iii) In any case, even **today no hint** of the presence of a **right-handed neutrino**
- iv) Before observing neutrino oscillations, this (very light) particle was widely thought to be **massless** → **no need for the presence of its right-handed component**

MICRO-COSMOS

Three Generations of Matter (Fermions) spin 1/2

	I	II	III	
mass =	2.4 MeV	1.27 GeV	173.2 GeV	
charge =	2/3	2/3	2/3	0
name =	u up	c charm	t top	g gluon
	Left Right	Left Right	Left Right	0
	d down	s strange	b bottom	γ photon
Quarks	Left Right	Left Right	Left Right	0
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	91.2 GeV Z ⁰ weak force
	e electron	μ muon	τ tau	126 GeV H Higgs boson spin 0
Leptons	Left Right	Left Right	Left Right	80.4 GeV W [±] weak force

Bosons (Force) spin 1

Three Generations of Matter (Fermions) spin 1/2

	I	II	III	
mass	2.4 MeV	1.27 GeV	173.2 GeV	0
charge	2/3	2/3	2/3	0
name	u up	c charm	t top	g gluon
	Left Right	Left Right	Left Right	0
Quarks	d down	s strange	b bottom	γ photon
	Left Right	Left Right	Left Right	0
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	91.2 GeV Z weak force
	Left Right	Left Right	Left Right	125 GeV H Higgs boson
Leptons	e electron	μ muon	τ tau	spin 0
	Left Right	Left Right	Left Right	
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV W weak force
	Left Right	Left Right	Left Right	

Bosons (Forces) spin 1

- **No DIRAC mass**

$$\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L$$

Need of a new particle:
the RH neutrino ν_R

NO MAJORANA mass

$$\nu_R^T \nu_R \text{ Or } \boxed{\nu_L^T \nu_L}$$

No $SU(2)_L$ and
 $U(1)_Y$ invariant

To obtain a neutrino mass in the renormalizable SM
--> need of new particles (ν_R , Δ scalar triplet of $SU(2)_L$)

$U(1)_B$: $B(q) = 1/3$; $B(\text{all other SM fields}) = 0$

$U(1)_L$: $L(\text{leptons}) = 1$; $L(\text{all other SM fields}) = 0$

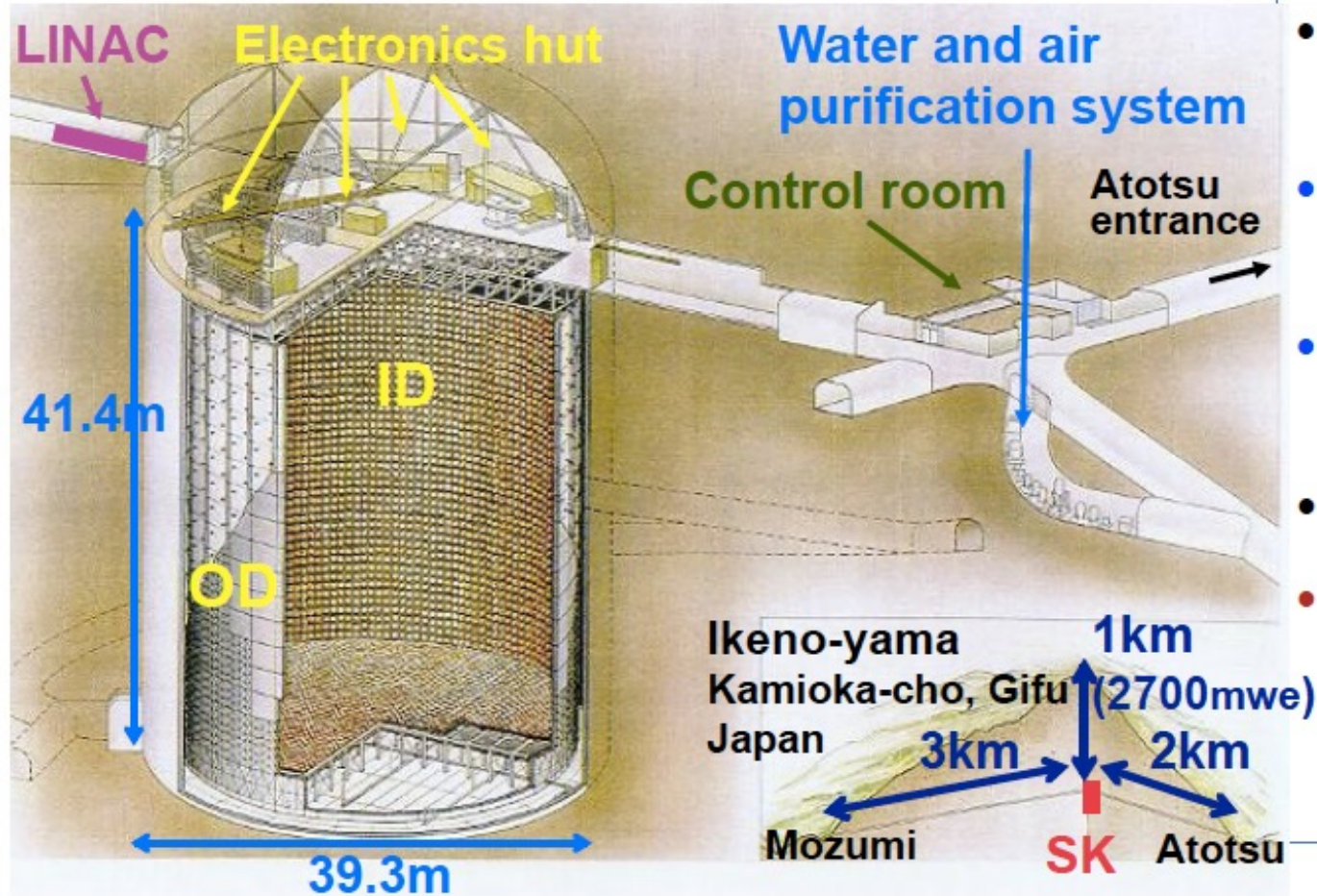
LEPTON NUMBER and
LEPTON FLAVOR NUMBERS
CONSERVATION in the **SM**

- *BARYON (B) AND LEPTON (L) numbers are **AUTOMATICALLY** conserved in the SM* (at all orders of the perturbation expansion), i.e. with the fields of the SM particle spectrum it is **not** possible to write any **operator of dim. ≤ 4** which respects the SM gauge symmetry and violates B or L

Super-Kamiokande detector



M. Nakahata, Erice School, 2023



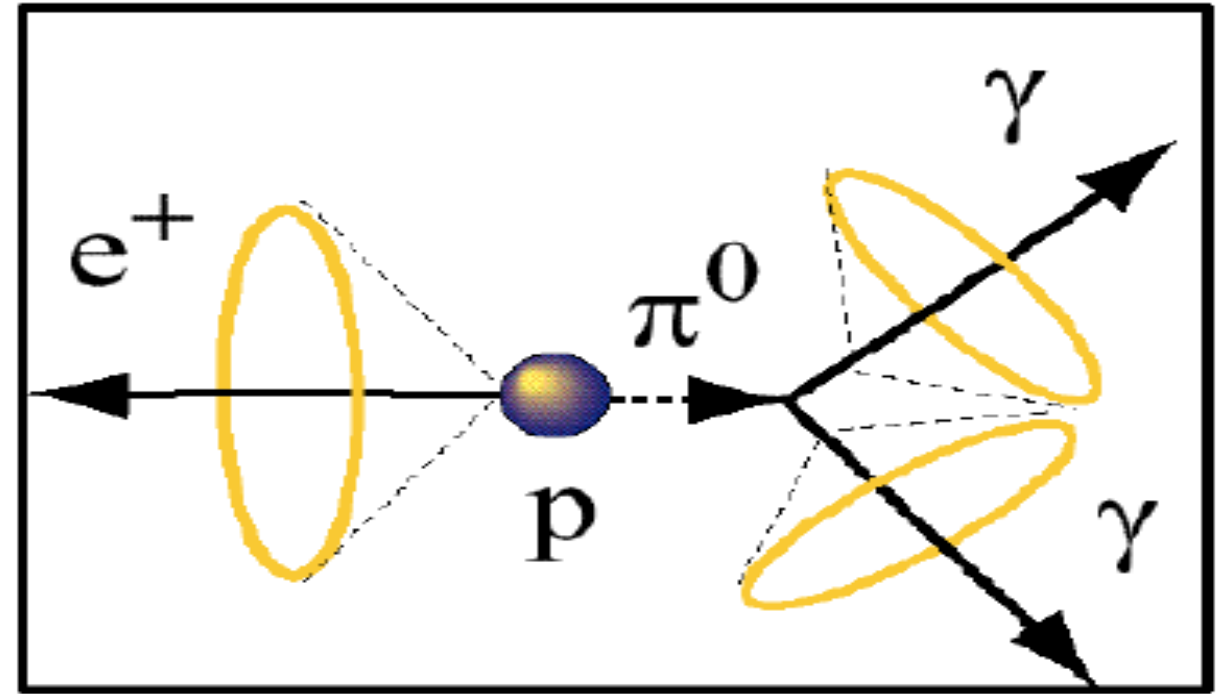
- 50 kton water Cherenkov
- 32kt photo-sensitive volume
- 22.5kt fid. vol. (2m from ID wall)
- SK-I: April 1996~
- **SK-VII is running**

Inner Detector (ID) PMT: ~11,000 20-inch PMTs
Outer Detector (OD) PMT: 1885 8-inch PMTs

MATTER STABILITY

are protons FOREVER ?

Search for $p \rightarrow e^+ \pi^0$



- Positron and π^0 run back-to-back
 - Momentum 459 MeV/c
- All particles in the final state are visible with Super-K
 - Able to reconstruct p mass and momentum

Results on $p \rightarrow e^+ \pi^0$ and $p \rightarrow \mu^+ \pi^0$

	Eff(%)	Exp. BG (event)	Observed (event)
$p \rightarrow e^+ \pi^0$			
Lower	18.1	0.02	0
Upper	19.5	0.58	0
$p \rightarrow \mu^+ \pi^0$			
Lower	17.3	0.05	0
Upper	17.2	0.89	1

Lifetime limit (90% CL, 450 kton·yrs data)

$p \rightarrow e^+ \pi^0$: $> 2.4 \times 10^{34}$ years

$p \rightarrow \mu^+ \pi^0$: $> 1.6 \times 10^{34}$ years

Baryon number violation in the
 SM as an **Effective low-energy
 remnant** of a more fundamental
 theory at a **higher mass scale M**


$$qqql \rightarrow \text{es. } U_R U_R D_R E_R \rightarrow \quad p \rightarrow e^+ \pi^0$$

B – L conserved

$$qqql \quad \text{dim 6} \quad M^{-2} \quad qqql$$

$$\tau_p > 10^{34} \text{ years} \rightarrow M > 10^{15} \text{ GeV}$$

NEUTRINO MASSES and a “NON-TRIVIAL” NEW PHYSICS

- If no RH neutrino \rightarrow enlargement of the SM scalar sector (Higgs triplet) + introduction of a NEW ENERGY SCALE (some new mass parameter of the enlarged Higgs potential must give rise to a VEV of the higgs triplet several orders of magnitude smaller than the VEV responsible for the electroweak symmetry breaking
- If RH neutrinos are introduced 
- A pure neutrino DIRAC mass (add to the gauge symmetry also a global $U(1)$ symmetry, L , and then introduce Yukawa couplings 5-6 orders of magnitude smaller than the electron Yukawa coupling
- B Dirac mass + Majorana mass of the RH neutrino (new parameter with dimension of a mass in the Lagrangian; most natural choice $M \gg$ electroweak scale since neutrino masses come from LLHH/M effective terms

Choice A) \rightarrow in this case $U(1)_L$ is no longer an AUTOMATIC SYMMETRY of the theory, rather it is a NEW GLOBAL SYMMETRY one imposes by hand IN ADDITION to the SM gauge symmetry.

THE FATE OF LEPTON NUMBER

L VIOLATED

ν Majorana ferm.

SMALLNESS of m_ν

PRESENCE OF A NEW PHYSICAL MASS SCALE

L CONSERVED

ν Dirac ferm.
(dull option)

$$h \bar{\nu}_L H \nu_R \longrightarrow m_\nu = h \langle H \rangle \quad M_\nu < 5 \text{ eV} \longrightarrow h < 10^{-11}$$

EXTRA-DIM. ν_R in the bulk: small overlap?

NEW HIGH SCALE

NEW LOW SCALE

SEE - SAW MECHAN.

Minkowski; Gell-Mann,
Ramond, Slansky,
Vanagida

ν_R ENLARGEMENT OF THE
FERMIONIC SPECTRUM

$$M \nu_R \nu_R + h \bar{\nu}_L \phi^- \nu_R$$

$$\begin{array}{ccc} \nu_L & \nu_L & \nu_R \\ \nu_R & \sim O_- & h \langle \phi^- \rangle \\ & h \langle \phi^- \rangle & M \end{array} \quad \text{LR Models?}$$

MAJORON MODELS

Gelmini, Roncadelli;
Glashow et al.

Δ ENLARGEMENT OF THE
HIGGS SCALAR SECTOR

$$h \nu_L \nu_L \quad \Delta$$

$$m_\nu = h \langle \Delta \rangle$$

ν mass in the
SM as an **EFFECTIVE** low-energy **theory**

LLHH dim 5 $\rightarrow M^{-1} LL \langle H \rangle \langle H \rangle$

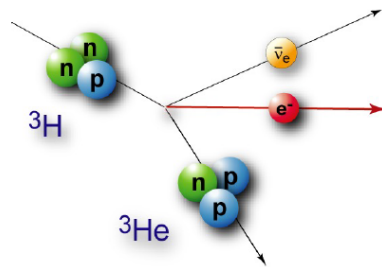
$$m_\nu \rightarrow \langle H \rangle^2 / M$$

$$m_\nu < 100 \text{ meV} \rightarrow M > 10^{14} \text{ GeV}$$

The signature

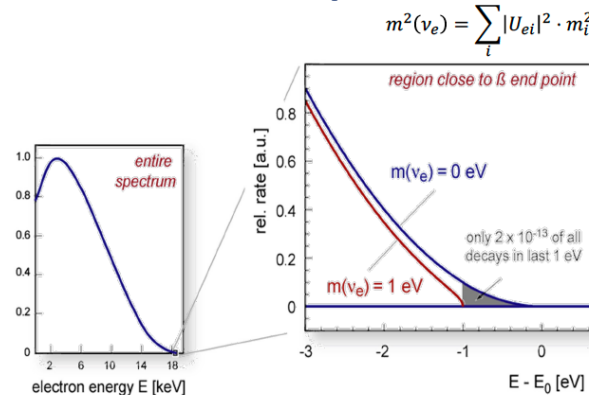
Neutrino Masses, Mixings and CP Violation

S. Mertens, ICHEP 2024



- ✓ Incoherent sum of neutrino masses
- ✓ Independent of neutrino nature (Dirac or Majorana)

KATRIN Experiment



$$m^2(\nu_e) = \sum_i |U_{ei}|^2 \cdot m_i^2$$

- New limit:
 $m_\nu < 0.45 \text{ eV (90\% CL)}$
Neutrino-24 (2024), arXiv:2406.13516 (2024)

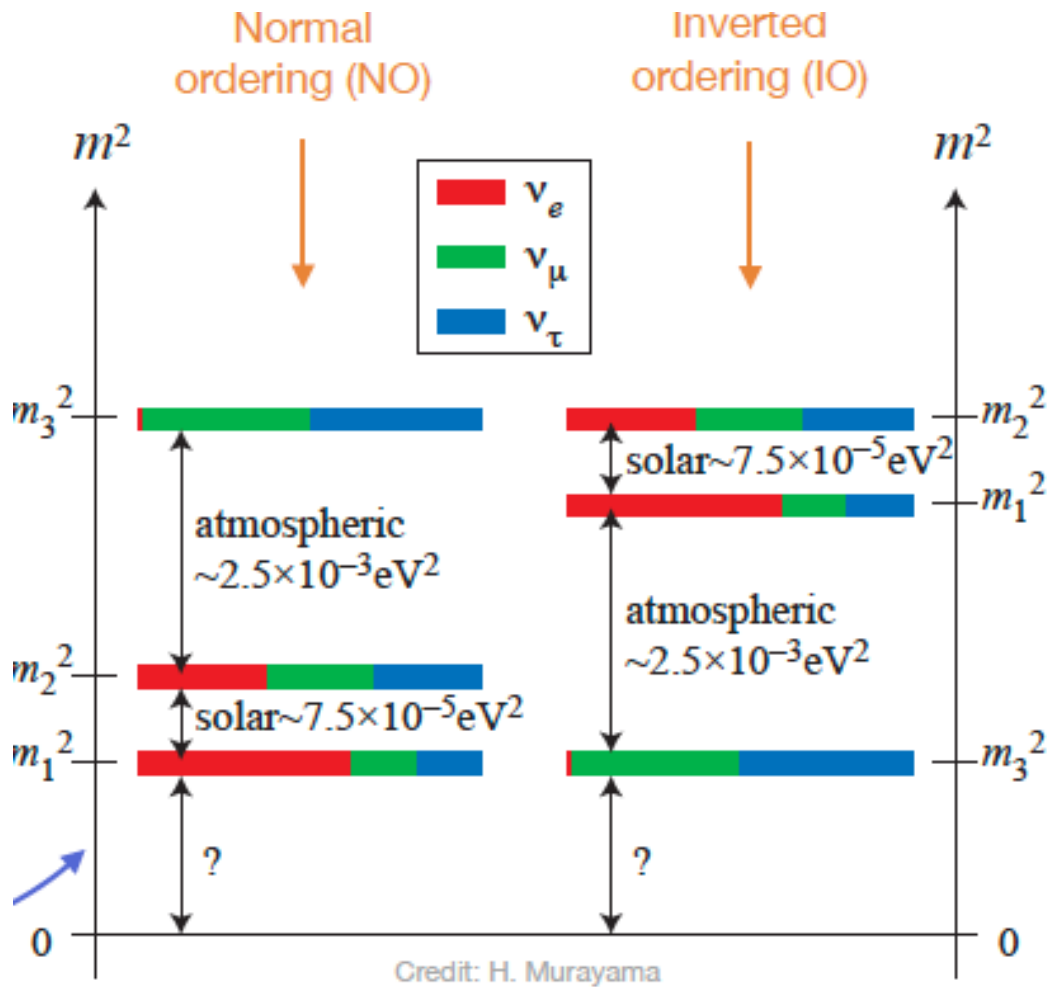
Final goal (in 2026):

- $< 0.3 \text{ eV}$ sensitivity

Constraints from COSMOLOGY

- ✓ With current cosmological observations, we can measure combinations of cosmological parameters with high precision. Still Λ CDM fits very well the data
- ✓ No evidence **yet** for nonzero neutrino masses or an enhanced radiation density (N_{eff}). Bounds $\Sigma m_\nu < 0.072\text{-}0.5 \text{ eV}$ (95% CL) and $N_{\text{eff}} = 3.10 \pm 0.17$ (68% CL), depending on data and model
- ✓ Cosmological constraints in non-standard neutrino physics

S. Pastor, Erice School 2024



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta_{CP}} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Atmospheric
(+Accelerator)

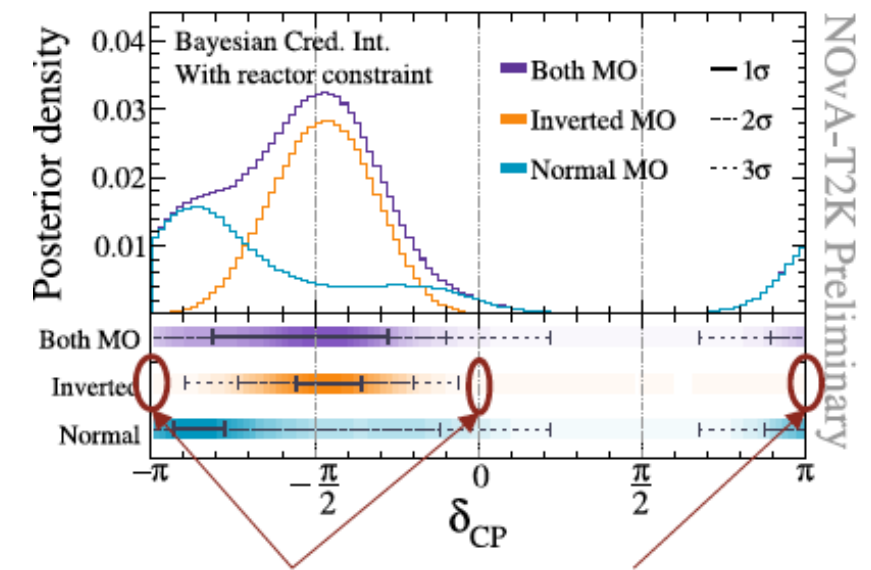
Reactor
(+Accelerator)

Solar
(+Reactor)

Mild preference for Inverted Ordering
but influenced by θ_{13} constraint

NOvA+T2K only	NOvA+T2K + 1D θ_{13}	NOvA+T2K + 2D ($\theta_{13}, \Delta m^2_{32}$)
IO (71%)	IO (57%)	NO (59%)

Strongly favor CP violation in
Inverted Ordering scenario

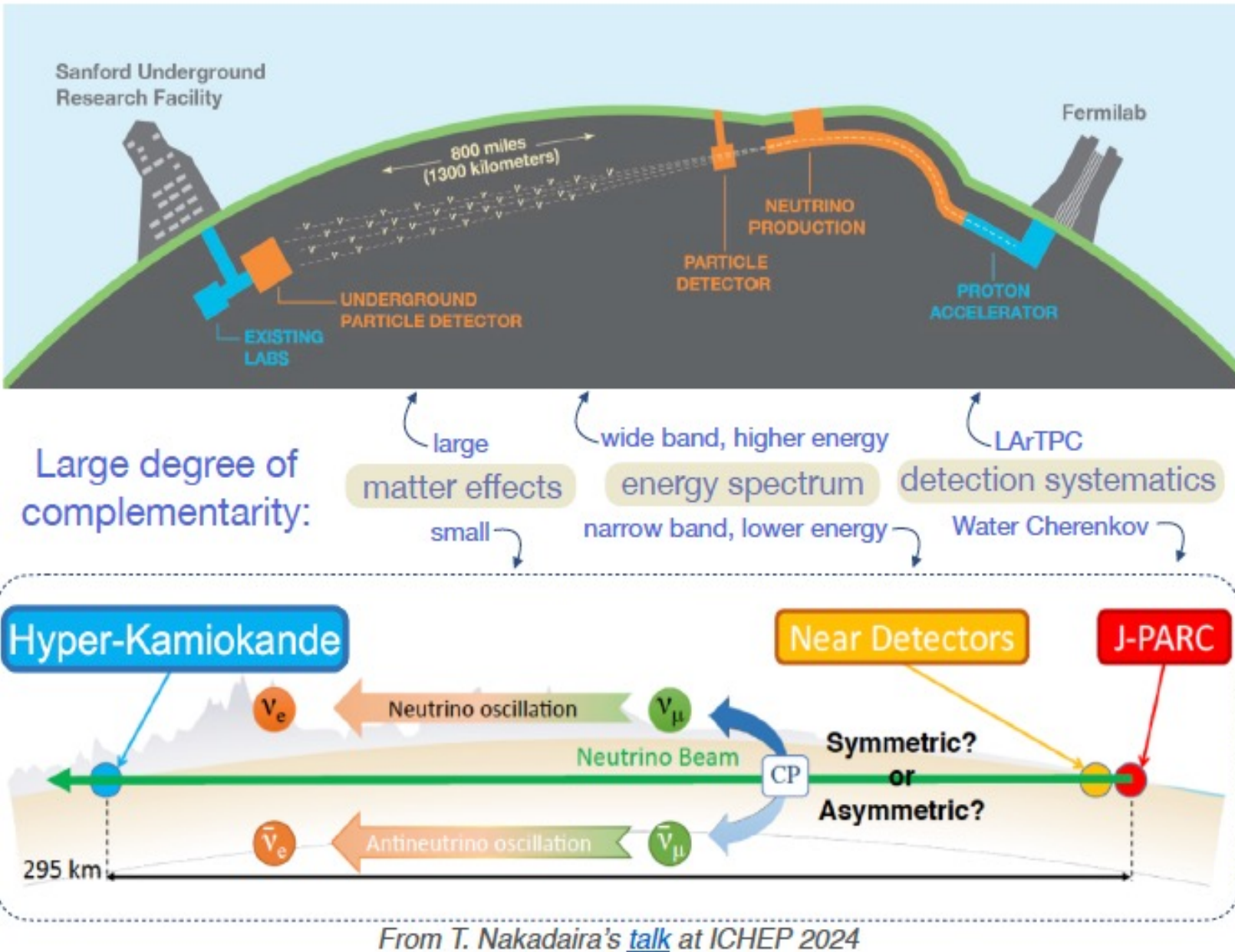


CP-conserving points are *outside*
3 σ intervals in IO
Expect CPV *if* ordering is inverted

Currently, we have some
indications of what is the mass
ordering but none above 3 σ

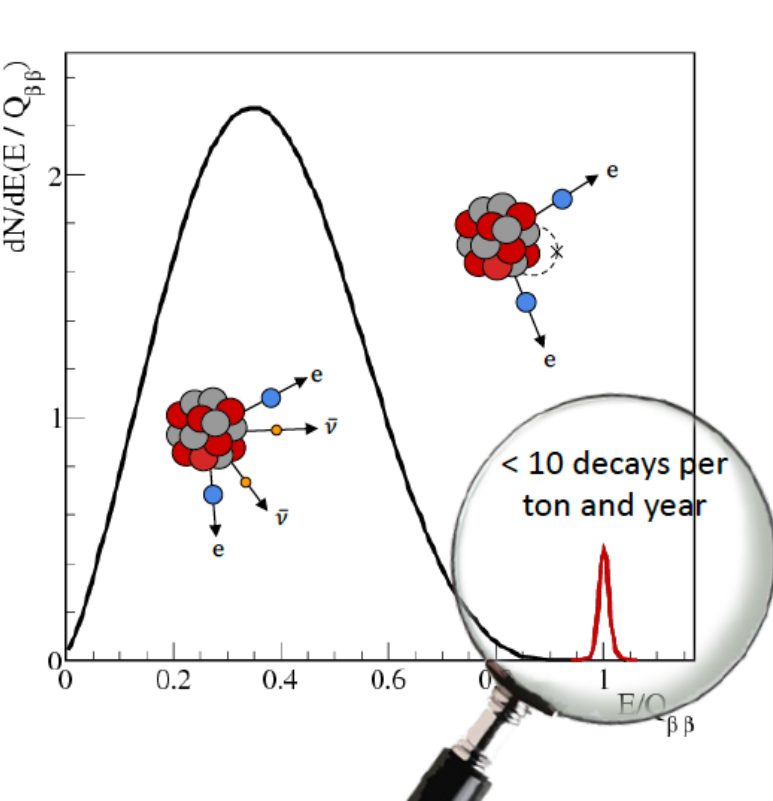
Prospects

- Mass ordering:
 - DUNE: 5σ between 1 and 3 years (depending on how kind nature is)
- Precision measurement of oscillation parameters:
 - Long term high precision for Δm_{31}^2 and θ_{13} sensitive to new physics in comparison with reactor measurements
- CP violation:
 - Long term establishment of CP violation at 3σ over 75% of δ_{CP} values
 - Similar 10-year precision of $\sim 6-18^\circ$ in δ_{CP} in both experiments



Is LEPTON Number a (global) symmetry of Nature?

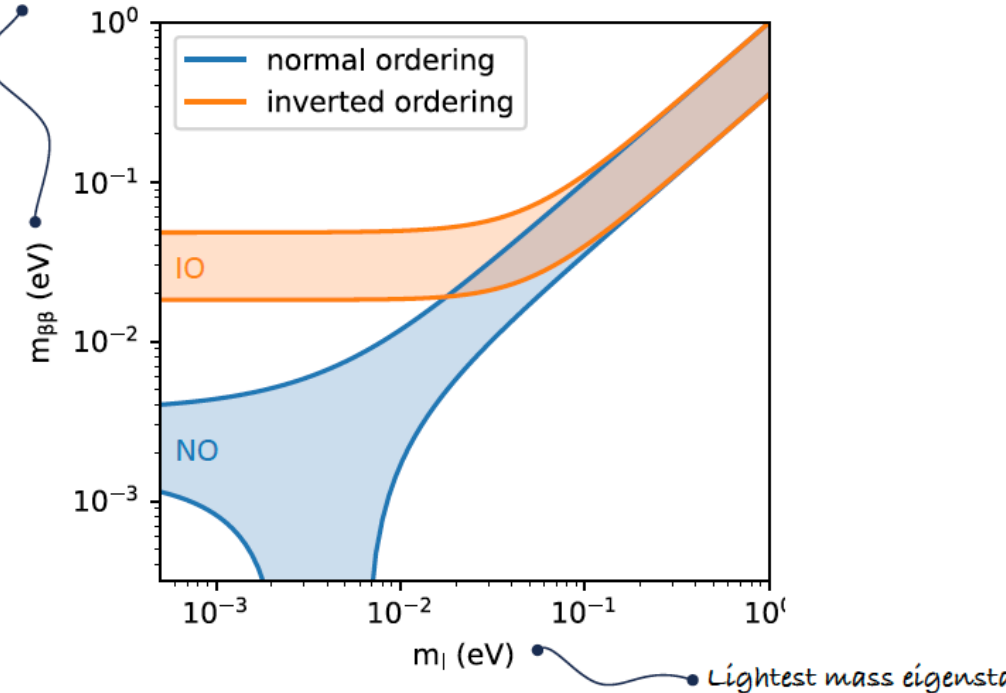
The **Neutrinoless Double Beta-Decay** to verify if the neutrino has a MAJORANA mass



Key requirements:

- Large exposure (ton-scale)
- Low background (< 1 cts/year/t/RC)
- Excellent energy resolution (< 1% @ $E_{\beta\beta}$)

Coherent sum of mass eigenstates



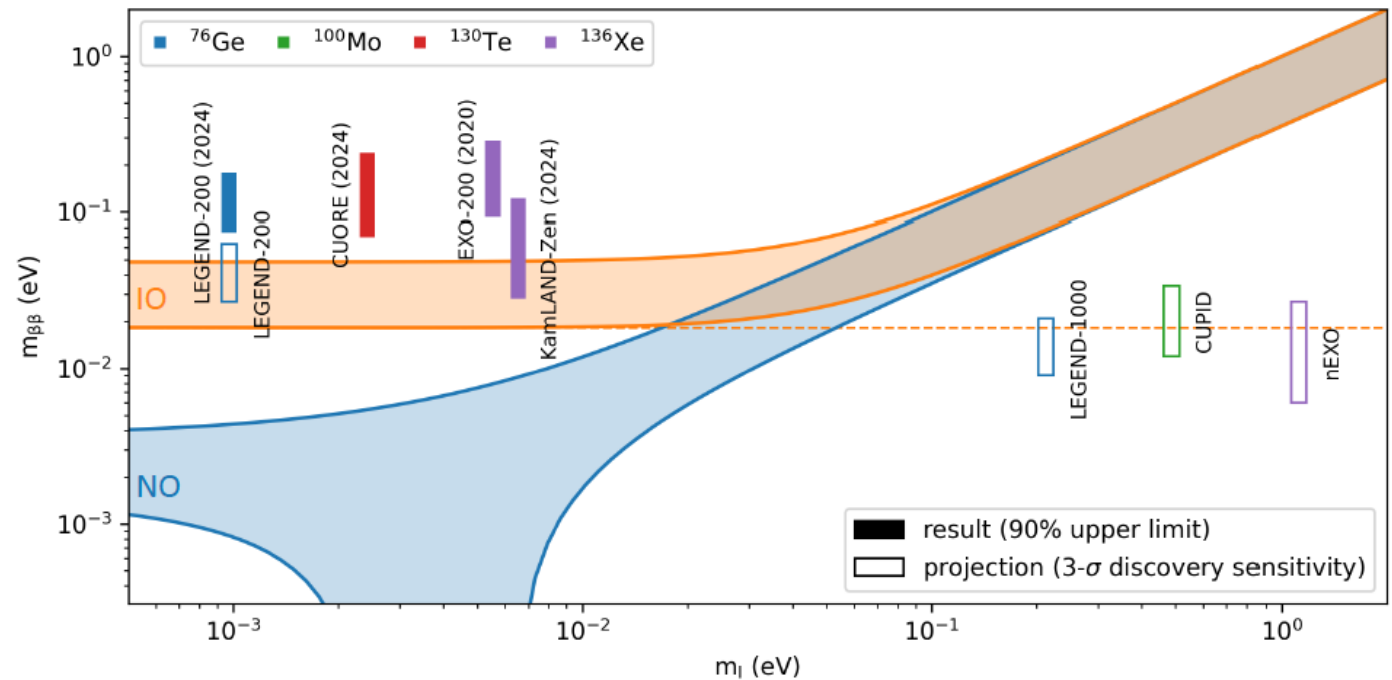
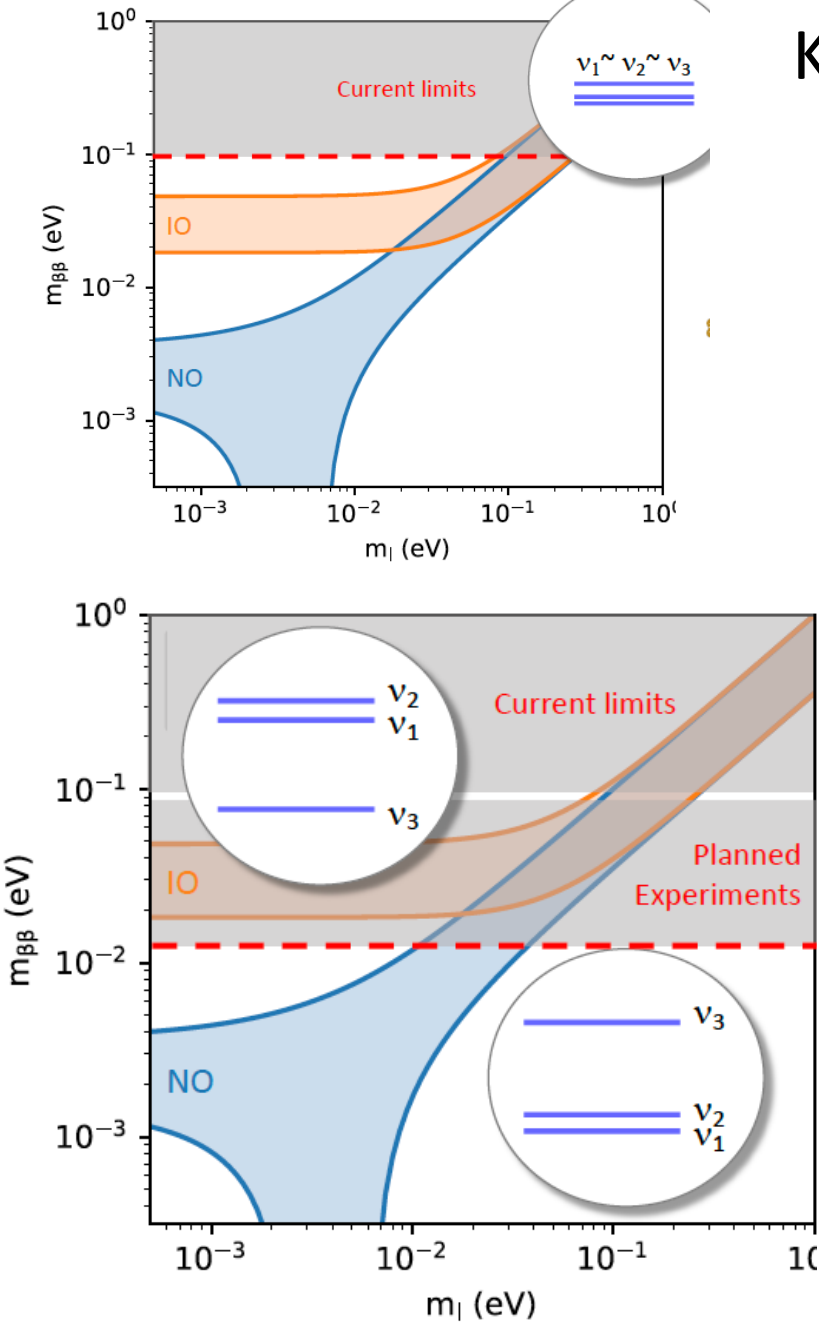
KamLAND-Zen Xe-loaded liquid scintillator

$$m_{\beta\beta} < 122 \text{ meV (90\% CL)}$$

arXiv:2406.11438 (2024)

Planned projects (e.g., LEGEND-1000, CUPID, nEXO) should **fully cover the inverted ordering range**

Overview $0\nu\beta\beta$



but ***B and L are NOT conserved at the QUANTUM LEVEL in the SM***

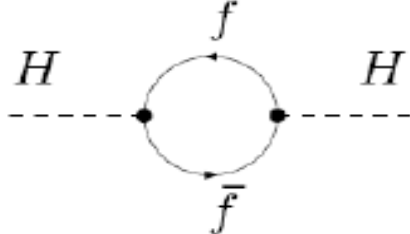
- B and L are NOT conserved at the quantum (non-perturbative) level.
- no visible implications (like proton decay) at zero (or low – like the Universe today)) temperature
- But at early epochs when such temperature exceeded the electroweak energy scale (i.e. $T > 100$ GeV) the “tunneling toll” could be avoided so that **B and L violating transitions could proceed at large rates possibly larger than the expansion rate of the Universe at that time.**

Take-home message from the **HIGH-ENERGY and HIGH-INTENSITY frontiers**

- **No** firm evidence (or at least strong hints) of new physics beyond the SM (BSM) from the **High Energy and High Intensity (Flavour Physics)** frontiers.
- Some **tensions** are present in **Low-Energy very high precision physics** (muon g-2) with interesting prospects for the further investigation of **magnetic and electric dipole moments**
- **Firm observable evidence for BSM physics: non-vanishing neutrino masses.** We don't know yet :
 - i) whether such mass is linked to a **violation of the Lepton number symmetry** (neutrino Majorana mass);
 - ii) how neutrino masses are ordered (**NO** – Normal Ordering **or IO** – Inverse Ordering); **if** and how much **CP is violated in the neutrino sector.**

ON THE RADIATIVE CORRECTIONS TO THE SCALAR MASSES

Free propagation: $H \text{-----} H$ inverse propagator: $i(p^2 - M_H^2)$

Loop corrections:  inverse propagator: $i(p^2 - M_H^2 + \Sigma_H^f)$

$$\Sigma_H^f \sim N_f \lambda_f^2 \int d^4 k \left(\frac{1}{k^2 - m_f^2} + \frac{2m_f^2}{(k^2 - m_f^2)^2} \right)$$

$$\text{for } \Lambda \rightarrow \infty : \quad \Sigma_H^f \sim N_f \lambda_f^2 \left(\underbrace{\int \frac{d^4 k}{k^2}}_{\sim \Lambda^2} + 2m_f^2 \underbrace{\int \frac{dk}{k}}_{\sim \ln \Lambda} \right)$$

Notice that, on the contrary, for **fermion masses** the **radiative corrections** are **only logarithmically divergent**


QUADRATIC DIVERGENCE

DESTABILIZATION OF THE ELW. SYMMETRY BREAKING SCALE

For $\Lambda = M_{\text{Pl}}$:

$$\Sigma_H^f \approx \delta M_H^2 \sim M_{\text{Pl}}^2 \quad \Rightarrow \quad \delta M_H^2 \approx 10^{30} M_H^2$$

(for $M_H \lesssim 1 \text{ TeV}$)

SCALAR MASSES ARE “**UNPROTECTED**” AGAINST LARGE CORRECTIONS
WHICH TEND TO PUSH THEM UP TO THE LARGEST ENERGY SCALE
PRESENT IN THE FULL THEORY

EX: Grand Unified Theory (GUT): $\delta M_H^2 \approx M_{\text{GUT}}^2$

Naturalness or Un-naturalness?

- **New SYMMETRY** giving rise to a cut-off at

$$m_{NP} \ll M$$

Low-energy **SuperSymmetry**

- **Space-time modification** (extra-dim., warped space)
- **COMPOSITE HIGGS** : the Higgs is a pseudo-Goldstone boson (pion-like) \rightarrow new interaction getting strong at

$$m_{NP} \ll M$$

- The scale at which the electroweak symmetry is spontaneously broken by $\langle H \rangle$ results from **COSMOLOGICAL EVOLUTION**
- H is a fundamental (elementary) particle \rightarrow we live in a universe where **the fine-tuning at M arises (anthropic solution, multiverse, Landscape of string theory)**

The most serious “fine –tuning problem”:
the **COSMOLOGICAL CONSTANT**
(or **quantum vacuum energy density**)
PROBLEM

The value of the H field in the vacuum state , i.e. the H vacuum expectation value $\langle H \rangle$, is of $O(10^2 \text{ GeV}) \rightarrow V(\langle H \rangle) \sim 10^8 \text{ GeV}^4$.

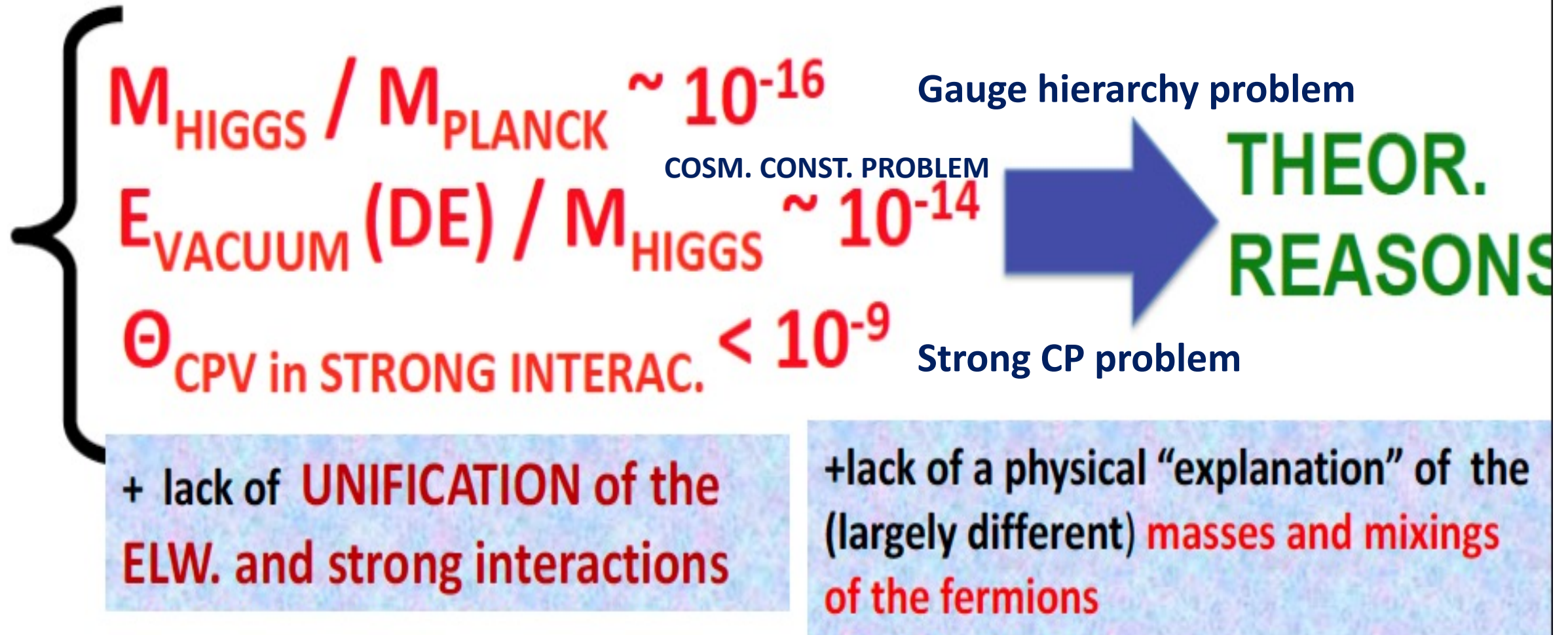
On the other hand, the value of **the vacuum energy** (expected to be the value of the **Einstein cosmological constant** should correspond to:

dark energy density \sim **critical energy density** $\sim (2.24 \times 10^{-3} \text{ eV})^4$

Notice that **any phase transition** we know - for instance also the $O(1\text{GeV})$ QCD quark-gluon phase transition, i.e. from free quarks and gluons to their confinement inside composite hadrons (protons, neutrons, etc. – corresponds to **energy scales** \gg **cosmological constant energy scale**

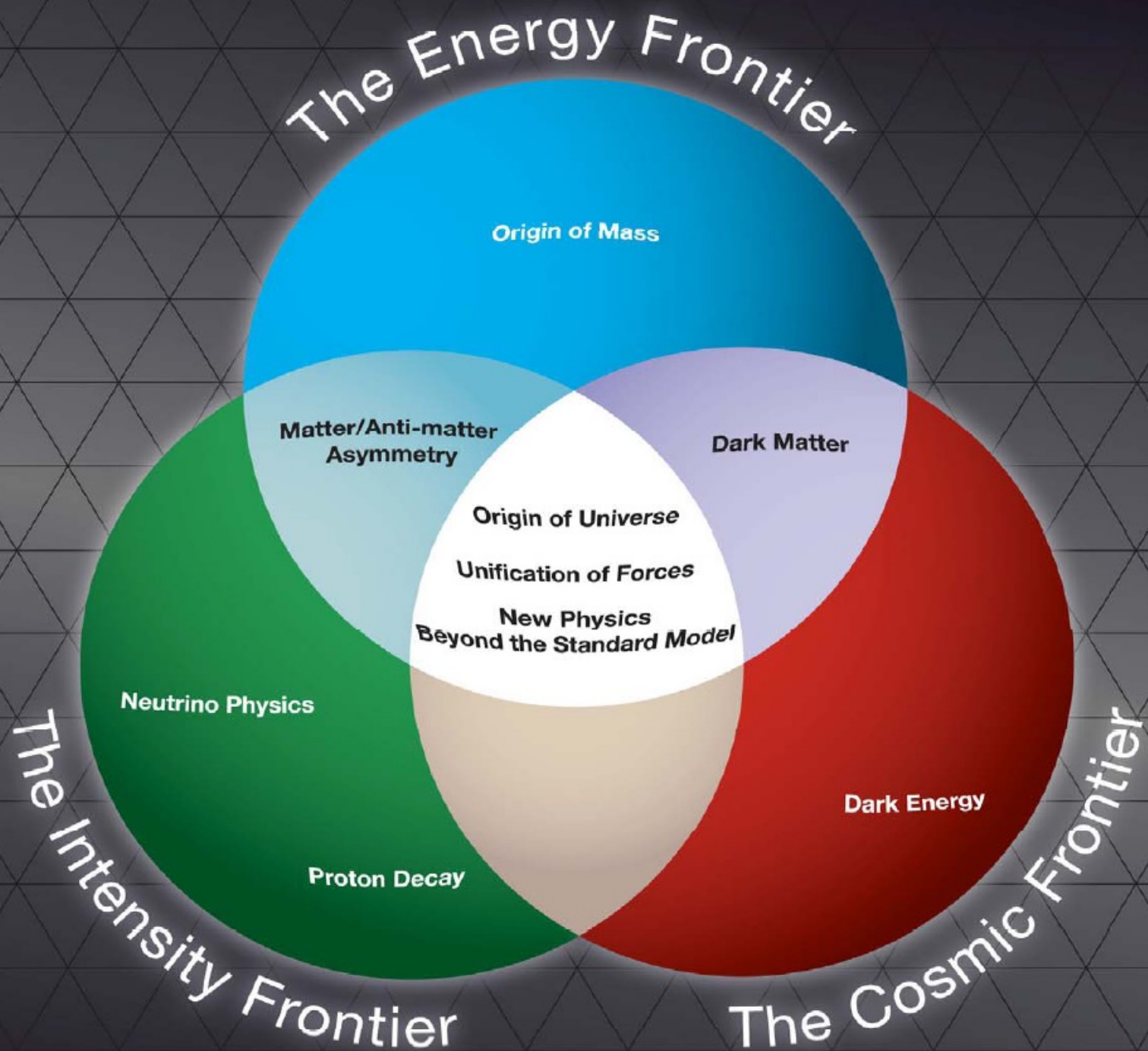
2nd take home message:

theoretical reasons of dissatisfaction with the SM

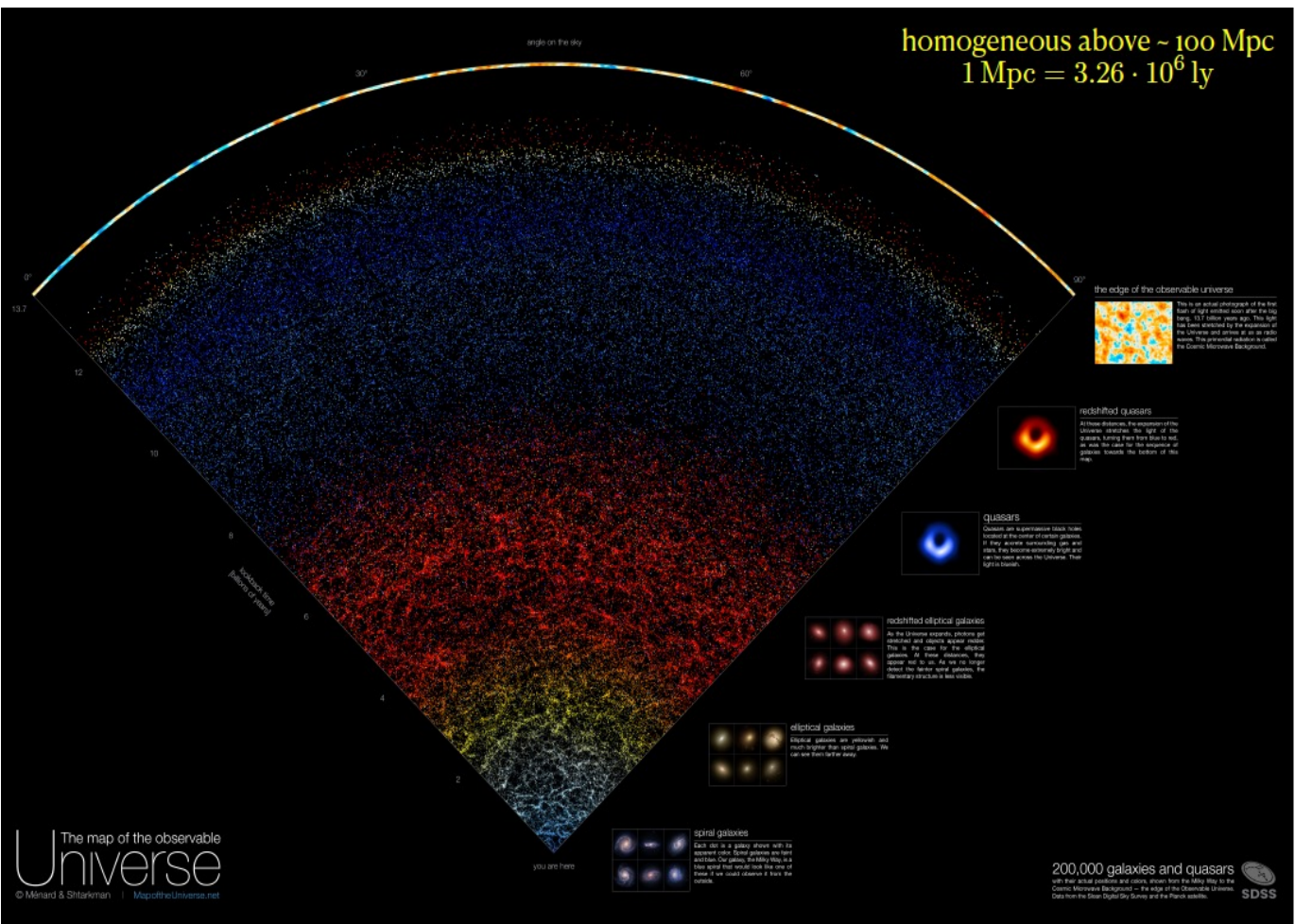


UNI- or MULTI-VERSE ?

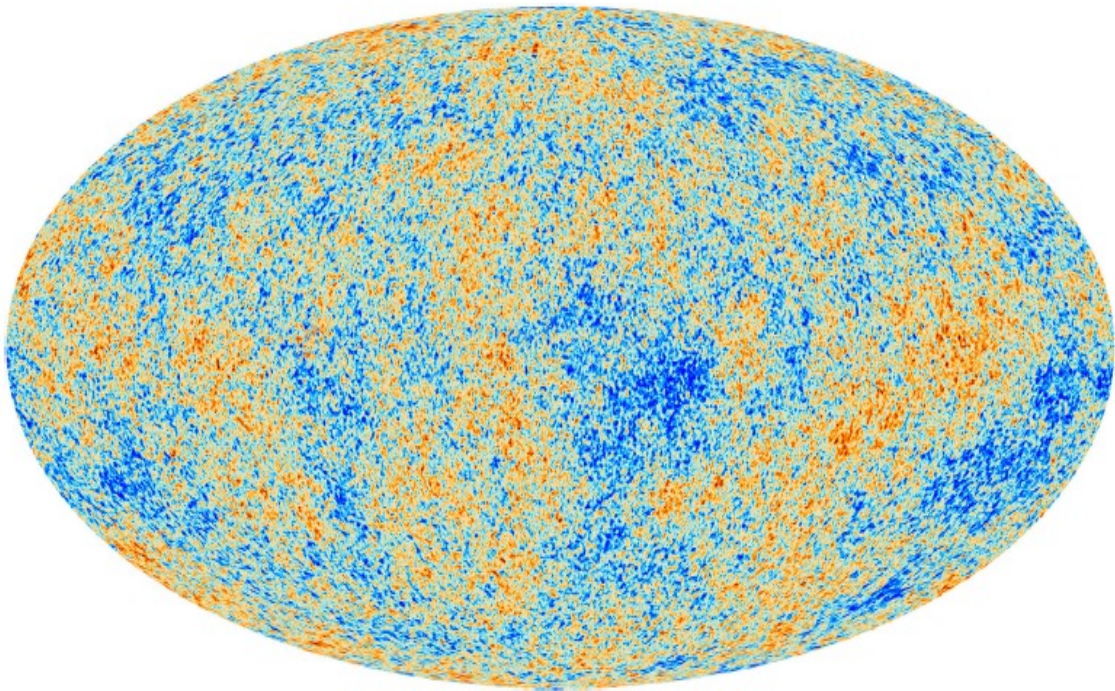
- Gauge hierarchy, cosmological constant, DE – DM – Ordinary Matter energy densities, values of the running coupling constants, neutron-proton mass difference, ... **FINE-TUNING of Fundamental Parameters**, a **Fundamental Theory** accounting for such apparent fine-tuning (maybe the Theory of Everything (**TOE**)), **Anthropic Principle** or ...?
- **String Theory Landscape**: many (infinite?) **DEGENERATE VACUA** → each vacuum corresponds to a different universe, i.e. a universe with different values of the fundamental parameters → we live and study the **ONLY** universe where our life is allowed, i.e. just “OUR” universe where the fundamental parameters take the particular values allowing for our existence;
- In the **ETERNAL INFLATION** theory some regions of space stop stretching , form distinct bubbles – with different SSB and hence different physical constants
- **Weinberg’s anthropic explanation** of the small (but not exactly zero) value of **the cosmological constant** (his paper was written in 1987 long before the exp. discovery of the accelerated expansion of the universe).



Our universe is **ISOTROPIC** and (very likely) **HOMOGENEOUS**



CMB temperature map from PLANCK
~ 380,000 years after the Bang



$$T \simeq 2.73 \text{ K} \quad \frac{\Delta T}{T} \simeq 10^{-5}$$

The Standard Universe

- It is homogeneous and isotropic on large scales;
- It expands;
- It was hot and close to thermal equilibrium in the past;
- Light nuclei (D, ^3He , ^4He , ^7Li) formed $<$ few seconds after the Bang;
- Photons decoupled ~ 380000 yrs after the Bang

**Well accounted for by the
SM Cosmology
+
SM Particle Physics**

Puzzles from the Universe

- The expansion accelerates;
- Normal matter makes up less than 5% of the present energy content;
- Structure formation is driven by ~25% of an unknown pressureless component;
- Initial conditions on density and velocities is extremely unlikely;
- Antimatter is missing.

**NEW PHYSICS BEYOND THE SMs
is needed!!**

Units: $\hbar = c = k_B = 1$
 \uparrow Boltzmann const.

NATURAL UNITS

$\Rightarrow M, E, T$ have the same dimension

$$[E] = [mc^2], \quad [E] = [k_B T]$$

$$1 \text{ K} \approx 10^{-4} \text{ eV} = 10^{-13} \text{ GeV}$$

dim. of t and $L \rightarrow \frac{1}{M}$

$$[E] = [\hbar \omega]; \quad [\omega] = [t^{-1}]; \quad [L] = [ct]$$

$$1 \text{ GeV}^{-1} \sim 10^{-14} \text{ cm} = 10^{-16} \text{ m}$$

$$1 \text{ GeV} \sim 10^{-27} \text{ sec.}$$

$$G_N = \frac{1}{M_{\text{Pl}}^2} \rightarrow M_{\text{Pl}} = 1.2 \cdot 10^{19} \text{ GeV}$$

$$\downarrow$$

$$V = -G \frac{m_1 m_2}{r} \quad [V] = M \quad [r^{-1}] = M$$

Planck length: $l_{\text{Pl}} = \frac{1}{M_{\text{Pl}}} = 1.6 \cdot 10^{-33} \text{ cm}$

Planck time: $t_{\text{Pl}} = \frac{1}{M_{\text{Pl}}} = 5.4 \cdot 10^{-44} \text{ s.}$

Planck mass: $M_{\text{Pl}} = 2.2 \cdot 10^{-5} \text{ g.}$

$$1 \text{ Mpc} = 3.1 \cdot 10^{24} \text{ cm}; \quad 1 \text{ year} = 3.16 \cdot 10^7 \text{ s.}$$

$$1 \text{ light year} \approx 10^{18} \text{ cm}$$

HOMOGENEOUS EXPANDING UNIVERSE

Homogeneity and isotropy: the metric tensor is invariant under translations (3) and rotations (3)

$$ds^2 = dt^2 - a^2(t) f(R) \delta_{ij} dx^i dx^j$$

(cartesian coordinates)

$$R^2 = \delta_{ij} x^i x^j$$

scale factor

3-dim line element

$$H \equiv \frac{\dot{a}}{a}$$

Hubble parameter

$$f(R) = \frac{1}{\left(1 + \frac{KR^2}{4}\right)^2}$$

K=0, flat (euclidean)

K>0, closed (finite volume)

K<0, open

$$\int_0^\infty \frac{dR}{1 + \frac{KR^2}{4}} = \pi/\sqrt{K}$$

Friedmann-Lemaître-Robertson-Walker Metric

Polar coordinates: $r = R \left(1 + \frac{KR^2}{4}\right)^{-1}$

$$dR \left(1 + \frac{KR^2}{4}\right)^{-1} \rightarrow dr/\sqrt{1 - Kr^2}$$

$$ds^2 = dt^2 - a^2(t) \left[\frac{dr^2}{(1 - Kr^2)} - r^2 (d\theta^2 + \sin^2 \theta d\phi^2) \right] = dt^2 - a(t)^2 d\vec{l}^2$$

scale factor

curvature constant: [K]=[L]⁻²

K=0, flat (euclidean)

K>0, closed (finite volume)

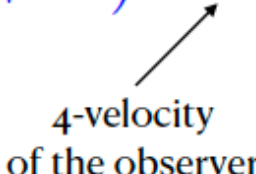
K<0, open

cosmological redshift

$$1 + z \equiv \frac{\lambda^{\text{ph}}(t_0)}{\lambda^{\text{ph}}(t)} = \frac{1}{a(t)}$$

Energy-Momentum tensor in FLRW

Energy-momentum tensor: $T^\mu_\nu = -Pg^\mu_\nu + (\rho + P)u^\mu u_\nu \rightarrow \text{diag}(\rho, -P, -P, -P)$

FLRW frame

 4-velocity
of the observer

$\rho(t)$ energy density
 $P(t)$ pressure

$$d(\rho a^3) = -P da^3$$

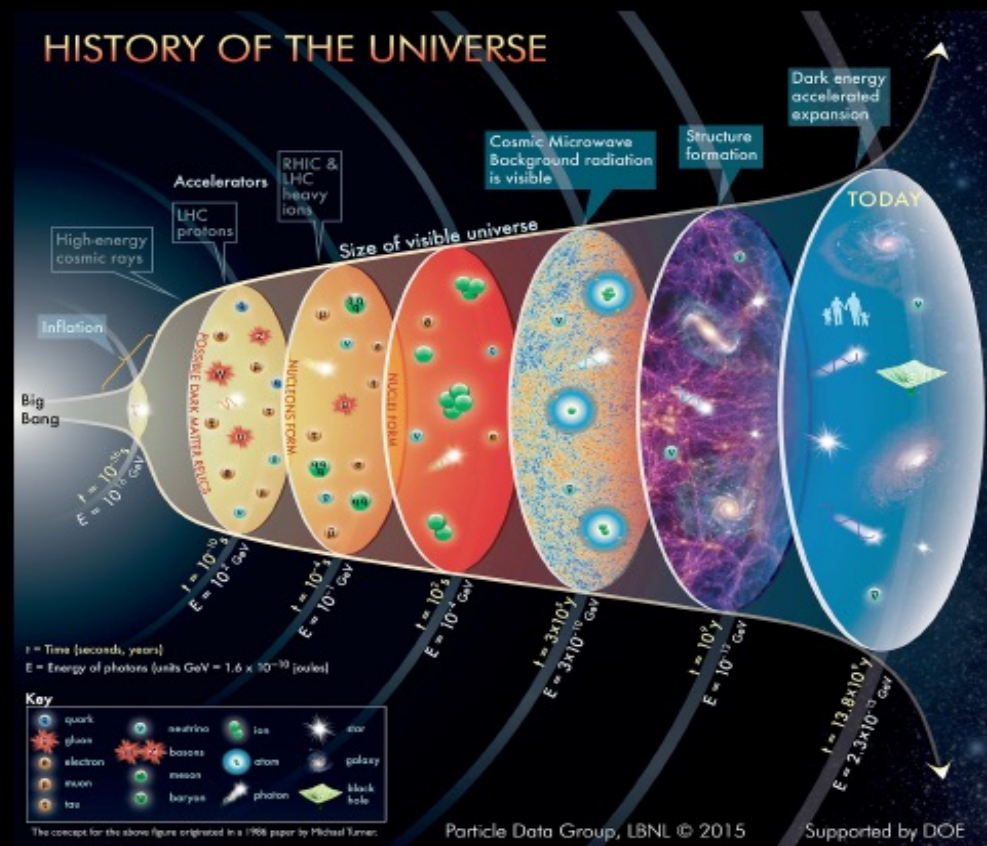
1st principle of thermodynamics
in an expanding universe

$$w(a) \equiv \frac{P(a)}{\rho(a)}$$

equation of state

$$\rho(a) = \rho_0 e^{-3 \int_1^a \frac{da'}{a'} (1+w(a'))} \xrightarrow{w \text{ constant}} \rho_0 a^{-3(1+w)}$$

K. Olive Particle cosmology



scale
factor
 a/a_0

energy density: $\rho(a) = a^{-3(1+w)}$

$$\rho_R \sim a^{-4} \quad , \quad w = 1/3 \quad \text{(Radiation)}$$

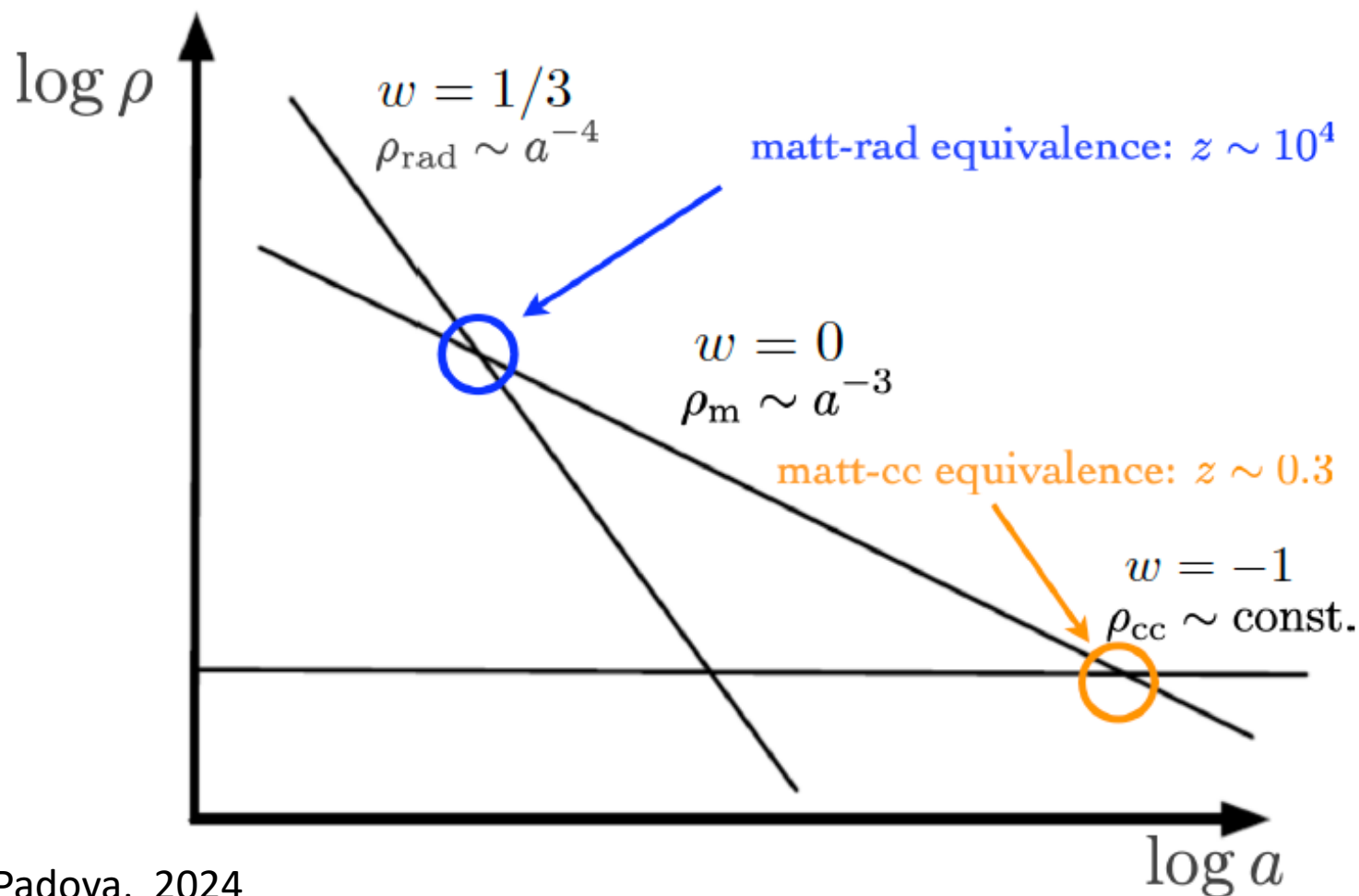
$$\rho_M \sim a^{-3} \quad , \quad w = 0 \quad \text{(Matter)}$$

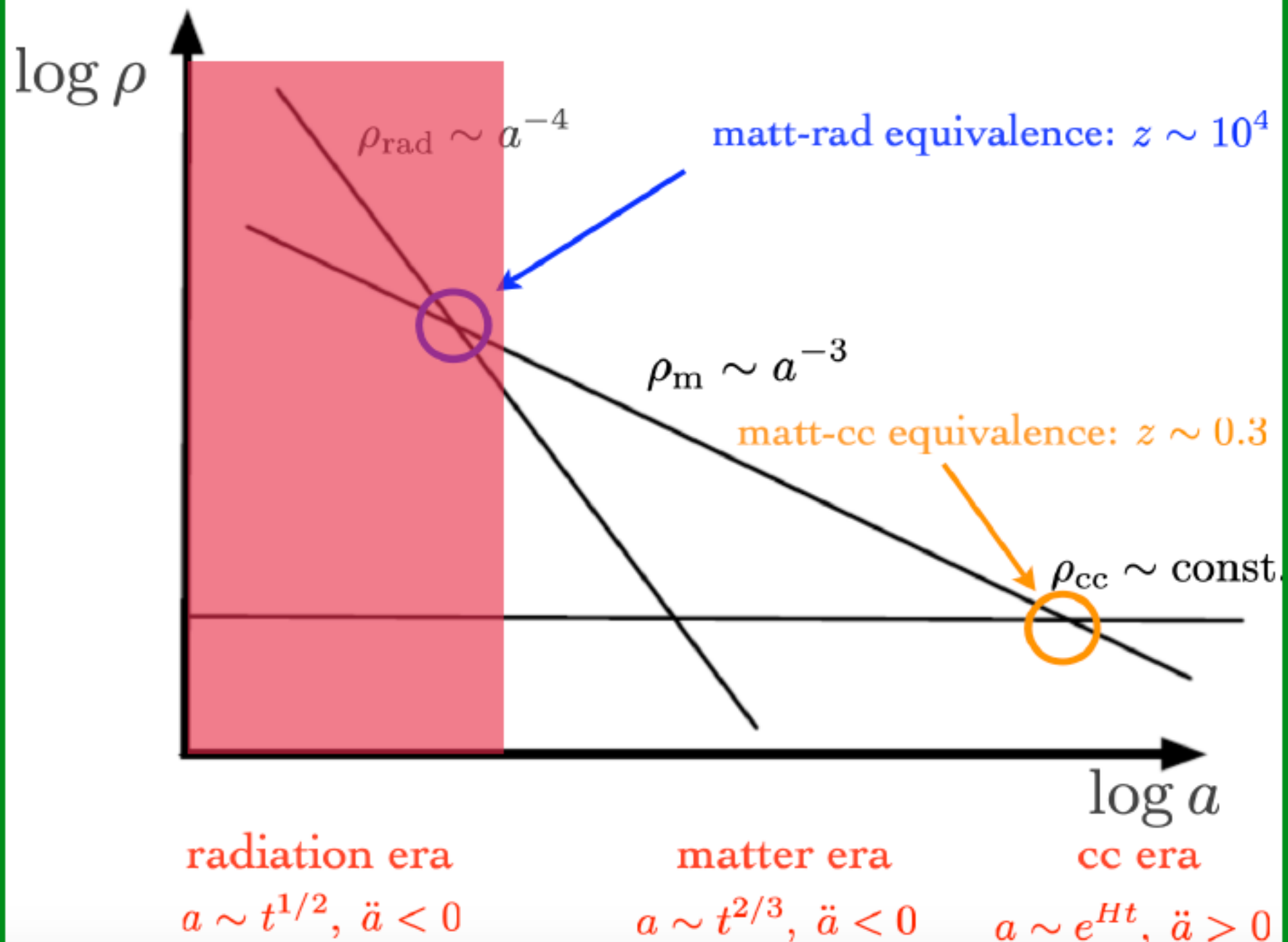
$$\rho_\Lambda \sim \text{const.} \quad , \quad w = -1 \quad \text{(Cosmological constant)}$$

L. Covi, Dark side of the Universe

Cosmological epochs

Λ CDM Model: $\rho = \rho_{\text{m}} + \rho_{\text{rad}} + \rho_{\Lambda} = \rho_{\text{m}}^0 a^{-3} + \rho_{\text{rad}}^0 a^{-4} + \rho_{\Lambda}$ different components dominate at different epochs





Epoch of the RADIATION DOMINANCE

$$\rho_R \gg \rho_M$$

↓

$$\rho \approx \rho_R$$

$$\rho_R = \rho_R/3$$

$$; \quad a(t) \propto \sqrt{t}$$

$$H \approx 1.66 \sqrt{g_*} \frac{T^2}{M_{\text{Planck}}}$$

$$M_{\text{Planck}} = \frac{1}{\sqrt{G_N}} = 1.22 \times 10^{19} \text{ GeV}$$

↓ expansion rate of the Universe

Relation between T and $t =$ age of the Universe at temperature T

$$t = \sqrt{\frac{90}{32\pi^3} \frac{1}{G_N g_*}} \frac{1}{T^2}$$


$$t T^2 \approx \frac{2.4}{\sqrt{g_*}}$$

$$t \approx \left(\frac{T}{\text{TeV}} \right)^{-2} \text{ sec.}$$

The “unbearable” acceleration of the expansion of the Universe

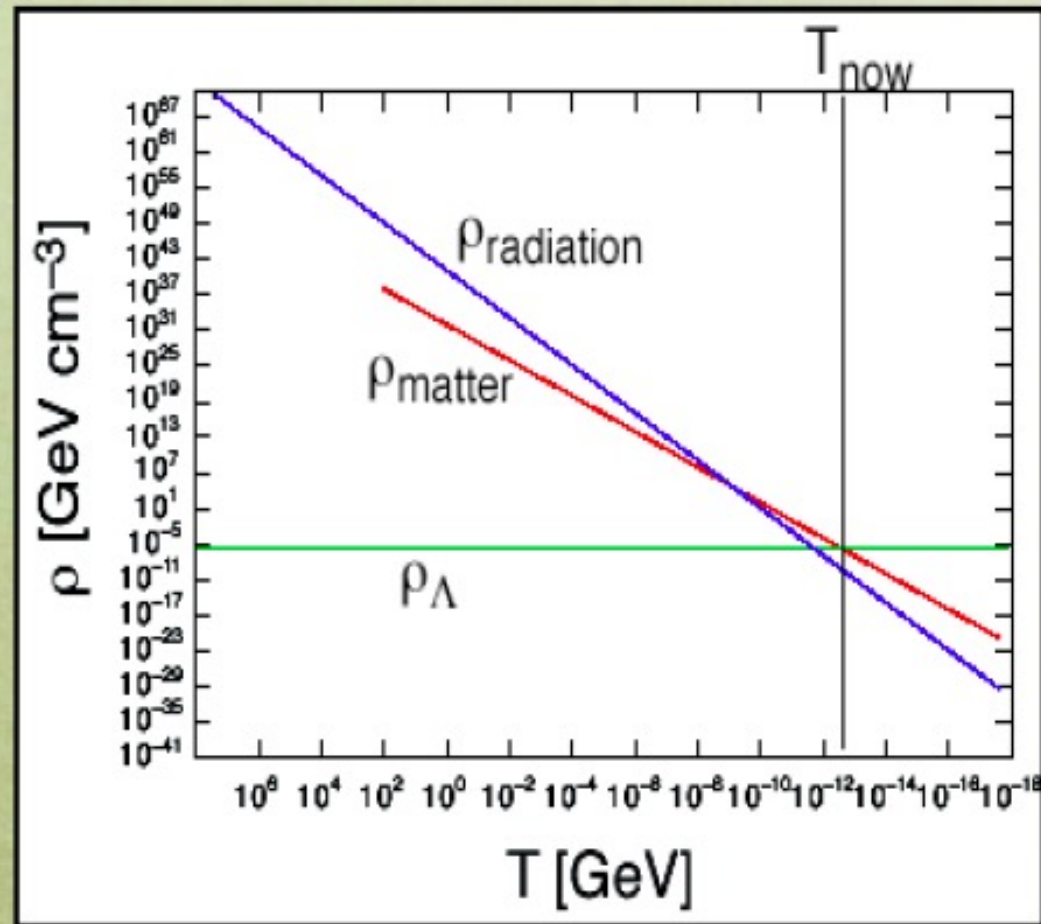
- Until the end of the past century the debate was if the universe was **open** (matter energy density $<$ critical energy density) or **closed**, hence whether the universe would never end to expand or if its expansion was to stop at some point with the universe collapsing into a Big Crunch. **But no “reasonable” physicist was doubting that in any case the attractive force of gravity had to slow down the expansion of the universe** (indeed, a de-acceleration parameter was introduced to measure such slow down).
- **But**, on the contrary ...

DARK ENERGY

- What is causing the acceleration of the expansion of the universe?
 - Einstein's cosmological constant Λ ?
 - Some new dynamical field ("quintessence," Higgs-like)?
 - Modifications to General Relativity? "Dark Energy"
- Dark energy effects can be studied in two main cosmological observables:
 - The history of the expansion rate of the universe: supernovae, weak lensing, baryon acoustic oscillations (BAO), cluster counting, etc.
 - The history of the rate of the growth of structure in the universe: weak lensing, large-scale structure, cluster counting, redshift-space distortions, etc.
- For all probes other than SNe, **large galaxy surveys are needed**:
 - **Spectroscopic**: 3D (redshift), medium depth, low density, selection effects
 - **Photometric**: "2.5D" (photo-z), deeper, higher density, no selection effects

THE “**WHY NOW**” PROBLEM

- Why do we see matter and cosmological constant almost equal in amount?
- “Why Now” problem
- Actually a *triple coincidence problem* including the radiation
- If there is a deep reason for $\rho_\Lambda \sim ((\text{TeV})^2/M_{Pl})^4$, coincidence natural



Arkani-Hamed, Hall,
Kolda, HM

To be or not to be in **THERMAL EQUILIBRIUM**,

i.e. what are the conditions for a particle i to be in thermodynamical equilibrium in the primordial plasma of particles in the early universe

- Should the universe **not be expanding**, i.e. having particles in a box with fixed walls
→ after some time **each particle would realize the thermal equilibrium** with the other particles present in the plasma
- However **the universe IS EXPANDING** (box with sliding walls) at a certain **rate H** → the particle i is in equilibrium **only if it has some of its interactions with the other particles in the plasma proceeding with a rate larger than H** , i.e. some of its interactions should be (much) **faster** than time scale of the expansion

$$\text{interaction rate } \Gamma \gg H \text{ expansion rate}$$

interaction rate $\Gamma \gg H$ expansion rate

$$f(\vec{x}, \vec{p}, t, \mu) \xrightarrow[\text{kinetic equilibrium}]{\text{homogeneity, isotropy}} f_T(p, \mu) = \frac{1}{e^{(E-\mu)/T} \pm 1}$$

distribution function

$$E = \sqrt{p^2 + m^2}$$

$$p = |\vec{P}| \sim 1/a$$

$$\rho = \boxed{g} \int \frac{d^3 p}{(2\pi)^2} E f_T(p, \mu) = \begin{cases} T \gg m, \mu & g \frac{\pi^2}{30} T^4 \times \begin{cases} 1 & \text{boson} \\ 7/8 & \text{fermion} \end{cases} \\ T \ll m & m n = g m \left(\frac{mT}{2\pi} \right)^{3/2} e^{-(m-\mu)/T} \end{cases}$$

energy density

$$n = \boxed{g} \int \frac{d^3 p}{(2\pi)^3} f_T(p, \mu) \simeq g \frac{2\zeta(3)}{\pi^2} T^3 \left[\frac{3}{4} \right]$$

number density

$T \gg m, \mu$ [fermion]

$$P = \boxed{g} \int \frac{d^3 p}{(2\pi)^3} \frac{k^2}{3E} f_T(p, \mu) \simeq \frac{1}{3} \rho$$

pressure

$T \gg m, \mu$

Thermodynamical variables EQUILIBRIUM THERMODYNAMICS

VARIABLE	RELATIVISTIC		NON REL.
	BOSE	FERMI	
n	$\frac{\zeta(3)}{\pi^2} g T^3$	$\frac{3}{4} \frac{\zeta(3)}{\pi^2} g T^3$	$g \left(\frac{mT}{2\pi} \right)^{3/2} e^{-m/T}$
ρ	$\frac{\pi^2}{30} g T^4$	$\frac{7}{8} \frac{\pi^2}{30} g T^4$	mn
p	$\frac{\rho}{3}$		$nT \ll \rho$
$\langle E \rangle$	$2,701T$	$3,151T$	$m + \frac{3}{2}T$

$$n = g_i \int \frac{d^2 \vec{p}}{(2\pi)^3} f_i(p, T) \quad \rho = g_i \int \frac{d^2 \vec{p}}{(2\pi)^3} E_i f_i(p, T)$$

$$p = g_i \int \frac{d^2 \vec{p}}{(2\pi)^3} \frac{p^2}{3E_i} f_i(p, T) \quad \langle E \rangle = \rho/n$$

$$\rho_{\text{tot}} = \sum_i \rho_i \simeq g_* \frac{\pi^2}{30} T^4$$

$$g_* = \sum_b g_b + \frac{7}{8} \sum_f g_f$$

sum over relativistic d.o.f's

g_* = total number of the EFFECTIVE RELATIVISTIC degrees of freedom

weighted by the temperature of each contributing d.o.f.
(if the corresponding particle is in thermal equilibrium, i.e. for a COUPLED particle, the temperature is the same as the T of thermal bath and, hence, no suppression factor is present)

$$g_b (T_b / T)^4$$

$$g_f (T_f / T)^4$$

g_* is a function of the temperature T of the plasma of particles $\rightarrow g_*(T)$

ex. :

$$1) \text{ for } T \ll \text{MeV} \Rightarrow \begin{cases} \gamma \\ 3\nu \end{cases} \quad T_\nu = \sqrt[3]{\frac{4}{11}} T_\gamma \quad (\text{see later})$$

$$g_* \Big|_{T \ll \text{MeV}} = \underset{\gamma}{2} + \frac{7}{8} \times 3 \times 2 \times \left(\frac{4}{11}\right)^{4/3} = \boxed{3.36}$$

$$2) \text{ for } 1 \text{ MeV} < T < 100 \text{ MeV}$$

$$\begin{cases} \gamma \\ 3\nu \\ e^-, e^+ \end{cases} \quad g_* \Big|_{1 \text{ MeV} < T < 100 \text{ MeV}} = 2 + \frac{7}{8} (3 \times 2 + 1 \times 4) = \boxed{10.75}$$

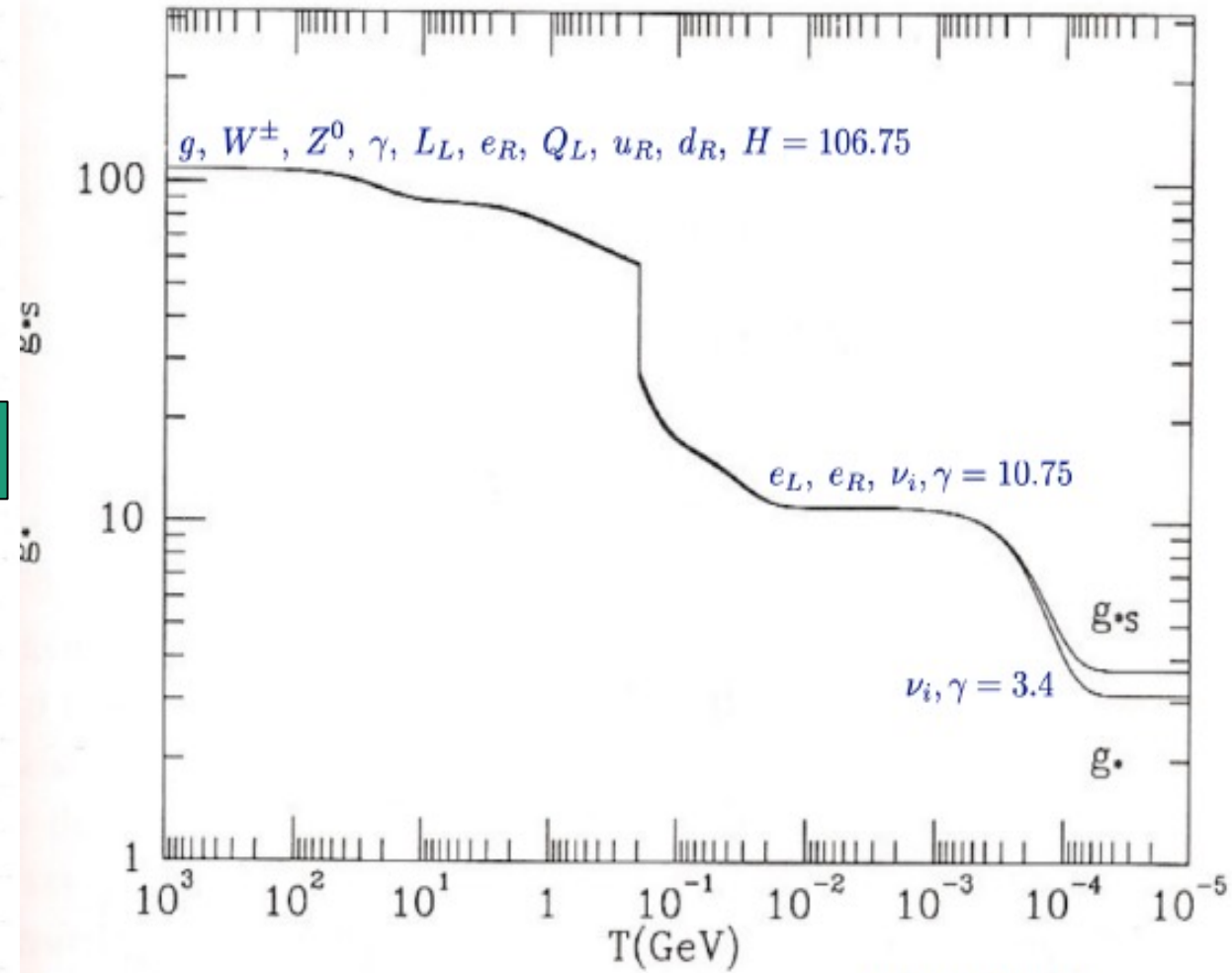
\downarrow \downarrow
 3×2 4
 2 d.o.f. 4 d.o.f.

$$3) \text{ for } T > 200 \text{ GeV}$$

all particles of the SM: $g_{\text{gluons}}, \gamma, W^\pm, Z^0$
 $6q, e, \mu, \tau, 3\nu, H^0 \rightarrow$ *high energy*

$$g_* \Big|_{T > 200 \text{ GeV}} \approx \boxed{106.75}$$

If only the SM particles are present!



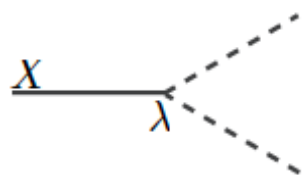
Kolb & Turner

Time-Scales

- expansion (rad. dom.):

$$H = \sqrt{\frac{8\pi G}{3}\rho} \simeq 0.33 g_*^{1/2} \frac{T^2}{M_p} \quad [t/\text{sec} \simeq (T/\text{MeV})^{-2}]$$

- interactions:

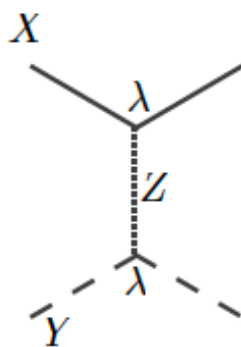


decay

$$\Gamma_D \sim \lambda^2 m_X \begin{cases} m_X/T & T \geq m_X \\ 1 & T \leq m_X \end{cases}$$

inv. decay

$$\Gamma_{ID} \sim \Gamma_D \begin{cases} 1 & T \geq m_X \\ \left(\frac{m_X}{T}\right)^{3/2} e^{-\frac{m_X}{T}} & T \leq m_X \end{cases}$$




scattering (annihilation)


$$\Gamma_{S,X} \sim n_Y \lambda^4 \frac{T^2}{(T^2 + m_Z^2)^2} \sim \begin{cases} \lambda^4 T & T \gg m_{Y,Z} \\ \lambda^4 T^5 / m_Z^4 & m_Y \ll T \ll m_Z \\ \propto e^{-m_Y/T} & T \ll m_Y \end{cases}$$

In or Out?

rule of thumb: in equilibrium if $\Gamma \gg H$

- gauge interactions: $\Gamma \sim \alpha^2 T \gg H \longrightarrow T \ll \alpha^2 M_p / 0.33 / g_*^{1/2} \simeq O(10^{15} \text{ GeV})$
- weak interactions: $\Gamma \sim G_F^2 T^5 \gg H \longrightarrow T \gg 1 \text{ MeV}$
- baryon-photon coupling: $\Gamma \sim n_e \sigma_T \gg H \longrightarrow \overset{n_e \rightarrow 0}{O(1 \text{ eV})} \ll T \ll O(10^{15} \text{ GeV})$


free-electron density


Thomson cross-section
- DM annihilations: $\Gamma \sim n_\chi \sigma_{\text{ann}} \gg H \longrightarrow T \gg m_\chi$

NEUTRINO DECOUPLING (or NEUTRINO FREEZE-OUT)

Neutrino coupled to the thermal bath
via weak interactions as

$$n \nu \leftrightarrow p e^-$$

$$n \leftrightarrow p e^- \bar{\nu}$$

$$n e^+ \leftrightarrow p \bar{\nu}$$

$$\nu \bar{\nu} \leftrightarrow e^- e^+$$

NEUTRINO MASSES $\ll M_W$

- New limit:

$$m_\nu < 0.45 \text{ eV (90\% CL)}$$

Neutrino-24 (2024), arXiv:2406.13516 (2024)

oscillations

$$|\Delta m_{12}^2| = (5.4 - 9.5) \times 10^{-5} \text{ eV}^2$$

solar

$$|\Delta m_{23}^2| = (1.2 - 4.8) \times 10^{-3} \text{ eV}^2$$

atmospheric

$$\Gamma_W \sim G_F^2 T^5 < H \sim 0.33 g_*^{1/2} \frac{T^2}{M_p}$$

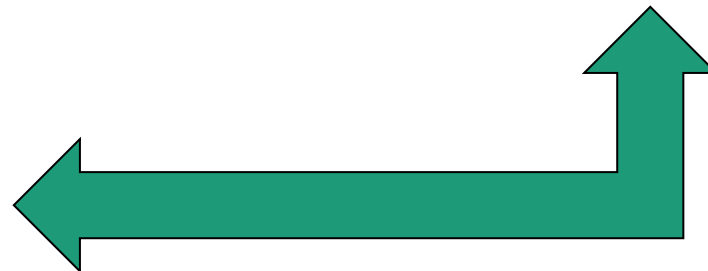


$$T < 0.8 \text{ MeV}$$

weak interaction decoupling

RELIC NEUTRINOS

TODAY!



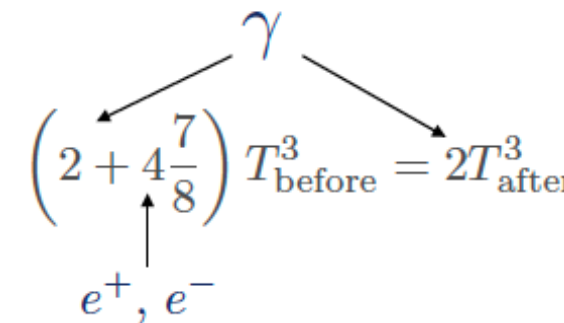
$$m_\nu/T_W < 10^{-6} \quad \text{Neutrinos are relativistic at decoupling} \quad \left. \frac{n_{\nu i}}{n_\gamma} \right|_{T_{\text{dec}}} = \frac{2 \times 3/4}{2} = \frac{3}{4}$$

At $T \sim m_e < T_W$ electrons become non-relativistic: $e^+e^- \rightleftharpoons \gamma\gamma$ annihilate in photons (mostly)

Entropy conservation: $g_*^s T^3 a^3|_{\text{before}} = g_*^s T^3 a^3|_{\text{after}}$

$\Gamma_{\text{ann}} \sim \alpha^2 m_e \gg H(T \sim m_e)$ annihilations are “instantaneous”: $a_{\text{before}} = a_{\text{after}}$

Neutrinos are already decoupled:



$$\left(2 + 4 \frac{7}{8}\right) T_{\text{before}}^3 = 2 T_{\text{after}}^3$$

$$\frac{T_\nu}{T_\gamma} = \frac{T_{\text{before}}}{T_{\text{after}}} = \left(\frac{4}{11}\right)^{1/3}$$

$$\left. \frac{n_{\nu i}}{n_\gamma} \right|_{\text{today}} = \frac{3}{11}$$

entropy of electrons transferred to photons
(% correction due to residual $e^+e^- \rightarrow \nu\bar{\nu}$)

TODAY: $T_\nu \sim T_\gamma / 1.4 \sim 1.96 \text{ K}$ and $n_\nu \sim \text{O}(100) \text{ cm}^{-3}$!!

- Number density

At present $112 (\nu + \bar{\nu}) \text{ cm}^{-3}$ per flavour

- Energy density

Contribution to the energy density of the Universe

$$\Omega_\nu h^2 \simeq 1.7 \times 10^{-5} \quad \text{Massless}$$

$$\Omega_\nu h^2 = \frac{\sum_i m_i}{93.2 \text{ eV}} \quad \text{Massive}$$

$m_\nu \gg T$

BBN – BIG BANG NUCLEOSYNTHESIS

- An astonishingly successful fruit of the **marriage between the TWO STANDARD MODELS** of particle physics and cosmology
- **TWO** crucial pieces of information on the universe:
 - i) **how much "ordinary" matter** (i.e. baryonic matter, e.g. protons, neutrons) is present in the universe;
 - ii) are there **new (non SM) light particles** other than neutrinos present in the early universe?

When did BBN start?

first nucleus. Deuterium: $n p \leftrightarrow D \gamma$ $B_D = m_n + m_p - m_D = 2.2 \text{ MeV}$

Equilibrium: $\mu_n + \mu_p = \mu_D$ $\mu_\gamma = 0$ due to other processes, e.g. $e^+ e^- \leftrightarrow \gamma \gamma$



$$\frac{n_D}{n_n n_p} = \frac{n_D^{eq}}{n_n^{eq} n_p^{eq}} \simeq \frac{3}{4} \left(\frac{4\pi}{m_p T} \right)^{3/2} e^{B_D/T}$$

OUTPUT PARAMETER



$$n_p \simeq n_n \simeq n_b, \quad n_\gamma \sim T^3$$

$$\frac{n_D}{n_b} \sim \left(\frac{n_b}{n_\gamma} \right) \left(\frac{T}{m_p} \right)^{3/2} e^{B_D/T}$$

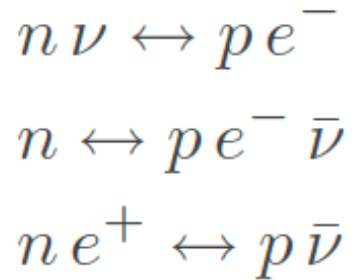
$O(10^{-10})$

The large entropy density (n_γ/n_b) delays D production from $T \sim B_D$ to $T \sim 0.1 \text{ MeV}$

Helium abundance

When nucleosynthesis starts, all neutrons go to Helium-4 (excellent approximation)

How many neutrons are around at $T \sim 0.1 \text{ MeV}$?



$$\frac{n_n}{n_p} = e^{-\Delta m/T} e^{(\mu_n - \mu_p)/T}$$

1.293 MeV

$$\frac{\mu_n}{T} \simeq \frac{\mu_p}{T} \sim \frac{n_b}{n_\gamma} \sim 10^{-10}$$

$$l'_W = H$$

$$T_W = \left(0.33 \frac{g_*^{1/2}}{G_F^2 M_p} \right)^{1/3} \sim 0.8 \text{ MeV}$$

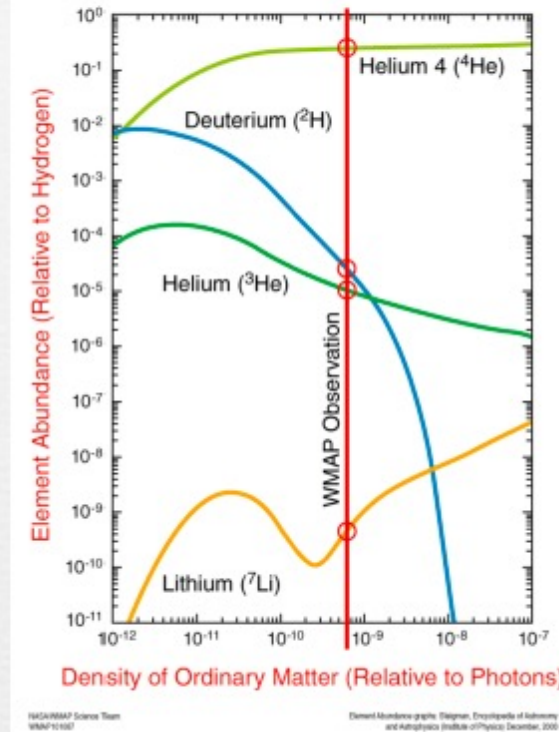
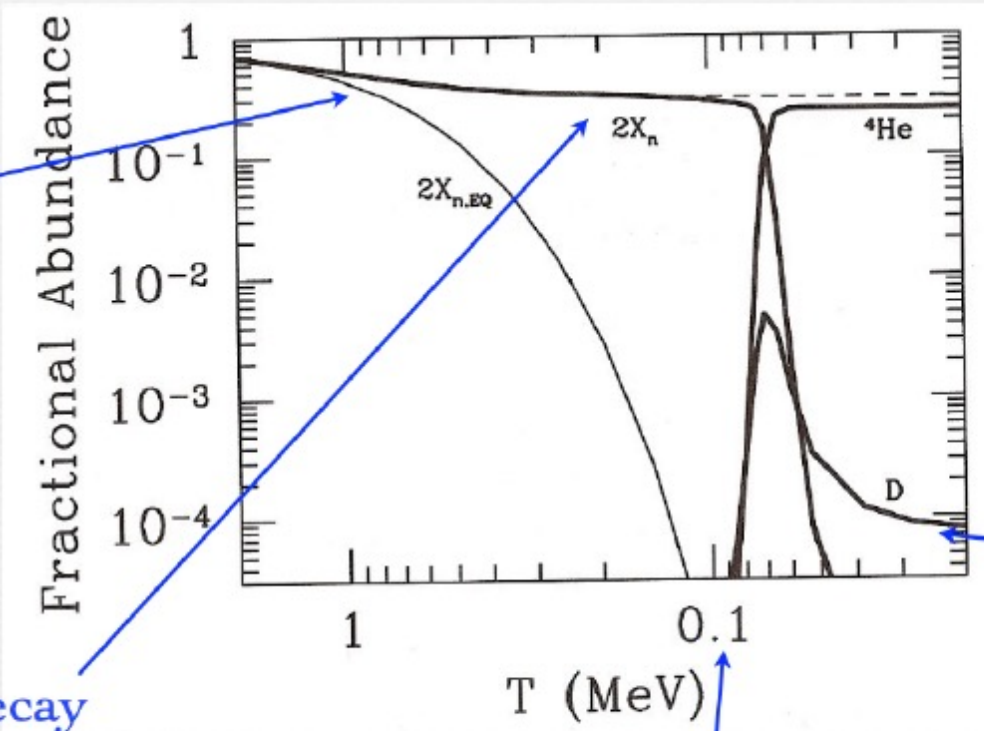
**OUTPUT
PARAMETER**

INPUT PARAMETER - if we extract the exp. value of G_F from the measurement of the neutron lifetime

$$\left. \frac{n_n}{n_p} \right|_{T=0.8 \text{ MeV}} \simeq \frac{1}{6} \xrightarrow[\text{Boltzmann eq.}]{\text{n-decay}} \left. \frac{n_n}{n_p} \right|_{T=0.1 \text{ MeV}} \simeq \frac{1}{8}$$

~ all neutrons finally go in ${}^4\text{He}$

$$X_4 \equiv \frac{4 n_{{}^4\text{He}}}{n_b} = \frac{2 n_n}{n_n + n_p} \simeq 0.22$$



residual D
abundance
 $D p \rightarrow {}^3\text{He} \gamma$
inefficient at low n_b/n_γ

$$T_W = \left(0.33 \frac{g_*^{1/2}}{G_F^2 M_p} \right)^{1/3} \sim 0.8 \text{ MeV}$$

$$g_* = g_*^{\text{standard}} + \Delta g_*$$

$$T_W = T_W^{\text{standard}} + \Delta T_W$$

$$\frac{n_n}{n_p} = \left. \frac{n_n}{n_p} \right|_{\text{standard}} + \Delta \frac{n_n}{n_p}$$

$$X_4 = X_{4,\text{st.}} + \Delta X_4$$

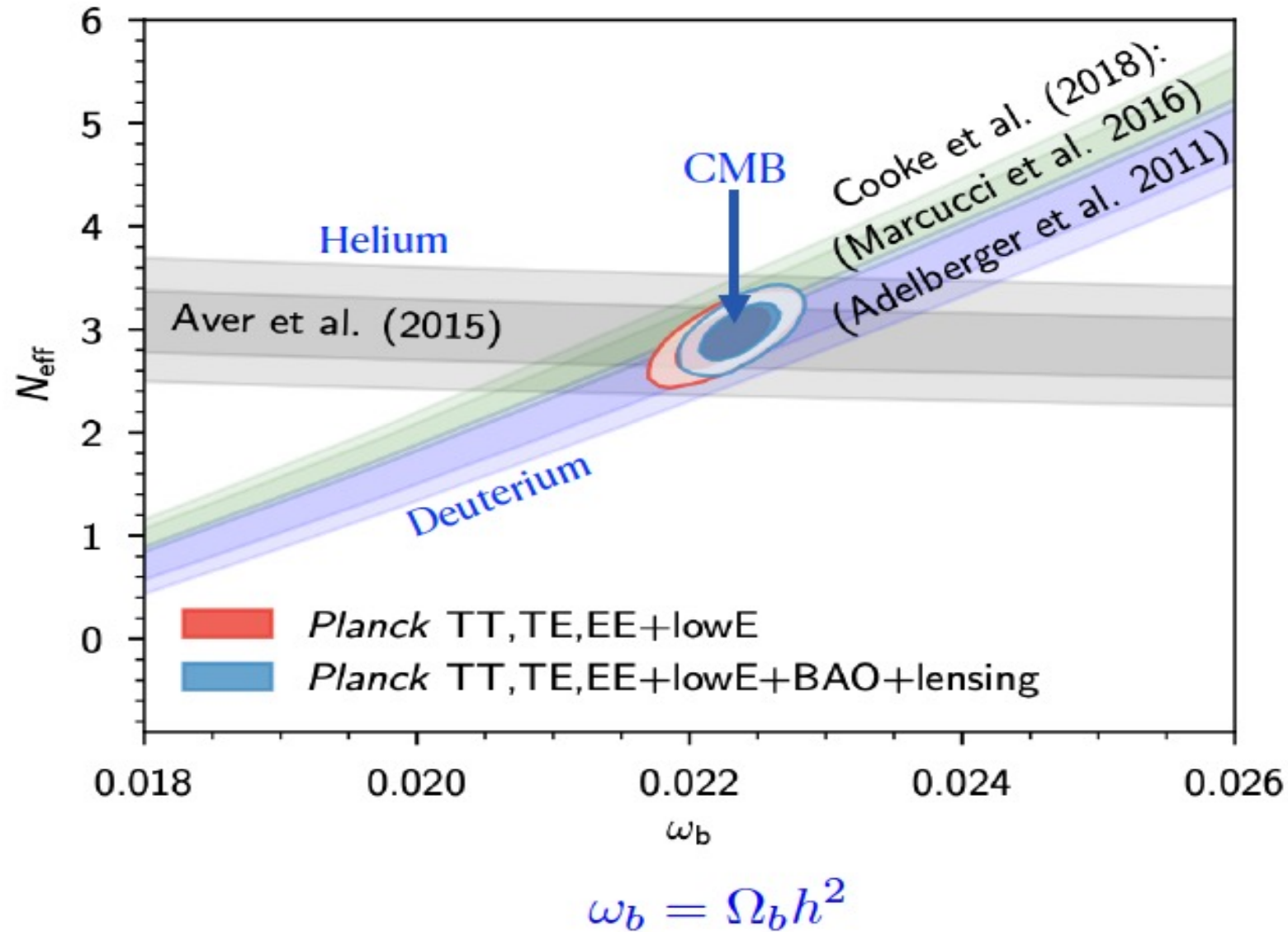


$$\Delta N_\nu < 0.1$$

bound on extra relativistic species

BBN is a powerful probe of n_b/n_γ and of $H(T \sim 1\text{MeV})$!

CMB+BBN: Baryons make up only ~ 4%



MICRO

GWS STANDARD MODEL

UNIVERSE EXPANSION +
WEAK INTERACTIONS
1 sec. after BB



MACRO

HOT BIG BANG STANDARD MODEL



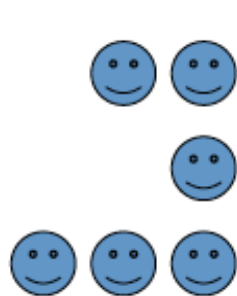
NUCLEOSYNTHESIS

NUMBER OF BARYONS and OF
NEUTRINO SPECIES →
CONFIRMED FROM CMB 350000
YEARS AFTER BB

BUT ALSO



Independent
confirmation from
the study of the CMB



-COSMIC MATTER-ANTIMATTER ASYMMETRY

New source(s) of CP violation

-INFLATION ???

New scalar potential

- DARK MATTER + DARK ENERGY

New particles and
interactions

OBSERVATIONAL EVIDENCE OF NEW PHYSICS

BEYOND THE STANDARD

THE COSMIC MATTER-ANTIMATTER ASYMMETRY PUZZLE:

-why only baryons

-why $N_{\text{baryons}}/N_{\text{photon}} \sim 10^{-10}$

- NO EVIDENCE OF ANTIMATTER WITHIN THE SOLAR SYSTEM
- ANTIPROTONS IN COSMIC RAYS: IN AGREEMENT WITH PRODUCTION AS SECONDARIES IN COLLISIONS
- IF IN CLUSTER OF GALAXIES WE HAD AN ADMIXTURE OF GALAXIES MADE OF MATTER AND ANTIMATTER \longrightarrow THE PHOTON FLUX PRODUCED BY MATTER-ANTIMATTER ANNIHILATION IN THE CLUSTER WOULD EXCEED THE OBSERVED GAMMA FLUX
- IF $N_{\text{ba.}} = N_{\text{antibar}}$ AND NO SEPARATION WELL BEFORE THEY DECOUPLE WE WOULD BE LEFT WITH $N_{\text{bar.}}/N_{\text{photon}} \ll 10^{-10}$
- IF BARYONS-ANTIBARYONS ARE SEPARATED EARLIER \longrightarrow DOMAINS OF BARYONS AND ANTIBARYONS ARE TOO SMALL TODAY TO EXPLAIN SEPARATIONS LARGER THAN THE SUPERCLUSTER SIZE



○ ONLY MATTER IS PRESENT

○ HOW TO DYNAMICALLY PRODUCE A BARYON-ANTIBARYON ASYMMETRY STARTING FROM A SYMMETRIC SITUATION

$$\text{WMAP+BBN: } B = \frac{n_b - n_{\bar{b}}}{s} = (8.6 \pm 0.4) \times 10^{-11}$$

Evidences of a baryon-asymmetric Universe

Direct searches:

Cosmic rays at $E > O(100 \text{ MeV})$ probe galactic scales, $r_{\text{Gal}} \sim 30 \text{ kpc}$

$$\frac{n_{\bar{p}}}{n_p} \sim 3 \cdot 10^{-4} \quad \text{compatible with secondary production in } pp \rightarrow ppp\bar{p}$$

Indirect searches:

Look for: 1) γ 's from $b\bar{b}$ annihilations;

2) CMB spectrum distortions due to Compton scattering.

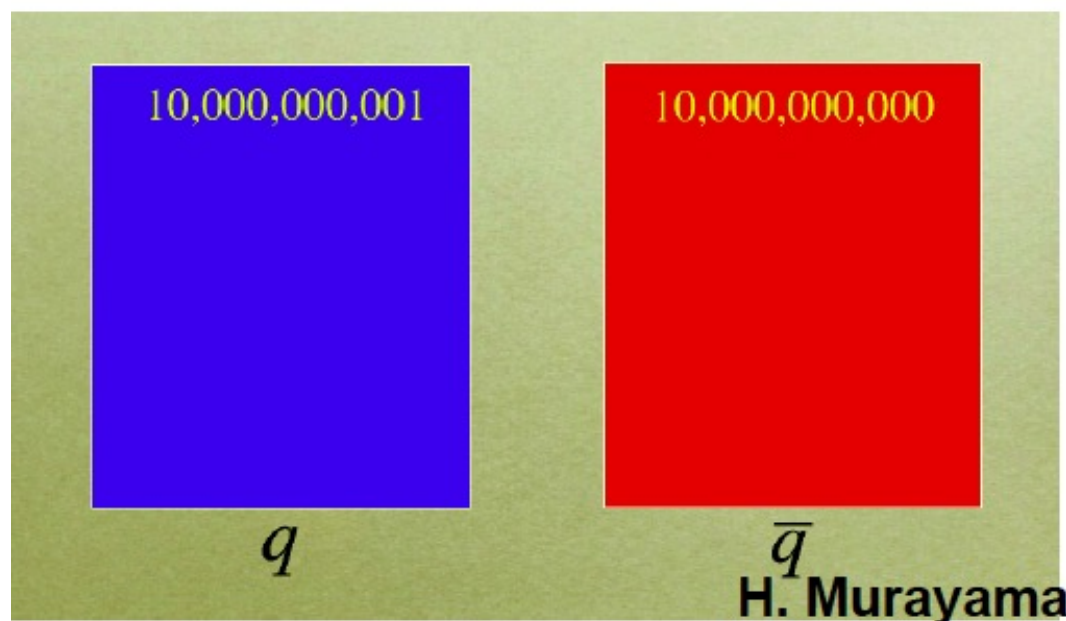
no signal of galaxy-antigalaxy annihilation from Virgo cluster, or X-rays emitting clusters: $r_{\text{Clust}} \sim 10 \text{ Mpc}$ (Steigman '76)

CMB+diffuse gamma ray background constrain matter-antimatter islands to be larger than $\sim O(10^3 \text{ Mpc}) \sim 1/H_0$ (Cohen, De Rujula, Glashow '98)

THE COSMIC MATTER-ANTIMATTER ASYMMETRY PUZZLE:

-why only baryons

-why $N_{\text{baryons}}/N_{\text{photon}} \sim 10^{-10}$



Peculiar initial conditions?

Or is there a **dynamics** allowing for matter to prevail over antimatter starting from a perfectly **symmetric situation in matter – antimatter** content of the plasma after inflation?

Sakharov's conditions

necessary conditions for a dynamical baryogenesis

- **B-violating interactions** (the global symmetry B-number is NOT an exact symmetry of Nature)

- **C and CP-violating interactions**

$$C: \Gamma[i \rightarrow f] = \Gamma[\bar{i} \rightarrow \bar{f}]$$

$$\text{no net result: } n_b - n_{\bar{b}} = 0$$

$$CP \equiv T: \Gamma[i \rightarrow f] = \Gamma[f \rightarrow i]$$

- the B-violating interactions giving rise to ΔB must **depart from thermal equilibrium** right after the ΔB production

th. equilibrium: $n_{b_i} = n_{b_i}(E_i, \mu_i, T)$
 $n_{\bar{b}_i} = n_{\bar{b}_i}(E_i, -\mu_i, T)$ + B-violation + charge neutrality



$$\mu_i = 0$$


$$n_{b_i} = n_{\bar{b}_i}$$

Standard Model: B-violation

B (and L) are **accidental symmetries** of the SM: $\partial_\mu J_{B(L)}^\mu = 0$

they are broken at the quantum level by **triangle anomalies**:

$$\partial_\mu J_B^\mu = \partial_\mu J_L^\mu = -\frac{3}{32\pi^2} g^2 F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \quad (+ \text{U(1)...})$$

 dual field strength tensor $\frac{1}{2} \epsilon^{\mu\nu\lambda\rho} F_{\lambda\rho}^a$

$$\Delta B = 3 \Delta N_{cs} = \Delta L$$

$$\left(N_{cs}(t) = \frac{g^2}{96\pi^2} \int d^3x \epsilon_{abc} \epsilon^{ijk} A_i^a A_j^b A_k^c \right)$$

$$B = \int d^3x J_B^0$$

in vacuum to vacuum transitions ΔN_{cs} is integer.

effective interaction: $O_{B+L} = \prod_{i=1 \dots 3} (q_{L_i} q_{L_i} q_{L_i} l_{L_i})$

$$\Delta(B + L) = 6, \quad \Delta(B - L) = 0$$

Sphalerons

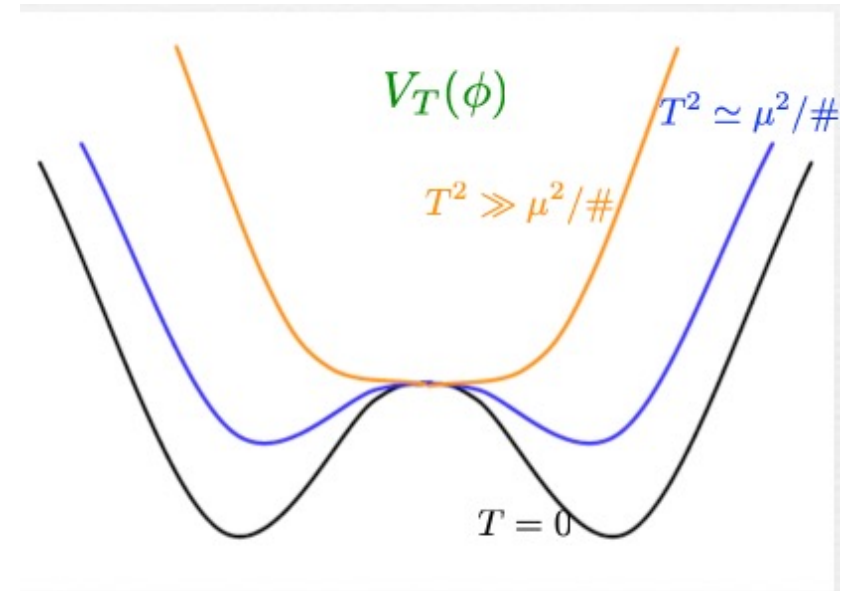
Higgs expectation value

different vacua are separated by an energy barrier $E_{sp} = \frac{4\pi v}{g} B(\lambda/g) = O(10 \text{ TeV})$

$T = 0$: vacuum tunnelling $\Gamma \sim e^{4\pi/\alpha_w} = O(10^{-165})$

$T \neq 0$: thermal fluctuations $\Gamma \sim e^{-\frac{E_{sp}(T)}{T}}$

$E_{sp}(T) \propto v(T) \rightarrow 0$ at high T!



in equilibrium for $T_{EWPT} \sim 100 \text{ GeV} < T < O(10^{12}) \text{ GeV}$

SM FAILS TO GIVE RISE TO A SUITABLE COSMIC MATTER-ANTIMATTER ASYMMETRY

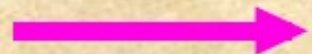
- NOT ENOUGH CP VIOLATION IN THE SM
NEED FOR **NEW SOURCES OF CPV IN
ADDITION TO THE PHASE PRESENT IN
THE CKM MIXING MATRIX**
- FOR $M_{\text{HIGGS}} > 80 \text{ GeV}$ THE ELW. PHASE TRANSITION
OF THE SM IS A SMOOTH CROSSOVER

NEED **NEW PHYSICS BEYOND SM**. IN PARTICULAR,
FASCINATING POSSIBILITY: THE ENTIRE MATTER IN
THE UNIVERSE ORIGINATES FROM THE
SAME MECHANISM RESPONSIBLE FOR THE
EXTREME SMALLNESS OF m_ν

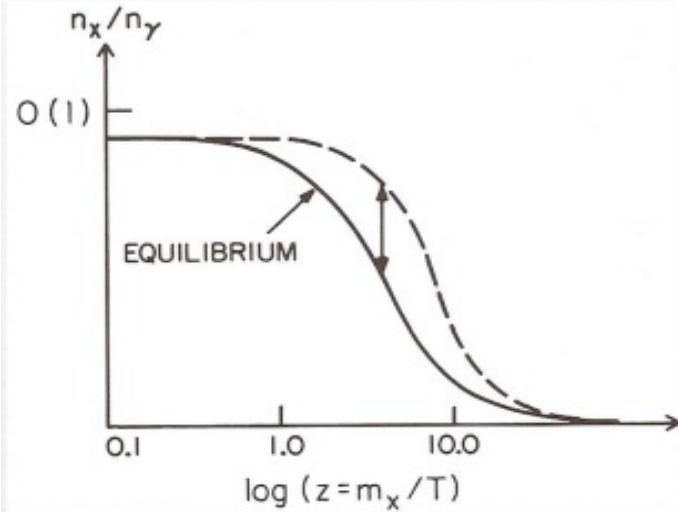
MATTER-ANTIMATTER ASYMMETRY ↔ NEUTRINO MASSES CONNECTION: BARYOGENESIS THROUGH LEPTOGENESIS

- Key-ingredient of the SEE-SAW mechanism for neutrino masses: **large Majorana mass for RIGHT-HANDED neutrino**
- In the early Universe the heavy RH neutrino decays with Lepton Number violation; if these decays are accompanied by a new source of CP violation in the leptonic sector, then

VANILLA LEPTOGENESIS !

 it is possible to create a lepton-antilepton asymmetry at the moment RH neutrinos decay. Since SM interactions preserve Baryon and Lepton numbers at all orders in perturbation theory, but violate them at the quantum level, such **LEPTON ASYMMETRY** can be converted by these purely quantum effects into a BARYON-ANTIBARYON ASYMMETRY (**Fukugita-Yanagida mechanism for leptogenesis**)

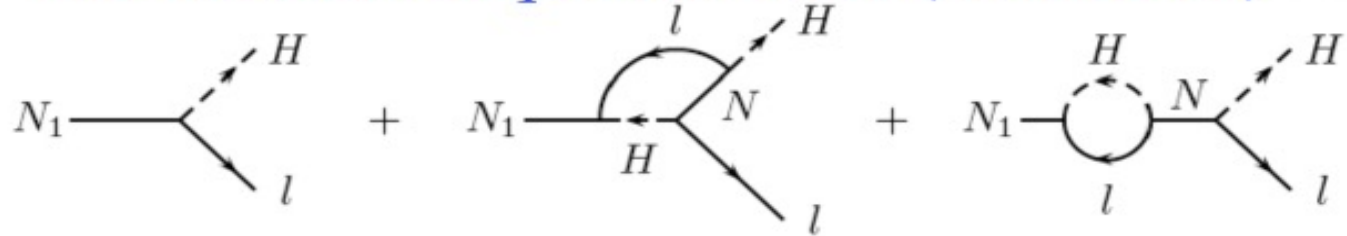
Out-of-equilibrium decay



$T_{\text{dec}} < M$: inverse decays are out of eq.

$$\epsilon = \frac{\Gamma(N_1 \rightarrow H l) - \Gamma(\bar{N}_1 \rightarrow \bar{H} \bar{l})}{\Gamma(N_1 \rightarrow H l) + \Gamma(\bar{N}_1 \rightarrow \bar{H} \bar{l})}$$

CP-violation is a quantum effect (interference)



$$L = \frac{n_l - n_{\bar{l}}}{s} \sim \frac{\epsilon n_N}{g_* n_N} = \frac{\epsilon}{g_*} \quad (\text{fully efficient})$$

$$B - L = -L = -K \frac{\epsilon}{g_*} \quad (\text{realistic}) \quad K = \text{efficiency factor} < 1 \quad (\text{need Boltz. eq.})$$

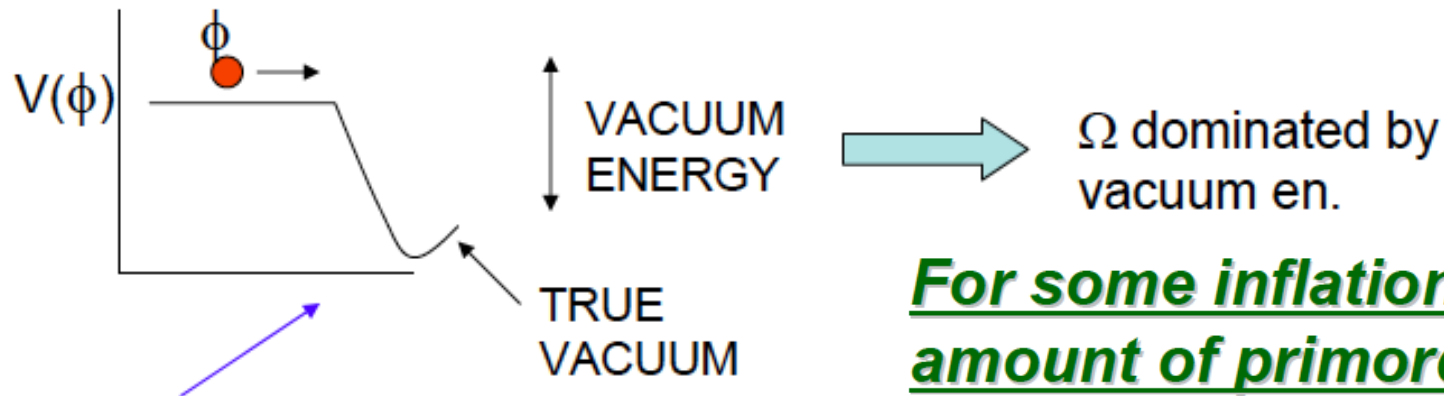
INFLATION

SEVERE
COSMOLOGICAL
PROBLEMS



- CAUSALITY
(isotropy of CMBR)
- FLATNESS
(Ω close to 1 today)
- AGE OF THE UNIV.
- PRIMORDIAL MONOPOLES

COMMON SOLUTION FOR THESE PROBLEMS
VERY FAST (EXPONENTIAL) EXPANSION IN THE UNIV.



For some inflationary models → large amount of primordial gravitational waves

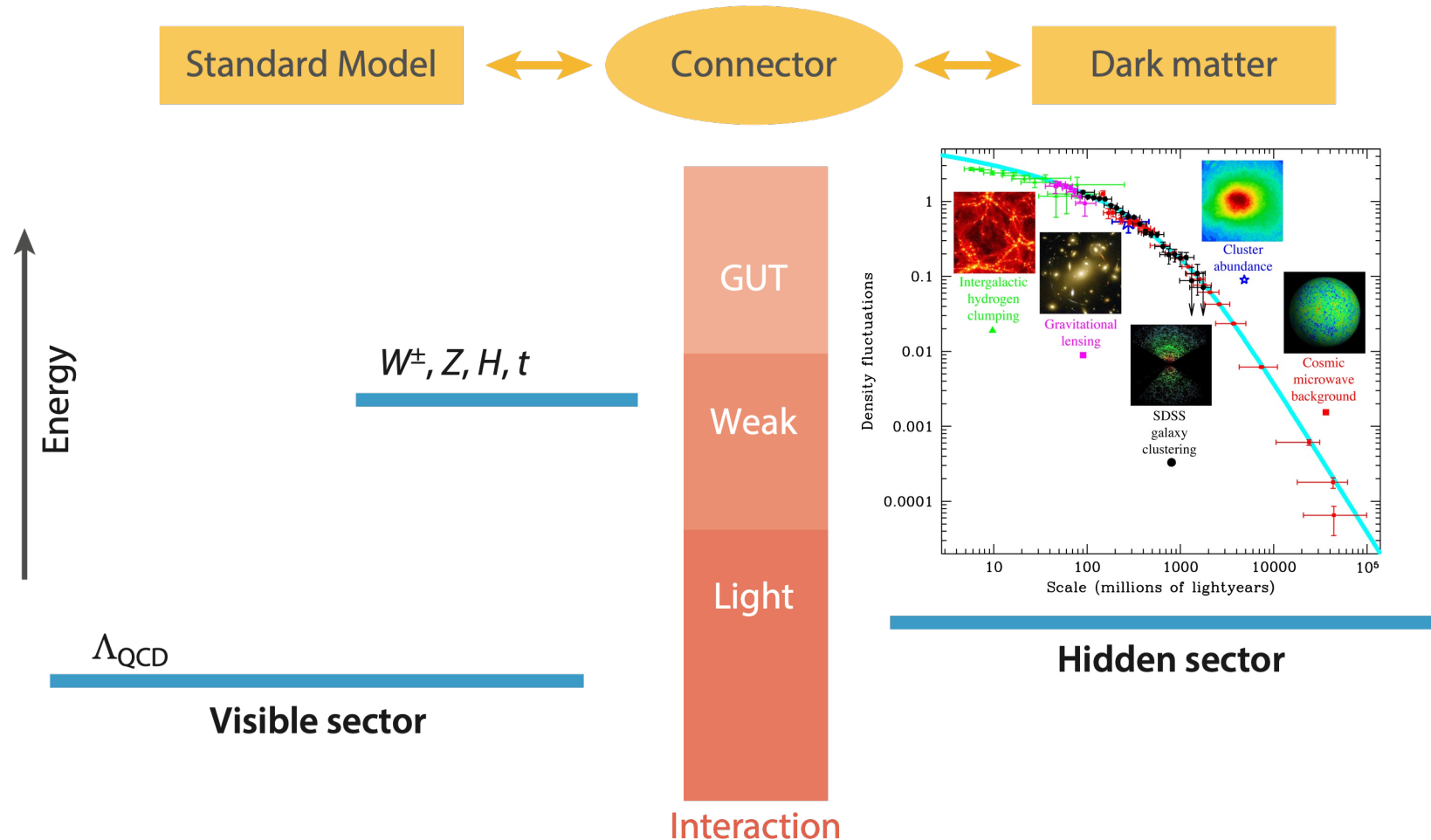
NO WAY TO GET AN INFLATIONARY SCALAR POTENTIAL IN THE SM, UNLESS THERE EXISTS A NON-MINIMAL COUPLING OF THE SM HIGGS FIELD TO GRAVITY

DARK MATTER

The Challenge.

All known properties of dark matter are via the gravitational interaction.

- Gravity is **weak**.
- Gravity gives the **gross properties** of dark matter — density and large-scale clustering.
- Learning about particle properties will require stronger-than-gravitational interactions.



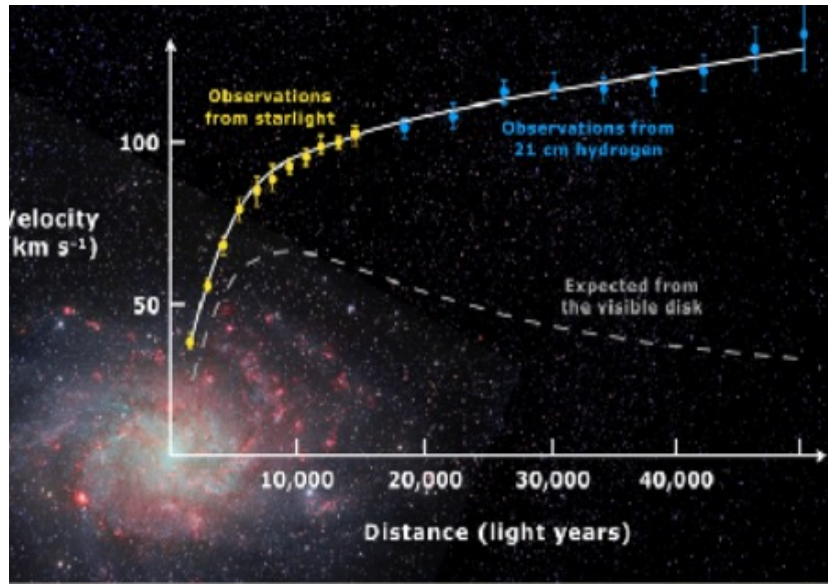
Inadequacy of the “ordinary” BARYONIC MATTER

- **CLUSTER SCALES:**

i) Already ~90 years ago (1933) F. **Zwicky** pointed out that to account for the velocity dispersion of the galaxies in the COMA **cluster** some large amount of new non-shining “**DUNKLE MATERIE**” **DARK MATTER (DM)**, was needed; ii)

Nowadays, from the observation of the **X-ray emission**, we infer that the temperature of the cluster gas is **TOO** high → it requires a **factor 5** more matter than the visible baryonic matter

- **GALACTIC SCALES:** but the existence of (a large amount of) NON-BARYONIC MATTER got firm credibility only ~40 years after Zwicky’s claim → Vera RUBIN (with K. Ford et al) ~70’s pointed out that stars in the outer part of galaxies are **faster** than expected



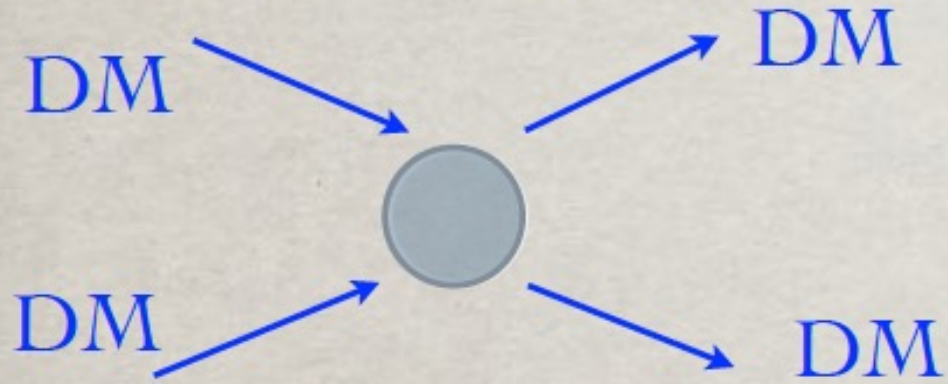
$$v_c^2 \propto G_N \frac{M(r)}{r} \propto \frac{M_{tot}}{r}$$

But instead it is constant ! Need

$$M(r) \propto r, \text{ i.e. } \rho_{DM} \propto r^{-2}$$

DM-DM INTERACTION

Self-interaction:



Bullett cluster bound on
self-interaction:

$$\sigma \leq 1.7 \times 10^{-24} \text{ cm}^2 \sim 10^9 \text{ pb} \quad (m = 1 \text{ GeV})$$

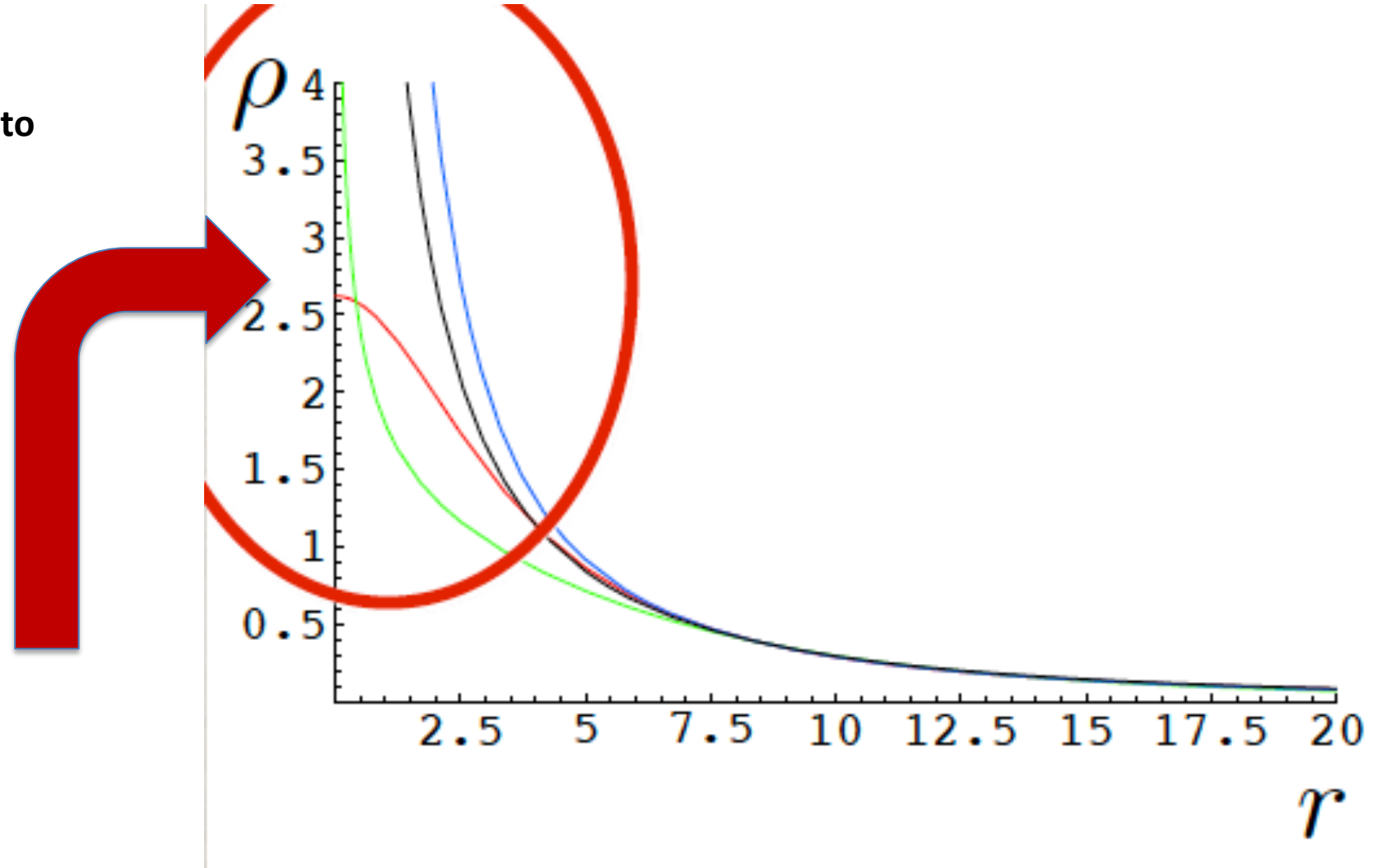
[Markevitch et al 03]



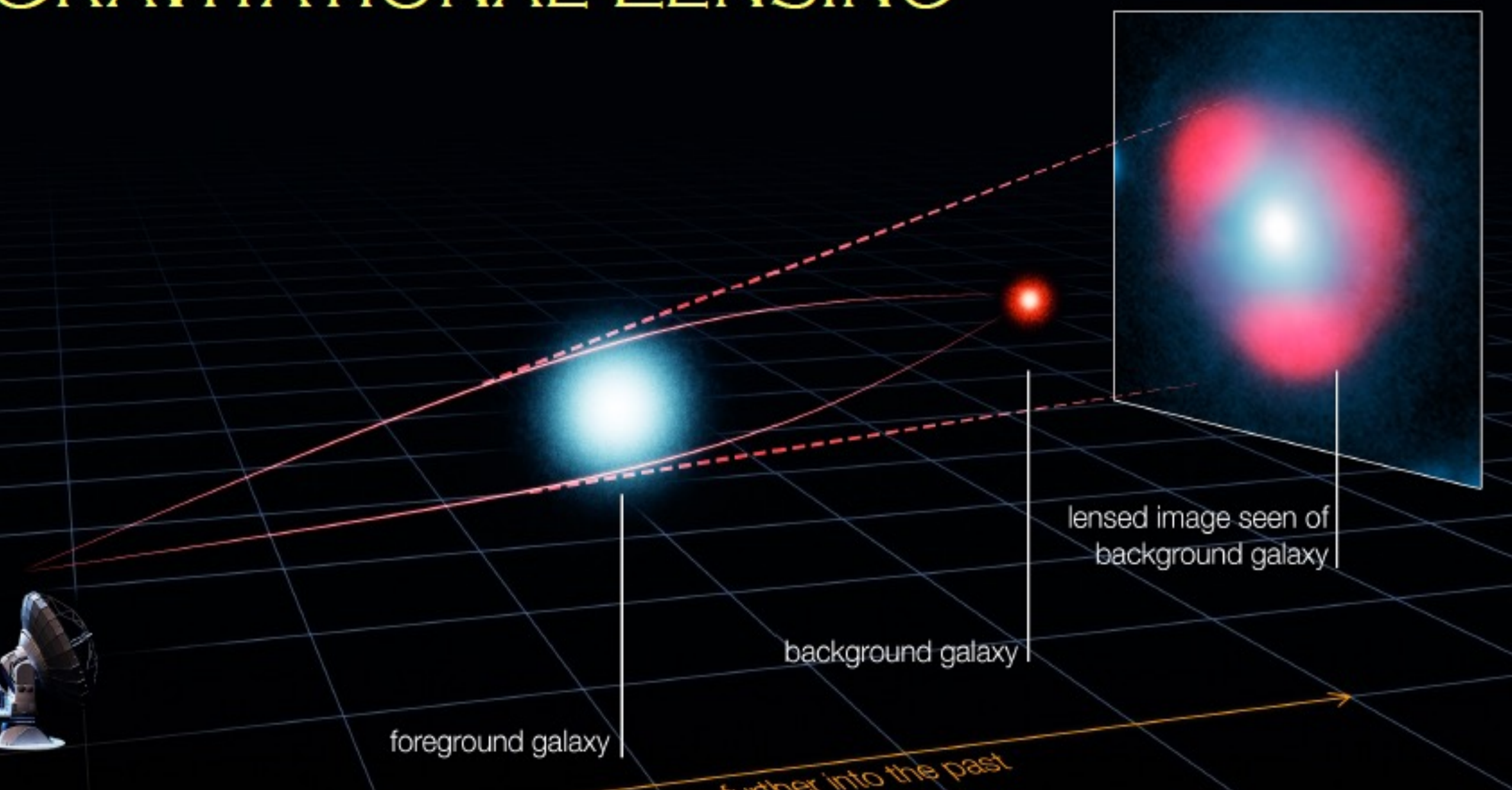
Galactic scales: **DM density profiles**

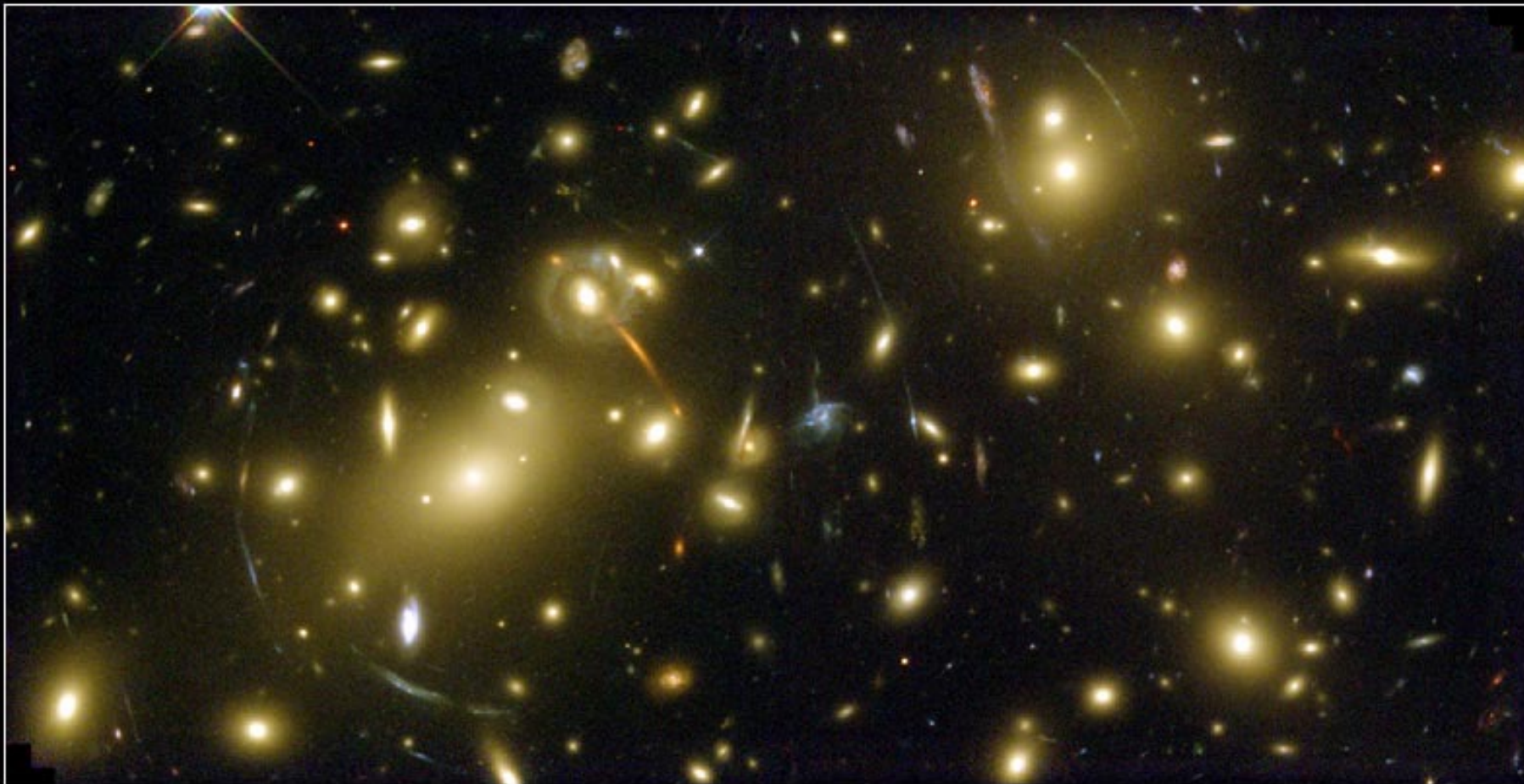
There exist **several DM density profiles** (related to data and/or numerical simulations) : Isothermal, NFW, Moore, Einasto, Kratsov, etc.

The **main difference** among such density profiles concerns the behaviour at the **centre** of the galaxy, either **cusped** or **cored**



GRAVITATIONAL LENSING





Galaxy Cluster Abell 2218

HST • WFPC2

GRAVITATIONAL LENSING

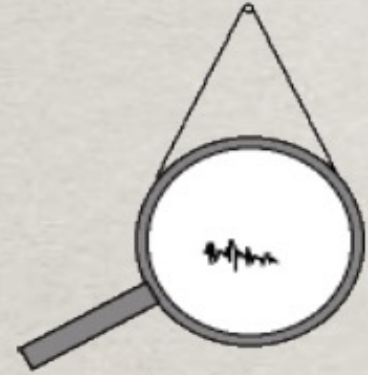
A LARGE AMOUNT OF MASS BETWEEN THE BACKGROUND GALAXIES AND US
CAN BE INFERRED BY THE LENSING EFFECT

N. Fornengo, Grav. Waves and Cosmology, Varenna, 2017

QUANTUM FLUCTUATION

$$\delta\varphi = \frac{H}{2\pi}$$

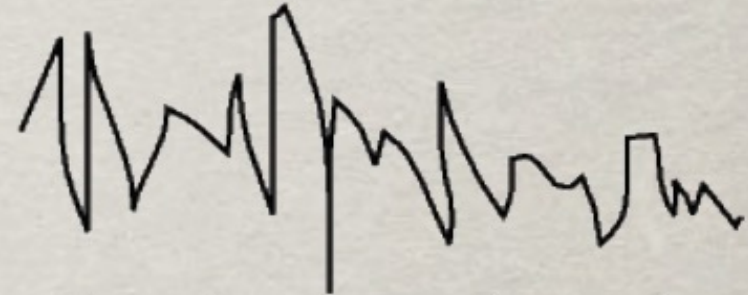
$$\Delta t \Delta E \geq \hbar$$



ultra-tiny
quantum
fluctuations

Making the “galaxy seeds”
with inflation

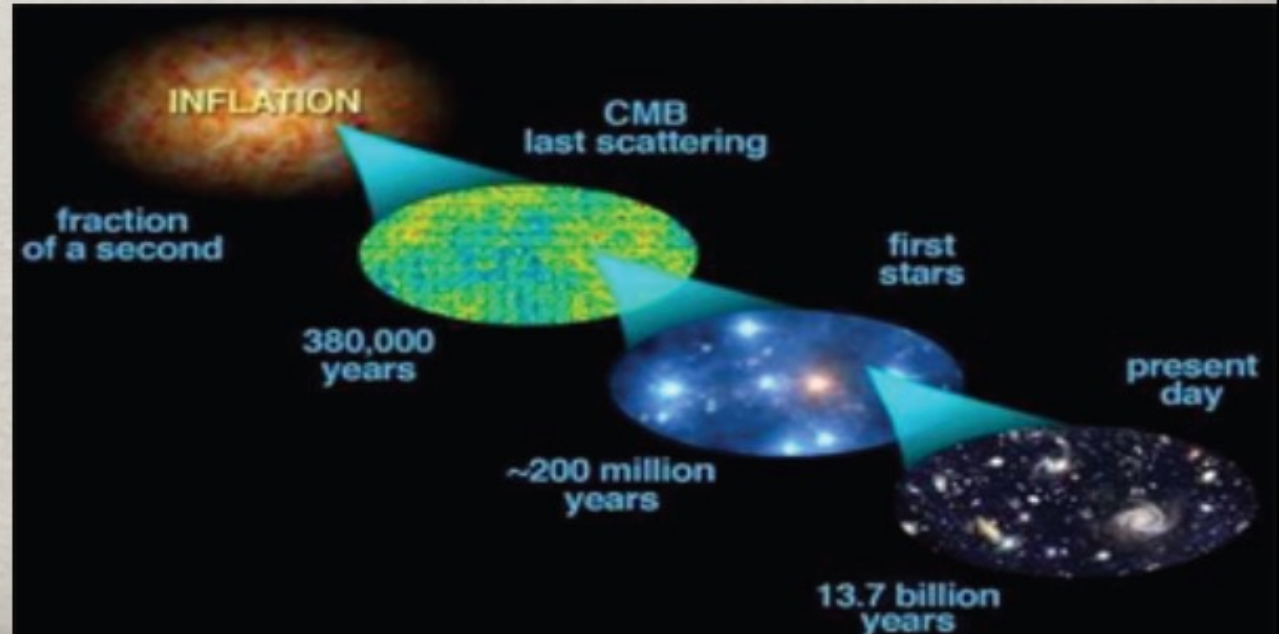
Time
→



become...

large lumps seen in cosmic
microwave background

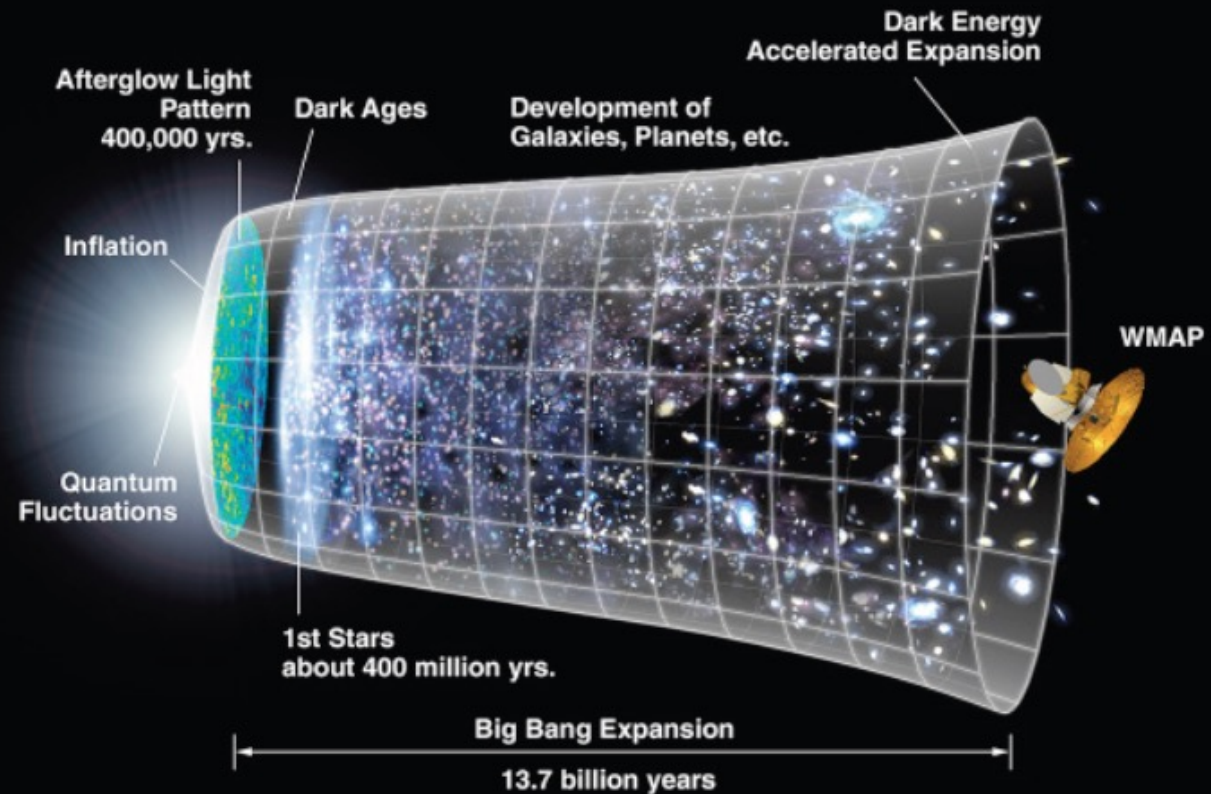
Gravity stretches
and amplifies
the microscopic
fluctuations to
macroscopic scales !!!



The need of NON-BARYONIC MATTER!

STRUCTURE FORMATION
from **PRIMORDIAL**
DENSITY FLUCTUATIONS
requires the presence of a
(large) amount of
NON-BARYONIC
MATTER

FOLLOWING THE FLUCTUATIONS

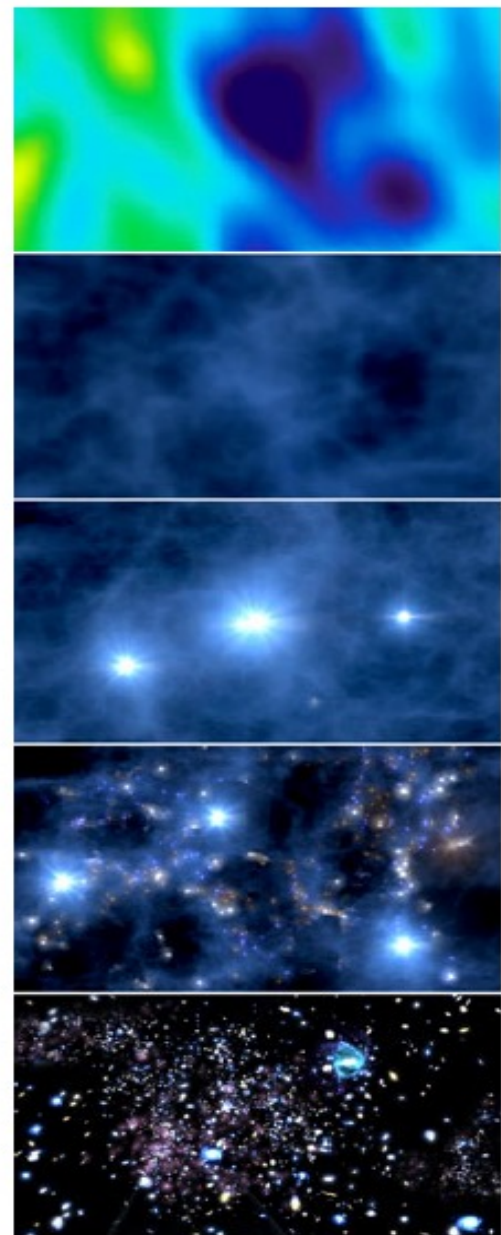
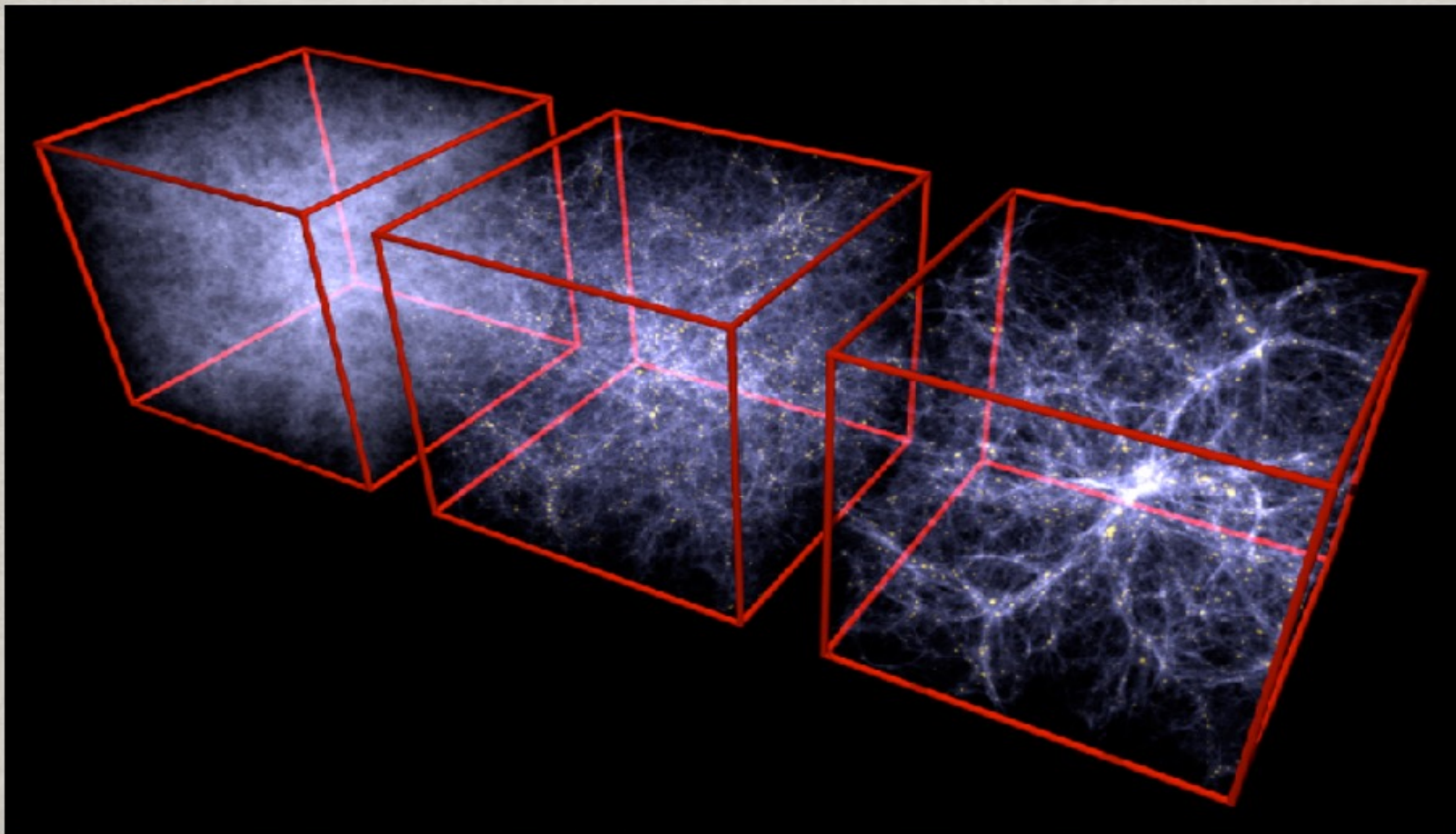


These small fluctuations are amplified by gravity & are the origin of the structure we see today

STRUCTURE FORMATION

V. Springel @MPA Munich

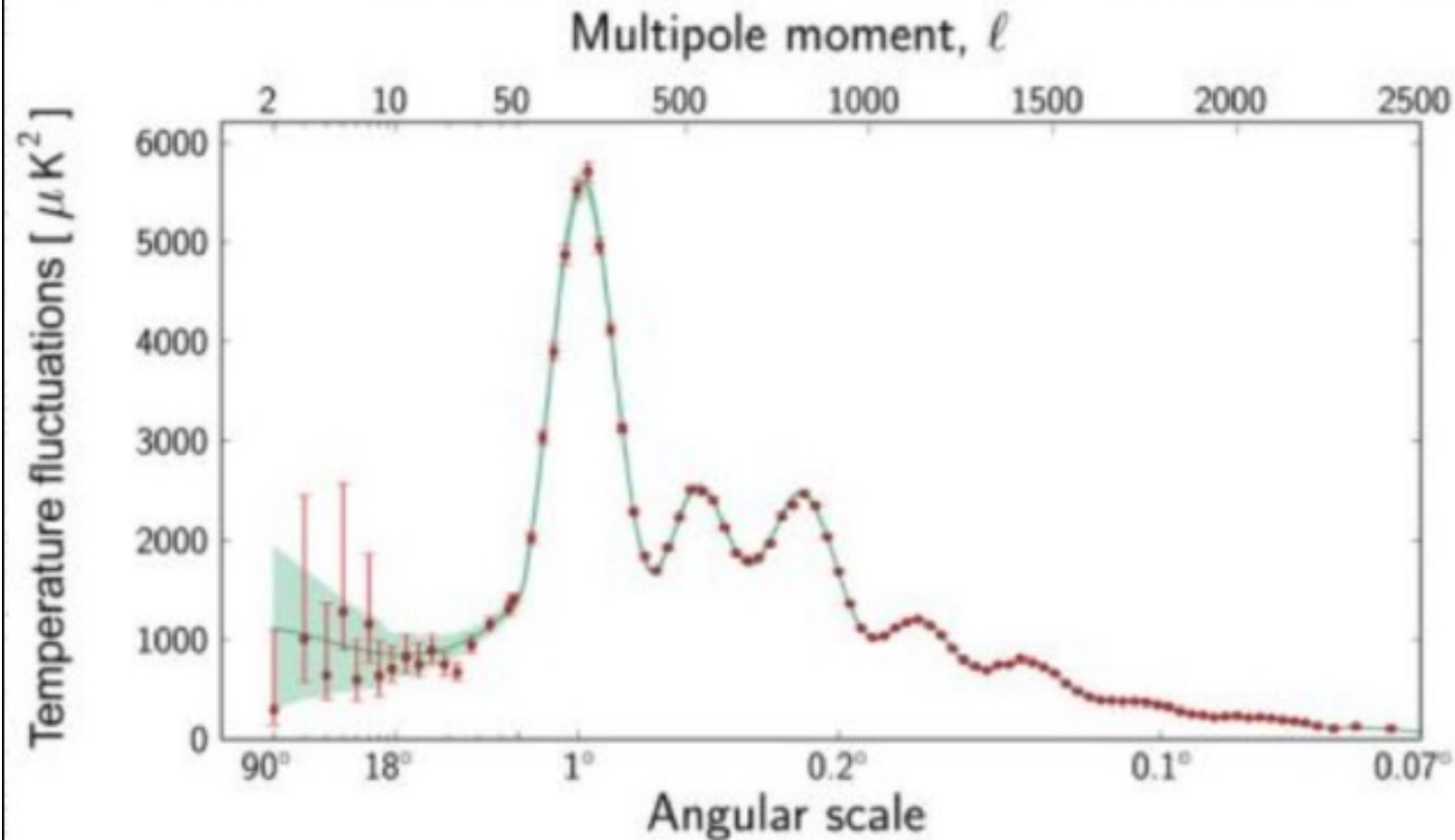
Yoshida et al 03



DM needs to be (mainly) cold
and (mainly) non-collisional

The need for a large amount of **NON-BARYONIC MATTER** from the study of the **Cosmic Microwave Background (CMB)**

Planck's power spectrum of temperature fluctuations in the CMB at different angular scales on the sky.



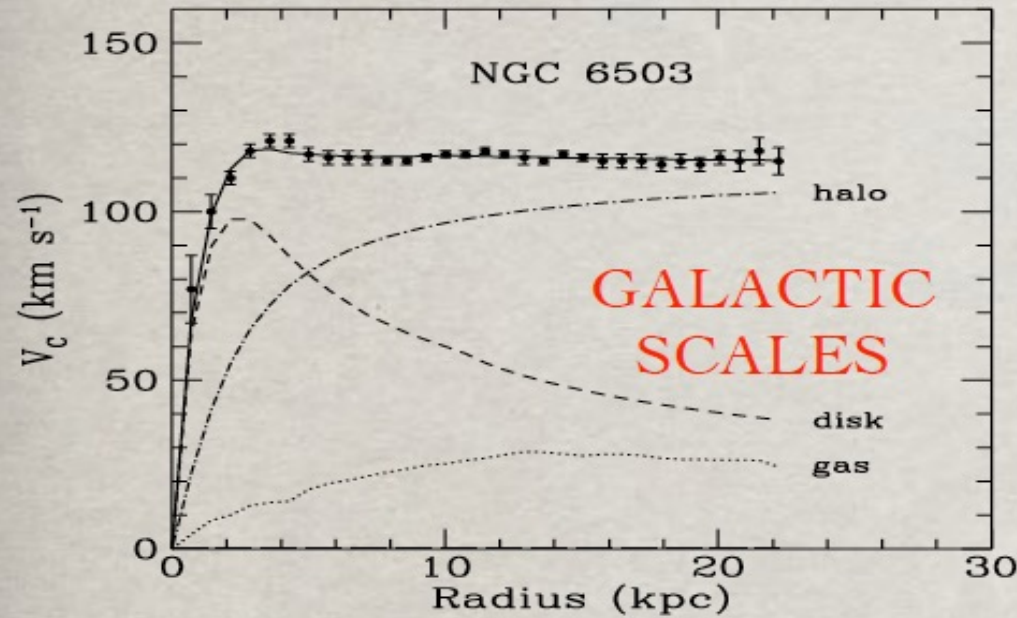
Red dots are the Planck data.

The peak at 1 degree is consistent with a **flat geometry of the universe**

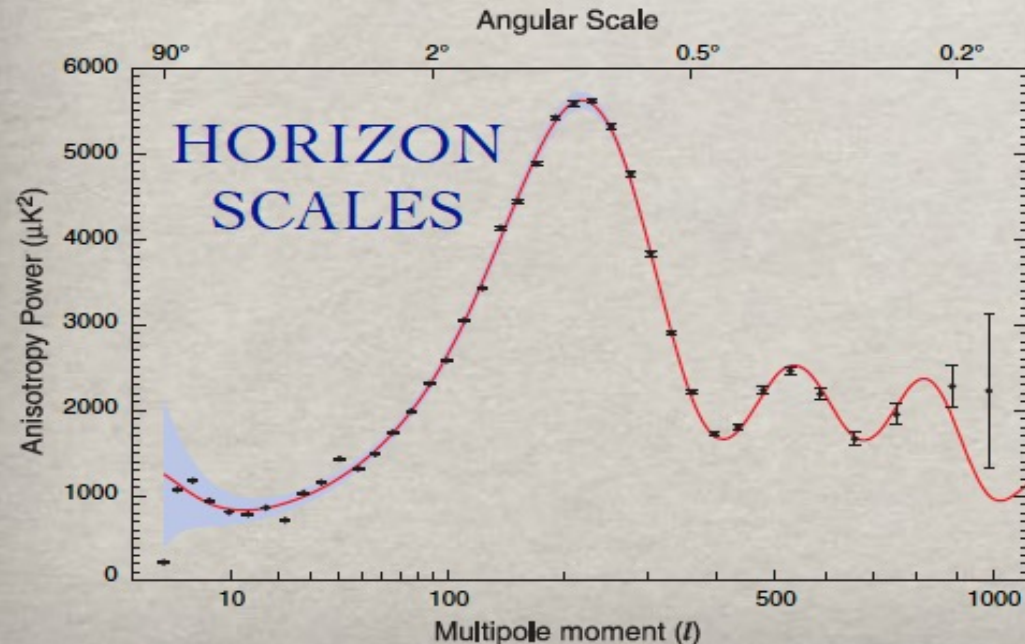
the height of the 2nd peak with **5% (baryonic matter)**

the 2nd and 3rd peaks with **26% dark matter**

DARK MATTER EVIDENCE



GALACTIC
SCALES



Particles	Ωh^2	Type
Baryons	0.0224	Cold
Neutrinos	< 0.01	Hot
Dark Matter	0.1-0.13	Cold

The Λ CDM Model

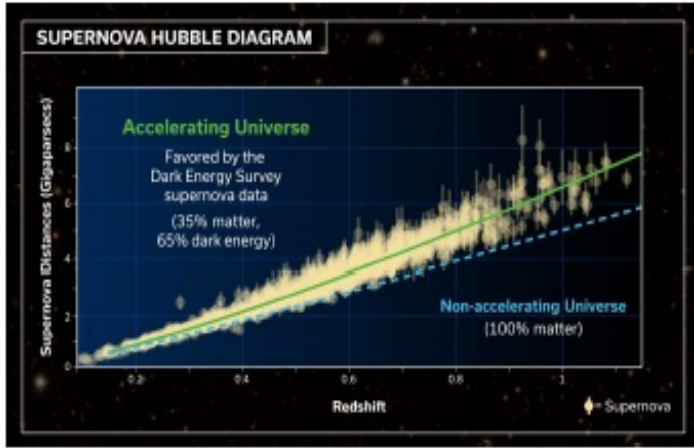
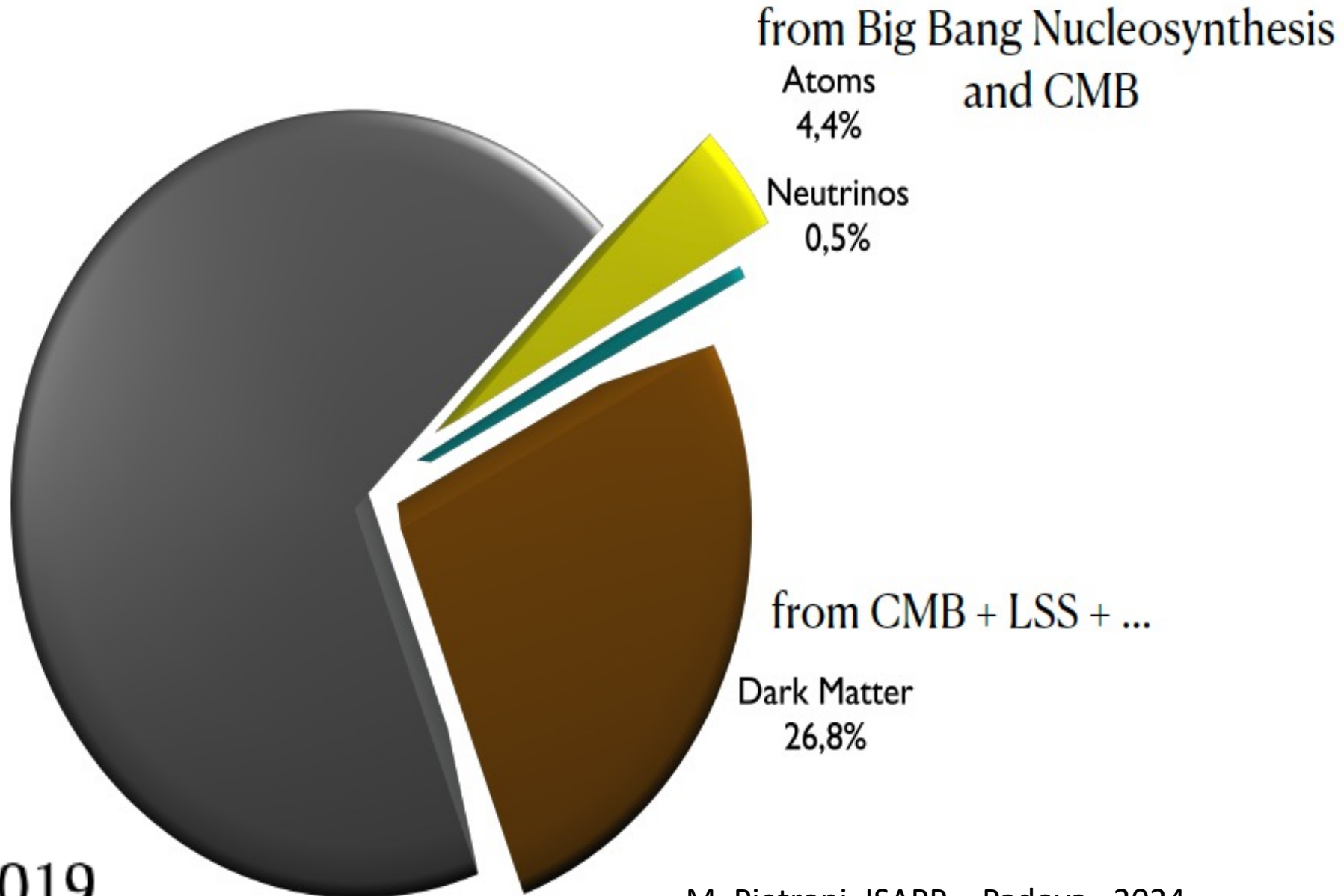


Image: DES collaboration

$d_L(z)$ from SNe Ia

Λ
68,3%

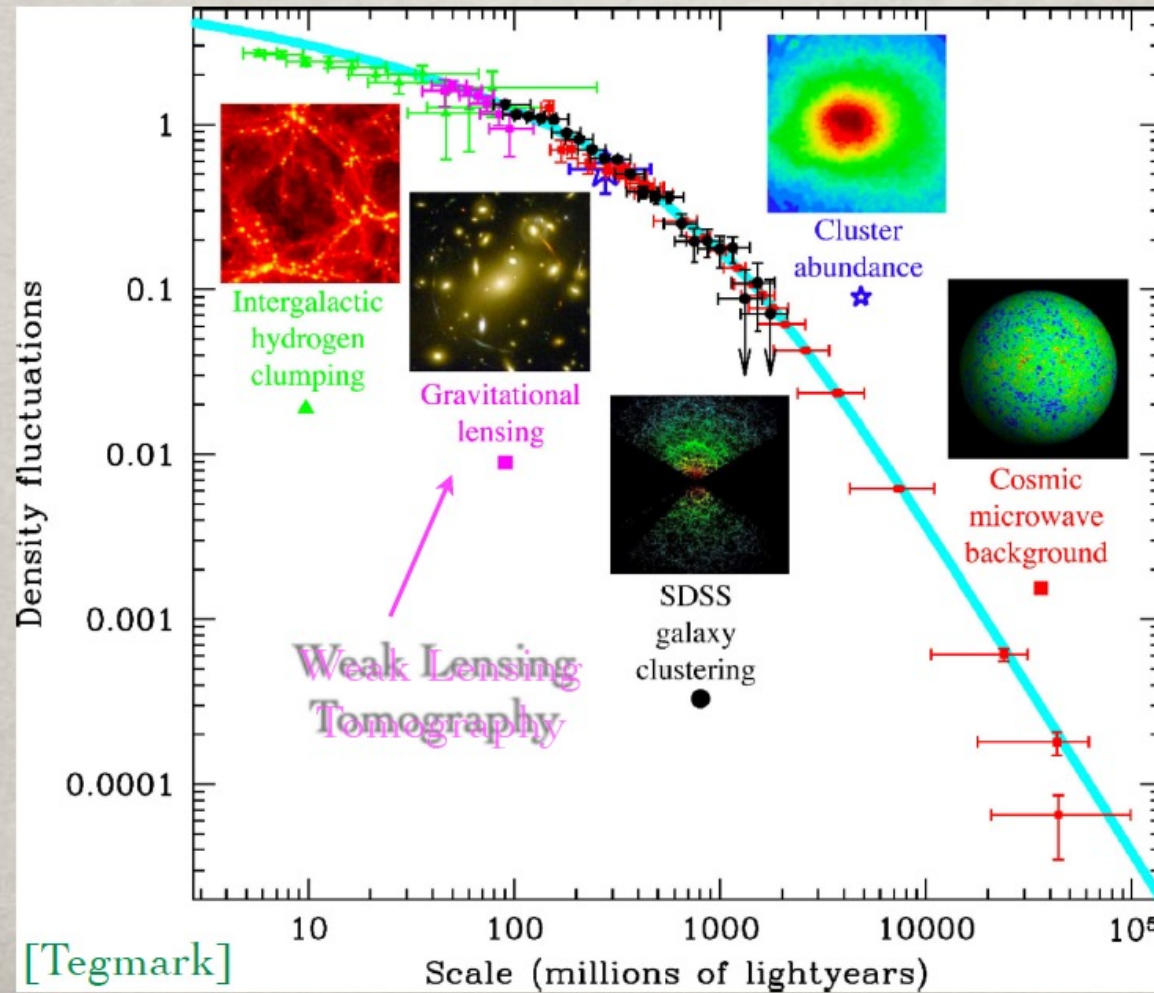
$$\Omega_K = 0.0007 \pm 0.0019$$



EVIDENCES FOR A CONSPICUOUS AMOUNT OF NON-BARYONIC DM AT SEVERAL (VERY) DIFFERENT LENGTH SCALES

FLUCTUATIONS ON ALL SCALES

Non-
linear



Linear

Dynamics of galaxy clusters

Rotational curves of galaxies

Gravitational lensing

Structure formation from primordial
density fluctuations

CMB spectrum → Energy density
budget

What's dark matter?



"I can't tell you what's in the dark matter sandwich. No one knows what's in the dark matter sandwich."

But, at least , we know **what CANNOT BE in the DM sandwich:**

NO SM PARTICLE CAN BE THE DOMINANT SOURCE OF DM

DARK MATTER PROPERTIES

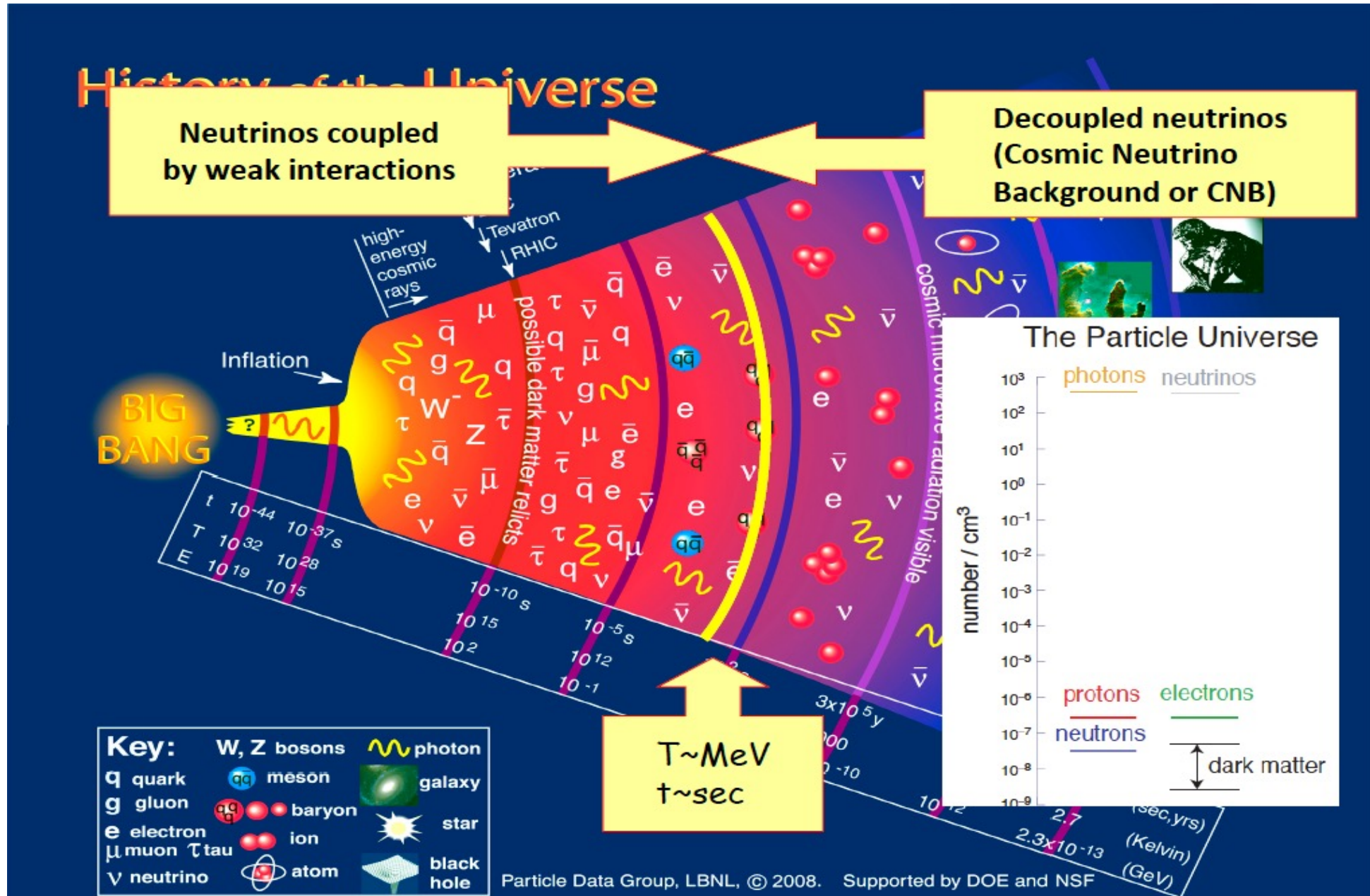
- Interacts very weakly, but surely gravitationally (electrically neutral, non-baryonic and decoupled from the primordial plasma !!!)
- It must have the right density profile to “fill in” the galaxy rotation curves, i.e. non-dissipative.
- No pressure and negligible free-streaming velocity, it must cluster & cause structure formation.



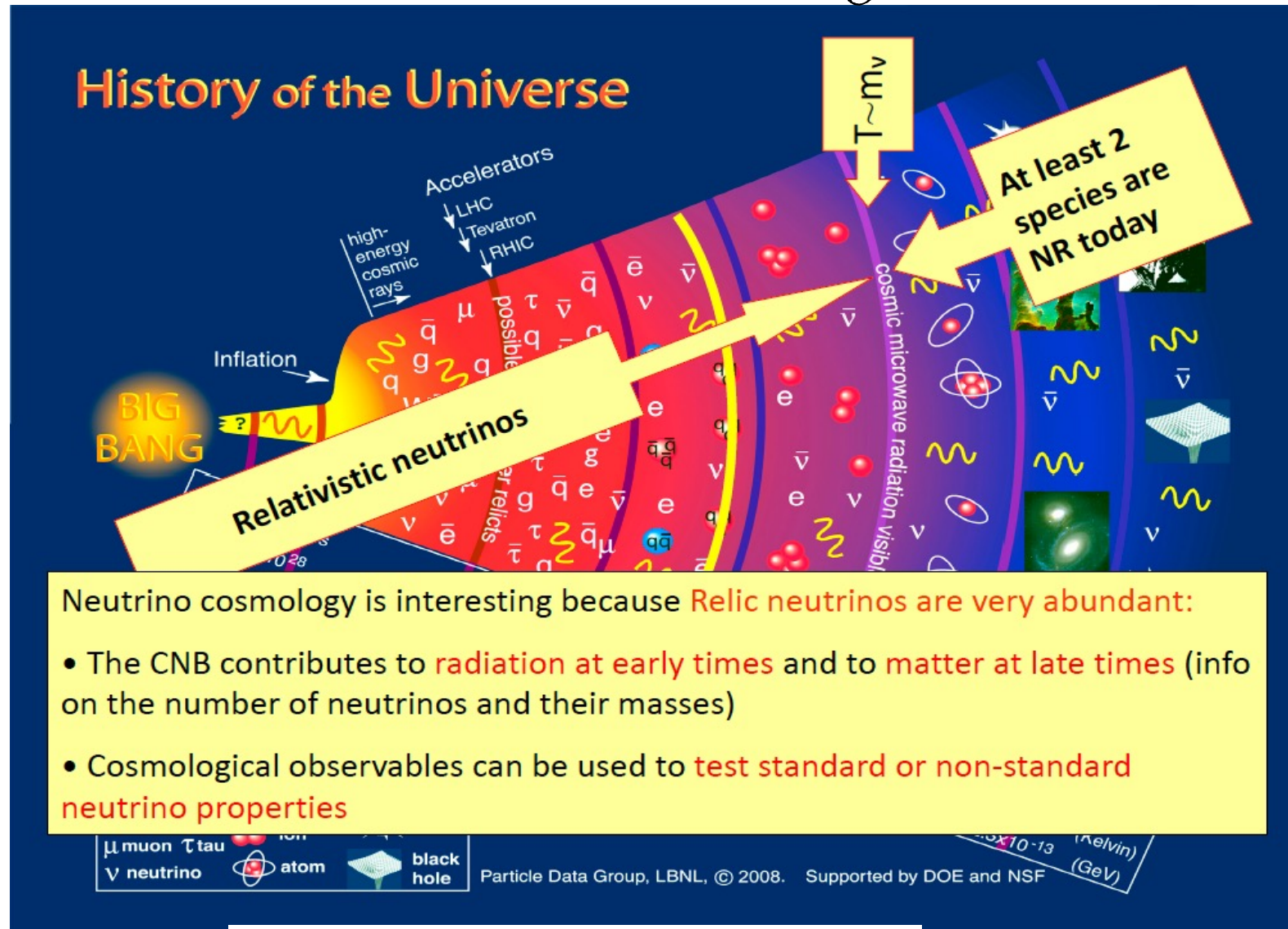
COLD DARK MATTER

But unfortunately too many realizations !

The role of neutrinos in the Early Universe



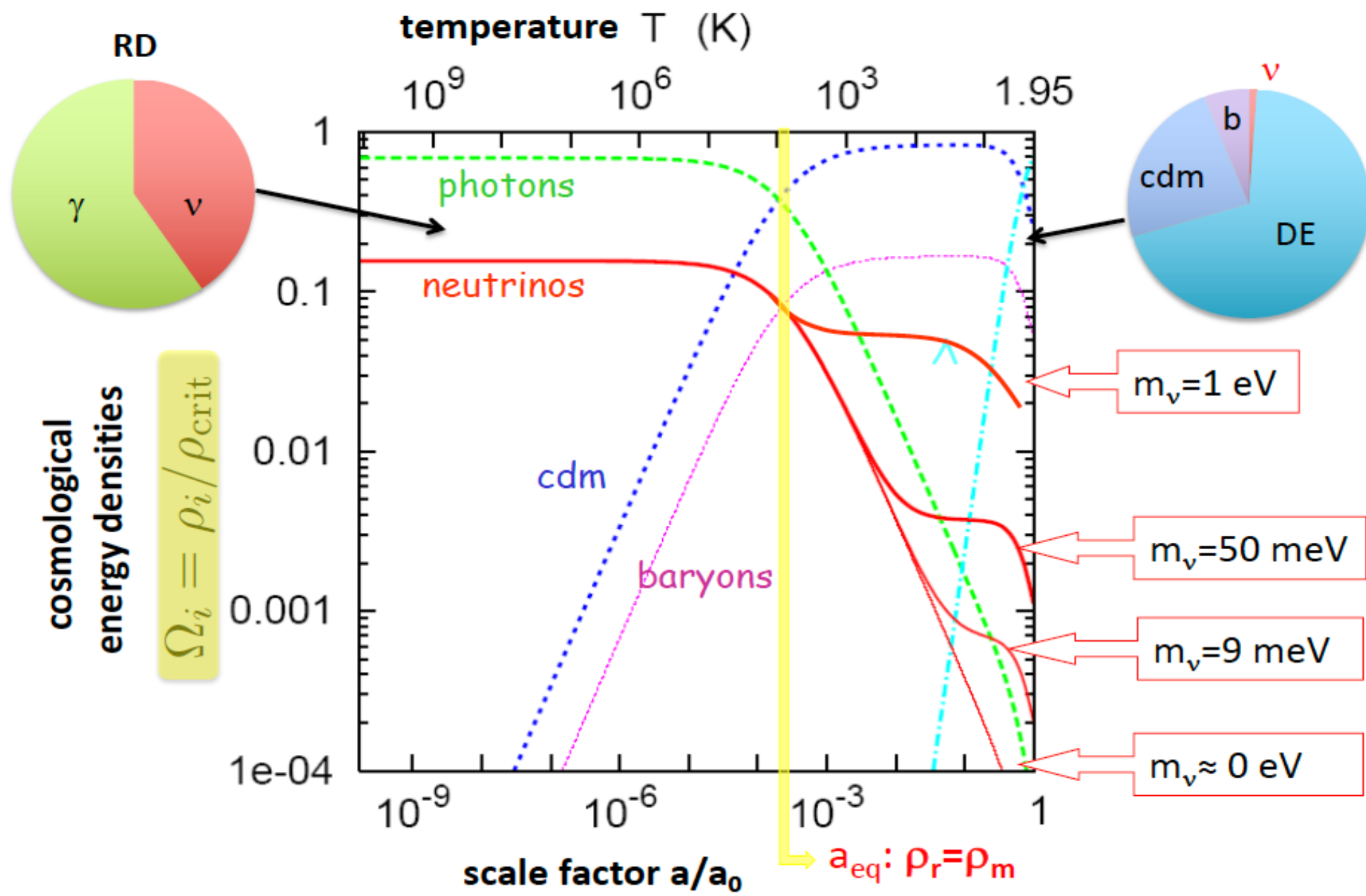
The role of neutrinos in the Early Universe



$$0.05(0.09) \text{ eV} \lesssim \sum_i m_i \lesssim 2.4 \text{ eV}$$

oscillations KATRIN

Evolution of the background densities: 1 MeV \rightarrow now



Neutrinos as Dark Matter



S. Pastor Erice 2024

- Neutrinos are natural **DM candidates**

$$\Omega_\nu h^2 = \frac{\sum_i m_i}{93.2 \text{ eV}} \quad \Omega_\nu < 1 \rightarrow \sum_i m_i \lesssim 46 \text{ eV}$$

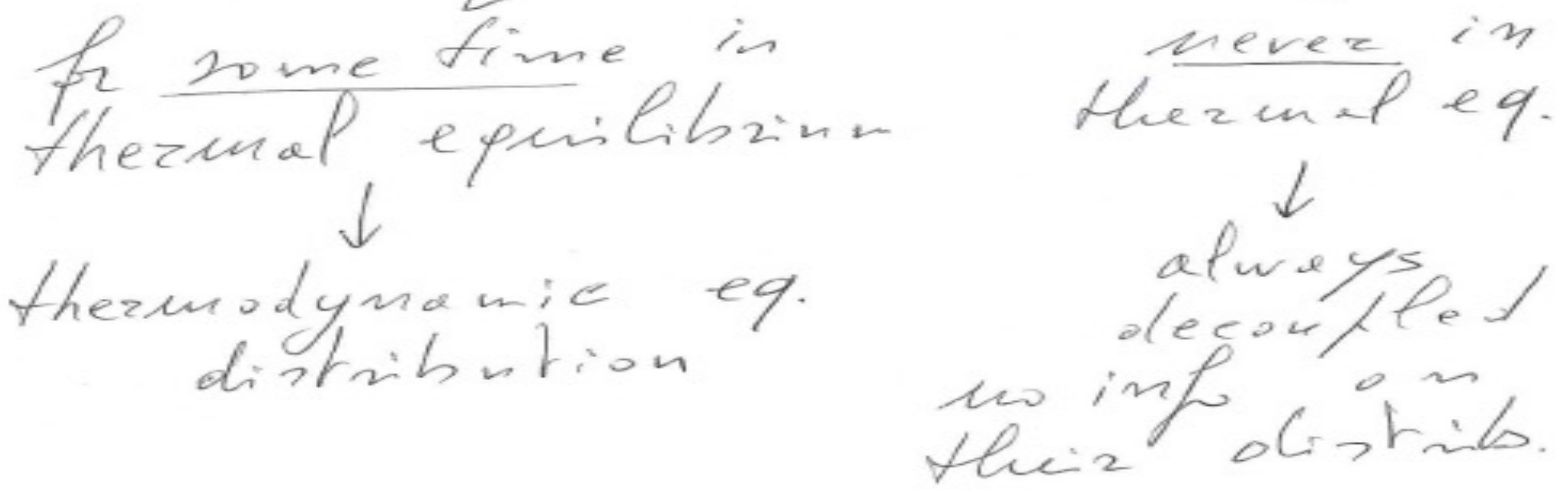
$$\Omega_\nu < \Omega_m \simeq 0.3 \rightarrow \sum_i m_i \lesssim 15 \text{ eV}$$

HOWEVER...

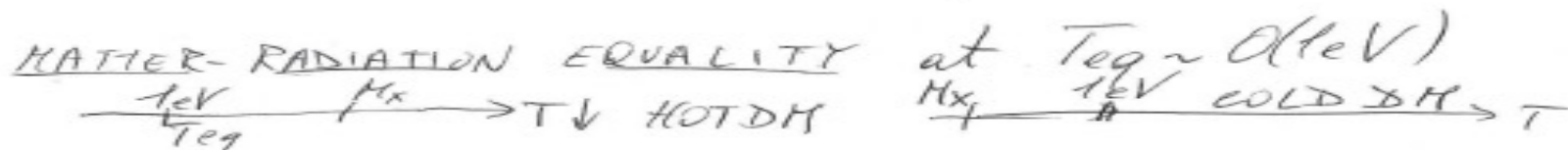
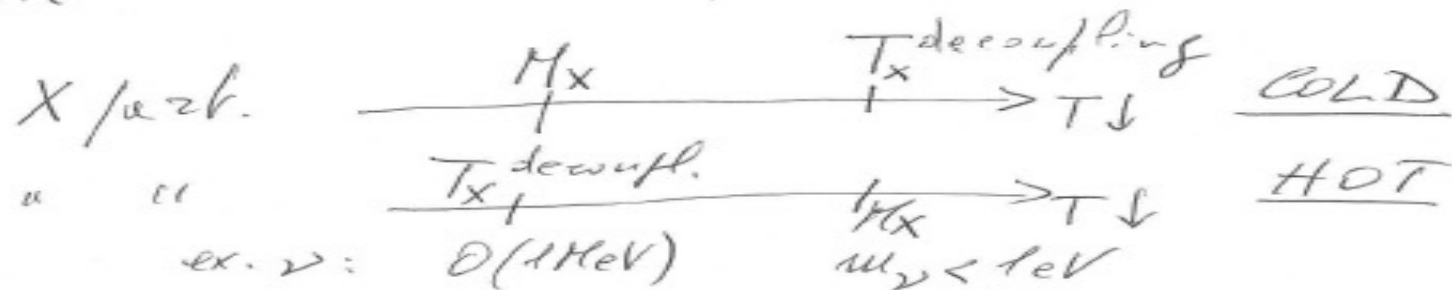
- They stream freely until non-relativistic (collisionless phase mixing) 
Neutrinos are HOT Dark Matter (large thermal motion)
- First structures to be formed when Universe became matter –dominated are very large
- Ruled out by structure formation  CDM

Massive Neutrinos can still be subdominant DM: **limits on m_ν from Structure Formation (combined with other cosmological data)**

DM: THERMAL and NON-THERMAL RELICS



DM: COLD and HOT THERMAL RELICS



from large structures \Rightarrow strong bounds
on the hot component of DM \Rightarrow most
of the DM must be COLD

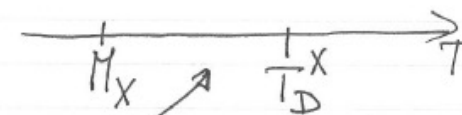
HOT DM can be only a small component
of the whole DM \rightarrow cannot be the dominant
source of DM !

THERMAL X (in thermal equil.)

case of STABLE HEAVY PARTICLE X

COMPUTATION OF $\Omega_X h^2$ under the
assumption

at $T < M_X$



$$n_X^{eq} = g_X \left(\frac{M_X T}{2\pi} \right)^{3/2} e^{-M_X/T}$$

number of X (in a comoving volume) changes
only because of ^{pair}annihilation \rightarrow light part.
or viceversa \leftarrow ^{pair}creation

$$X\bar{X} \rightarrow \text{light part.} \quad \text{light part} \rightarrow X\bar{X}$$

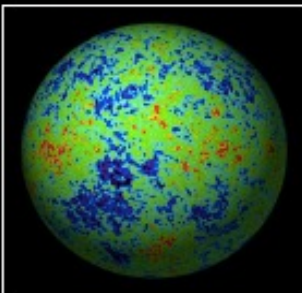
TEN COMMANDMENTS TO BE A “GOOD” DM CANDIDATE

BERTONE, A.M., TAOSO

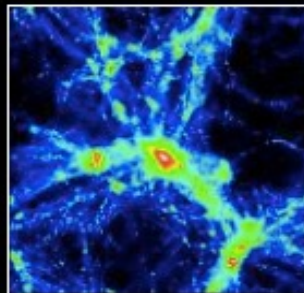
- TO MATCH THE APPROPRIATE RELIC DENSITY
- TO BE COLD
- TO BE NEUTRAL
- TO BE CONSISTENT WITH BBN
- TO LEAVE STELLAR EVOLUTION UNCHANGED
- TO BE COMPATIBLE WITH CONSTRAINTS ON SELF – INTERACTIONS
- TO BE CONSISTENT WITH DIRECT DM SEARCHES
- TO BE COMPATIBLE WITH GAMMA – RAY CONSTRAINTS
- TO BE COMPATIBLE WITH OTHER ASTROPHYSICAL BOUNDS
- “TO BE PROBED EXPERIMENTALLY”

The Ten Commandments to respect to be a “good” DM candidate

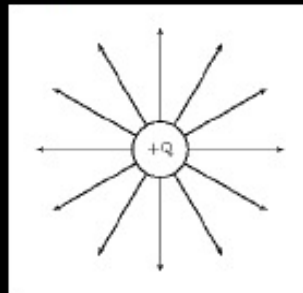
1) Abundance ok?



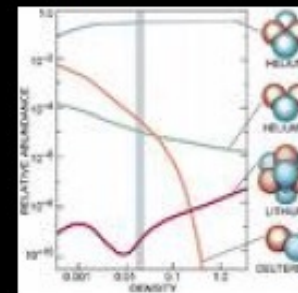
2) Cold?



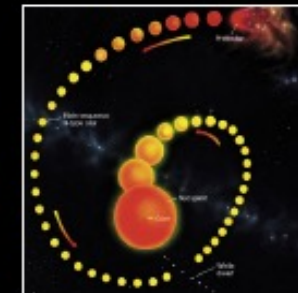
3) Neutral?



4) BBN ok?



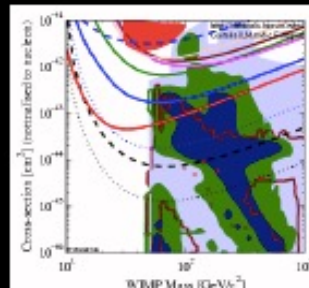
5) Stars OK?



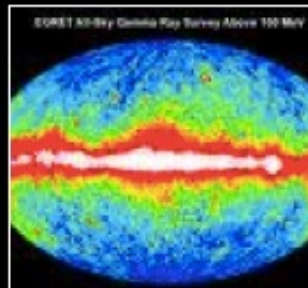
6) Collisionless?



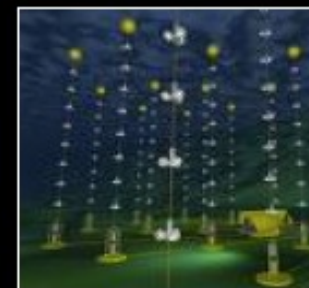
7) Couplings OK?



8) γ -rays OK?



9) Astro bounds?





10) Can probe it?



Taoso, GB, Masiero 0711.4996

**NONE OF THE SM PARTICLES CAN BE A
GOOD DM CANDIDATE !**

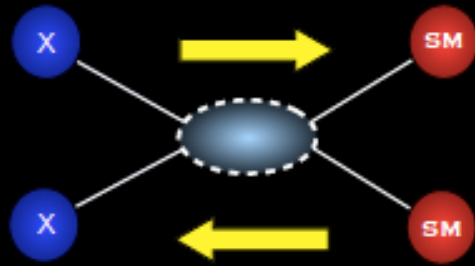
DM: the most impressive evidence at the “quantitative” and “qualitative” levels of New Physics beyond SM

- **QUANTITATIVE:** Taking into account the latest WMAP data which in combination with LSS data provide stringent bounds on Ω_{DM} and Ω_{B}  **EVIDENCE FOR NON-BARYONIC DM AT MORE THAN 10 STANDARD DEVIATIONS!! THE SM DOES NOT PROVIDE ANY CANDIDATE FOR SUCH NON-BARYONIC DM**
- **QUALITATIVE:** it is NOT enough to provide a mass to neutrinos to obtain a valid DM candidate; LSS formation requires DM to be COLD  **NEW PARTICLES NOT INCLUDED IN THE SPECTRUM OF THE FUNDAMENTAL BUILDING BLOCKS OF THE SM !**

DM and ELW. SYMMETRY BREAKING

*THE DM ROAD TO NEW
PHYSICS BEYOND THE SM:
IS **DM** A PARTICLE OF
THE **NEW PHYSICS AT
THE ELECTROWEAK
ENERGY SCALE ?***

The WIMP paradigm is based on a simple yet powerful idea:

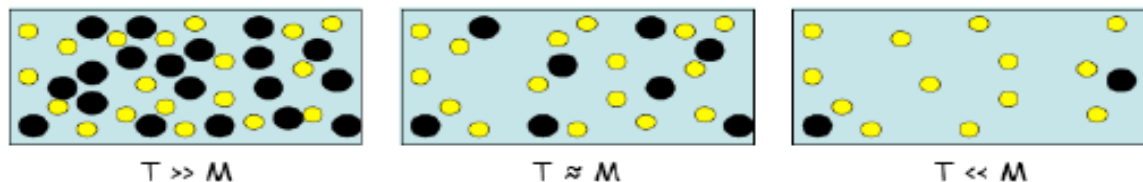


$$\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle [n_\chi^2 - (n_\chi^{\text{eq}})^2]$$

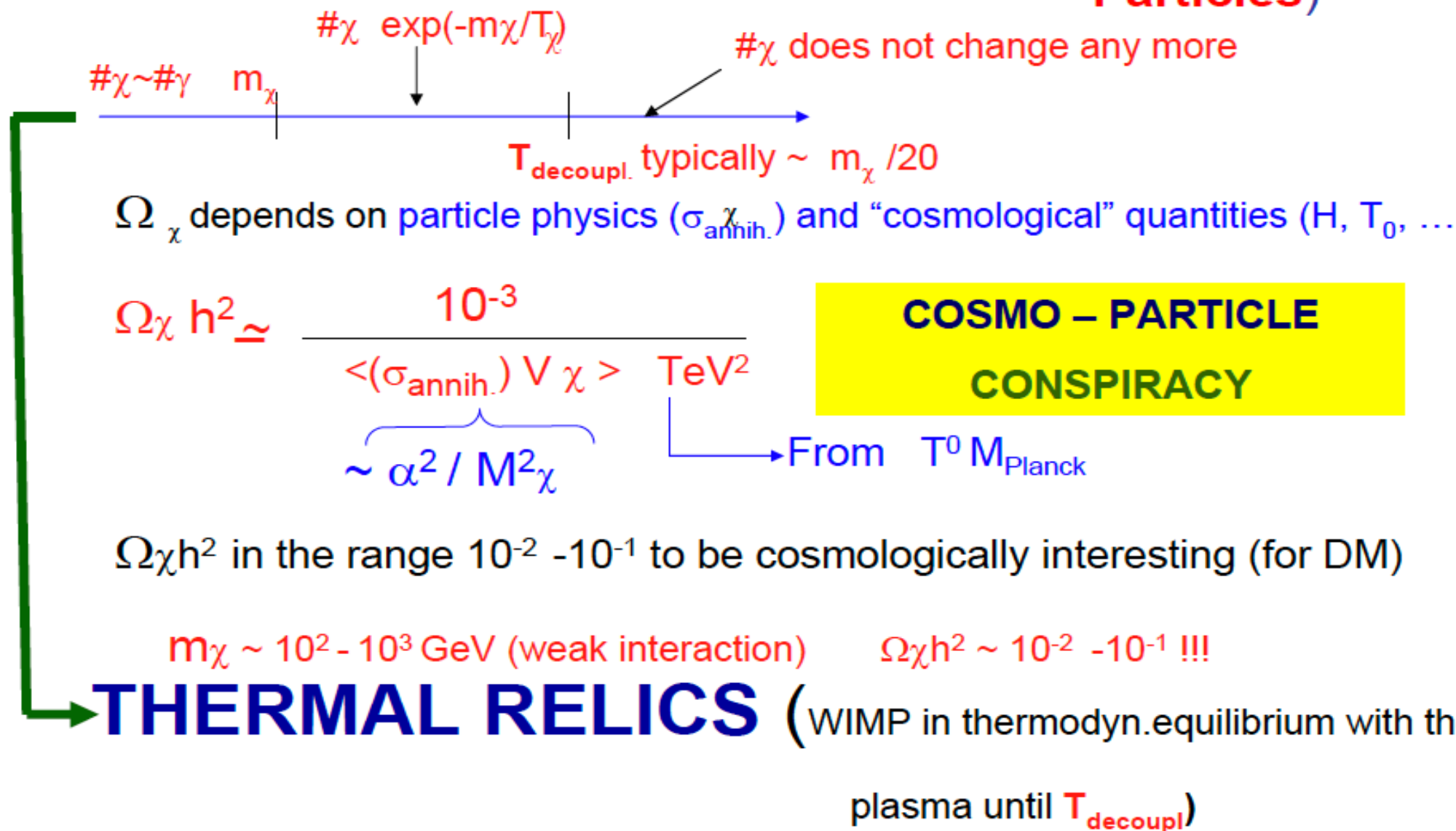
Weak-scale cross sections can
reproduce observed relic density

$$\Omega h^2 \approx \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle\sigma v\rangle}$$

‘WIMP miracle’: new physics at $\sim 1 \text{ TeV}$ solves at same time
fundamental problems of particle physics (*hierarchy problem*) AND DM



WIMPS (Weakly Interacting Massive Particles)



ROADS TO GO BEYOND THE STANDARD MODEL (I)

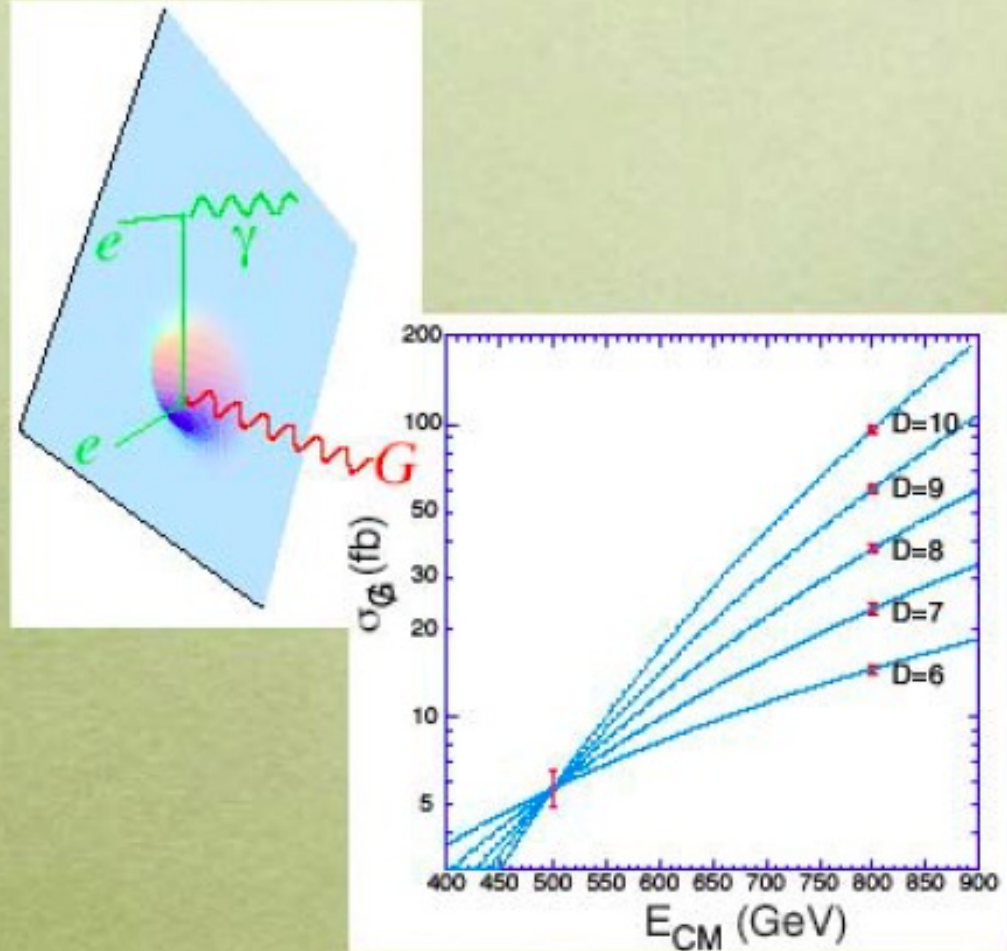
1) **THERE EXISTS NO NEW PHYSICAL ENERGY SCALE ABOVE THE ELW. SCALE:** gravity is an extremely weak force not because of the enormous value of the Planck scale, but because of the existence of **NEW DIMENSIONS** beyond the usual 3+1 space-time where (most of) the gravity flux lines get “dispersed”

→ **VISIBILITY AT LHC:** there exist “excited” states of the ordinary particles (**Kaluza-Klein states**) and some of them are accessible at LHC (the lightest KK state may be a stable particle and it can constitute the DM)

Hidden Dimensions

- *Hidden dimensions*
- *Can emit graviton into the bulk*
- *Events with apparent energy imbalance*

How many extra dimensions are there?



ROADS TO GO BEYOND THE STANDARD MODEL (II)

- 2) NO NEED TO “PROTECT” THE HIGGS MASS AT THE ELW. SCALE: **THE HIGGS IS A COMPOSITE OBJECT** (for instance, a fermion condensate) **WHOSE COMPOSITENESS SCALE IS THE ELW. SCALE** (cfr. the pion mass case)
→ **VISIBILITY AT LHC: THERE EXIST NEW (STRONG) INTERACTIONS AT THE ELW. SCALE WHICH PRODUCE THE HIGGS CONDENSATE** (new resonances,, new bound states, a new rescaled QCD at 1 TeV)

ROADS TO GO BEYOND THE STANDARD MODEL (III)

- 3) THE MASS OF THE ELEMENTARY HIGGS BOSON IS “PROTECTED” AT THE ELW. SCALE BECAUSE OF THE PRESENCE AT THAT ENERGY OF A NEW SYMMETRY, THE **SUPERSYMMETRY (SUSY)**

————→ **VISIBILITY AT LHC**: WE’LL SEE (SOME OF) THE **SUSY PARTICLES AND THEIR INTERACTIONS**. THE LIGHTEST SUSY PARTICLE (**LSP**) IS LIKELY TO BE STABLE AND PROVIDE THE **DM**. **AT THE SAME TIME, WE COULD DISCOVER SUSY AND THE SOURCE OF 90% OF THE ENTIRE MATTER PRESENT IN THE UNIVERSE.**

THE SUSY PATH

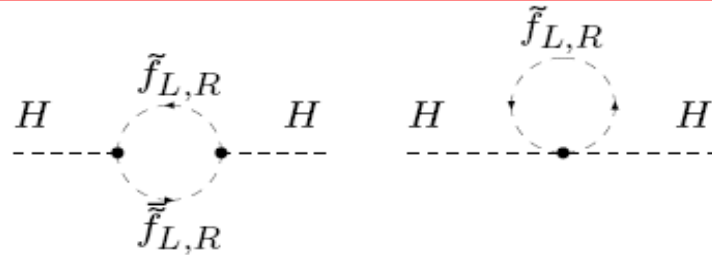
$$Q | boson \rangle = | fermion \rangle \quad Q | fermion \rangle = | boson \rangle$$

$$[b, b] = 0, \quad \{f, f\} = 0 \Rightarrow$$

$$\{Q_\alpha^i, \bar{Q}_{\dot{\beta}}^j\} = 2\delta^{ij} (\sigma^\mu)_{\alpha\dot{\beta}} P_\mu$$

Effectively: SM particles have **SUSY partners** (e.g. $f_{L,R} \rightarrow \tilde{f}_{L,R}$)

SUSY: additional contributions from scalar fields:



$$\Sigma_H^{\tilde{f}} \sim N_{\tilde{f}} \lambda_{\tilde{f}}^2 \int d^4 k \left(\frac{1}{k^2 - m_{\tilde{f}_L}^2} + \frac{1}{k^2 - m_{\tilde{f}_R}^2} \right) + \text{terms without quadratic div.}$$

for $\Lambda \rightarrow \infty$: $\Sigma_H^{\tilde{f}} \sim N_{\tilde{f}} \lambda_{\tilde{f}}^2 \Lambda^2$

⇒ quadratic divergences cancel for

$$N_{\tilde{f}_L} = N_{\tilde{f}_R} = N_f$$
$$\lambda_{\tilde{f}}^2 = \lambda_f^2$$

complete correction vanishes if furthermore

$$m_{\tilde{f}} = m_f$$

Soft SUSY breaking: $m_{\tilde{f}}^2 = m_f^2 + \Delta^2$, $\lambda_{\tilde{f}}^2 = \lambda_f^2$

$$\Rightarrow \Sigma_H^{f+\tilde{f}} \sim N_f \lambda_f^2 \Delta^2 + \dots$$

⇒ correction stays acceptably small if mass splitting is of weak scale

⇒ realized if mass scale of SUSY partners

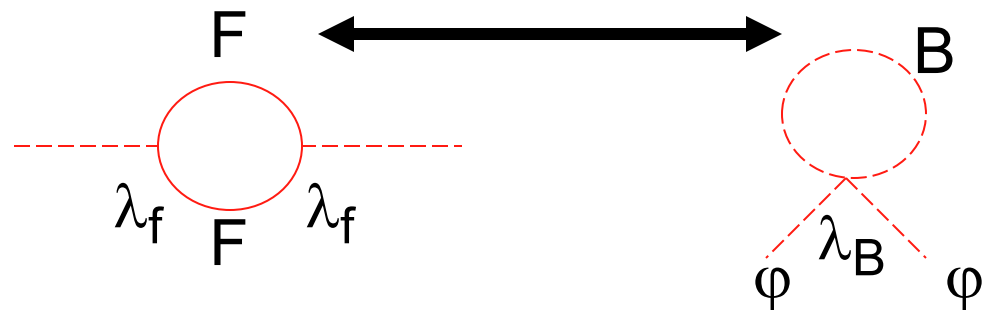
$$M_{\text{SUSY}} \lesssim 1 \text{ TeV}$$

⇒ SUSY at TeV scale provides attractive solution of hierarchy problem

HIERARCHY PROBLEM: THE SUSY WAY

SUSY HAS TO BE BROKEN AT A SCALE CLOSE TO 1TeV \longrightarrow **LOW ENERGY SUSY**

$m_\phi^2 \propto \Lambda^2$ \longrightarrow Scale of susy breaking



$$Sm_\phi^2 \sim \frac{(\lambda_B - \lambda_f^2)}{16\pi^2} \Lambda^2$$

$$\longrightarrow [m_B^2 - m_F^2]^{1/2} \sim 1/\sqrt{G_F}$$

$\begin{bmatrix} B \\ F \end{bmatrix}$ In SUSY multiplet

SPLITTING IN MASS BETWEEN B and F of O (ELW. SCALE)

Simplest (N=1) SUSY Multiplets

Bosons and Fermions come in pairs

$$(\varphi, \psi)$$

Spin 0

Spin 1/2

scalar

chiral fermion

$$(\lambda, A_\mu)$$

Spin 1/2

Spin 1

majorana fermion

vector

$$(\tilde{g}, g)$$

Spin 3/2

Spin 2

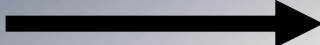
gravitino

graviton

Particle Content of the MSSM

Superfield	Bosons		Fermions	$SU_c(3)$	$SU_L(2)$	$U_Y(1)$	
Gauge							
G^a	gluon	g^a	gluino \tilde{g}^a	8	1	0	
V^k	Weak	$W^k (W^\pm, Z)$	wino, zino $\tilde{w}^k (\tilde{w}^\pm, \tilde{z})$	1	3	0	
V'	Hypercharge	$B(\gamma)$	bino $\tilde{b}(\tilde{\gamma})$	1	1	0	
Matter							
L_i	sleptons	$\tilde{L}_i = (\tilde{\nu}, \tilde{e})_L$ $\tilde{E}_i = \tilde{e}_R$	leptons	$L_i = (\nu, e)_L$ $E_i = e_R$	1	2	-1
E_i					1	1	2
Q_i	squarks	$\tilde{Q}_i = (\tilde{u}, \tilde{d})_L$ $\tilde{U}_i = \tilde{u}_R$ $\tilde{D}_i = \tilde{d}_R$	quarks	$Q_i = (u, d)_L$ $U_i = u_R^c$ $D_i = d_R^c$	3	2	1/3
U_i					3^*	1	-4/3
D_i					3^*	1	2/3
Higgs							
H_1	Higgses	H_1 H_2	higgsinos	\tilde{H}_1 \tilde{H}_2	1	2	-1
H_2					1	2	1

THE FATE OF **B** AND **L** IN THE SM AND MSSM

- **IN THE SM B AND L ARE “AUTOMATIC” SYMMETRIES**: NO B or L VIOLATING OPERATOR OF DIM. ≤ 4 INVARIANT UNDER THE GAUGE SYMMETRY $SU(3) \times SU(2) \times U(1)$ IS ALLOWED (B AND L ARE CONSERVED AT ANY ORDER IN PERTURBATION THEORY, BUT ARE VIOLATED AT THE QUANTUM LEVEL (ONLY $B - L$ IS EXACTLY PRESERVED)
- **IN THE MSSM**, THANKS TO THE EXTENDED PARTICLE SPECTRUM WITH NEW SUSY PARTNERS CARRYING B AND L, **IT IS POSSIBLE TO WRITE (RENORMALIZABLE) OPERATORS WHICH VIOLATE EITHER B OR L**
-  IF BOTH B AND L VIOLATING OPERATORS ARE PRESENT, GIVEN THAT SUSY PARTNER MASSES ARE OF $O(\text{TeV})$, THERE IS NO WAY TO PREVENT A **TOO FAST PROTON DECAY** UNLESS THE YUKAWA COUPLINGS ARE INCREDIBLY SMALL!

ADDITIONAL DISCRETE SYMMETRY IN THE MSSM TO SLOW DOWN P - DECAY

- SIMPLEST (and nicest) SOLUTION: ADD A SYMMETRY WHICH FORBIDS ALL B AND L VIOLATING OPERATORS

→ **R PARITY**

- SINCE B AND L 4-DIM. OPERATORS INVOLVE 2 ORDINARY FERMIONS AND A SUSY SCALAR PARTICLE, THE SIMPLEST WAY TO ELIMINATE ALL OF THEM:

$R = +1$ FOR ORDINARY PARTICLES

$R = -1$ FOR SUSY PARTNERS

IMPLICATIONS OF IMPOSING R PARITY:

- i) The superpartners are created or destroyed in pairs;
- ii) **THE LIGHTEST SUPERPARTNER IS ABSOLUTELY STABLE**

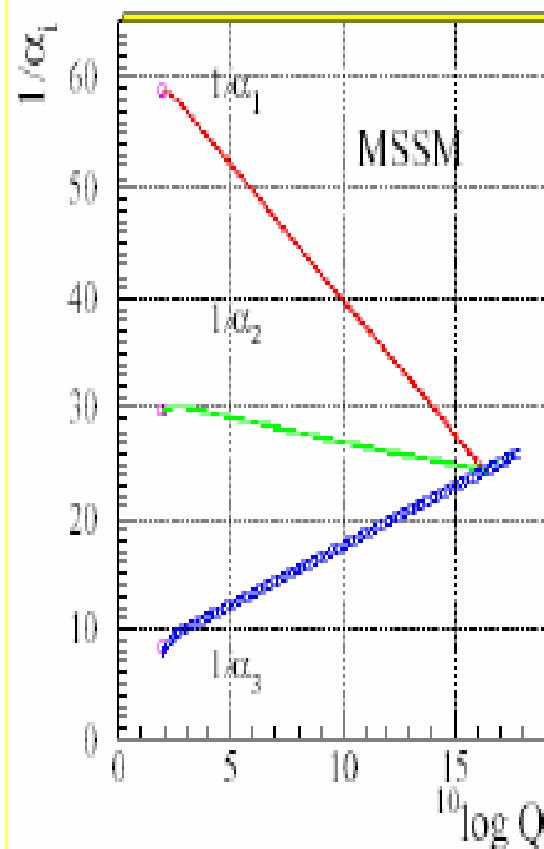
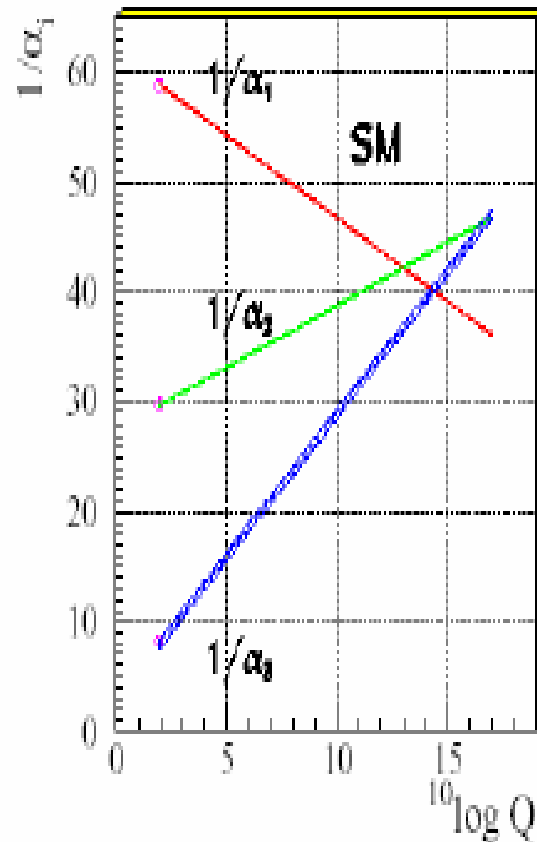
BROKEN **R** PARITY

- PROTON DECAY REQUIRES THE VIOLATION OF **BOTH B AND L**

————→ NOT NECESSARY TO HAVE R
PARITY TO KILL **B AND L** VIOLATING
OPERATORS

————→ ENOUGH TO IMPOSE AN
**ADDITIONAL DISCRETE SYMMETRY TO
FORBID EITHER B OR L VIOLATING
OPERATORS**; RESTRICTIONS ON THE
YUKAWA COUPLINGS OF THE SURVIVING B
OR L VIOLATING OPERATORS

LOW-ENERGY SUSY AND UNIFICATION



Input

$$\alpha^{-1}(M_Z) = 128.978 \pm 0.027$$

$$\sin^2 \theta_{\overline{MS}} = 0.23146 \pm 0.00017$$

$$\alpha_s(M_Z) = 0.1184 \pm 0.0031$$


Output

$$M_{SUSY} = 10^{3.4 \pm 0.9 \pm 0.4} \text{ GeV}$$

$$M_{GUT} = 10^{15.8 \pm 0.3 \pm 0.1} \text{ GeV}$$

$$\alpha_{GUT}^{-1} = 26.3 \pm 1.9 \pm 1.0$$

SUSY & DM : a successful marriage

- Supersymmetrizing the SM does **not** lead necessarily to a stable SUSY particle to be a DM candidate.
- However, the mere SUSY version of the SM is known to lead to a **too fast p-decay**. Hence, necessarily, the SUSY version of the SM has to be **supplemented with some additional (ad hoc?) symmetry to prevent the p-decay catastrophe**.
- Certainly the simplest and maybe also the most attractive solution is **to impose the discrete R-parity symmetry**
- **MSSM + R PARITY**  **LIGHTEST SUSY PARTICLE (LSP) IS STABLE** .
- The LSP can constitute an interesting DM candidate in several interesting realizations of the MSSM (i.e., with different SUSY breaking mechanisms including gravity, gaugino, gauge, anomaly mediations, and in various regions of the parameter space).

WHO IS THE LSP?

- **SUPERGRAVITY** (transmission of the SUSY breaking from the hidden to the observable sector occurring via gravitational interactions): best candidate to play the role of LSP:

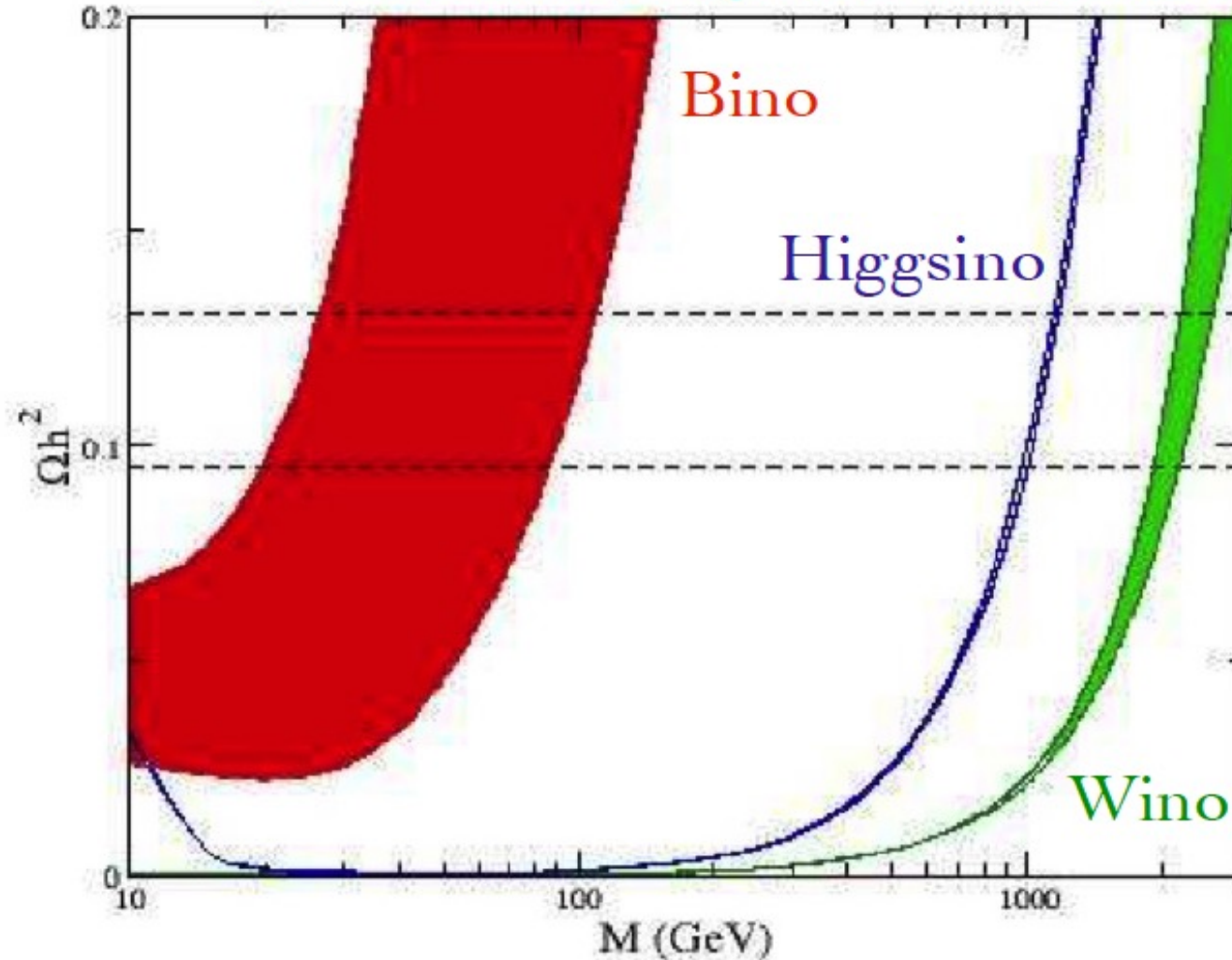
NEUTRALINO (i.e., the lightest of the four eigenstates of the 4×4 neutralino mass matrix)

In **CMSSM**: the LSP neutralino is almost entirely a **BINO**

WELL-TEMPERED NEUTRALINO

Relic density strongly dependent on neutralino nature !!!

[Arkani-Hamed, Delgado & Giudice 0601041]



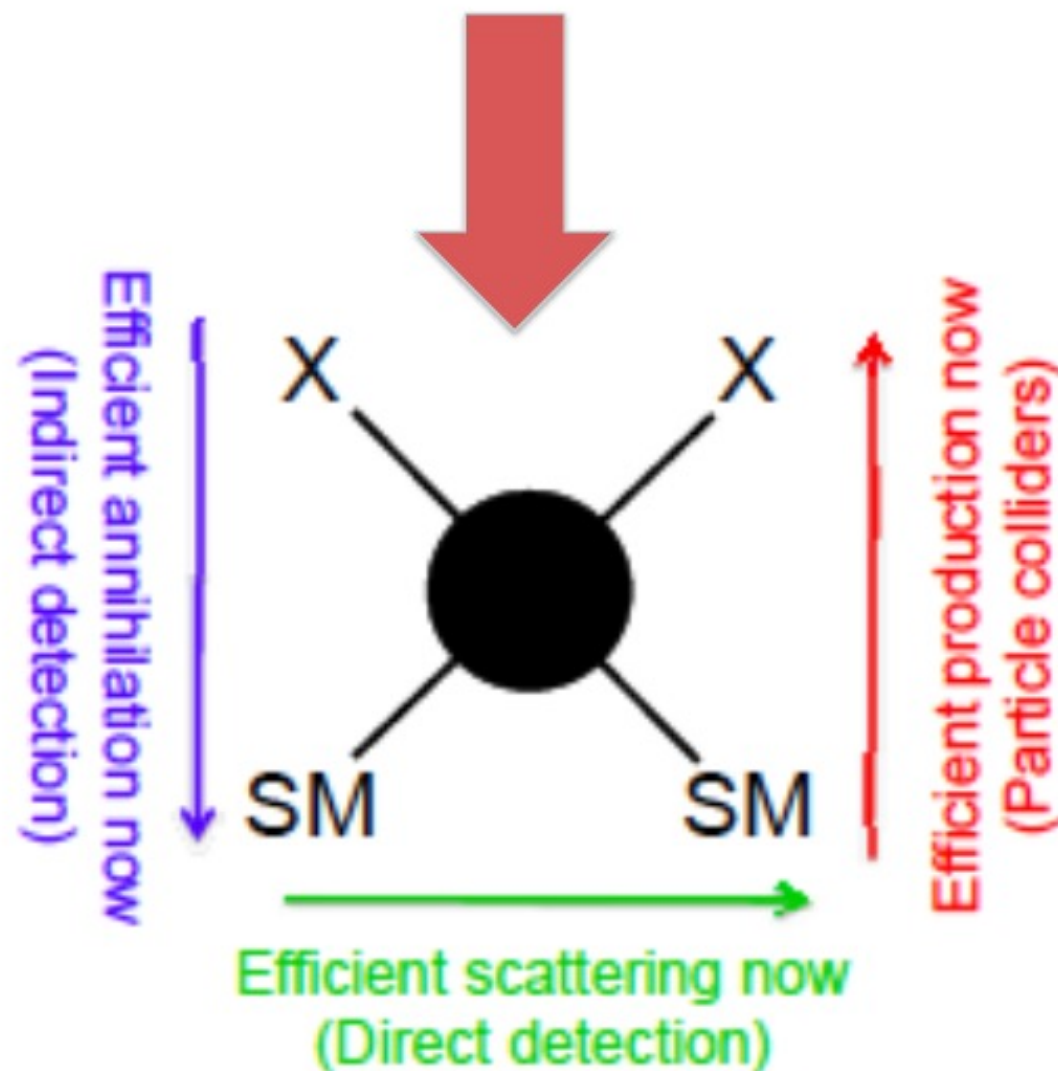
CONNECTION DM – ELW. SCALE

THE WIMP MIRACLE : STABLE ELW. SCALE WIMPs

	SUSY (x^μ, θ)	EXTRA DIM. (x^μ, j^i)	LITTLE HIGGS. SM part + new part
1) ENLARGEMENT OF THE SM	Anticomm. Coord.	New bosonic Coord.	to cancel Λ^2 at 1-Loop
2) SELECTION RULE	<u>R-PARITY LSP</u>	<u>KK-PARITY LKP</u>	<u>T-PARITY LTP</u>
→ DISCRETE SYMM.	Neutralino spin 1/2	spin1	spin0
→ STABLE NEW PART.			
3) FIND REGION (S) PARAM. SPACE WHERE THE “L” NEW PART. IS NEUTRAL + $\Omega_L h^2$ OK	m_{LSP} ~100 - 200 GeV	m_{LKP} ~600 - 800 GeV	m_{LTP} ~400 - 800 GeV

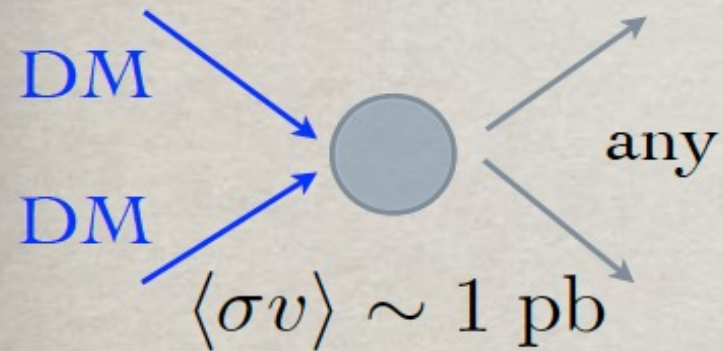
R-parity is an ADDITIONAL discrete symmetry imposed to prevent SUSY particles with masses at the electroweak scale to mediate a too fast proton decay!

DM COMPLEMENTARITY: efficient annihilation in the early Universe implies today

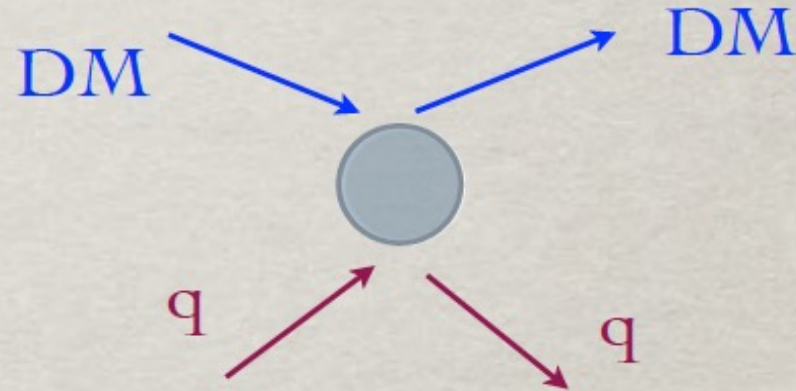


THE WIMP CONNECTION

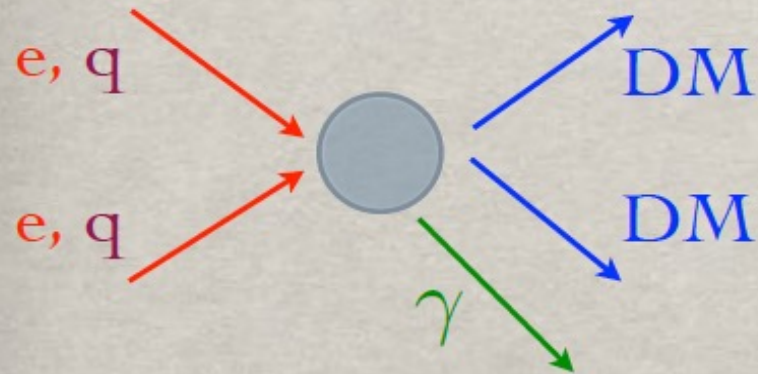
Early Universe: $\Omega_{CDM}h^2$



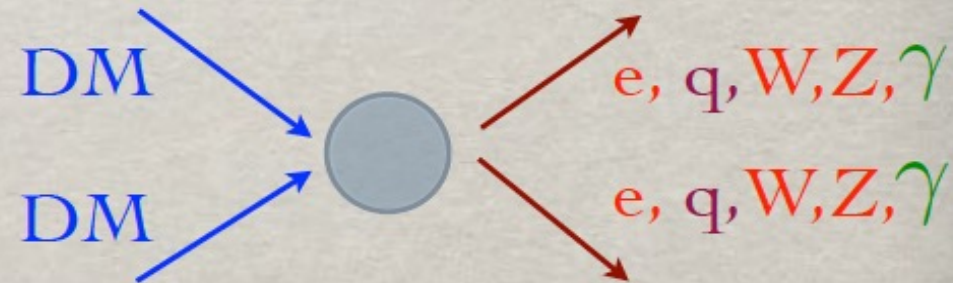
Direct Detection:



Colliders: LHC/ILC

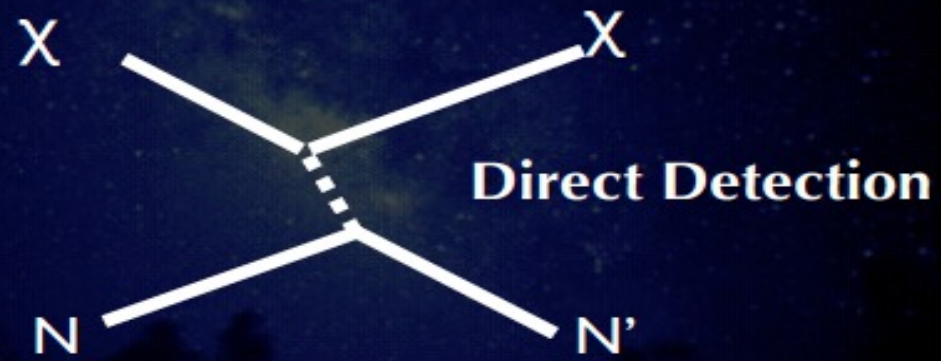


Indirect Detection:

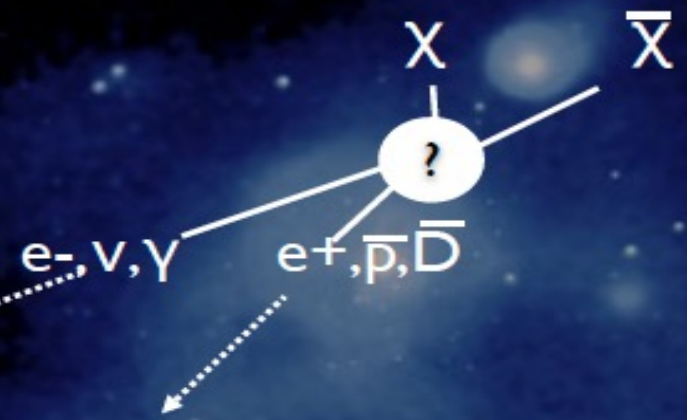


3 different ways to check this hypothesis !!!

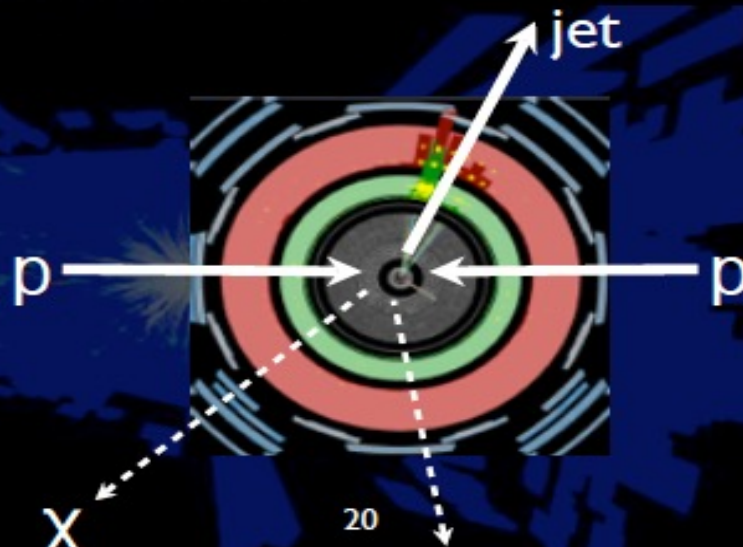
Experimentalist's View



Indirect Detection



Accelerator Production



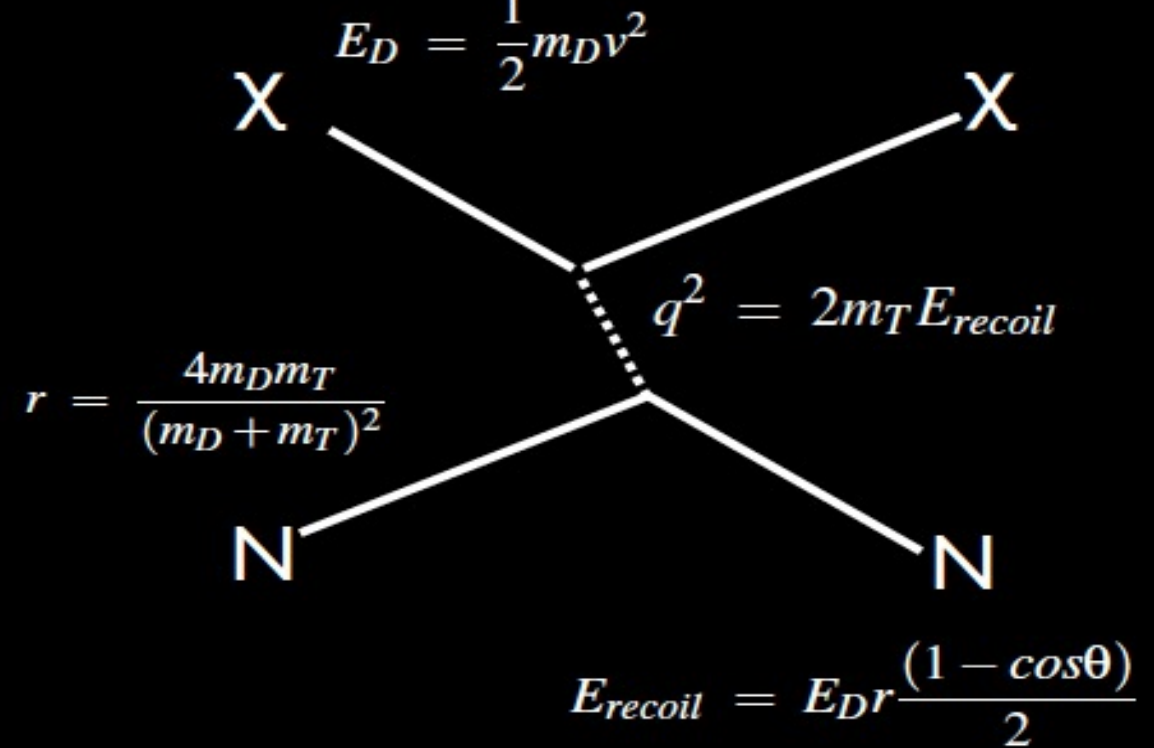
J. Mpnroe, IDM 2024



Direct Detection Strategies

scattering kinematics: $v/c \sim 8E-4!$

recoil angle strongly correlated
with incoming WIMP direction



Spin Independent:

χ scatters coherently off of
the entire nucleus A : $\sigma \sim A^2$

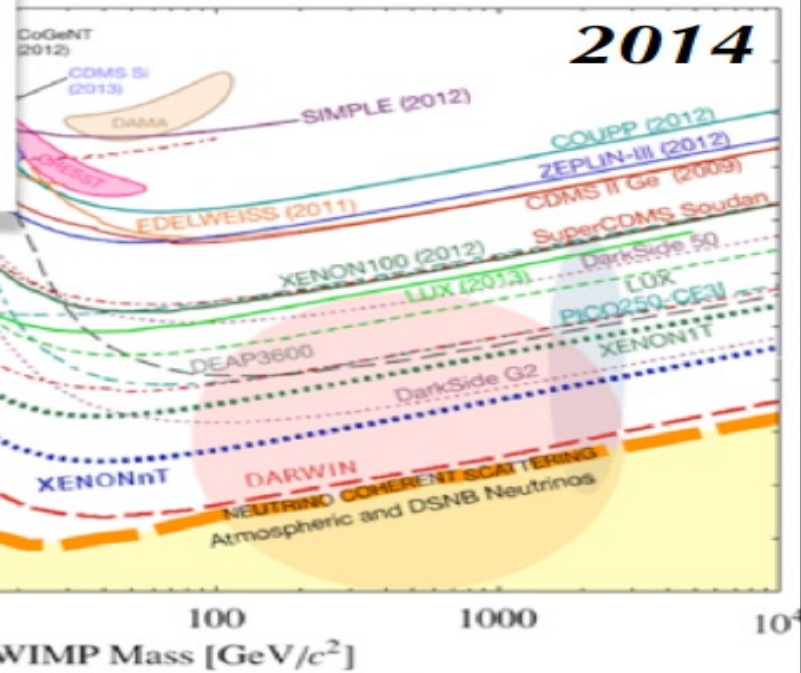
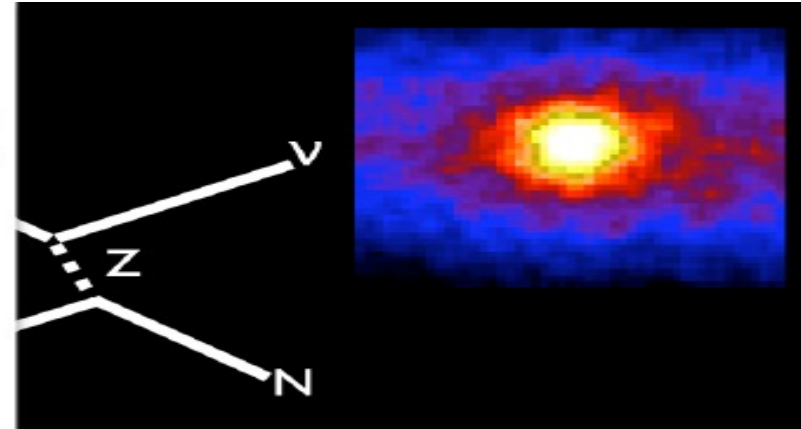
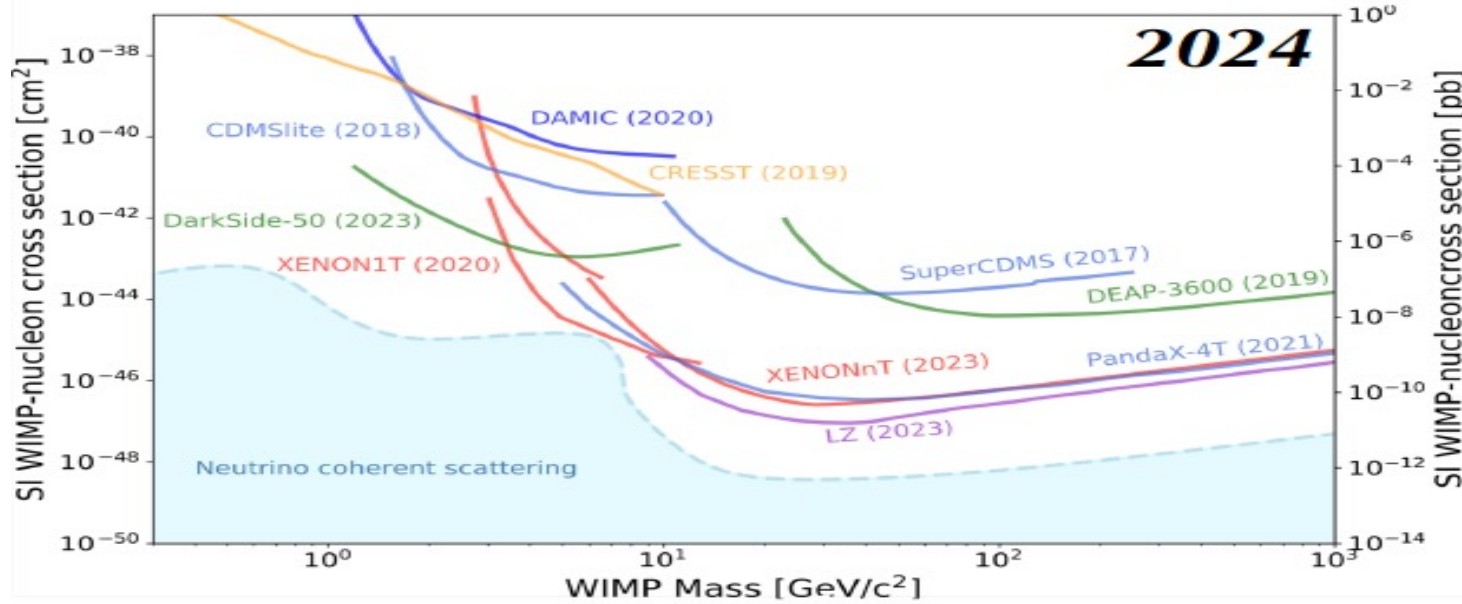
D. Z. Freedman, PRD 9, 1389 (1974)

Spin Dependent:

mainly unpaired nucleons contribute
to scattering amplitude: $\sigma \sim J(J+1)$

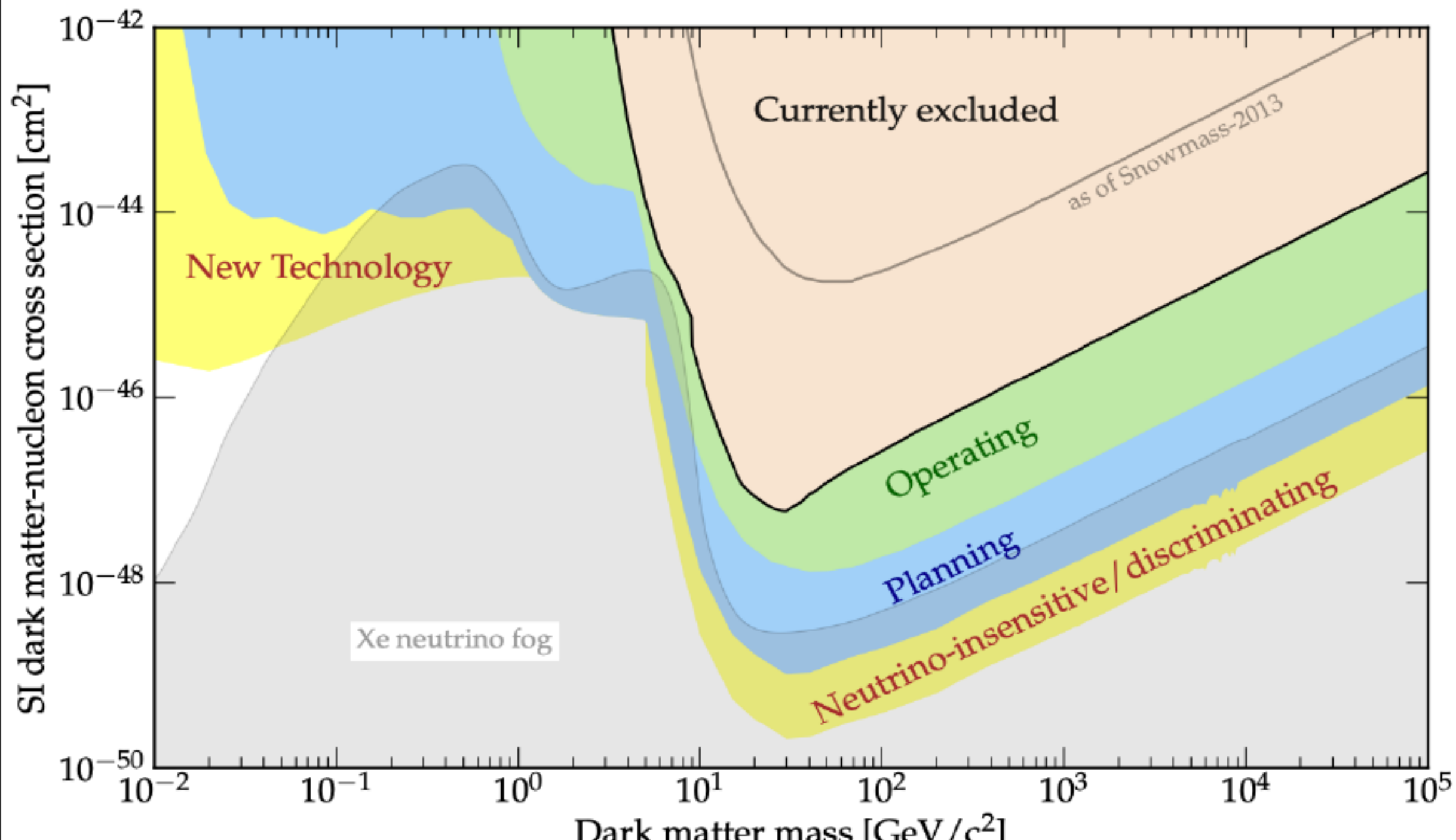
(Desperately?) seeking WIMPS

[Baudis & Profumo, PDG 2023]



**We have come
a long (10^2)
way...**

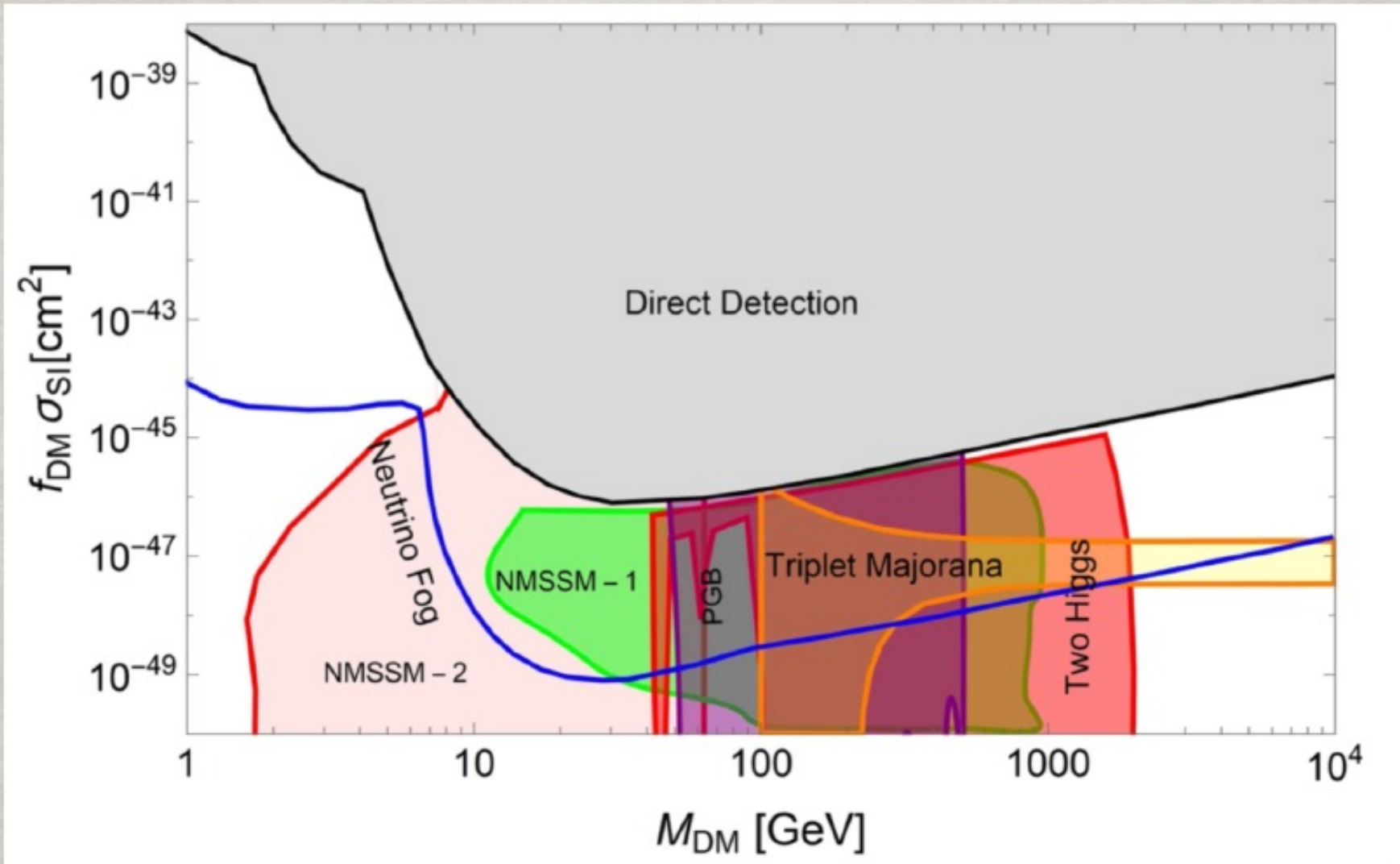
irreducible background, unless you measure the direction!



WIMP MODELS...

...NOT YET EXCLUDED !

[Snowmass 2021 Cosmic Frontier ArXiv:2203.08084]

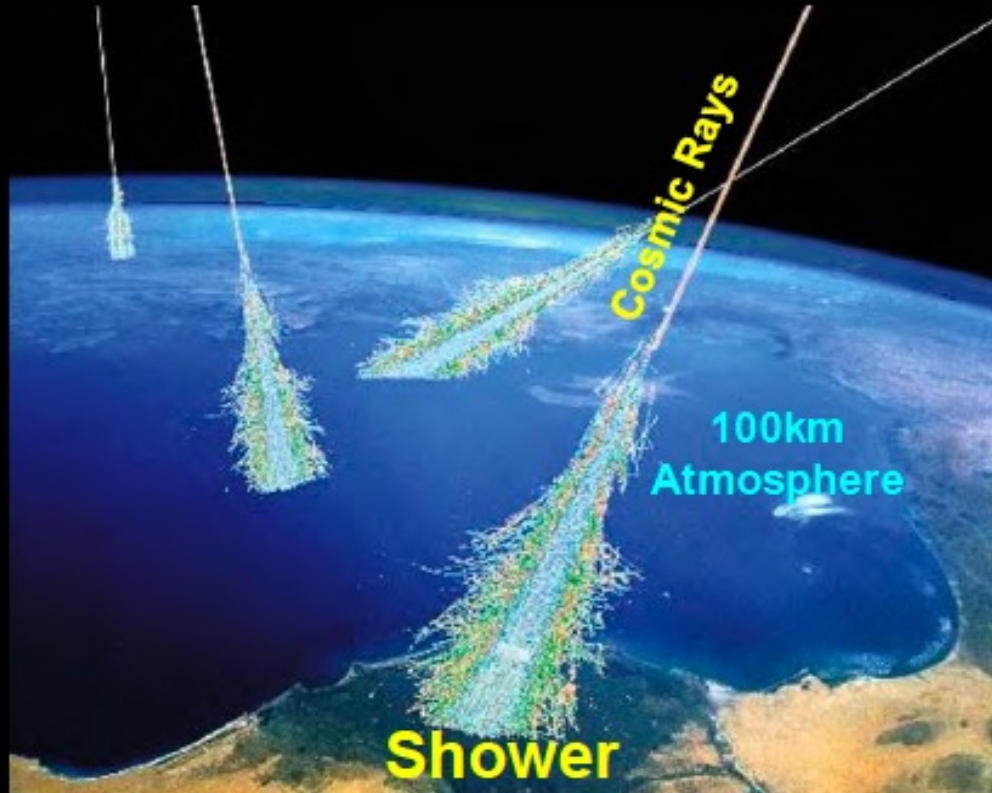


AMS on the Space Station

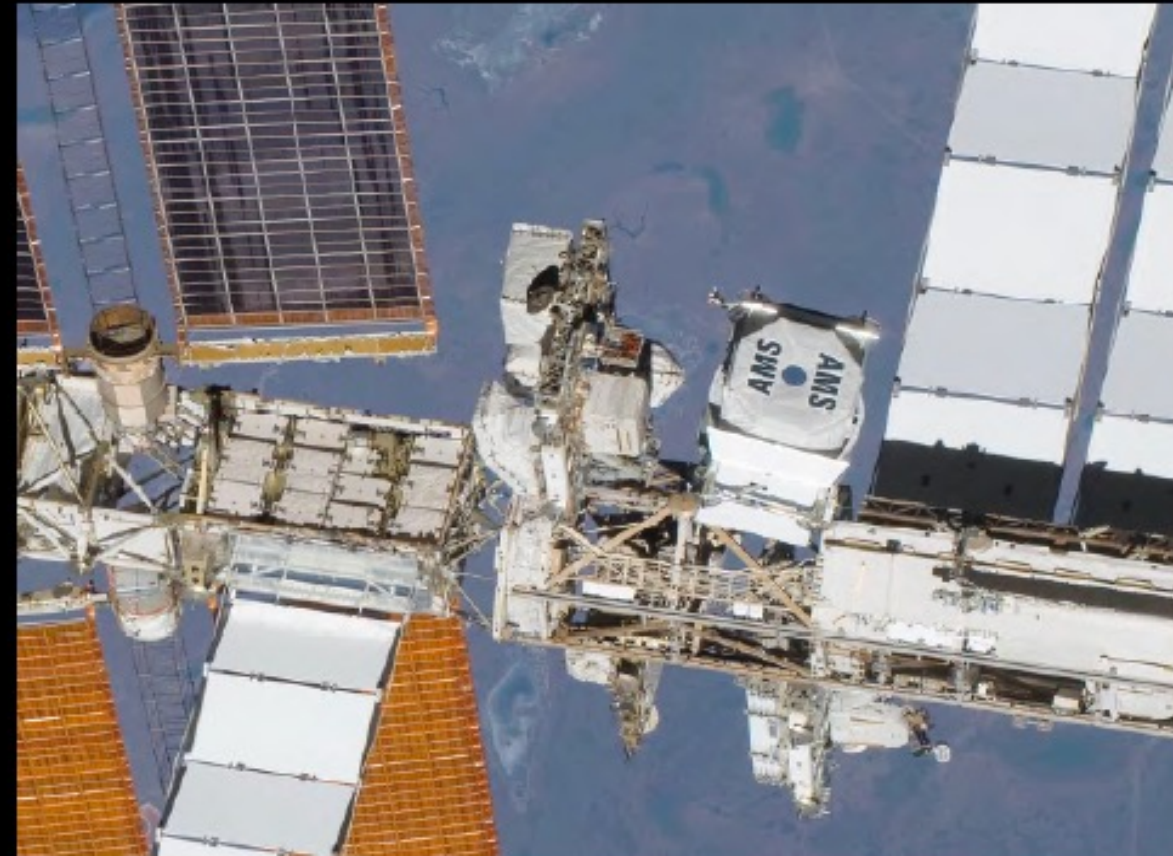
Provides precision, long-duration measurements of charged cosmic rays to study the Origin of the Cosmos, the physics of Dark Matter and of Antimatter

Charged cosmic rays have mass.

They are absorbed by the 100 km of Earth's atmosphere (10m of water).
The properties ($\pm Z$, P) of charged cosmic rays cannot be studied accurately on the ground.

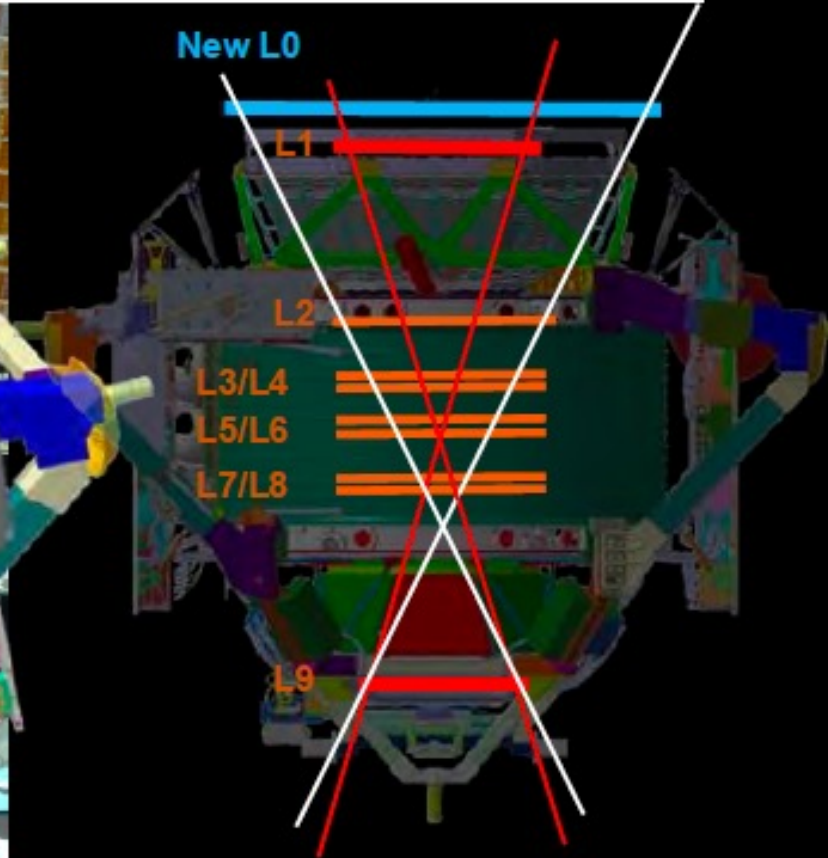
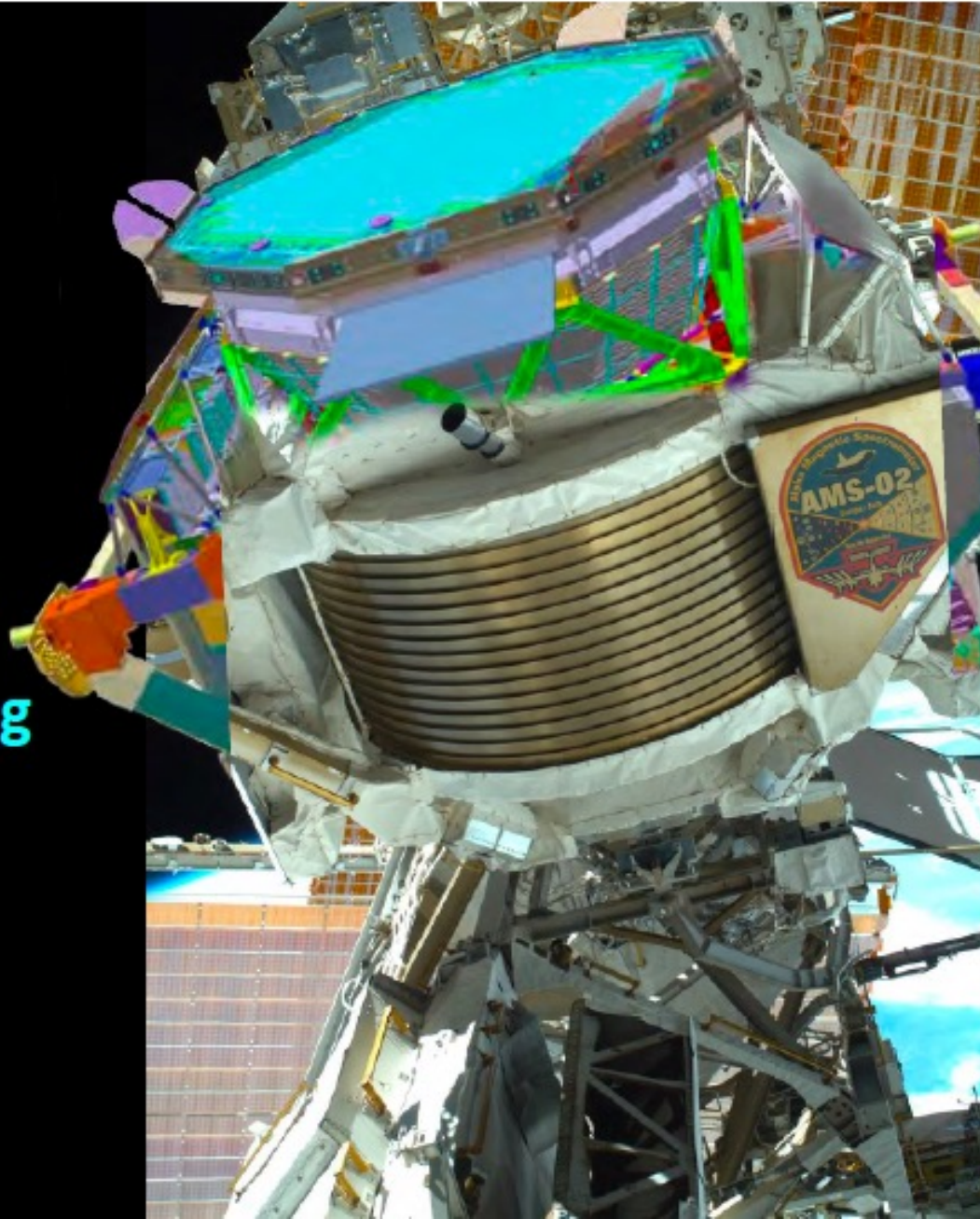


To measure cosmic ray charge and momentum requires a magnetic spectrometer in space



AMS 2011-2026

Continuous data-taking



AMS 2026-2030+

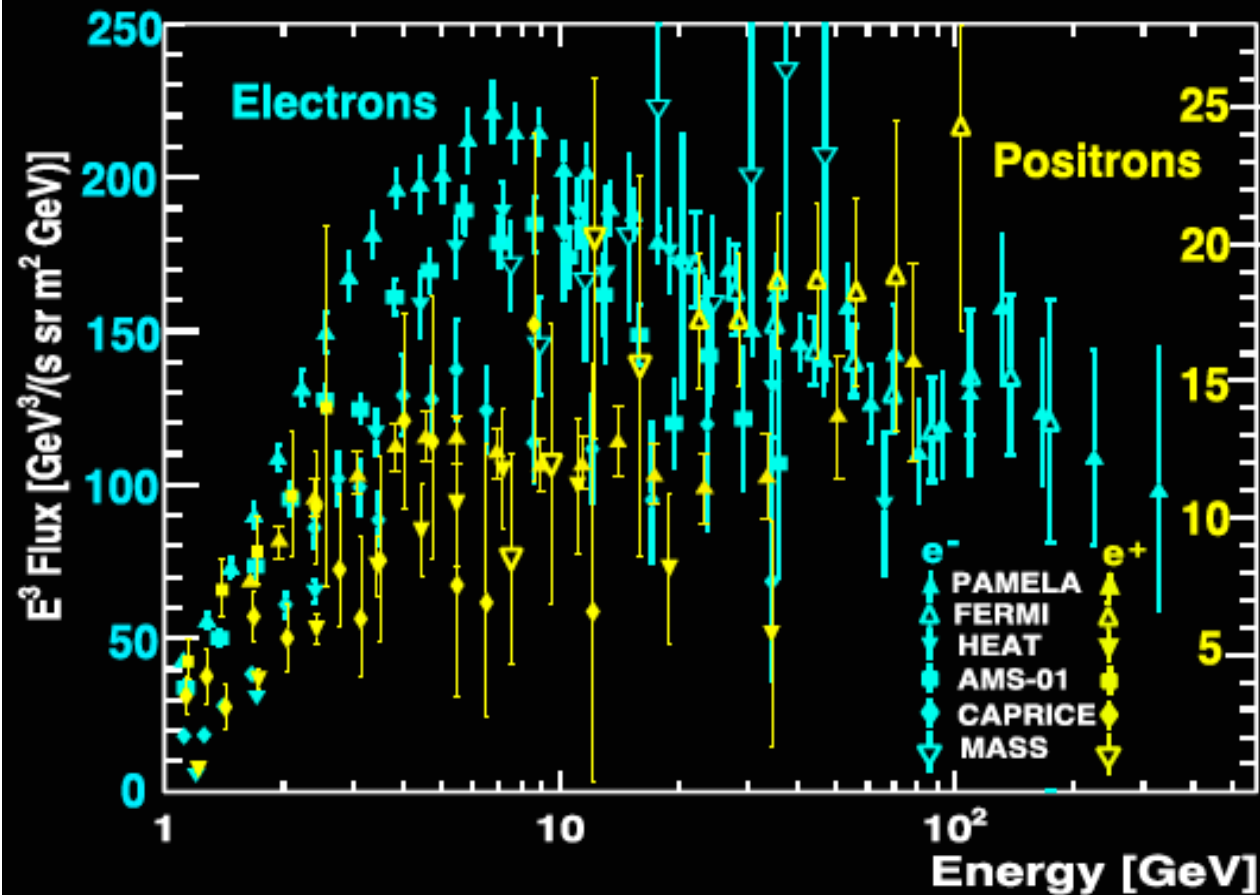
New 4+4m²

Silicon Tracker Planes

Acceptance increased to 300%

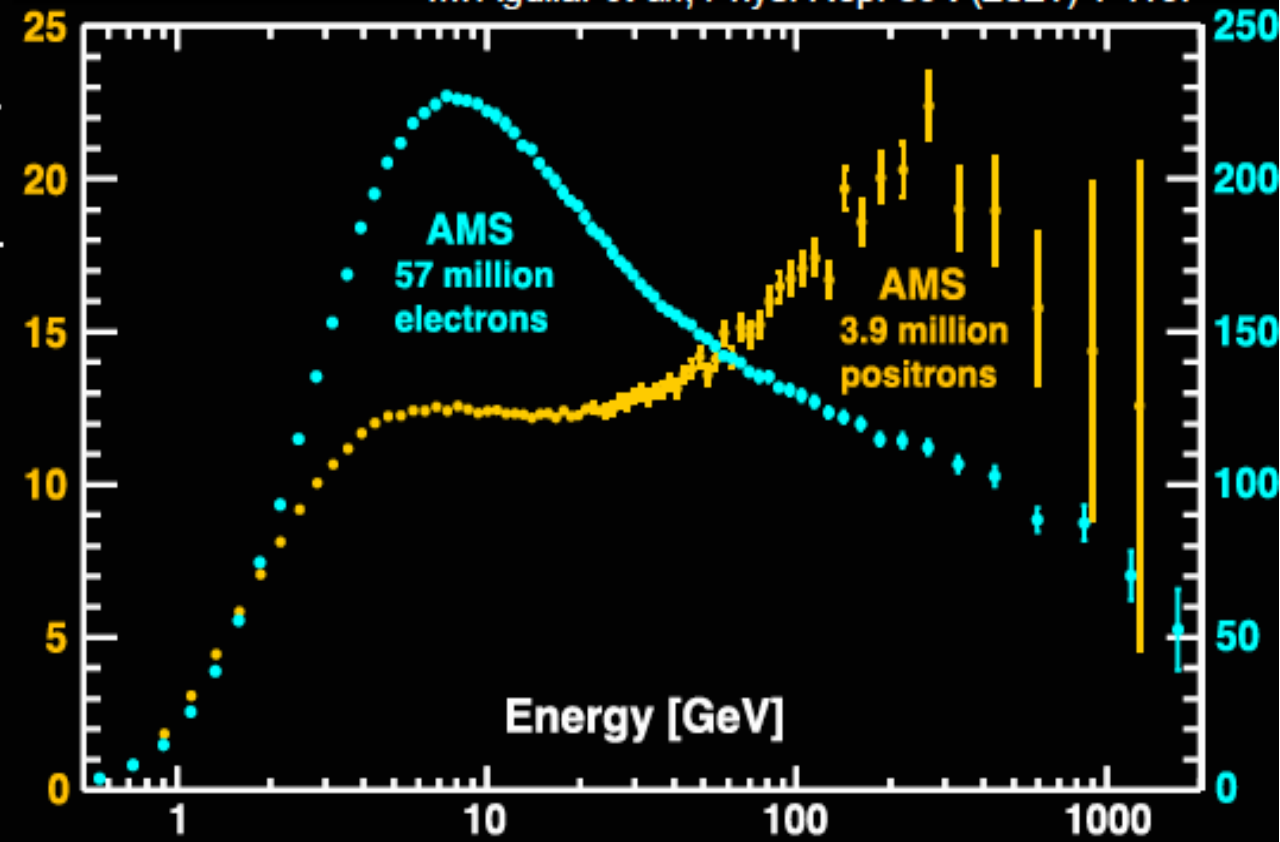
AMS Electron and Positron Fluxes

Measurements before AMS

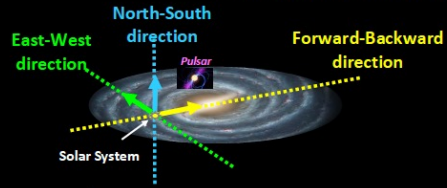


AMS measurements

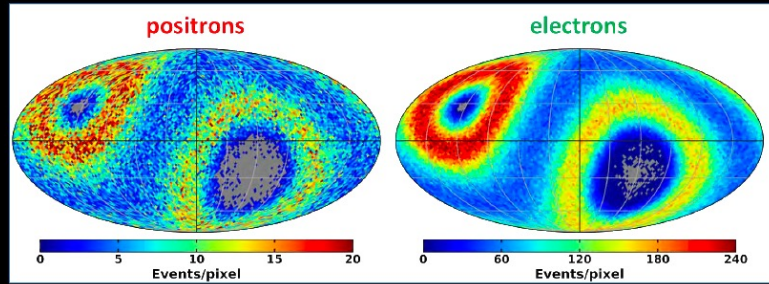
M. Aguilar *et al.*, Phys. Rep. **894** (2021) 1-116.



Positron Anisotropy and Dark Matter

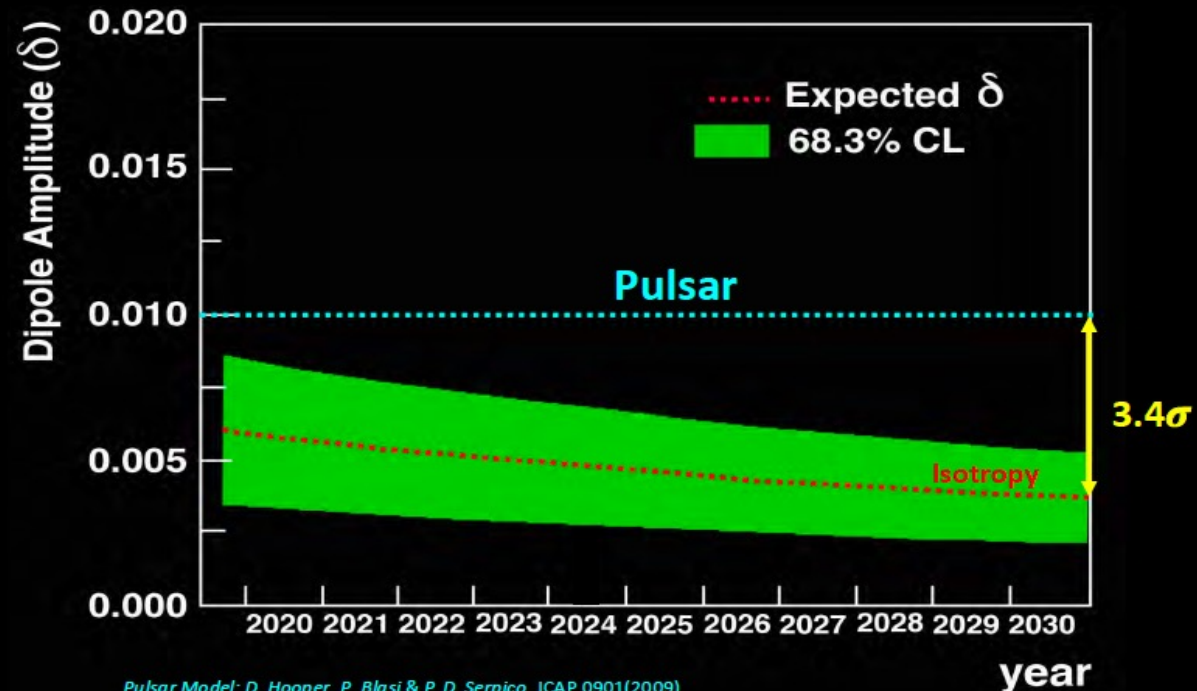


Astrophysical point sources will imprint a higher anisotropy on the arrival directions of energetic positrons than a smooth dark matter halo.



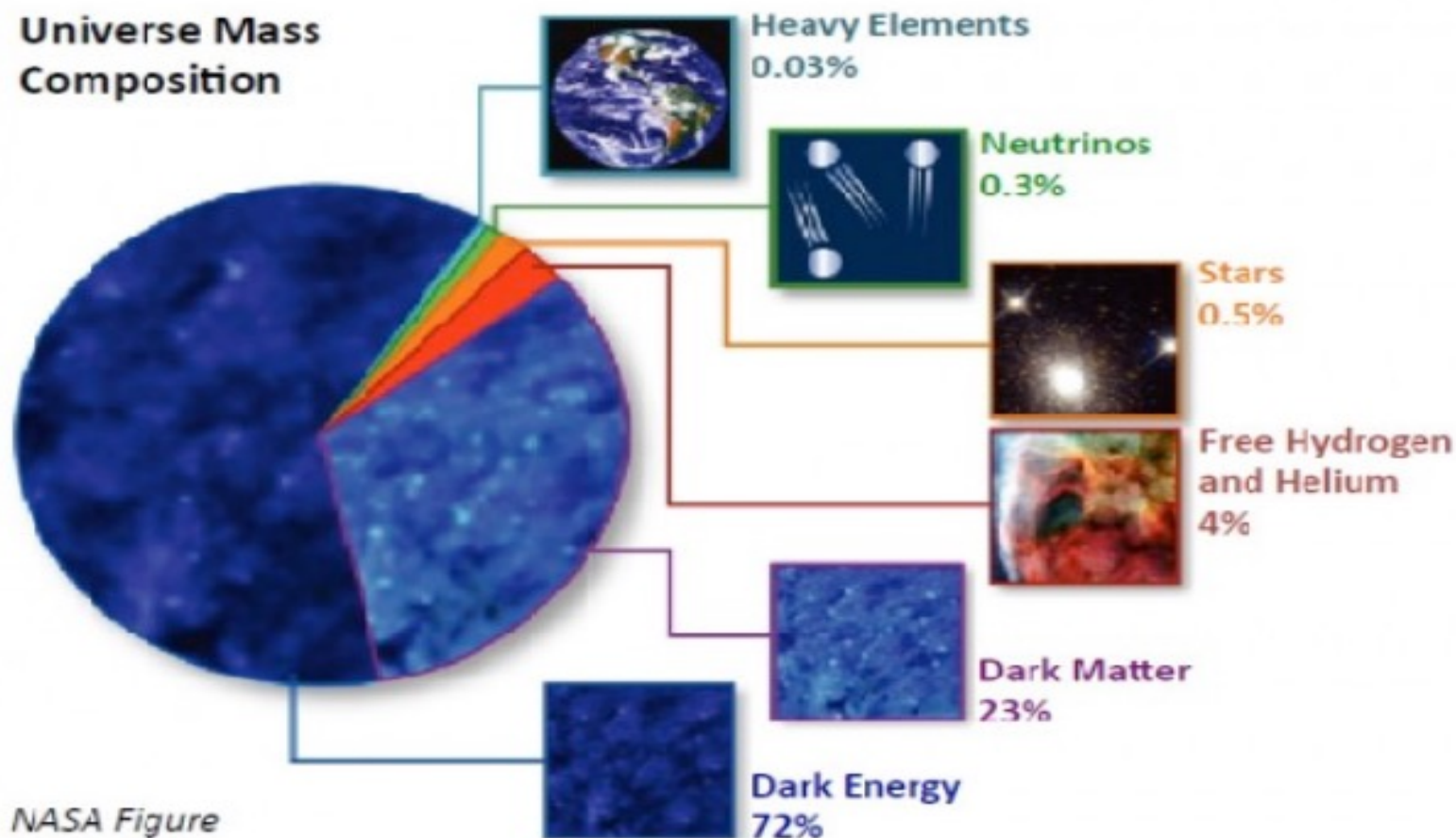
How to discriminate whether positrons come from a **pulsar** or from **DM**

By 2030, the positron statistics will allow us to measure the anisotropy accurately to permit a separation between dark matter and pulsars at the 99.93% C.L.



UNIVERSE COMPOSITION

Universe Mass
Composition



NASA Figure

Why $\Omega_{DM} h^2 \sim 5 \Omega_B h^2$?

ASYMMETRIC DARK MATTER

[Griest & Seckel '87, Kaplan, Luty & Zurek 90, ...]

Assume instead that there is an asymmetry stored in DM as in baryons: DM asymmetry generated in the same way as the baryon asymmetry..

It may also be generated together with the baryon asymmetry and then it is natural to expect the **SAME** asymmetry in both sectors.

$$\Psi \rightarrow B + X$$

$$n_{DM} \sim n_b \rightarrow \Omega_{DM} \sim 5 \Omega_b$$

$$\text{for } m_{DM} \sim 5 m_p = 5 \text{ GeV}$$

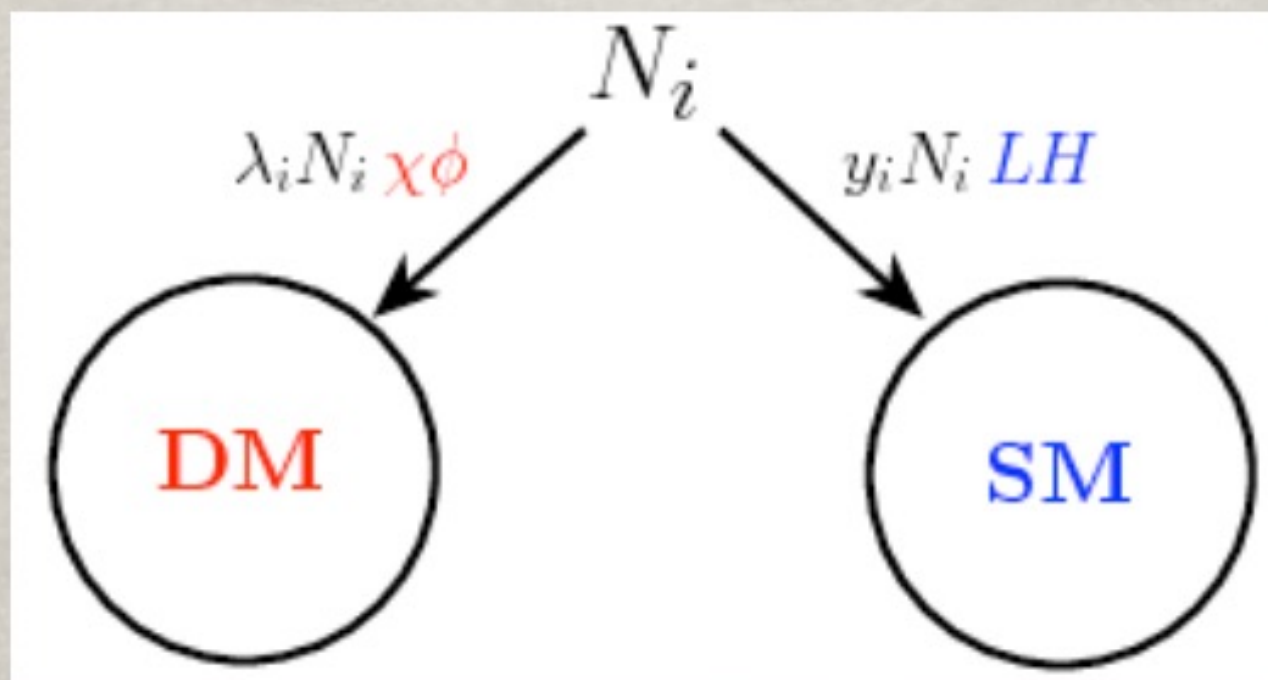
The puzzle of similar densities can be given by similar masses !

ASYMMETRIC DARK MATTER

[Griest & Seckel '87, Kaplan, Luty & Zurek 90, ...

Falkowski, Ruderman & Volansky 2011]

Simple mechanism to generate such case:
out-of-equilibrium decay of a particle producing
both B-L and DM, e.g. even decay of a RH neutrino



For the last ~ 30 years we have been focusing on the WIMP scenario



Our experimental effort is strongly focused on the WIMP!



New production mechanisms and mediation schemes often imply a hidden dark sector: Possibly with complex dynamics.



Such hidden sectors often include low scale particles, below the GeV scale.

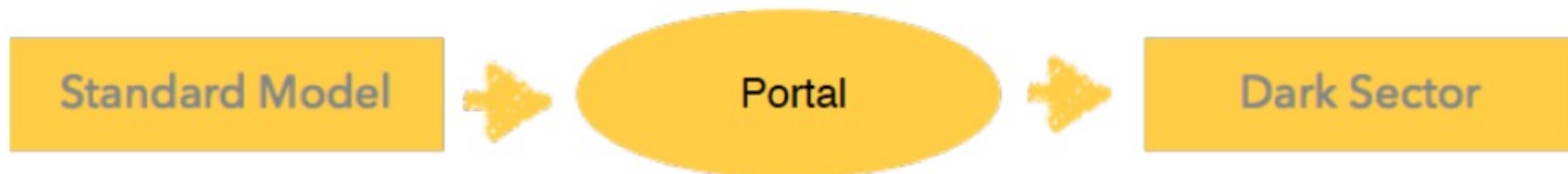
Very different from the WIMP paradigm!!

Or **very light axions**, or axion-like particles (**ALPs**) or **very heavy**, macroscopic objects DM, for instance **primordial Black Holes**

Dark Sectors

What is meant by a dark sector ?

A Hidden sector, with Dark matter, that talks to us through a Portal



Portal can be the Higgs boson itself or New Messenger/s

Dark sector has dynamics which is not fixed by Standard Model dynamics

→ New Forces and New Symmetries

→ Multiple new states in the dark sector, including Dark Matter candidates

Interesting, distinctive phenomenology

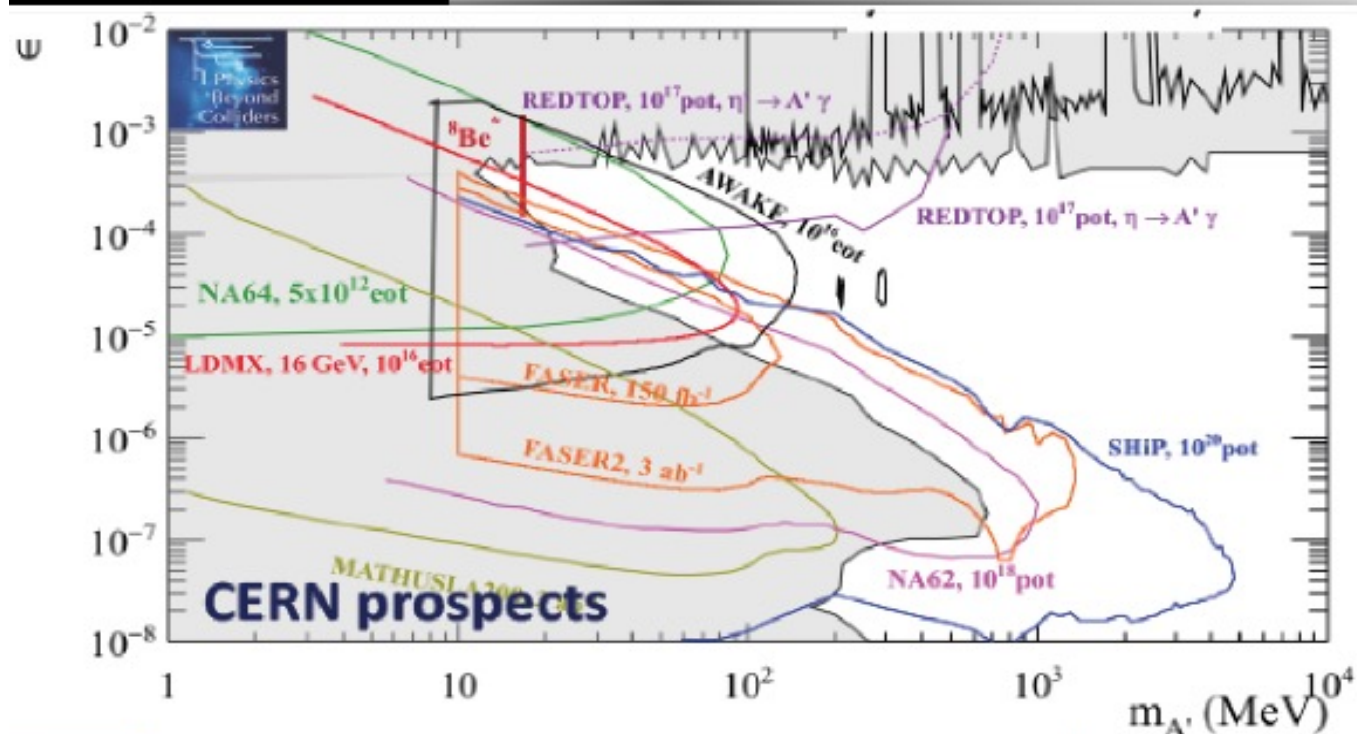
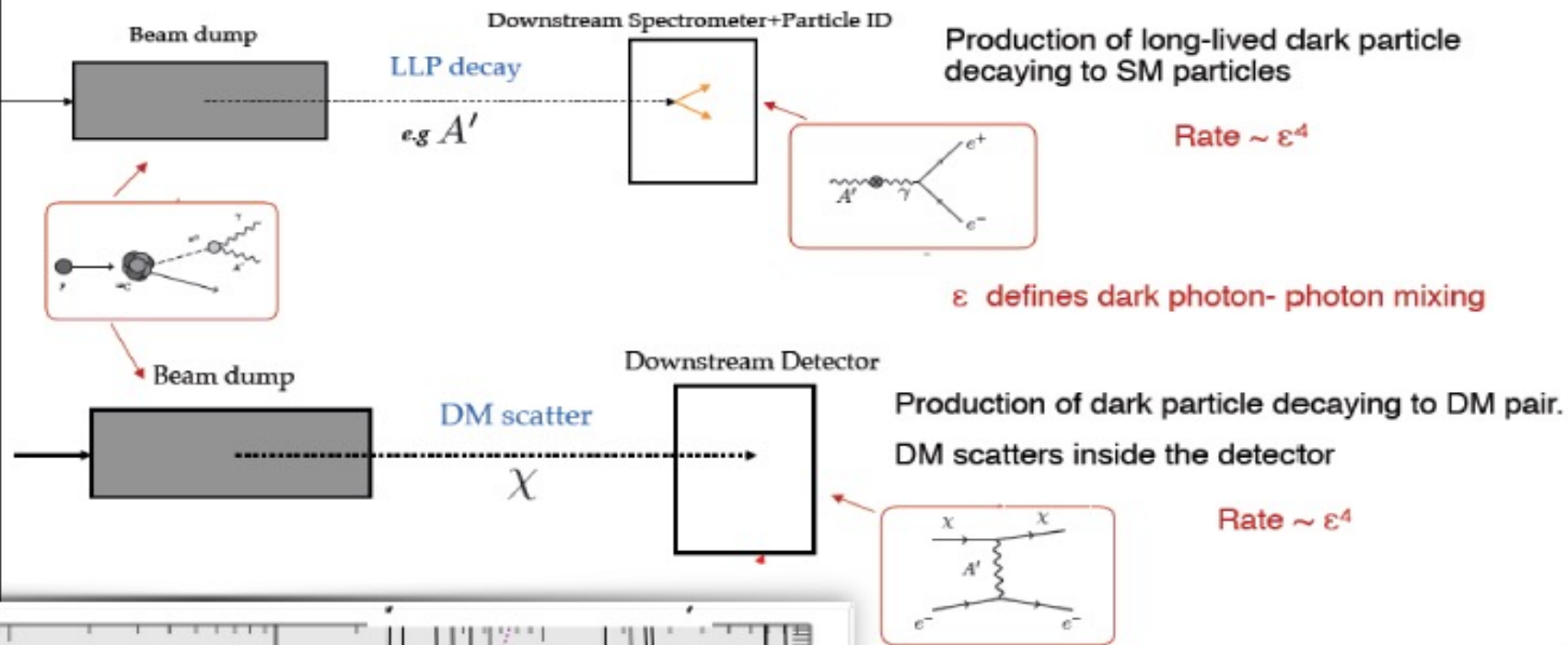
Long-Lived Particles

Feebly interacting particles (FIP's)

**Summary talk by Asai and
Catena of the DM WG at the EU
Strategy Granada Symposium**

Fixed-Target Strategies

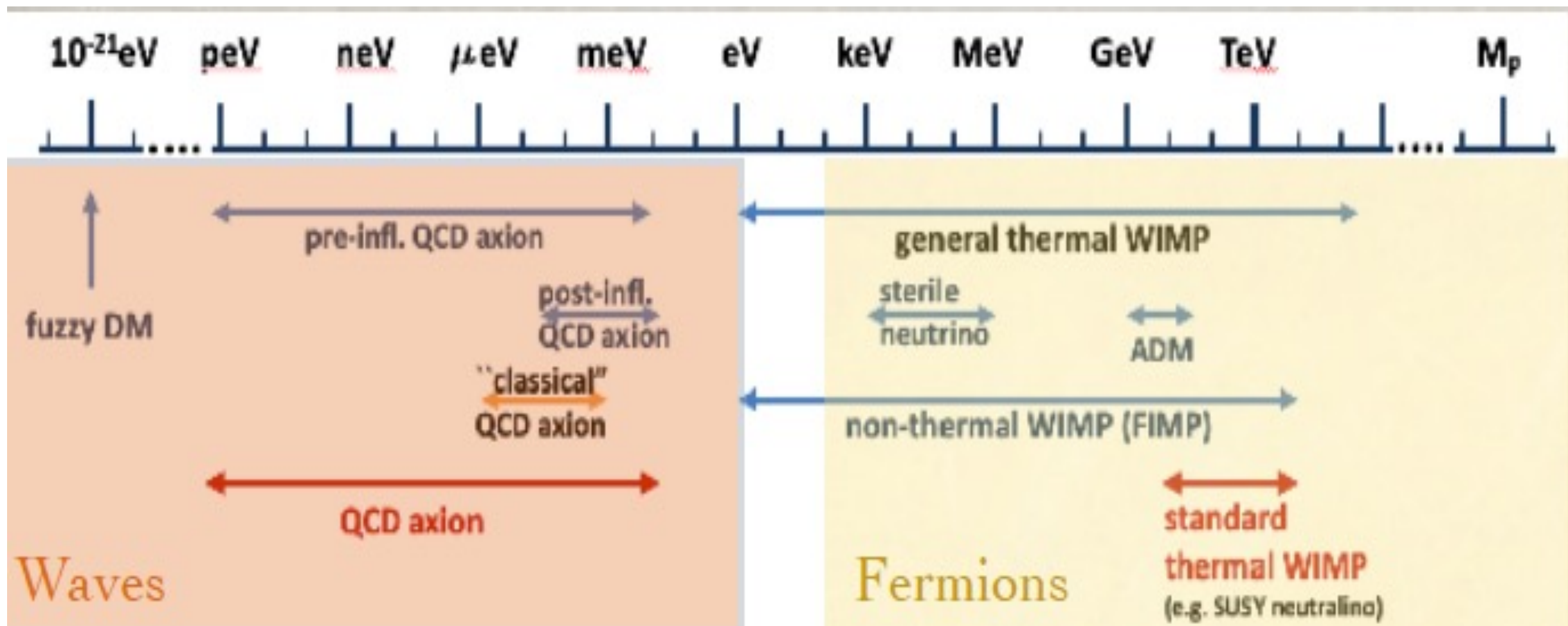
Renaissance of the fixed-target!



Many new experiments planned or proposed for hidden sector searches.

Major synergistic topic of Dark Sectors work at CERN.

Ellis et al., ESPPU Physics Briefing Book, CERN-ESU-004 (2019)



STRONG CP & THE AXION

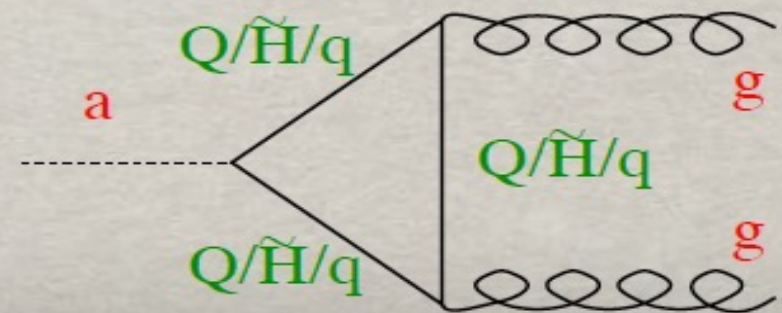
The QCD vacuum has a non trivial structure, as a superposition of different topological configurations, giving rise to strong CP problem from the term:

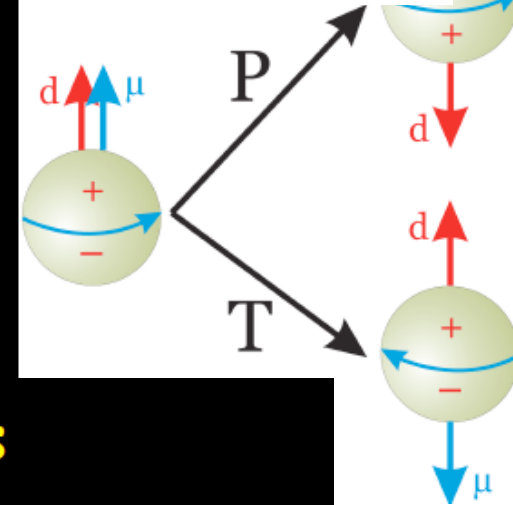
$$\mathcal{L} = \theta \frac{\alpha_s}{8\pi} F_{\mu\nu}^b \tilde{F}_b^{\mu\nu} \quad \text{['t Hooft 76]}$$

But from the bounds on neutron el. dipole moment $\theta < 10^{-9}$

Peccei-Quinn solution: add a chiral global U(1) and break it spontaneously at f_a , leaving the axion, a **pseudo-Goldstone boson**, interacting as

$$\mathcal{L}_{PQ} = \frac{\alpha_s}{8\pi f_a} a F_{\mu\nu}^b \tilde{F}_b^{\mu\nu}$$

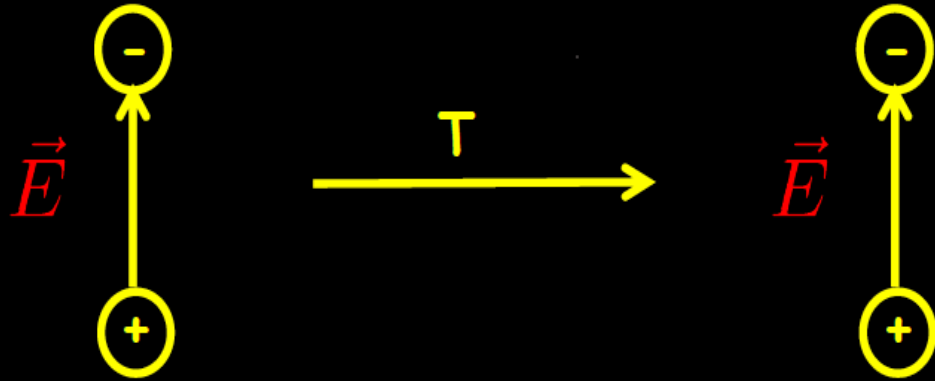




$$S = \int d^4x \left[-\frac{1}{4} G^{\mu\nu} G_{\mu\nu} - \frac{\theta}{4} G^{\mu\nu} \tilde{G}_{\mu\nu} + i\bar{\psi} D_\mu \gamma^\mu \psi - \right]$$

" $\sim \theta \vec{E} \cdot \vec{B}$ "

- The θ -term violates time reversal (T=CP)!



T=CP

$$\vec{E} \longrightarrow \vec{E}$$

$$\vec{B} \longrightarrow -\vec{B}$$

$$\vec{E} \cdot \vec{B} \longrightarrow -\vec{E} \cdot \vec{B}$$

**Electric
dipole moment
of the neutron!**

- Detailed calculation gives

$$|\vec{d}| \sim 1 - 10 \times 10^{-16} e cm \theta$$

$$\Rightarrow |\theta| \lesssim 10^{-10}$$

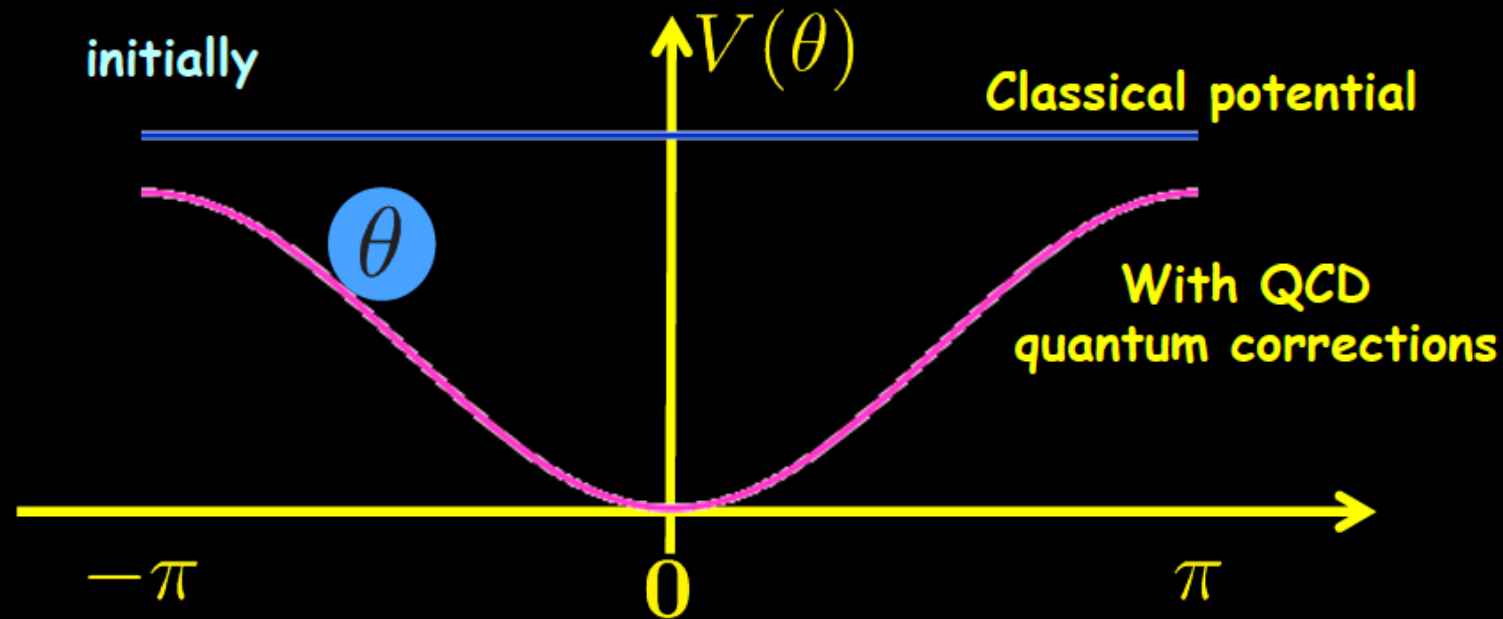
?

Extremely unnatural!

The axion solution to the strong CP problem

J. Jaeckel,
ISAPP – Padova 2024

- Make θ dynamical \rightarrow it can change its value



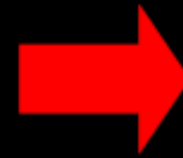
- Canonically normalize $\theta = a/f_a$

$$\Rightarrow V[a/f_a = \theta = 0] \leq V[\theta] \quad \forall \theta$$

$\Rightarrow \theta = a/f_a$ will evolve to $a = \theta = 0$

\Rightarrow CP is conserved

**a is Goldstone boson
of a U(1) symmetry**



Axion!

Peccei-Quinn Symmetry

J. Jaeckel,
ISAPP – Padova 2024

- **Toy model:**

$$\mathcal{L} = -\frac{1}{4}F^2 + i\bar{\psi}D_\mu\gamma^\mu\psi - |\partial_\mu\phi|^2 - \mu^2|\phi|^2 - \lambda|\phi|^4 \\ + i\bar{\psi}\left(Y\phi\frac{1+\gamma_5}{2} + Y^*\phi^*\frac{1-\gamma_5}{2}\right)\psi$$

- **U(1):** $\phi \rightarrow \exp(i\beta)\phi$
 $\psi \rightarrow \exp\left(-i\frac{\beta}{2}\gamma_5\right)\psi$
- **If $\mu^2 < 0$ we have SSB**



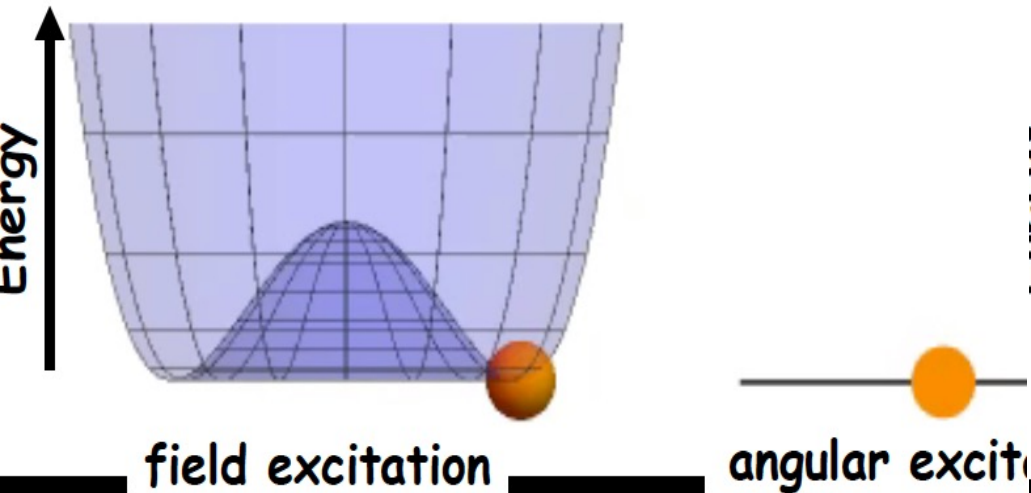
Phase is Goldstone



Use it as Axion

What is a Goldstone Boson?

- Let us start with a $U(1)$ /rotation symmetric potential

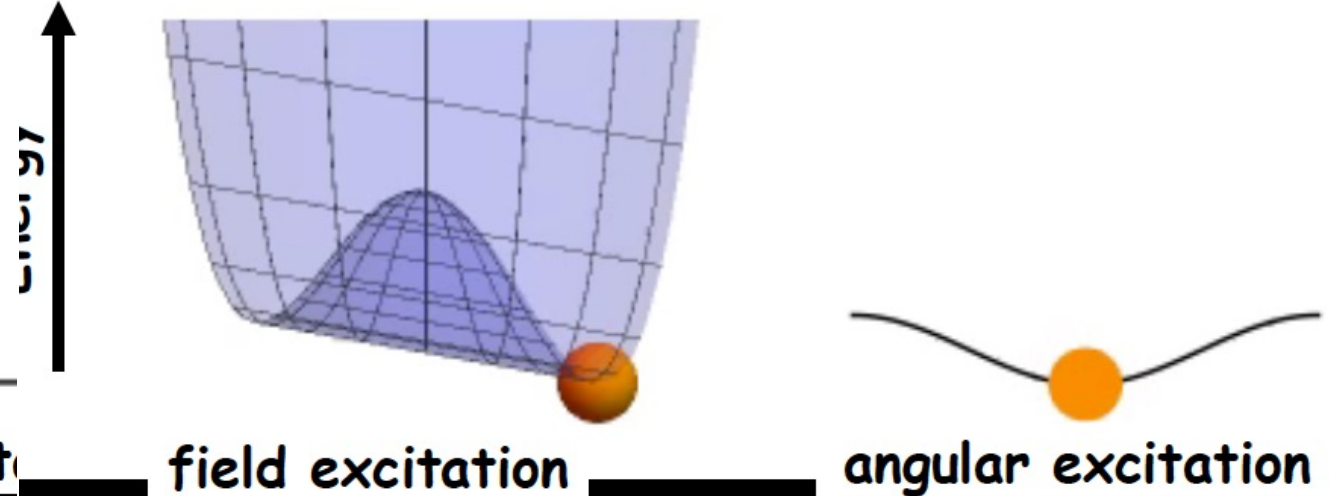


→ If you move along the minimum, it costs no energy to move around

→ Particle is massless

What is a **pseudo**-Goldstone Boson?

- Add a **small breaking** of $U(1)$ /rotation symmetry



→ If you move along the minimum, it costs a little bit of energy

→ Particle has a small mass

Breaking of the **exact $U(1)$ PQ symmetry** → axion is the resulting massless Goldstone boson

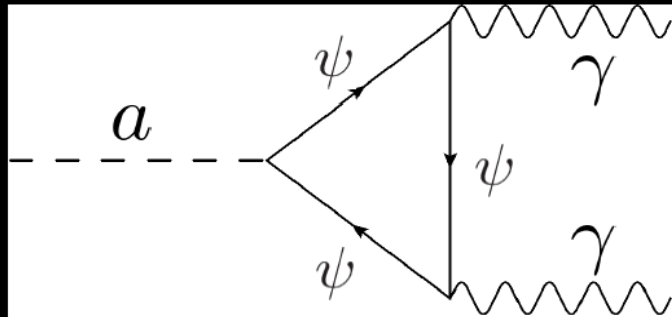
Wilczek, Weinberg → due to quantum effects, the PQ symmetry is ANOMALOUS, hence it is **NOT** an exact symmetry even before the SSB the axion is a massive **PSEUDO-Goldstone boson**

Mass and couplings of the axion as a function of the PQ symmetry breaking scale f_a

$$m_a \simeq 6 \text{ eV} \frac{10^6 \text{ GeV}}{f_a}$$

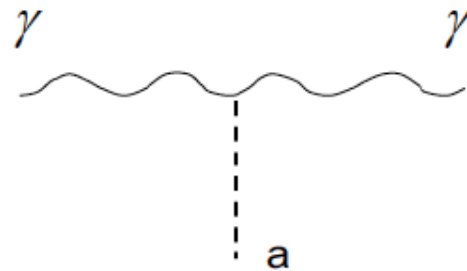
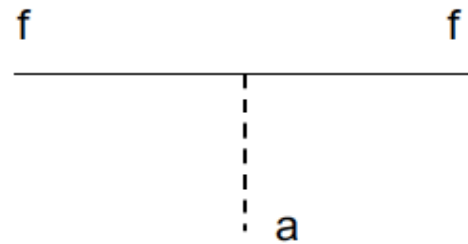
The Coupling to FF (GG analog)

• A diagram



• And a dimensional argument:

$$g \sim \frac{1}{\text{mass}} \sim \frac{1}{f_a}$$



$$\mathcal{L}_{a\bar{f}f} = ig_f \frac{a}{f_a} \bar{f} \gamma_5 f$$

$$\mathcal{L}_{a\gamma\gamma} = g_\gamma \frac{a}{f_a} \vec{E} \cdot \vec{B}$$

$$g_\gamma = \begin{array}{ll} 0.97 & \text{in KSVZ model} \\ 0.36 & \text{in DFSZ model} \end{array}$$

AXIONS AS DARK MATTER

Their energy density by misalignment is

$$\Omega_a h^2 = 0.5 \left(\frac{f_a}{10^{12} \text{GeV}} \right)^{7/6} \theta_i^2 \rightarrow P(\theta_i)$$

Axions can contribute to star/SN cooling and so

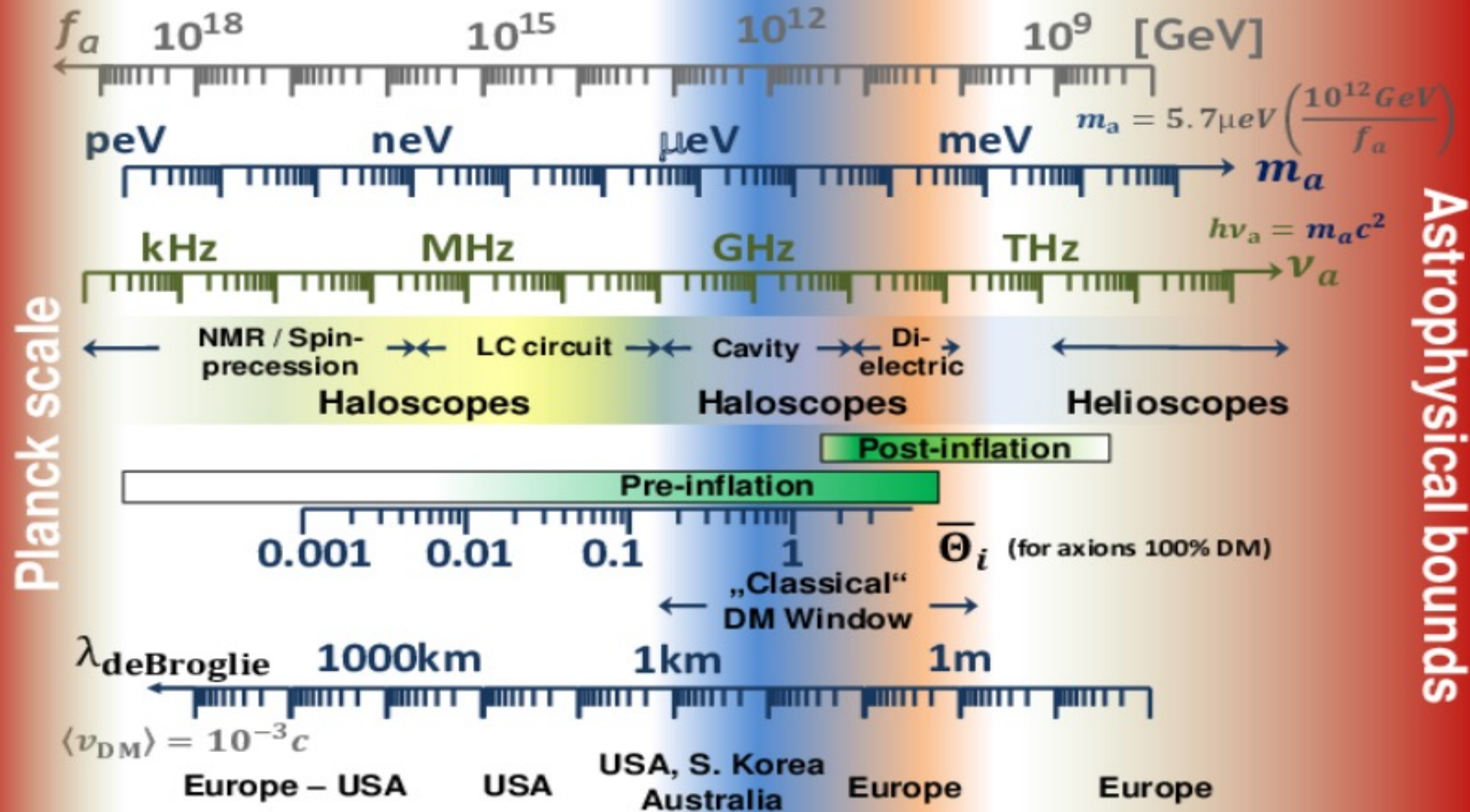
$$0.5 \times 10^{10} \text{GeV} \leq f_a \leq 10^{12} \text{GeV}$$

[Raffelt 98]

Therefore the mass for axion DM is very small:

$$m_a = \Lambda_{QCD}^2 / f_a \sim 6 \times 10^{-5} \text{eV} \left(\frac{f_a}{10^{11} \text{GeV}} \right)^{-1}$$

AXION'S CONSTRAINTS

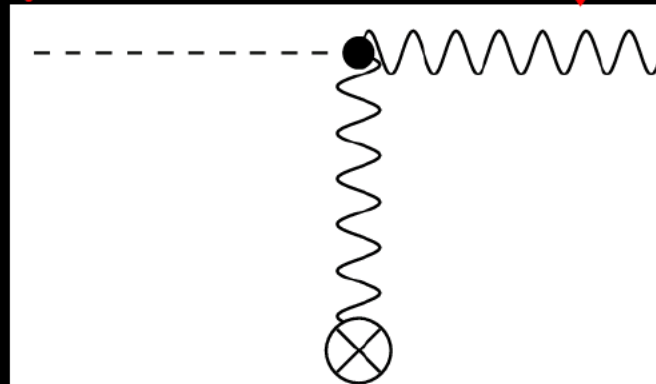


[Billard et al. 2104.07654]

• Photon Regeneration

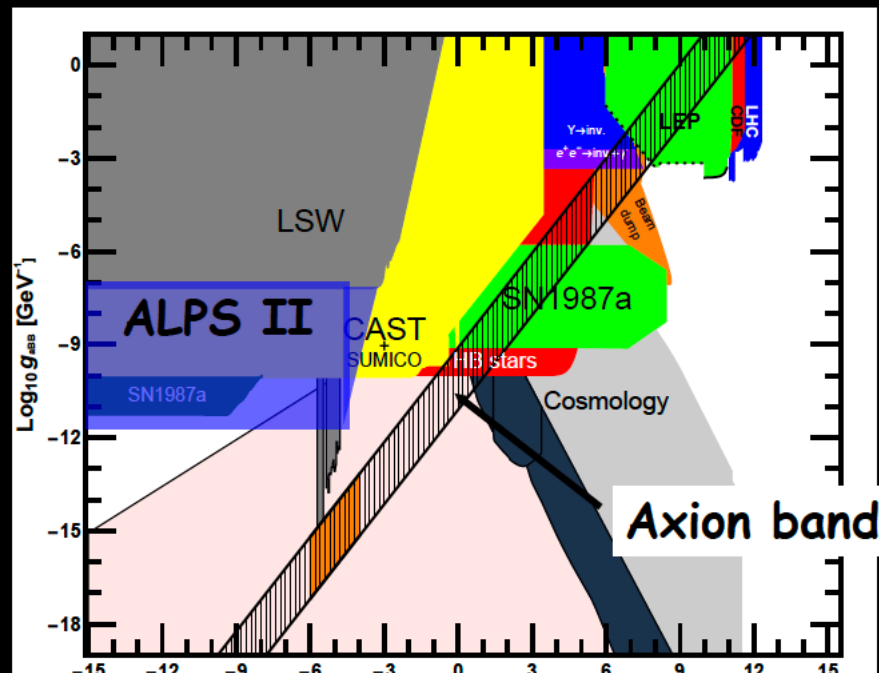
Photon
(amplified in resonator)

axion
(dark matter)



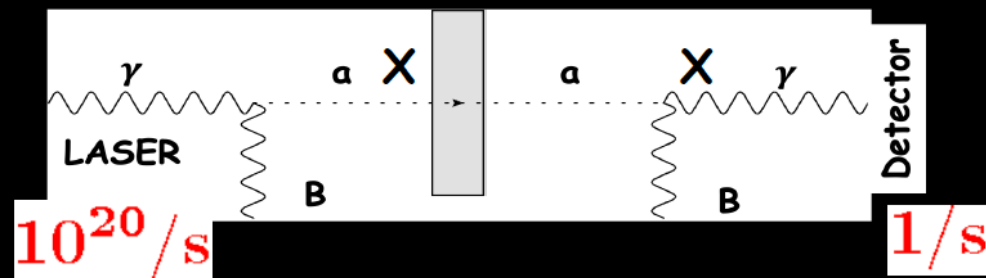
mass/energy

Weaker interaction



Light shining through walls

Light shining through walls

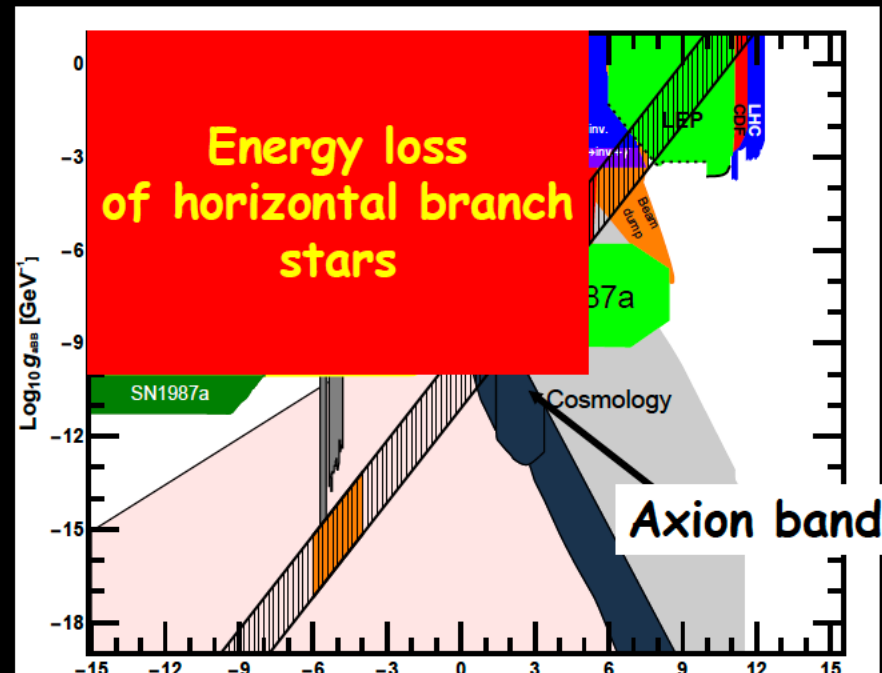


• Test $P_{\gamma \rightarrow X \rightarrow \gamma} \lesssim 10^{-20}$

• Enormous precision!

• Study extremely weak couplings!

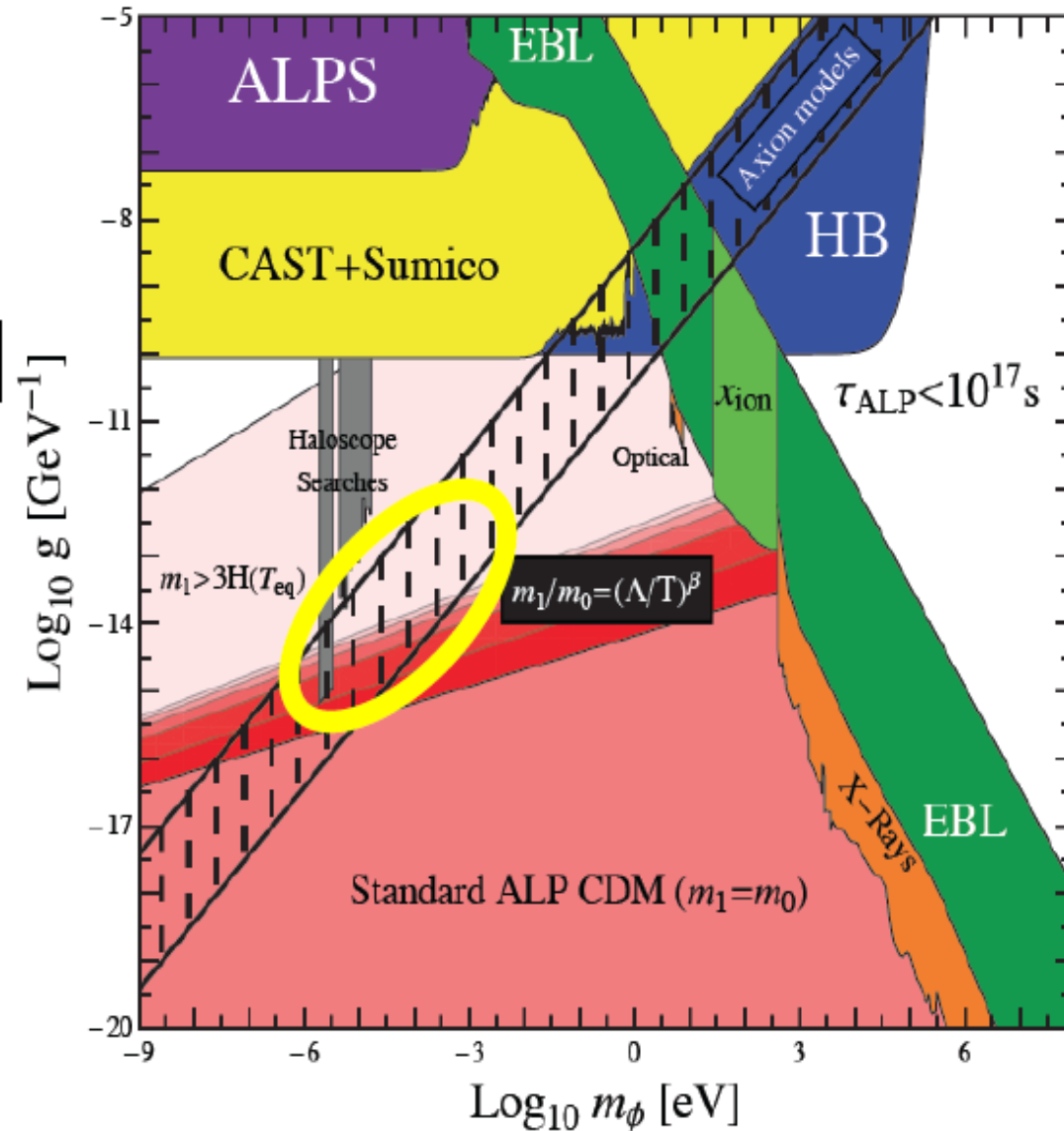
Weaker interaction



Axion(-like particle) Dark Matter

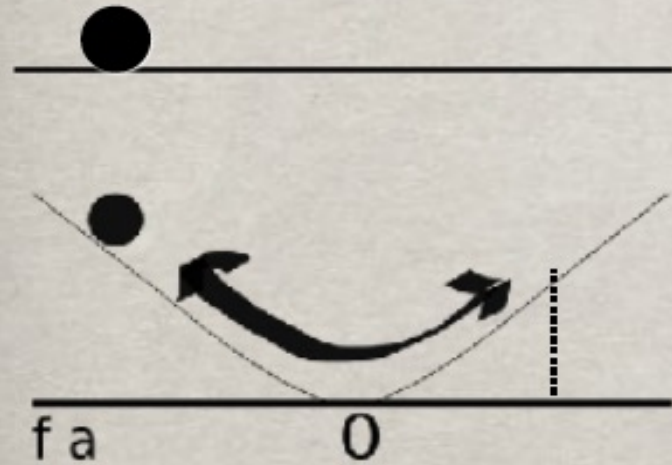
$\sim 10^7 \text{ GeV}$

$\sim 10^{12} \text{ GeV}$



AXIONS AS DARK MATTER

The axion is also a very natural DM candidate, but in this case in the form of a condensate, e.g. generated by the misalignment mechanism:



Before the QCD phase transition the potential for the axion is flat

After the QCD phase transition a potential is generated

$$V(a) = \Lambda_{QCD}^4 \left(1 - \cos \left(\theta + \frac{a}{f_a} \right) \right)$$

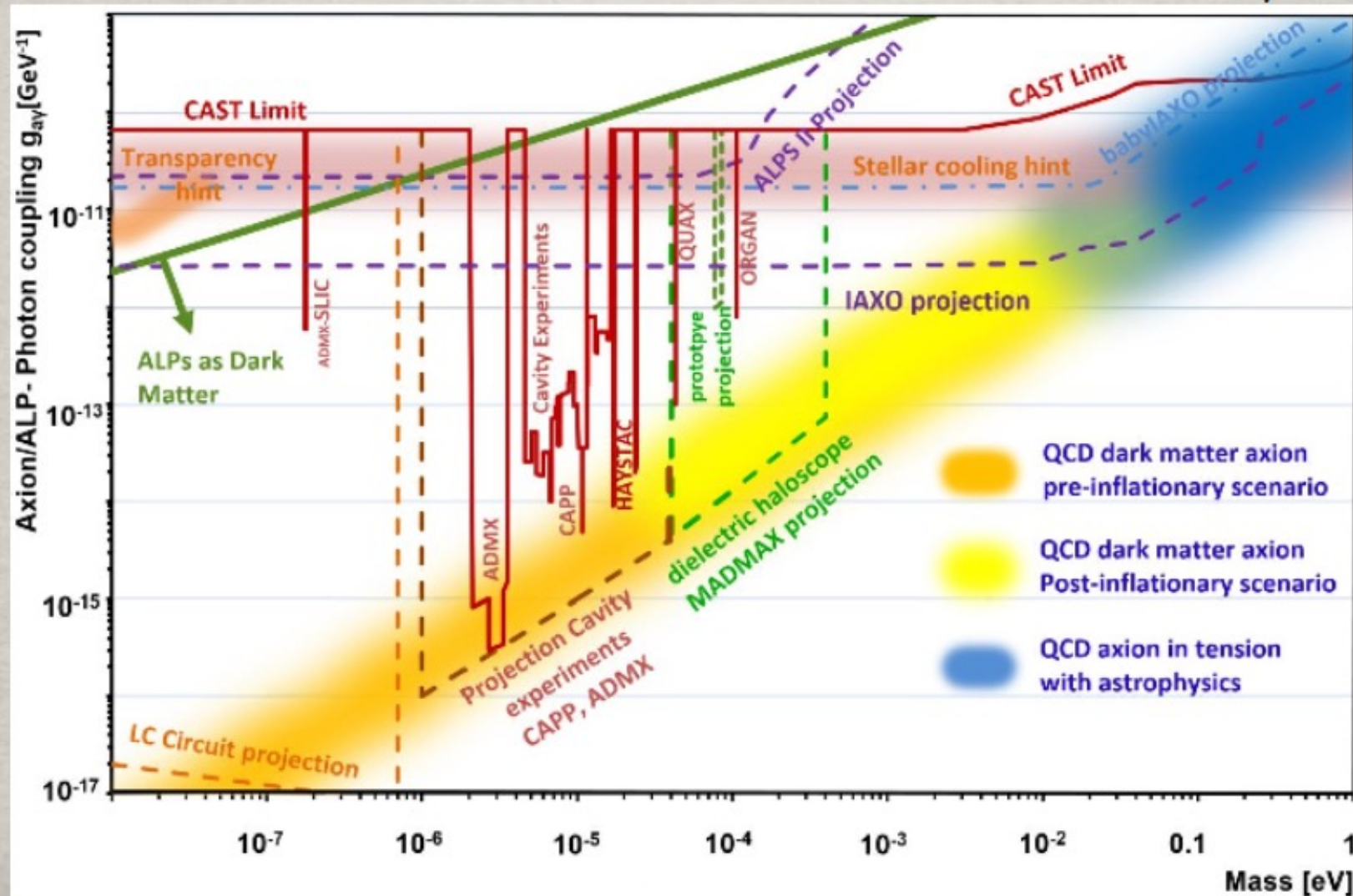
by instanton's effects and the axion starts to oscillate coherently around the minimum:

$$\Omega_a h^2 = 0.5 \left(\frac{f_a}{10^{12} \text{GeV}} \right)^{7/6} \theta_i^2$$

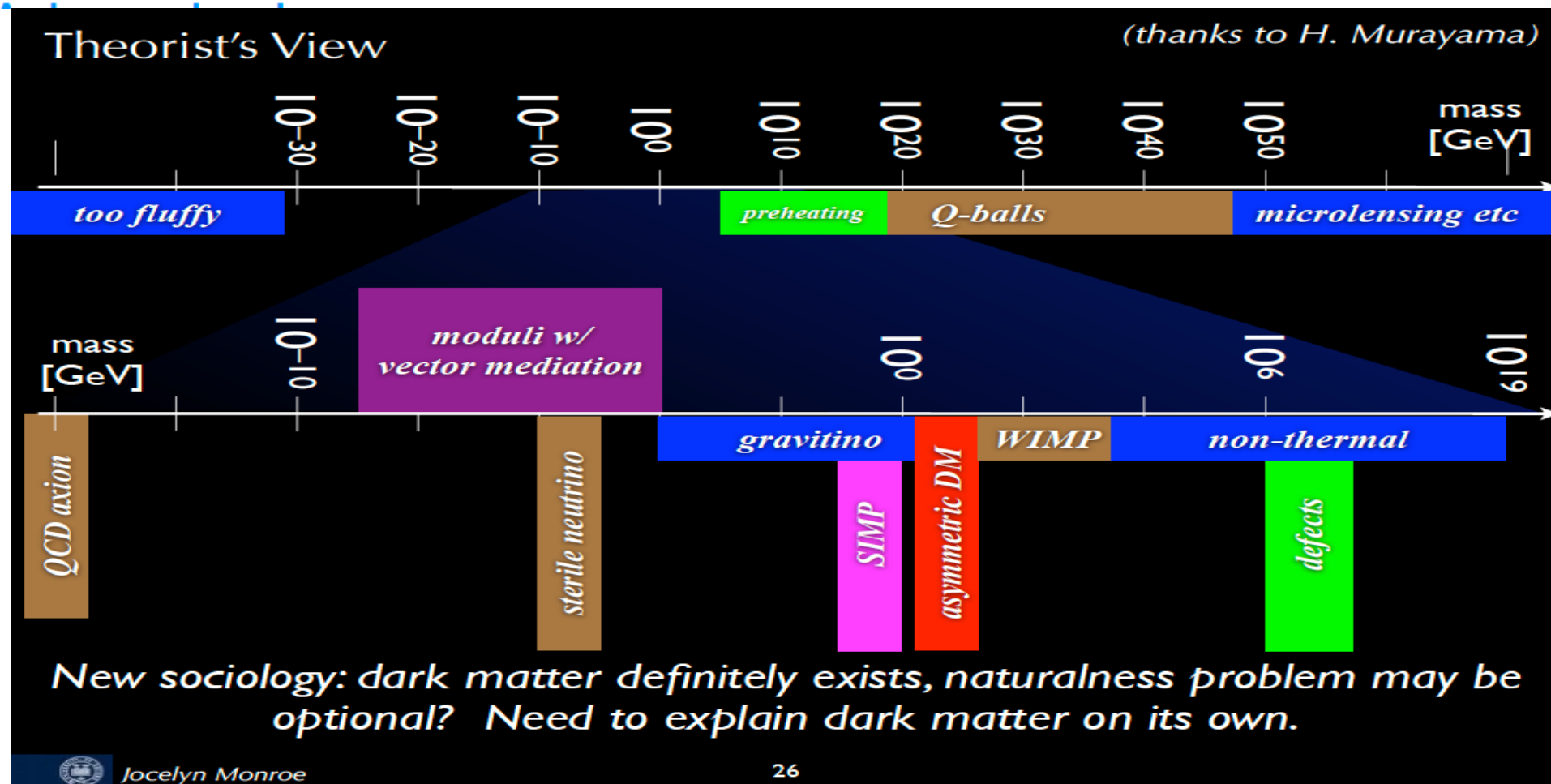
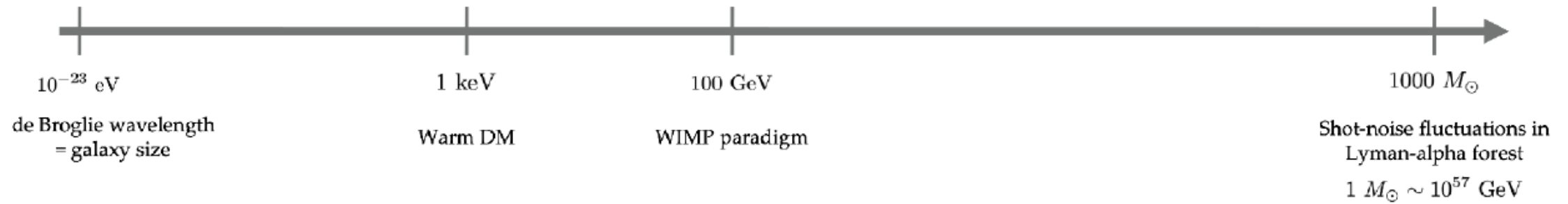
zero momentum particles \gg CDM !

AXION DM SEARCHES

The right abundance can be obtained if the Peccei-Quinn scale is of the order of 10^{11-12} GeV and the mass in the μ eV.



The Range of Possibilities is **Stunning!**



Very, Very Heavy Dark Matter

—P. Pani

Primordial BHs

$z \gg 3000$

Inflation

$z \sim 1000$

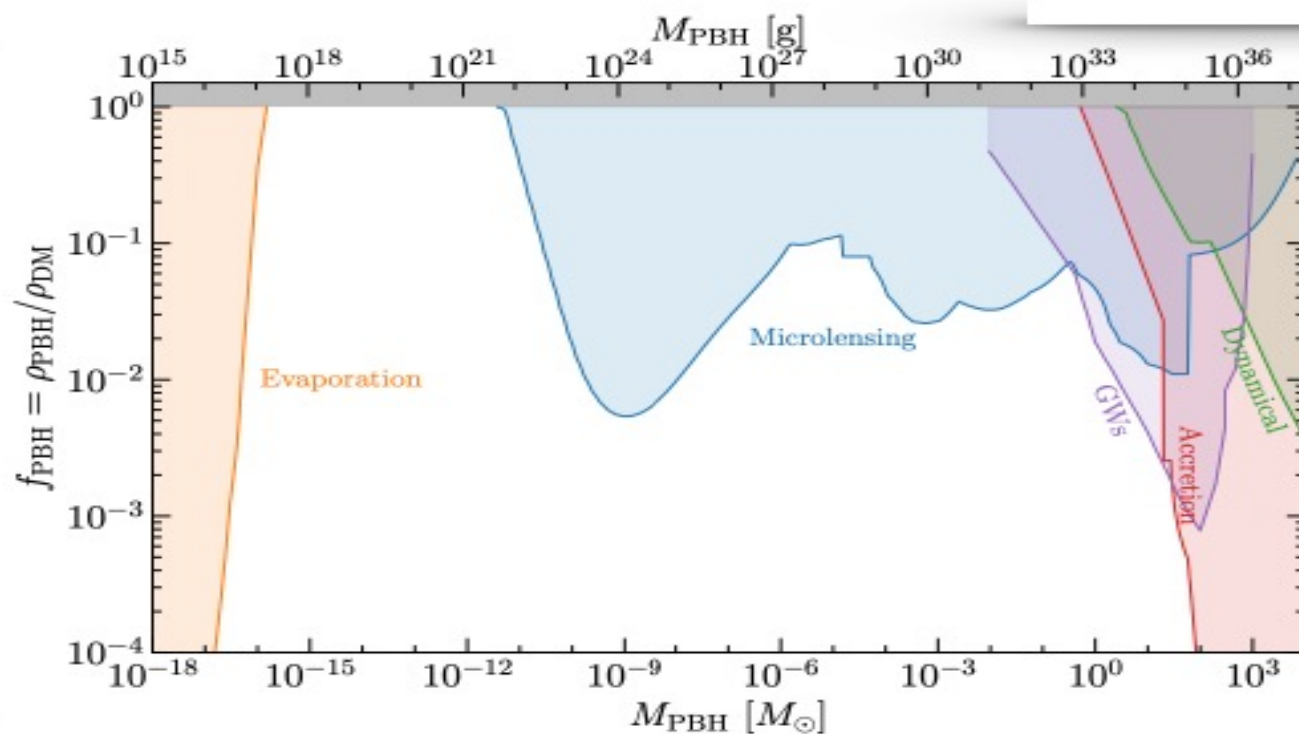
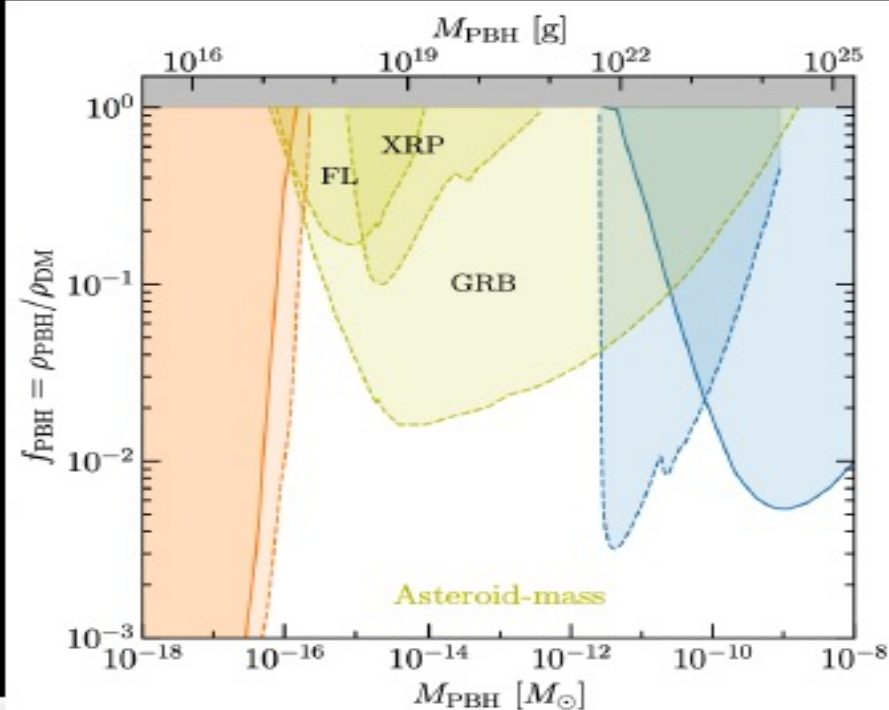
Primordial fluctuations

Cosmic microwave background

First stars $z \sim 10$

Astrophysical BHs

mass
[GeV]



non-thermal

defects

10¹⁹

Green et al, 2402.15211



Jocelyn

What the SM does not account for...

neutrino masses
dark matter
baryogenesis
inflation

OBSERVATIONAL
REASONS

3rd final take-home message

$M_{\text{HIGGS}} / M_{\text{PLANCK}} \sim 10^{-16}$
 $E_{\text{VACUUM}} (\text{DE}) / M_{\text{HIGGS}} \sim 10^{-14}$
 $\Theta_{\text{CPV in STRONG INTERAC.}} < 10^{-9}$

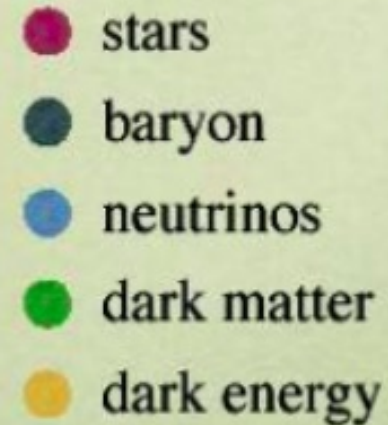
THEOR.
REASONS

+ lack of **UNIFICATION** of the
ELW. and strong interactions

+lack of a physical “explanation” of the
(largely different) **masses and mixings**
of the fermions

THE MYSTERY OF THE 5 NUMBERS THAT THE SM IS UNABLE TO EXPLAIN

- Stars and galaxies are only $\sim 0.5\%$
- Neutrinos are $\sim 0.1-1.5\%$
- Rest of ordinary matter
(electrons, protons & neutrons) are 4.4%



- Dark Matter 27 % WHAT IS DM MADE OF?
- Dark Energy 68 % ENERGY OF THE QUANTUM VACUUM?
- Anti-Matter 0% WHAT PRODUCED THE COSMIC MATTER-ANTIMATTER ASYMMETRY
- Higgs Bose-Einstein condensate
 $\sim 10^{62}\%??$ COSMOLOGICAL CONSTANT PROBLEM (QUANTUM VACUUM ENERGY?)

