

Heavy neutrino-antineutrino oscillations

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Standard Model (SM) neutrinos

SM particle content

0	$1/2$			1
H	u left $u\bar{d}\bar{u}$	c left $u\bar{d}\bar{u}$	t left $u\bar{d}\bar{u}$	g
	d left $u\bar{d}\bar{u}$	s left $u\bar{d}\bar{u}$	b left $u\bar{d}\bar{u}$	γ
	e left $u\bar{d}\bar{u}$	μ left $u\bar{d}\bar{u}$	τ left $u\bar{d}\bar{u}$	Z
	ν_e left	ν_μ left	ν_τ left	W
	I	II	III	

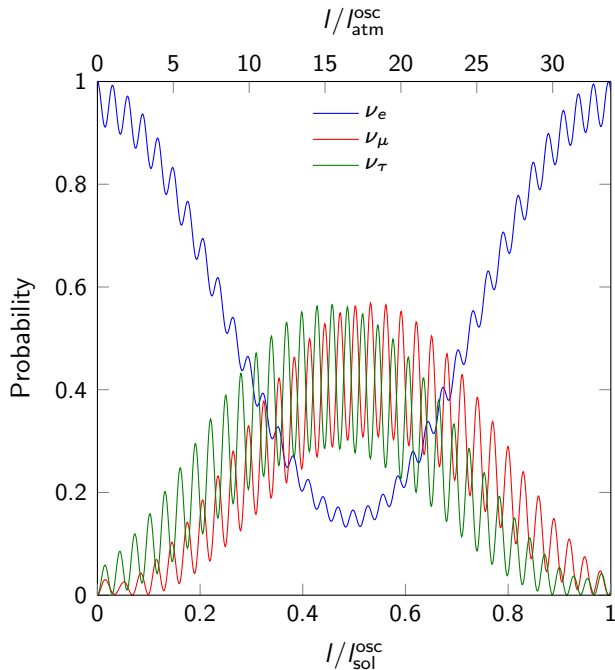
Neutrinos ν_α stand out

purely left-chiral and massless

Right-chiral or sterile Neutrinos

- neutral under SM symmetries
- allow mass term and explain oscillations

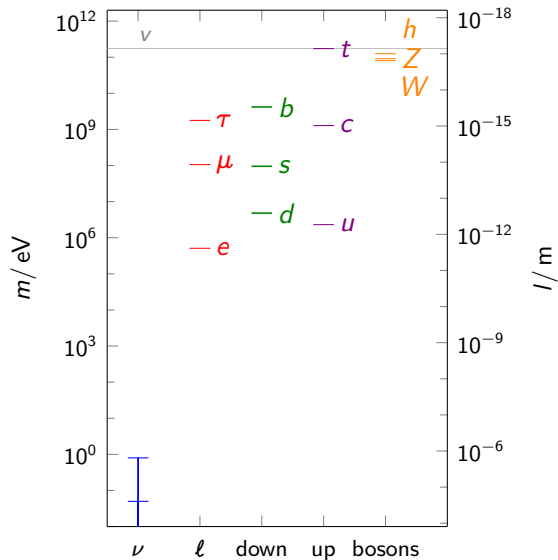
Observed neutrino flavour oscillations



Flavour oscillations are not explained within the SM

Flavour puzzle

Particle masses



Neutrinos are

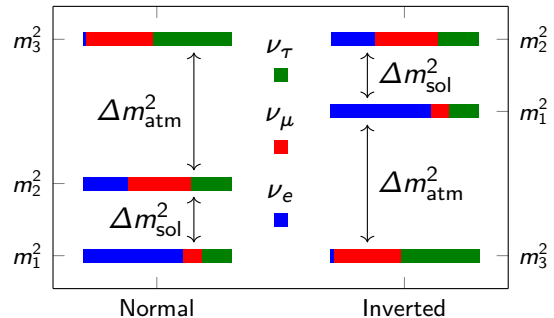
- not massless
- much lighter than other particles

Not all neutrino properties are well measured

- Lightest neutrino can still be massless
- Mass hierarchy is not known
- Angles and phases have large uncertainties

Neutrino mass hierarchy

$$\Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2$$



Model building work

- Explanation for flavour structure
- Mass generation mechanism

Seesaw mechanism

Right-handed Majorana neutrino N

$$\mathcal{L}_m = \begin{pmatrix} \bar{\nu} \\ N \end{pmatrix}^t \begin{pmatrix} 0 & \vec{m}_D \\ \vec{m}_D^T & m_M \end{pmatrix} \begin{pmatrix} \bar{\nu} \\ N \end{pmatrix}$$

Interaction governed by mixing parameter

$$\vec{\theta} = \frac{\vec{m}_D}{m_M} \quad \begin{array}{l} \text{Dirac mass} \\ \text{Majorana mass} \end{array}$$

Neutrino masses

$$m_\nu = \frac{\vec{m}_D \vec{m}_D^T}{m_M} = \frac{\vec{\theta} \vec{\theta}^T}{m_M}$$

Tiny neutrino masses are ensured for

- large m_M High scale seesaw
- small $\vec{m}_D$ Small coupling seesaw

Sterile neutrinos/Heavy neutral leptons

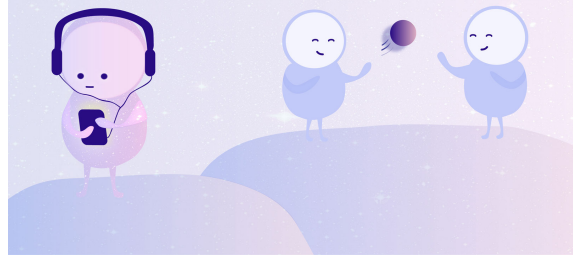
- Inaccessibly heavy or
- Tiny interactions

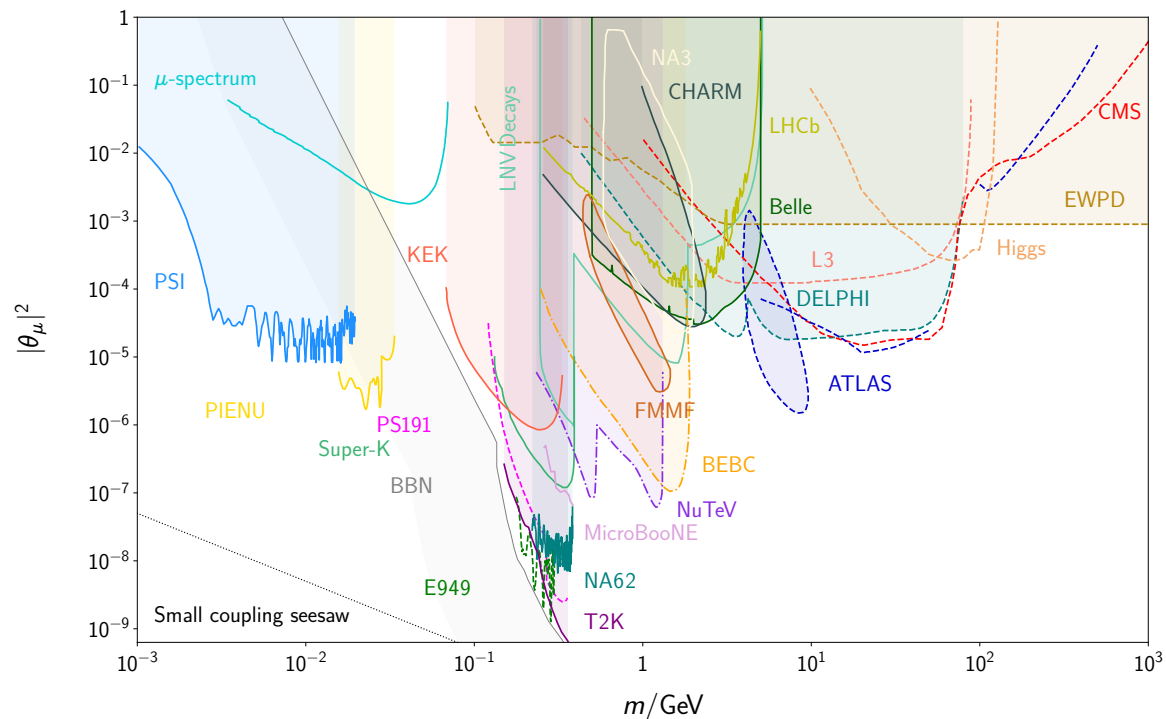
[SymmetryMagazine]



[SymmetryMagazine]

STERILE NEUTRINOS





Inaccessible: ■ Small coupling seesaw ■ High scale seesaw (at the GUT scale)

Symmetry-protected low-scale seesaw

Lepton number $L = n_\ell - n_{\bar{\ell}}$

Accidentally conserved in the SM

Generalisation: 'Lepton number'-like symmetry

e.g. $U(1)_L$	$\vec{\nu}$	N_1	N_2
with charges	L	+1	-1
		-1	+1

Symmetry breaking in the mass matrix

$$\mathcal{L}_m = \begin{pmatrix} \vec{\nu} \\ N_1 \\ N_2 \end{pmatrix}^t \begin{pmatrix} 0 & \vec{m}_D & \vec{\mu}_D \\ \vec{m}_D^T & \mu'_M & m_M \\ \vec{\mu}_D^T & m_M & \mu_M \end{pmatrix} \begin{pmatrix} \vec{\nu} \\ N_1 \\ N_2 \end{pmatrix}$$

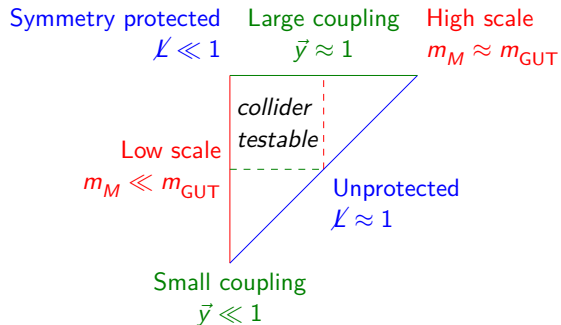
Symmetry L conserved

- Three massless neutrinos
 - Single Dirac heavy neutrino
- Corresponds to two degenerate Majoranas

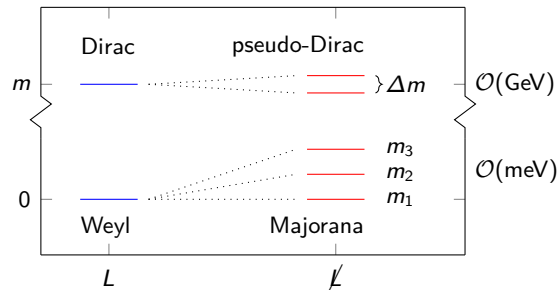
Small symmetry breaking $\mathcal{L}$

- Light neutrino masses $m_\nu \propto \mathcal{L}$
- Heavy neutrino mass splitting $\Delta m \propto \mathcal{L}$

Viable seesaw limits



Breaking induced neutrino mass splitting



Heavy neutrino-antineutrino oscillations ($N\bar{N}$ Os)

[2210.10738]

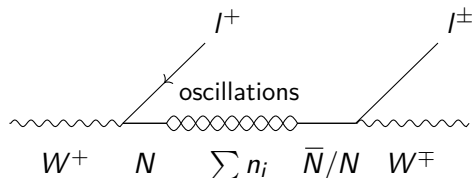
Oscillations between events that are

- lepton number conserving (LNC) $l^\pm l^\mp$
- lepton number violating (LNV) $l^\pm l^\pm$

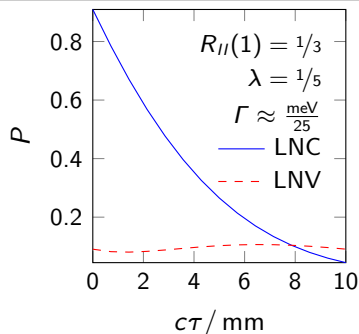
Oscillation frequency governed by Δm

$$P_{\text{osc}}^{\text{LNC/LNV}}(\tau) = \frac{1 \pm \cos(\Delta m \tau)}{2}$$

Oscillating mass eigenstates n_i

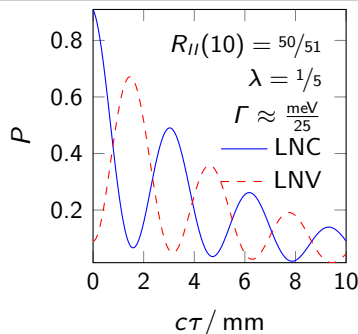


Slow oscillation



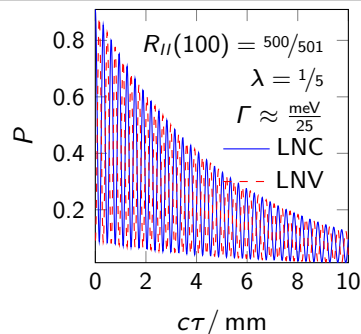
- Mostly LNC
- 'Dirac BM'-like

Intermediate oscillation

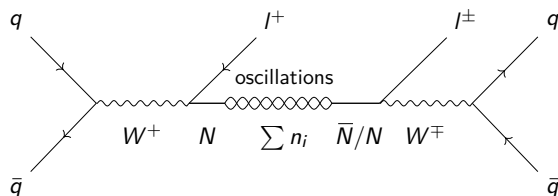


- Potentially resolvable
- $0 \leq R_{II} = \frac{P_{\text{LNC}}}{P_{\text{LNV}}} \leq 1$

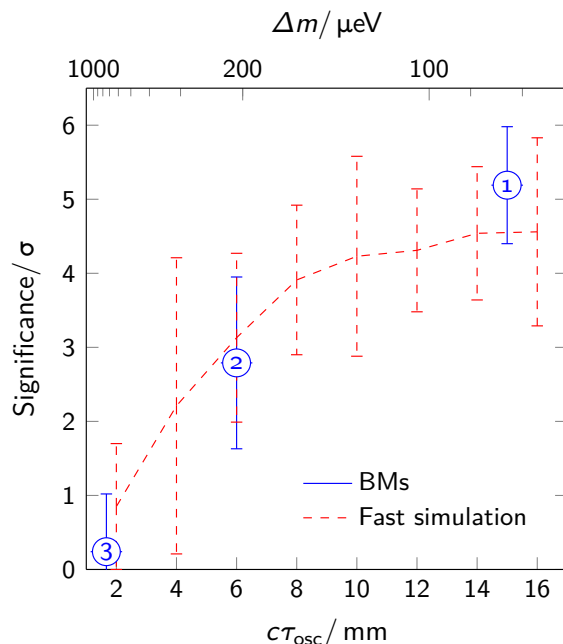
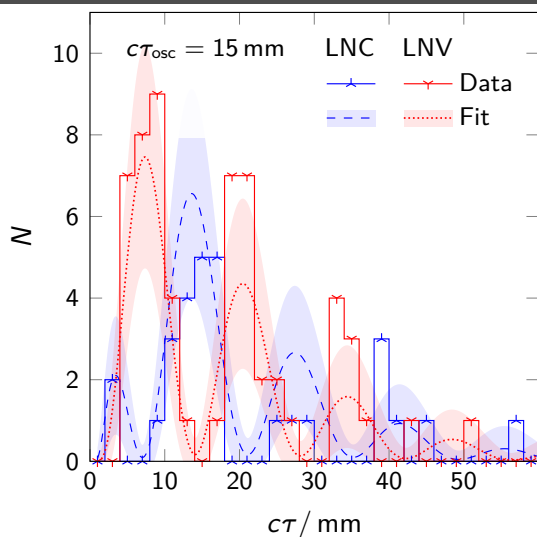
Fast oscillation



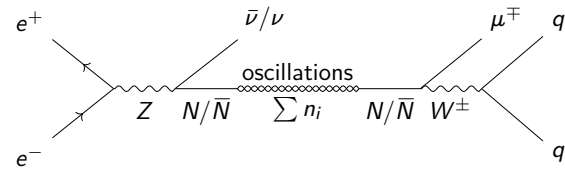
- Unresolvable
- LNV as frequent as LNC
- 'Majorana BM'-like



Lepton number violation (LNV) is measured by comparing the charges of the two leptons



Single charged lepton



Measurement

- LNV cannot be measured using two charges
- One can still measure angular distributions

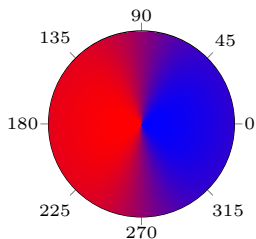
Angular dependent probability

$$P_{l^\mp}(\cos\theta, \tau) := \frac{1}{\sigma} \frac{d\sigma(\cos\theta)}{d\cos\theta} P_{\text{osc}}^{\text{LNC/LNV}}(\tau)$$

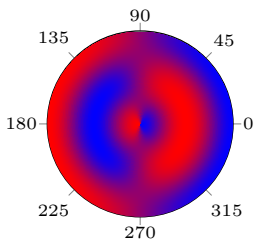
Probability of measuring charged leptons

- linked to forward backward asymmetry of neutrino production (see 'Dirac BM'-like)
- l^- from non-oscillating N or from oscillating $\bar{N}$ (similar for l^+)

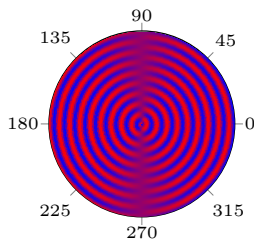
'Dirac BM'-like



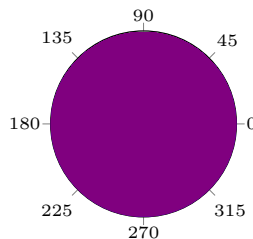
Slow oscillation



Fast oscillation



'Majorana BM'-like



Potential projects

- Detection potential at muon collider
- Decoherence at future colliders
- Loop contributions to neutrino masses
- ...

Contact

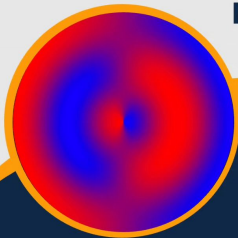
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BEST MEFT THESIS

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**Heavy Neutrino-Antineutrino
oscillations at the FCC-ee**

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S. Antusch, J. Hajer, B. M. S. Oliveira, and J. Roszkopp. 'pSPSS: Phenomenological symmetry protected seesaw scenario'. FeynRules model file. URL: feynrules.irmp.ucl.ac.be/wiki/pSPSS
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S. Antusch, J. Hajer, and J. Roszkopp. 'Beyond lepton number violation at the HL-LHC: resolving heavy neutrino-antineutrino oscillations'.
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S. Antusch, J. Hajer, and B. M. S. Oliveira. 'Heavy neutrino-antineutrino oscillations at the FCC-ee'.
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Oscillating particles in quantum field theory (QFT)

[2307.06208]

Inadequate frameworks for oscillating relativistic particles

- Quantum mechanics
- Plane-wave QFT

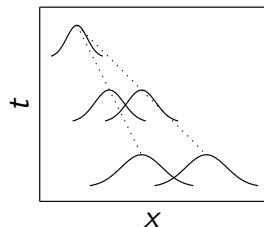
QFT with external wave packets

- Gaussian wave packets with width σ
- External widths are experiment depended parameters
- Internal widths are calculated

Transition amplitude in QFT with external wave packets Φ

$$\mathcal{A}(x) = \left\langle \Phi(x'') \left| \mathcal{T} \exp \left[-i \int [d^4 x'] \mathcal{H}(x') \right] - \mathbb{1} \right| \Phi(x') \right\rangle$$

Decoherence



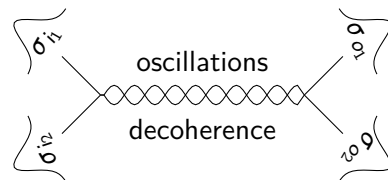
Result can be expressed with effective damping parameter λ

Damped oscillations

$$P_{\text{osc}}^{\text{LNC/LNV}}(\tau) = \frac{1 \pm \cos(\Delta m \tau) e^{-\lambda}}{2}$$

LNV can be drastically enhanced

Width of external wave packets σ



Impact on $N\bar{N}O$ s

