

Exploring Parton Showers in the presence of an extended QCD medium

André Cordeiro

In collaboration with:

Carlota Andrés, Liliana Apolinário, Nestor Armesto,
Fabio Dominguez, Guilherme Milhano

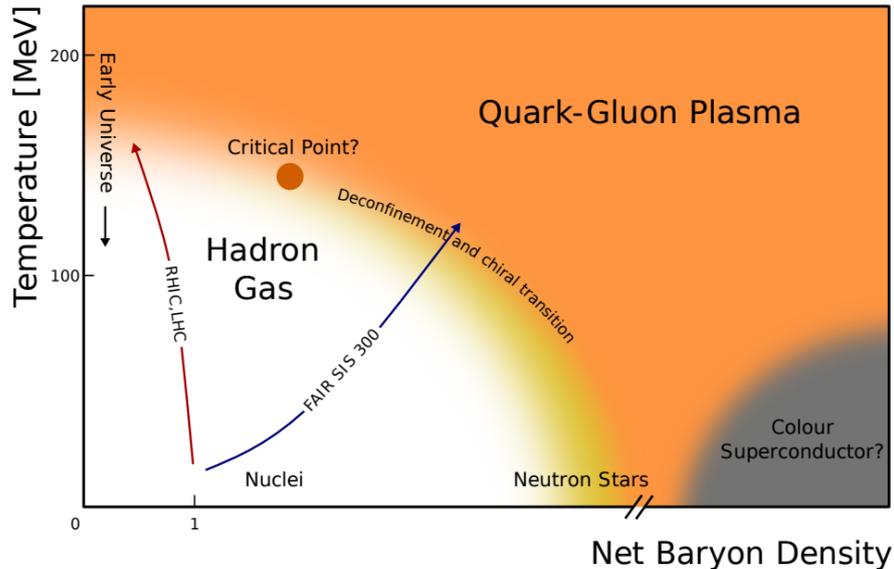


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Fourth Joint Workshop IGFAE / LIP

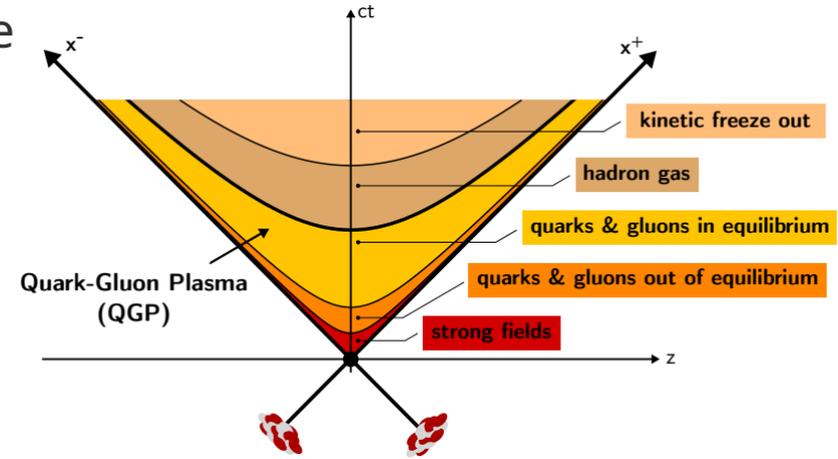
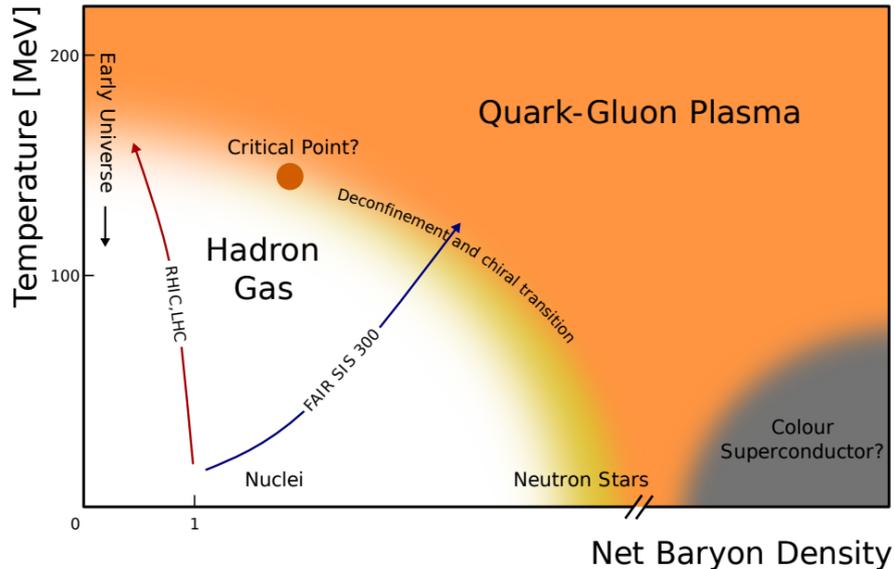
Why we study heavy ion collisions

- **Quantum matter in extreme conditions:** explore the QCD phase diagram
- **Collectivity:** emergent behaviour from fundamental d.o.f.
- **Cosmology:** the QGP filled the early universe



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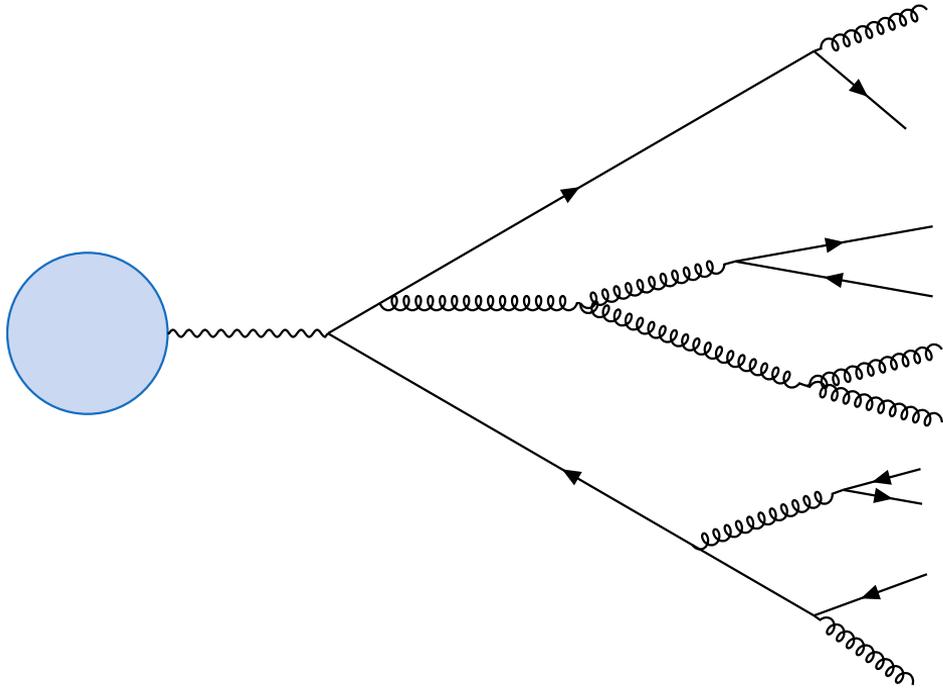


Main challenge: the QGP is extremely short lived ($\sim 10^{-24}$ s)

One approach: Probe it with (high-momentum) particles produced in the collision!

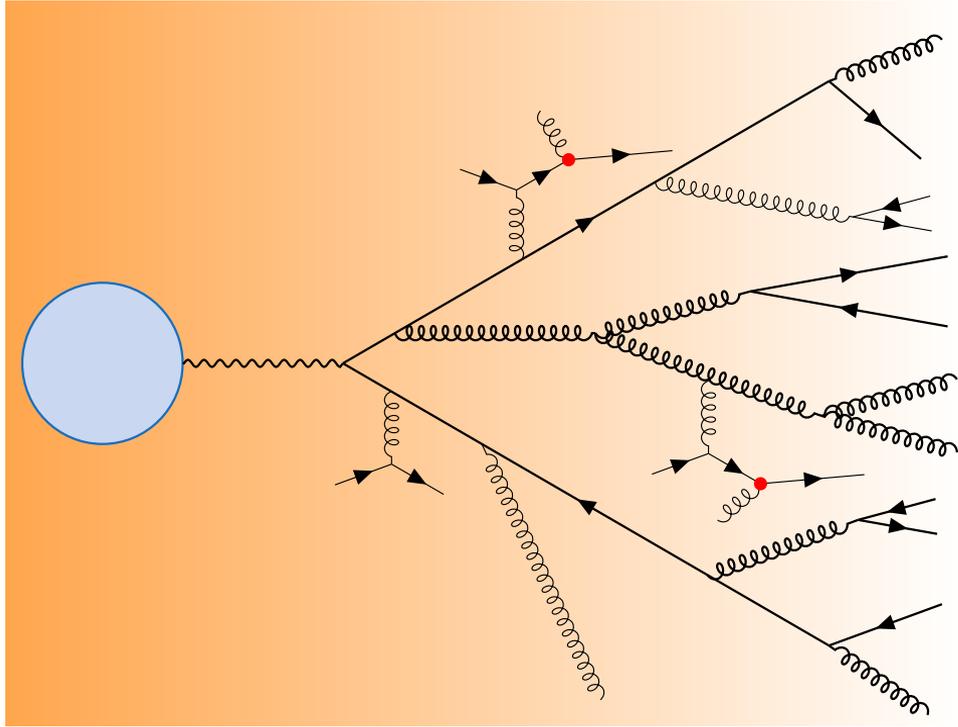
Probing the QGP with parton cascades

Hard partons radiate until the hadronisation scale →
Parton cascades provide a multi-scale object



Probing the QGP with parton cascades

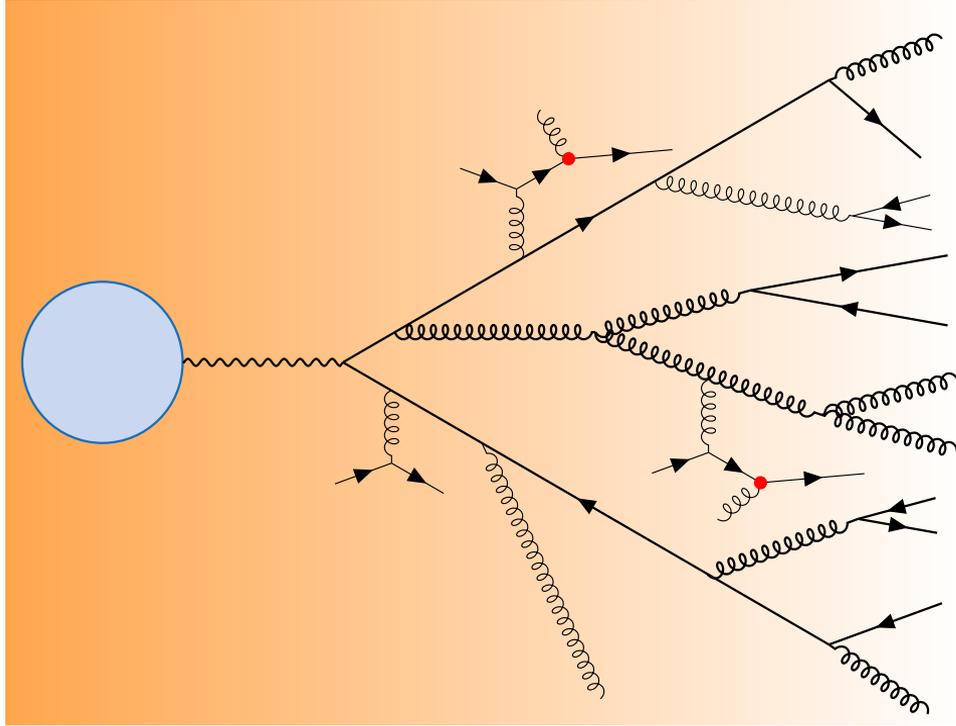
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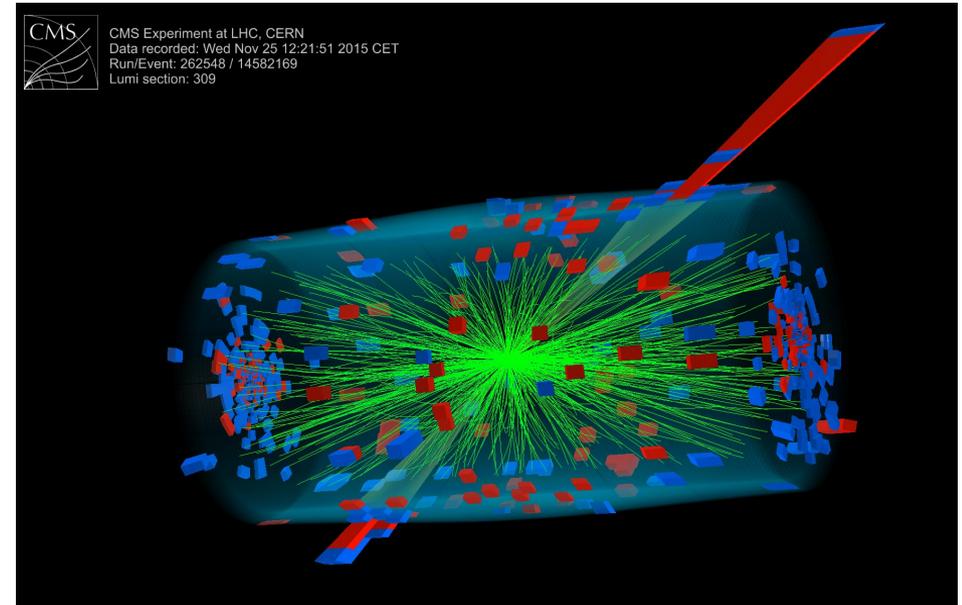
In-medium cascades require an interface with the evolving
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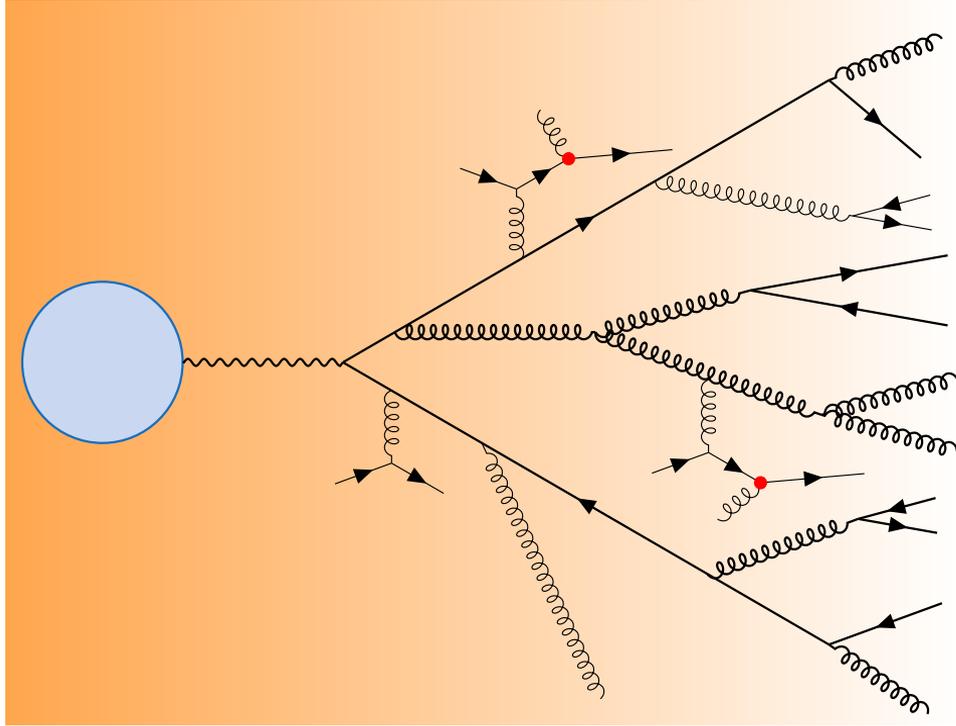
Experimental objects: jets
Different jets suffer different energy loss



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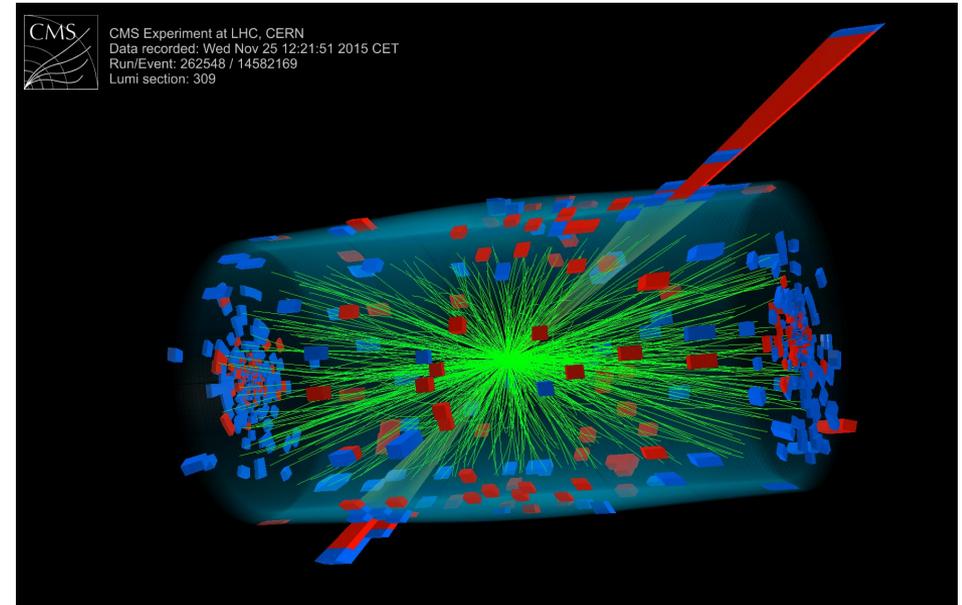
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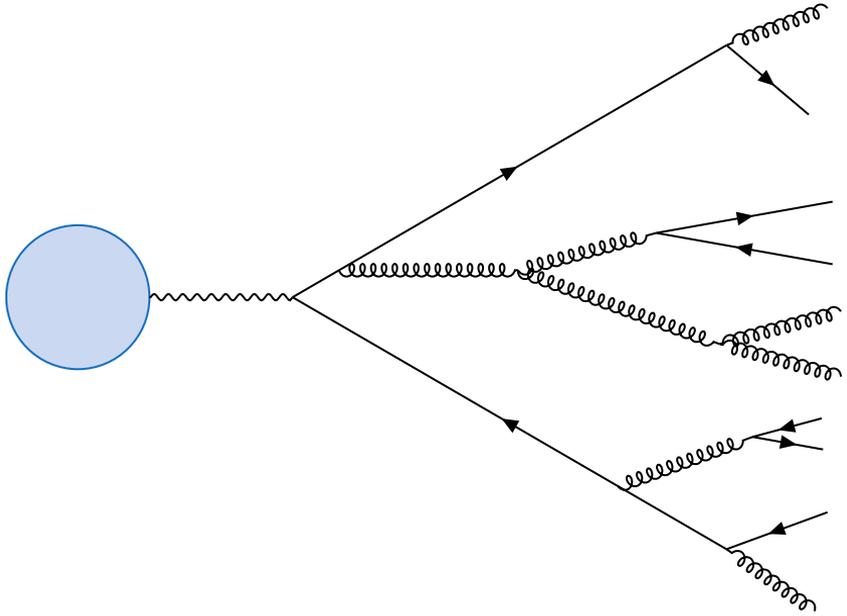


Are the medium modifications sensitive to the vacuum evolution?

First, a look at vacuum showers

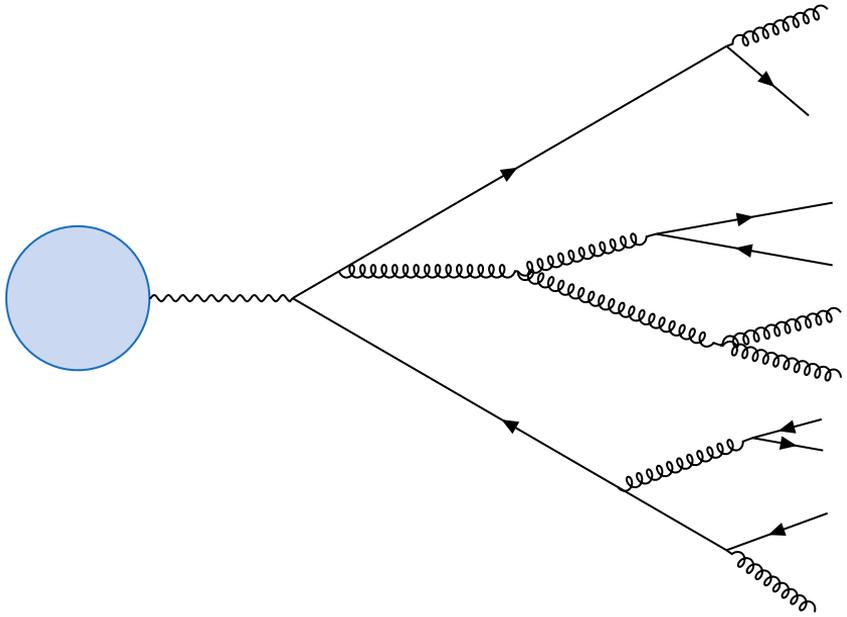
Parton Cascades vs Jets

Parton Cascade: Sequence of QCD splittings, defined in perturbation theory → Can be sampled numerically

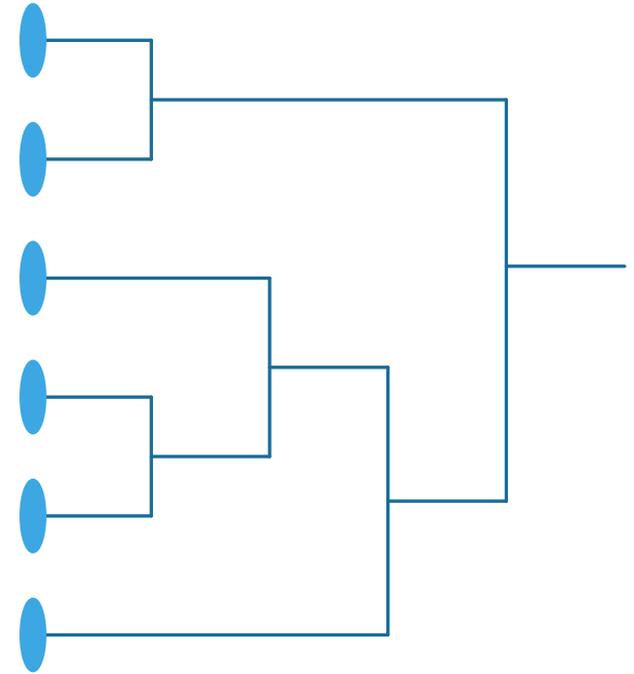


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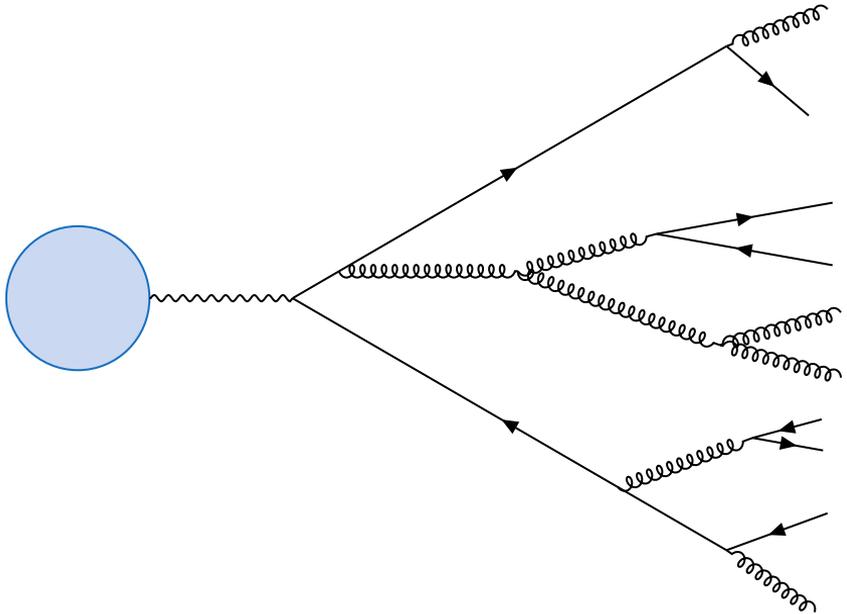


Jet: Sequence of hadron clusterings, according to some (arbitrary) definition → Proxy for initial parton

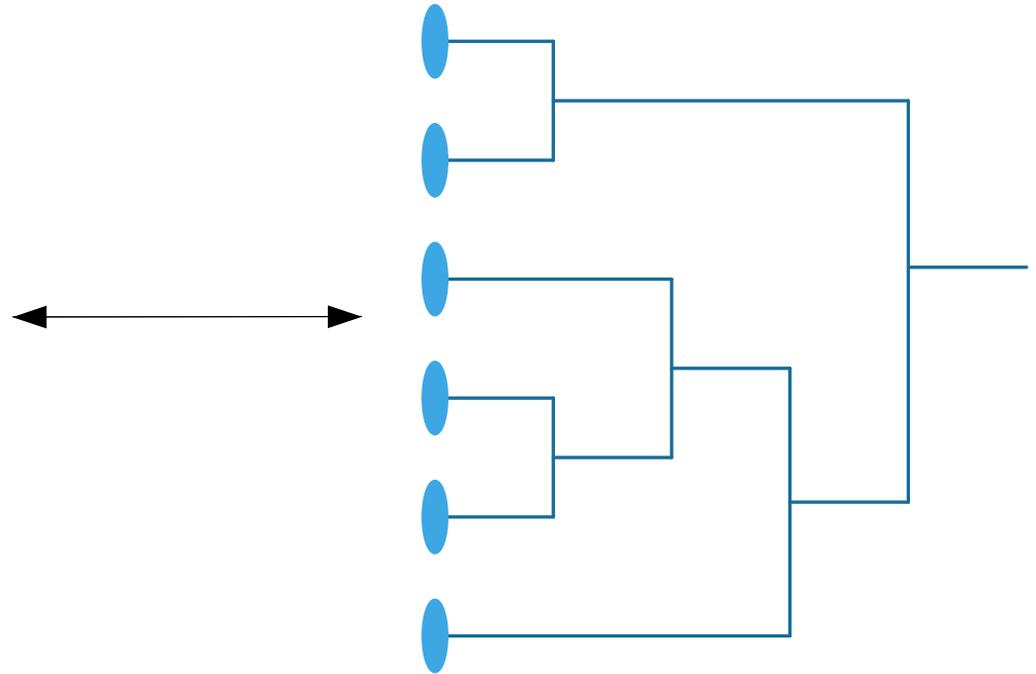


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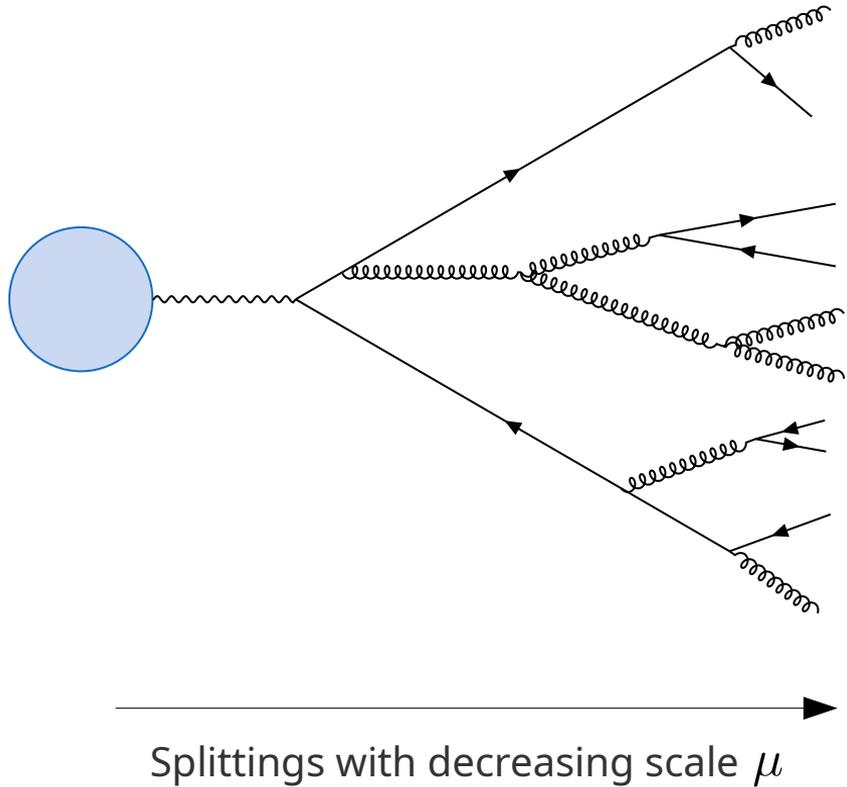


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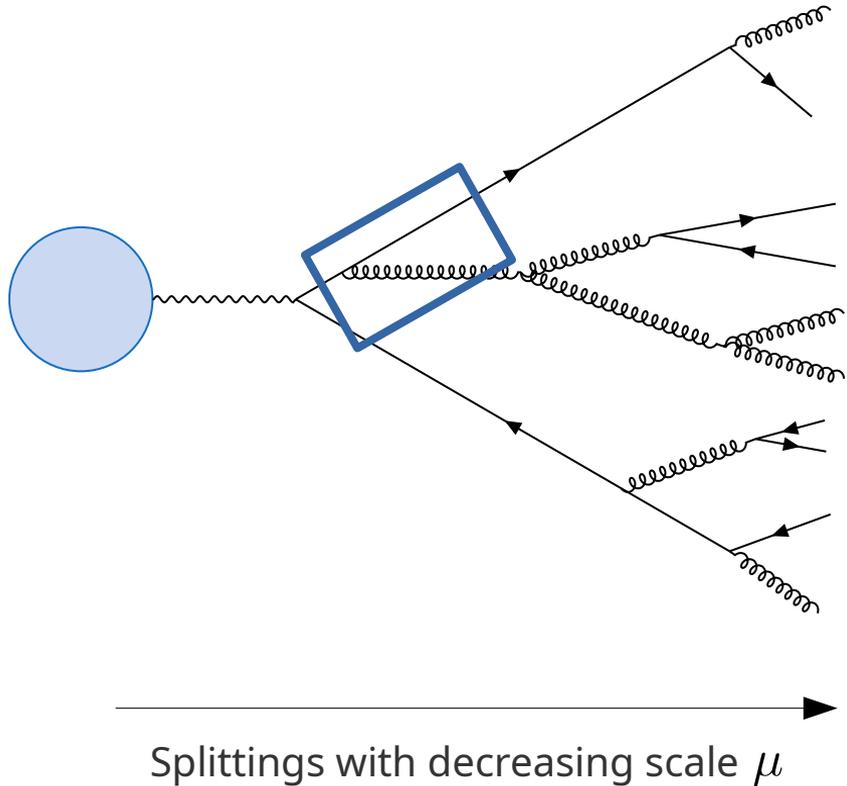
For appropriate definitions jet structure coincides with the cascade ordering

How to build a parton shower



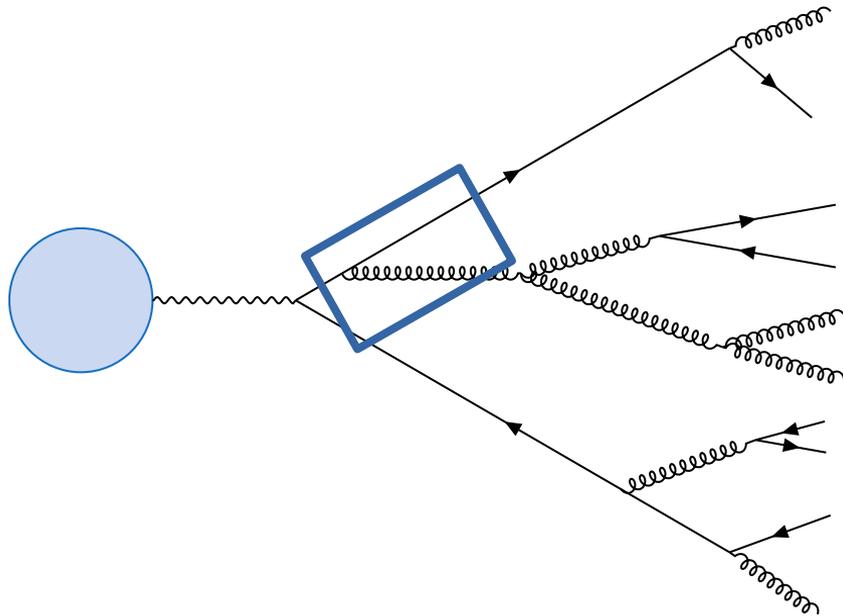
How to build a parton shower

Building blocks: QCD splittings



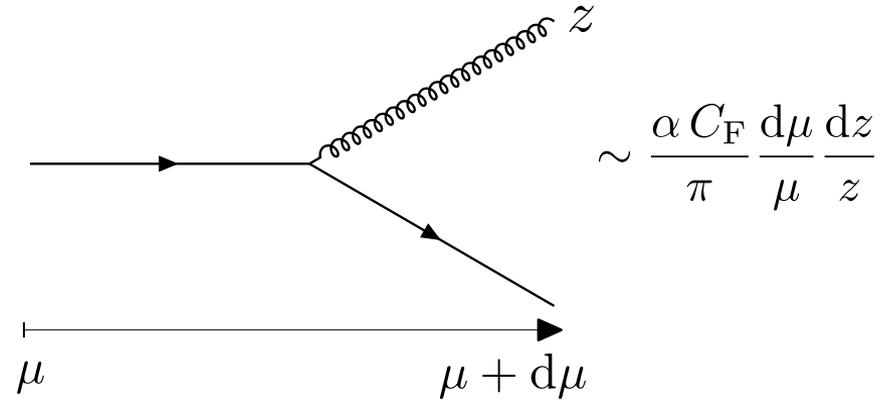
How to build a parton shower

Building blocks: QCD splittings



→ Splittings with decreasing scale μ

Splitting probability given by pQCD:



Building differently ordered cascades

No-emission probability:

$$\Delta(s_{\text{prev}}, s) = \exp \left\{ -\frac{\alpha C_R}{\pi} \int_s^{s_{\text{prev}}} \frac{d\mu}{\mu} \int_{z_{\text{cut}}(\mu)}^1 \frac{dz}{z} \right\}$$

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Interpretations for the scale:

$$s \rightarrow t_{\text{form}}^{-1} = \frac{|\ell|^2}{2p^+ z(1-z)}$$

(Formation time)

$$s \rightarrow \tilde{m}^2 = 2p^+ t_f^{-1}$$

(Virtuality)

$$s \rightarrow \tilde{\theta}^2 = \frac{|\ell|^2}{(p^+)^2 [z(1-z)]^2}$$

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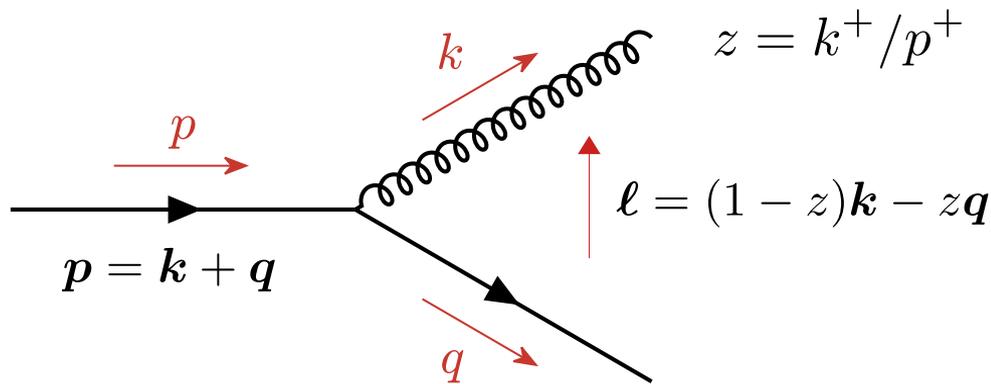
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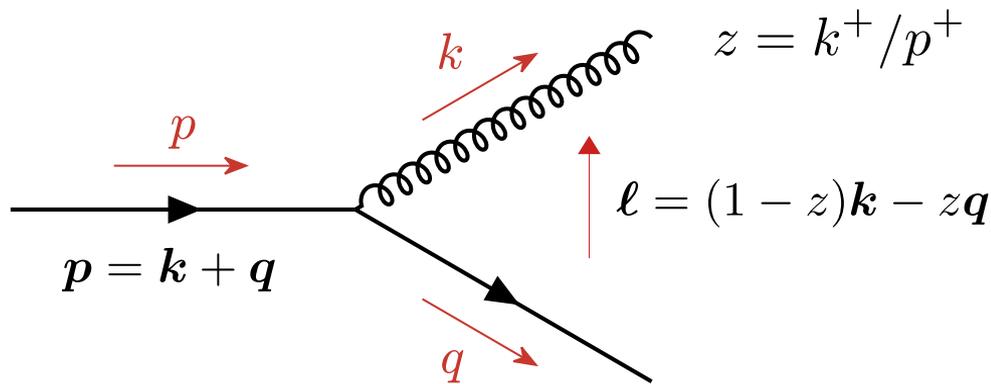
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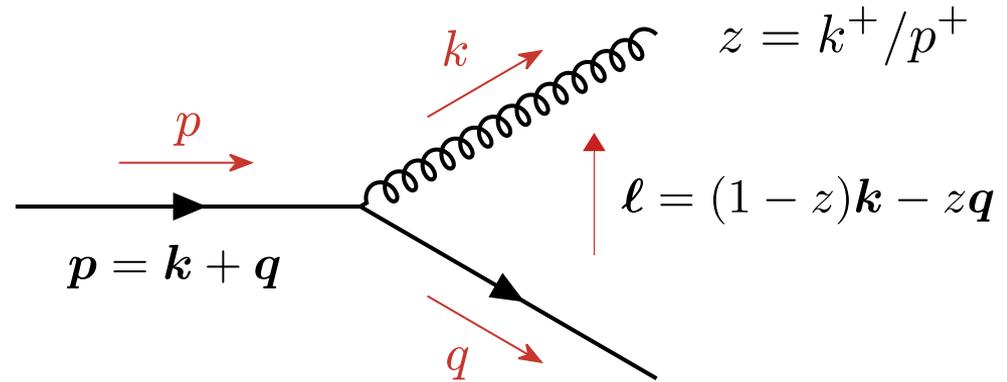
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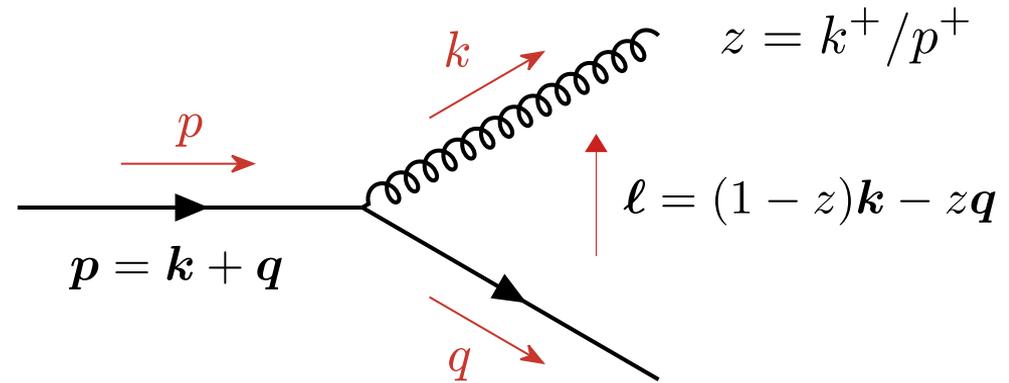
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To generate a splitting:



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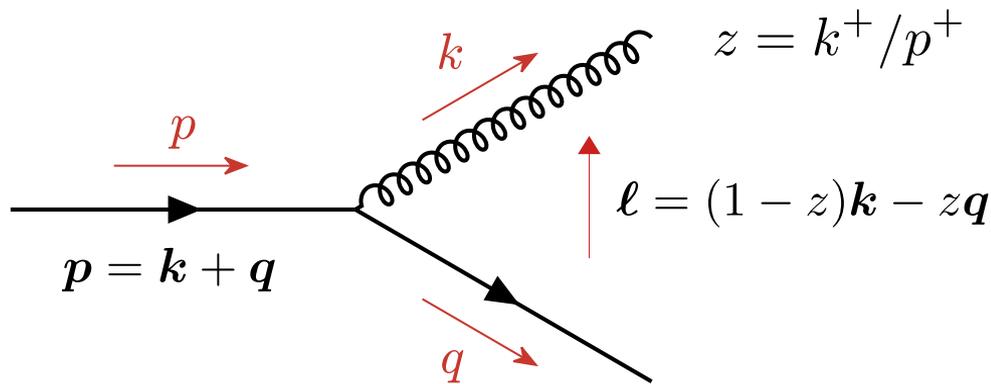
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Ensure that $|\ell|^2 > k_{\text{had}}^2$

Parton Shower Details

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How to set up a toy Monte Carlo:

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How to set up a toy Monte Carlo:

- Splittings happen above some hadronization scale $|\ell|^2 > k_{\text{had}}^2$

E.g. Formation time:

$$z_{\text{cut}} = \frac{k_{\text{had}}^2}{2p^+ t_{\text{form}}^{-1}}$$

- Can be rewritten as a condition $z > z_{\text{cut}}$
- Initialization condition: $t_{\text{form}}^{-1} < p^+$

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Opening angle:

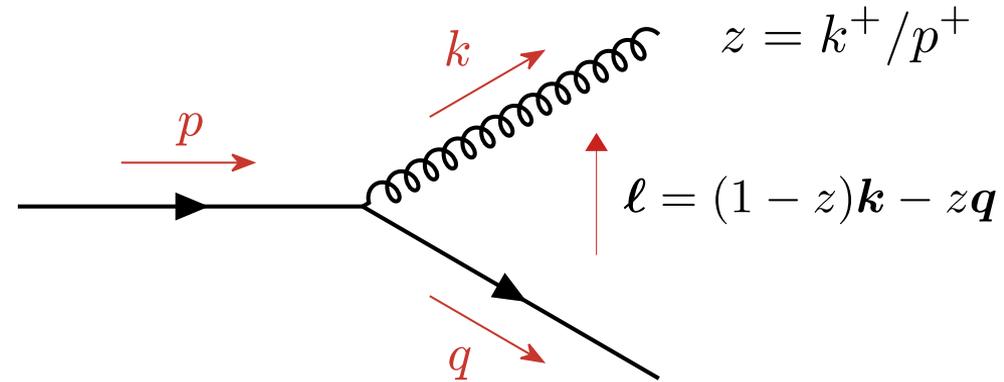
- To avoid large angles: $\tilde{\theta} < 2\sqrt{2}$

$$\tilde{\theta}^2 = \frac{|\ell|^2}{(p^+)^2 [z(1-z)]^2}$$

Determining Splitting Kinematics

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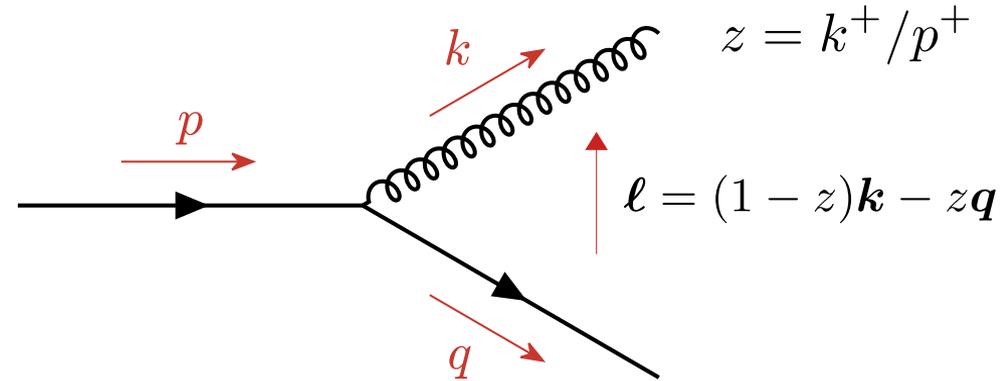


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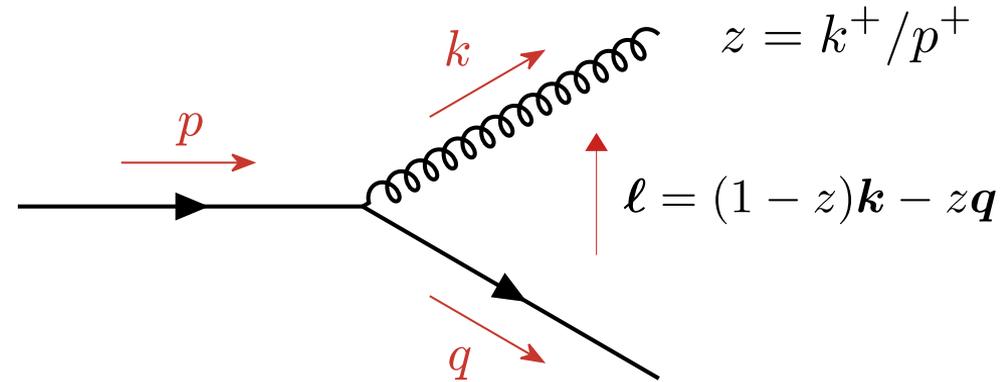


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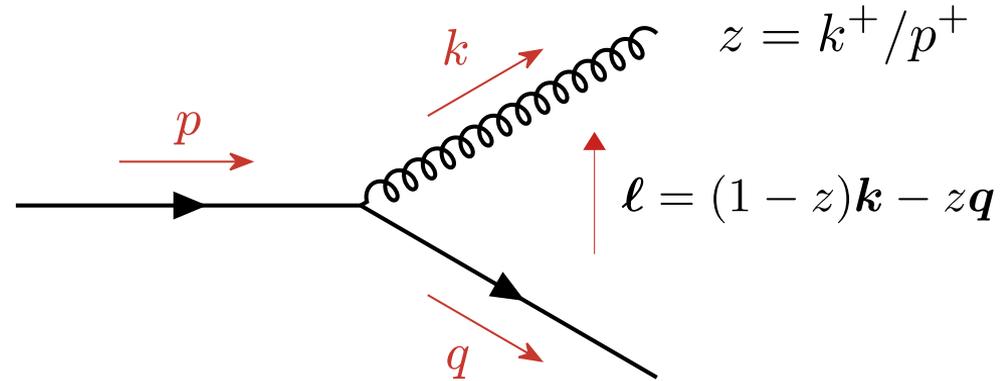
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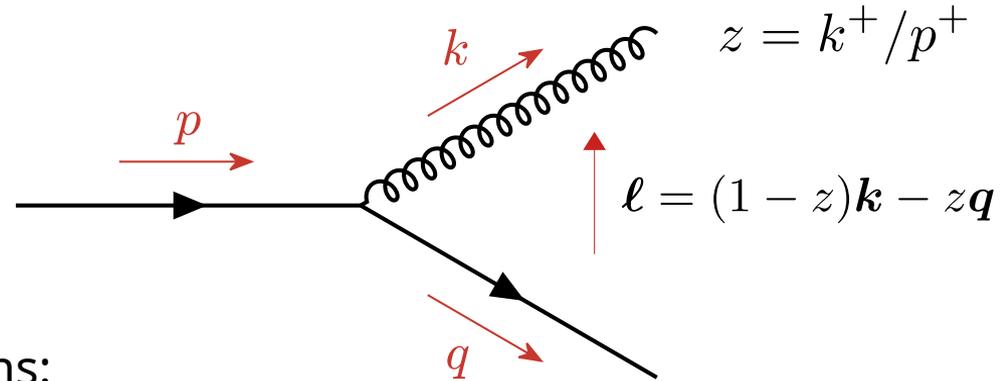
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4. Obtain transverse momenta from definitions:

$$\ell = (1-z)\mathbf{k} - z\mathbf{q}$$

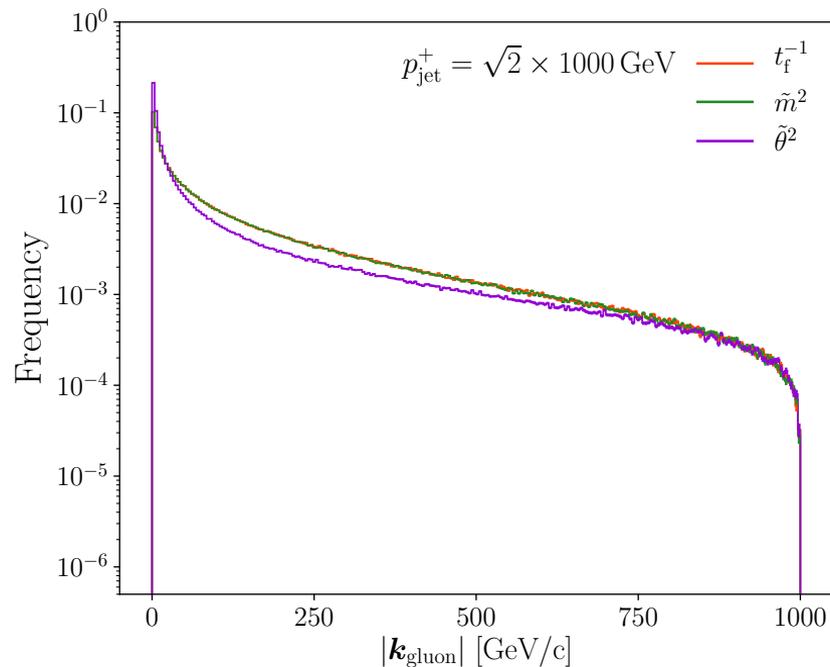
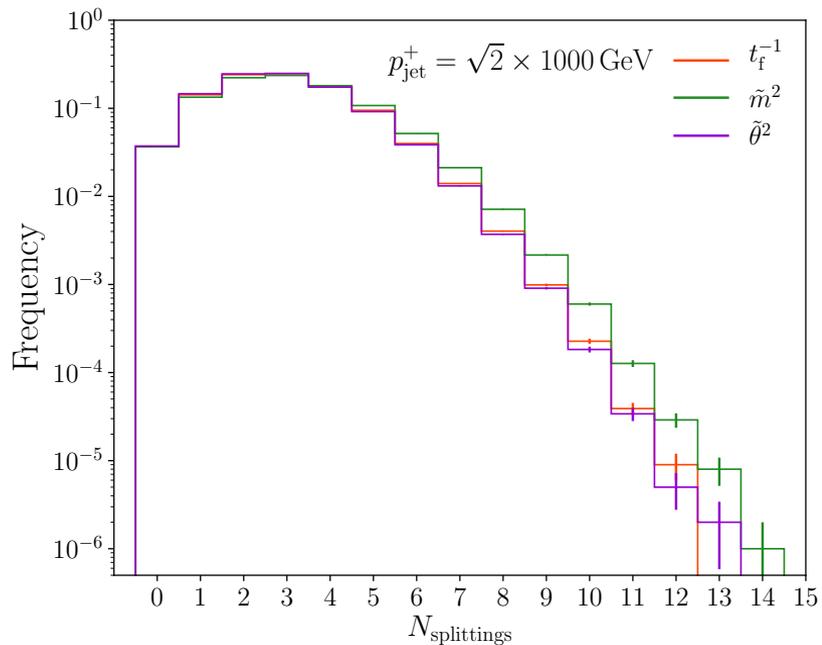
$$\mathbf{k} = \ell + z\mathbf{p}$$

$$\mathbf{p} = \mathbf{k} + \mathbf{q}$$

$$\mathbf{q} = -\ell + (1-z)\mathbf{p}$$

Differences in ordering choices

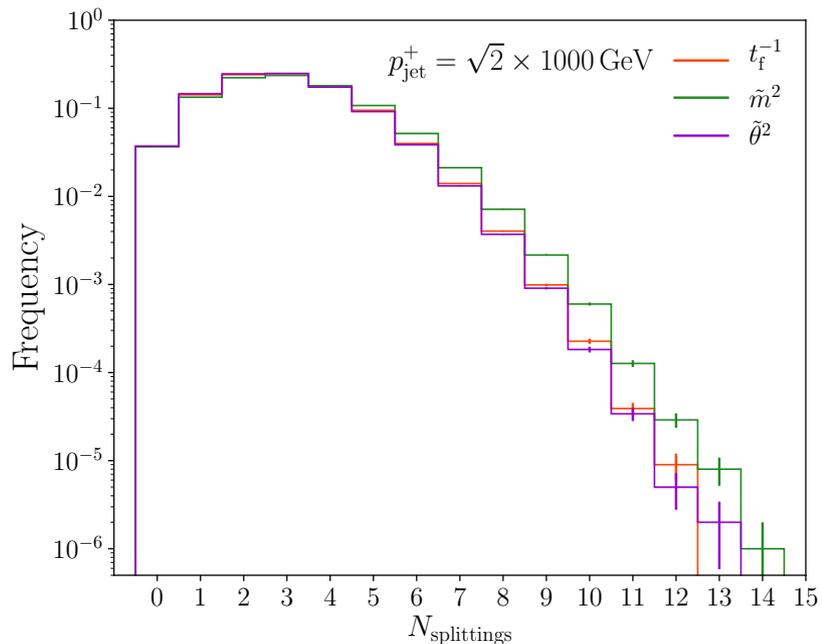
Splittings along the quark branch



Different orderings \rightarrow Different phase-space for allowed splittings

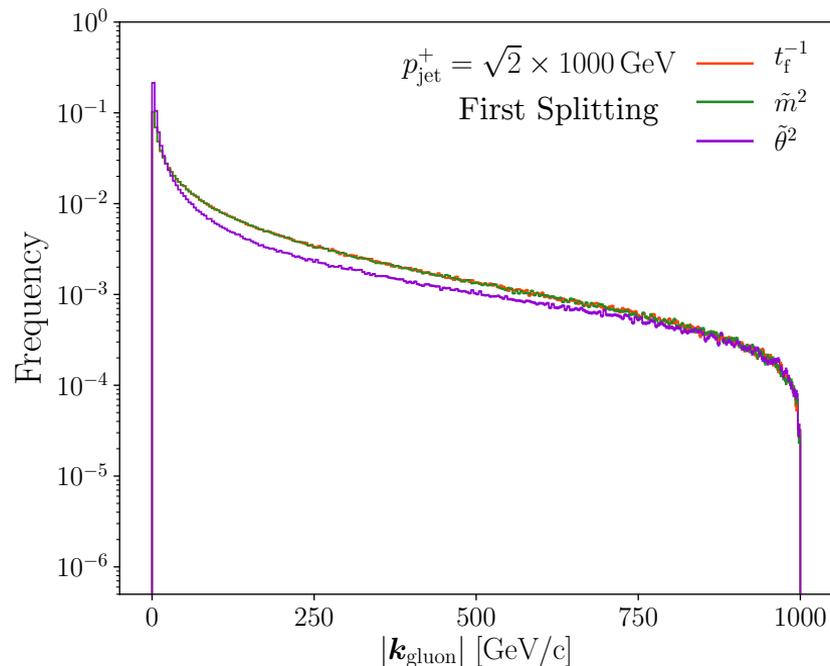
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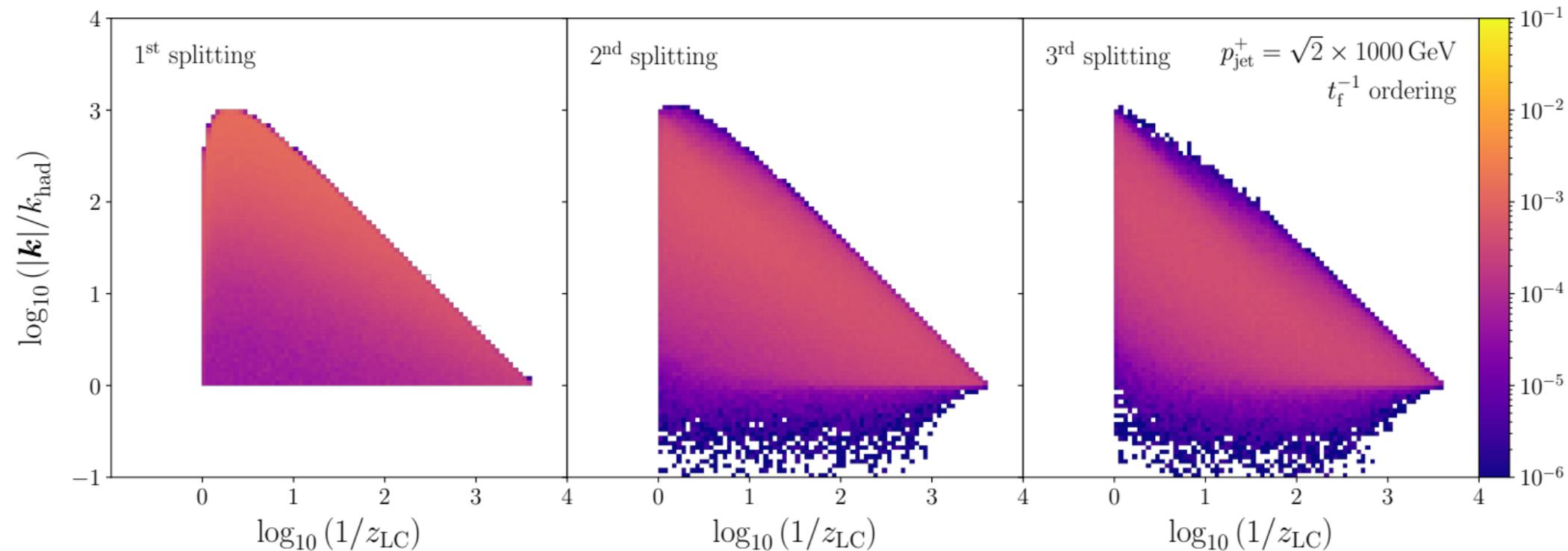
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Transverse momentum of 1st splitting



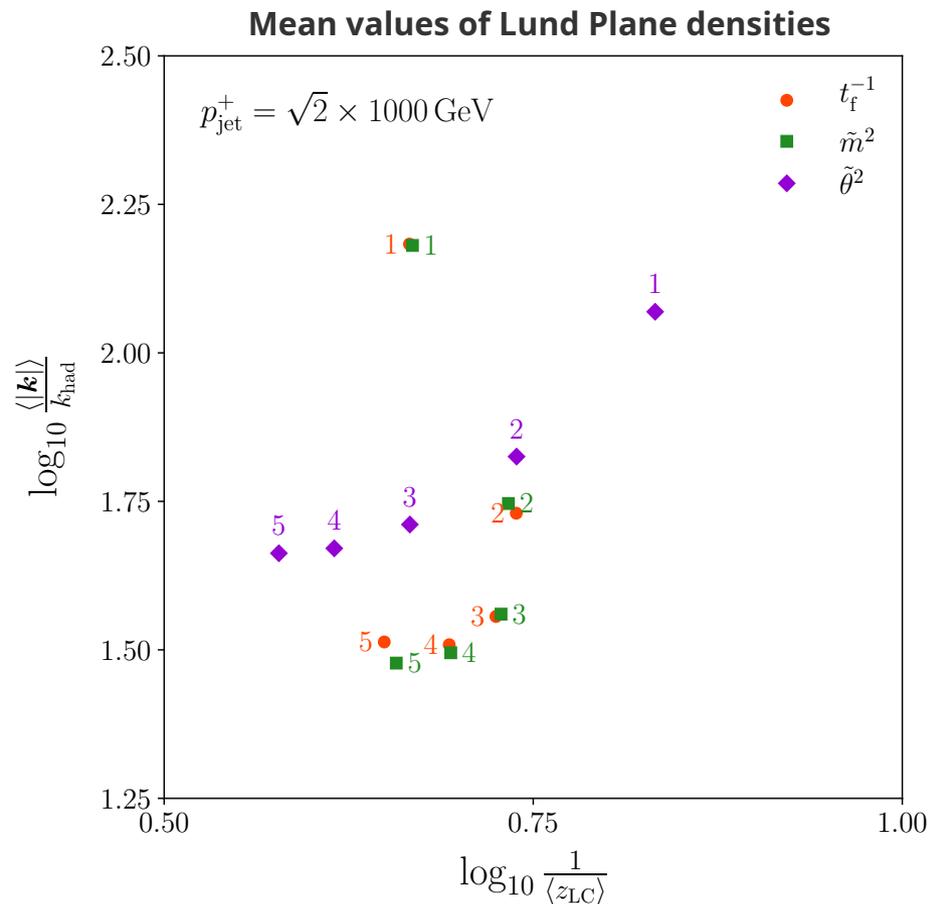
Transverse momentum distribution follows $\frac{d|\mathbf{k}|^2}{|\mathbf{k}|^2}$

Lund Plane Densities

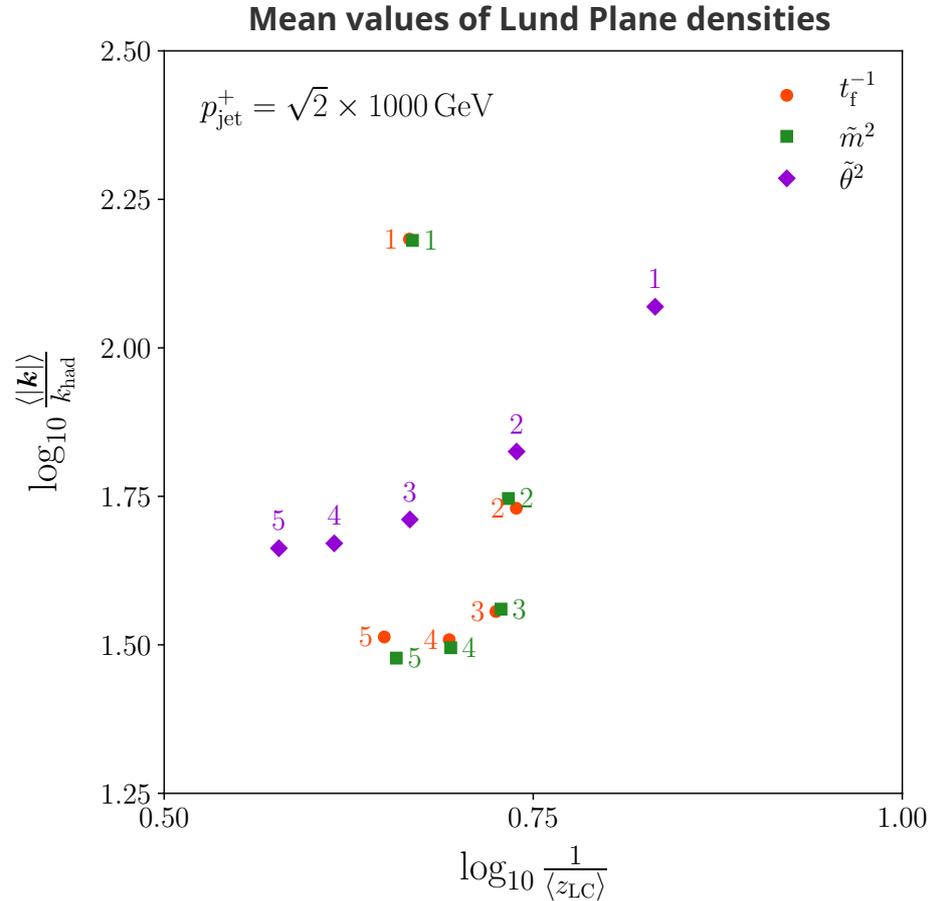


Shower evolution: Transverse momentum decreases, momentum fraction increases.

Lund Plane Trajectories

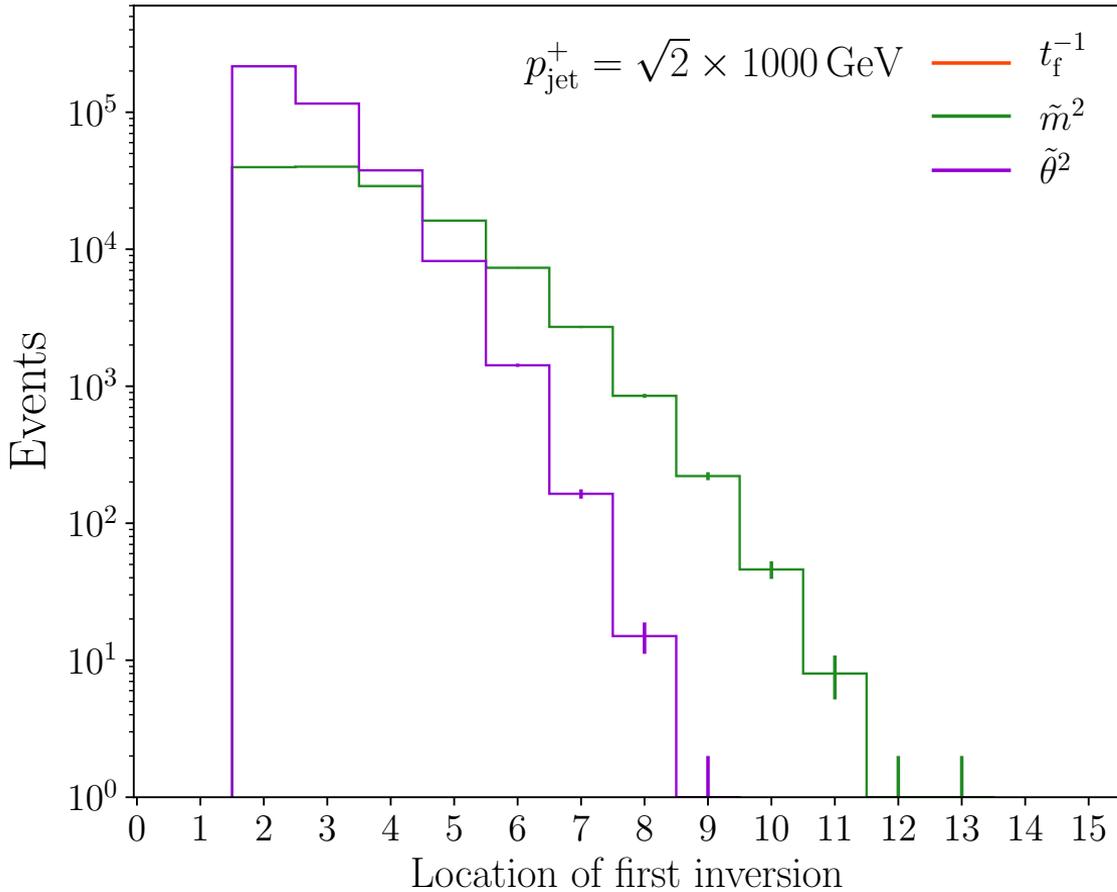


Lund Plane Trajectories



Differences between phase-space trajectories

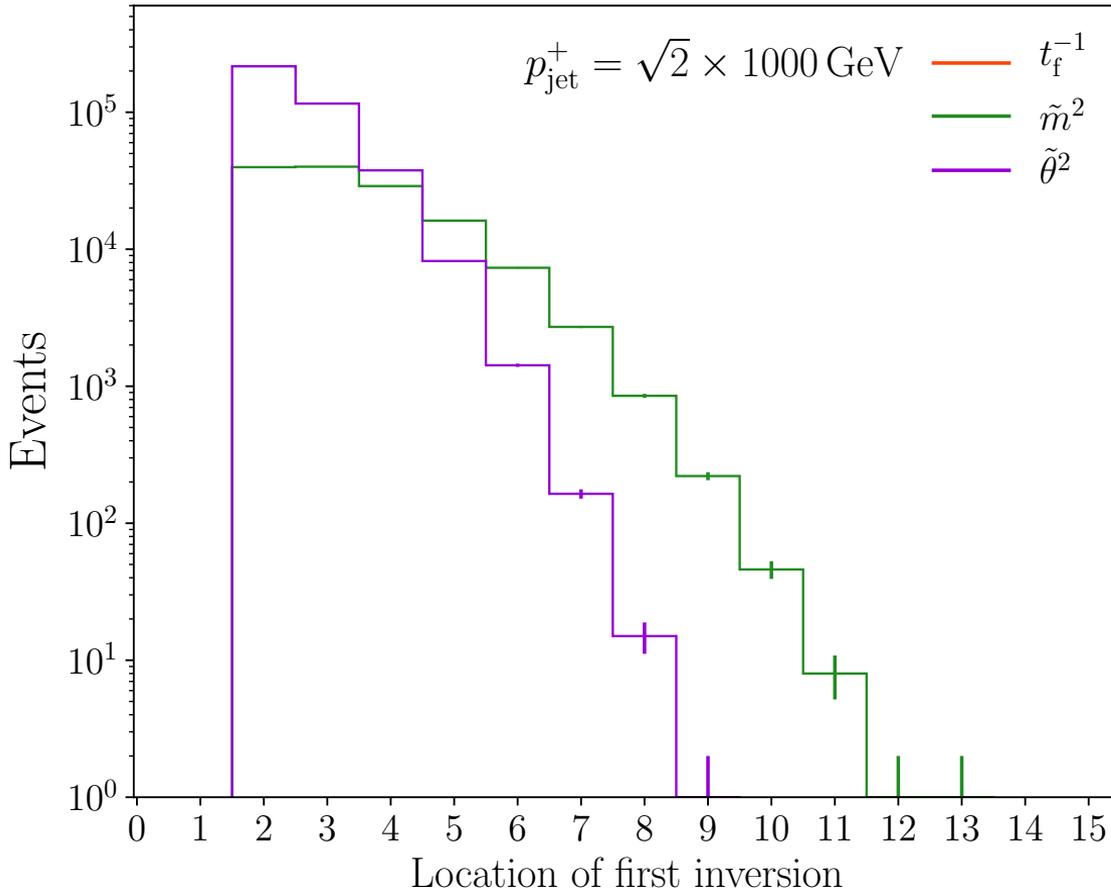
Formation Time Inversions



Formation Time Inversions:

Splittings with a formation time shorter than their immediate predecessor.

Formation Time Inversions



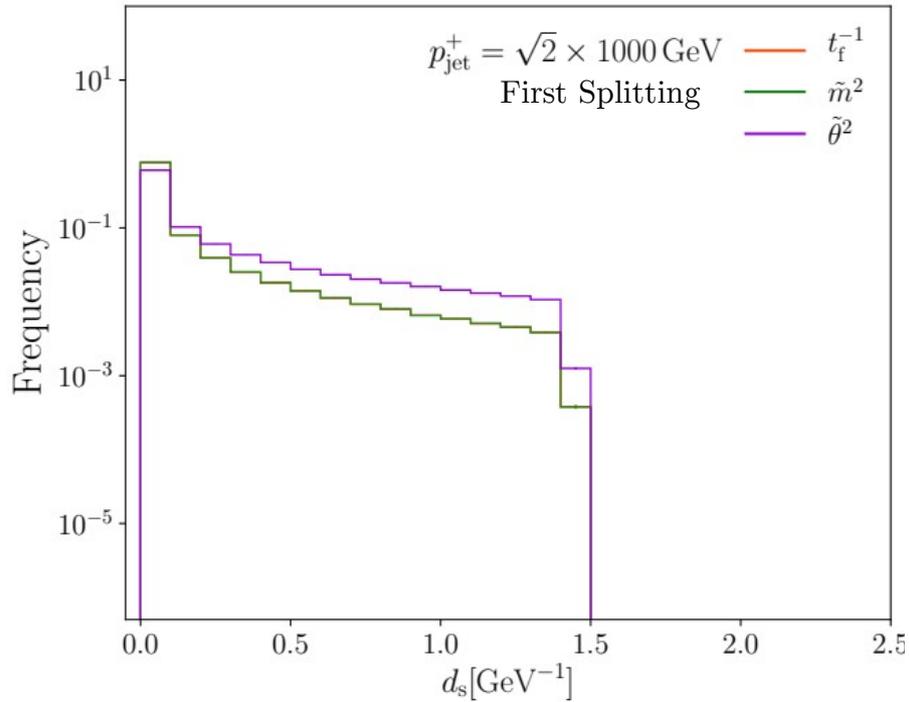
Formation Time Inversions:

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Does this discrepancy translate into differences in quenching magnitude?

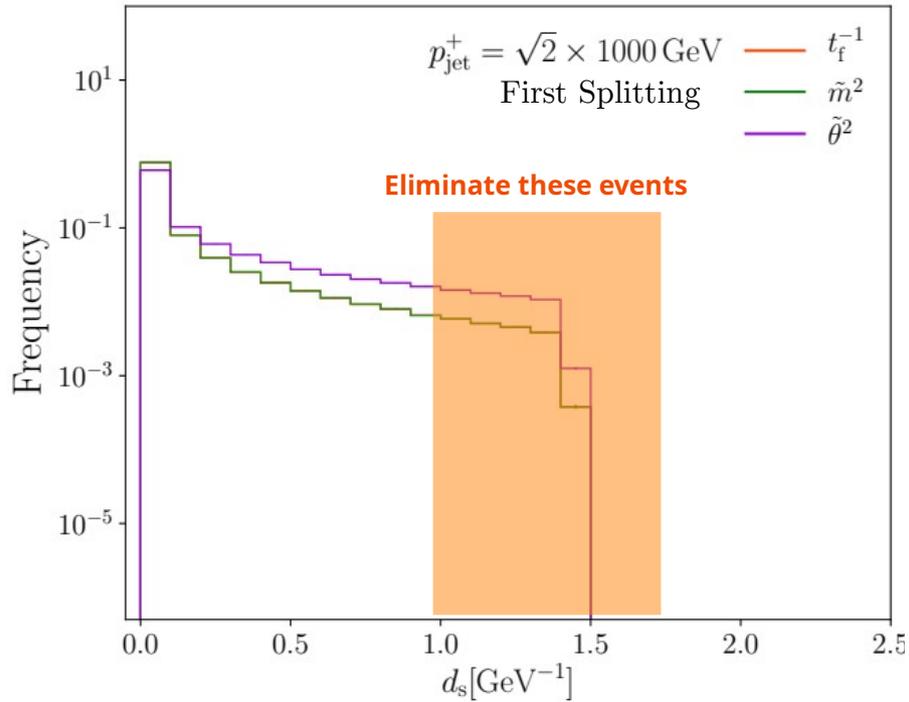
Let's look at jet quenching!

Simple (Pseudo-)Quenching Models



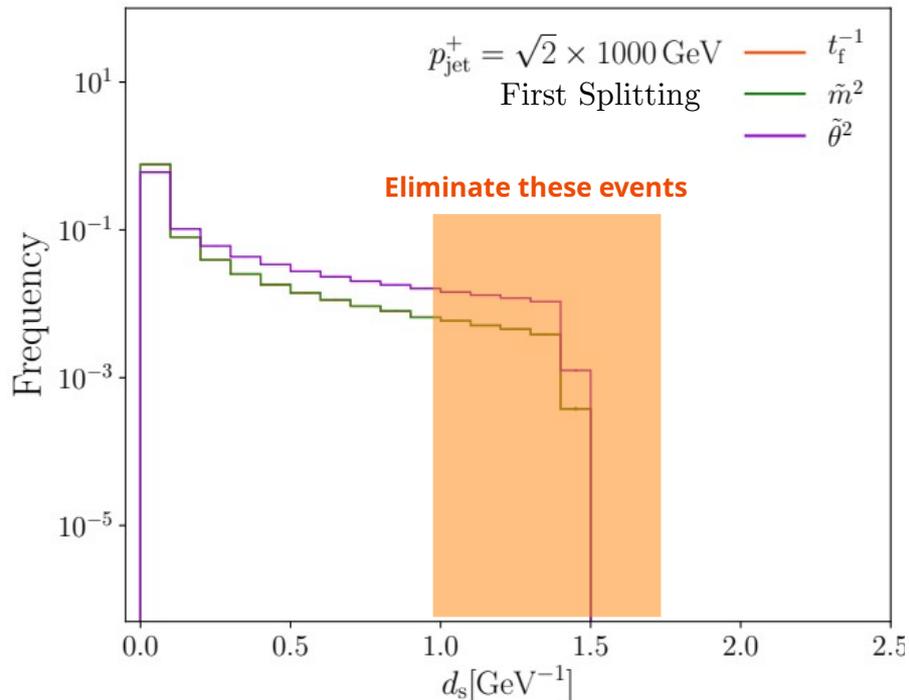
- Consider distance between daughters: $d_s = \sqrt{\frac{t_{\text{form}}}{k^+}}$
- **A simplistic model:**
 - Eliminate event if $d_s > d_{\text{coh}} = \frac{1}{\sqrt{\hat{q}L}}$ (Decoherence)

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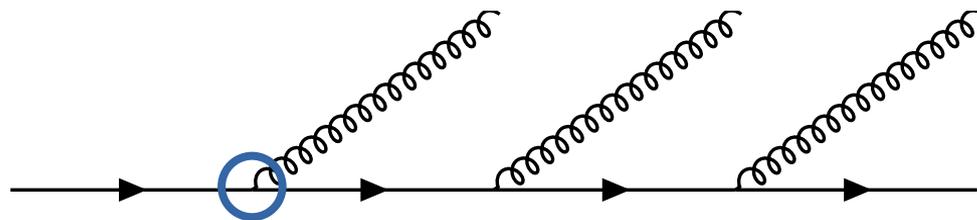
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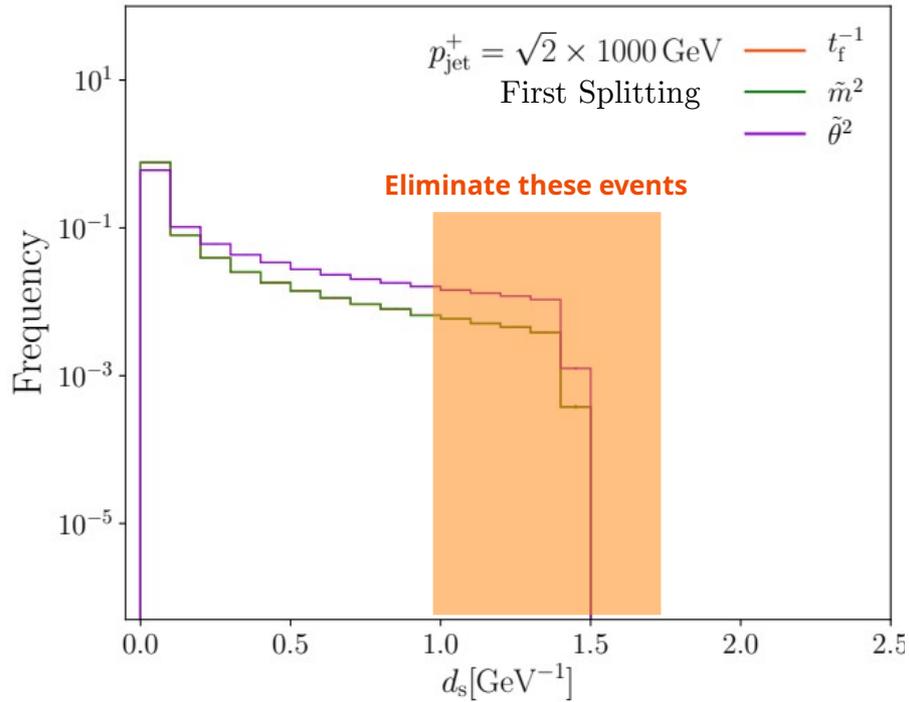
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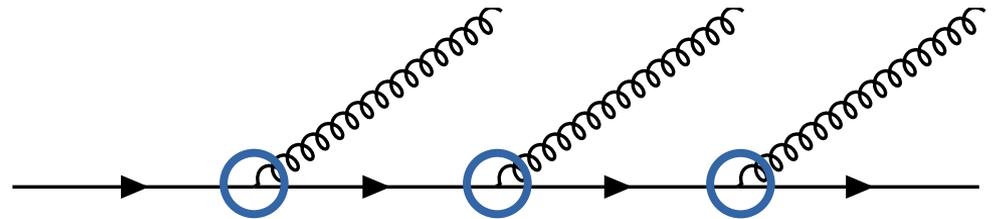


- Option 1: Apply only to first splitting

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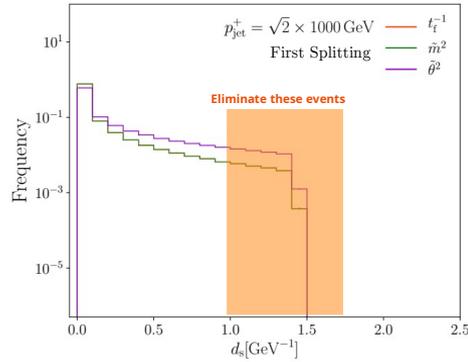


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- Option 1: Apply only to first splitting
- Option 2: Apply to whole quark branch

Simple (Pseudo-)Quenching Models



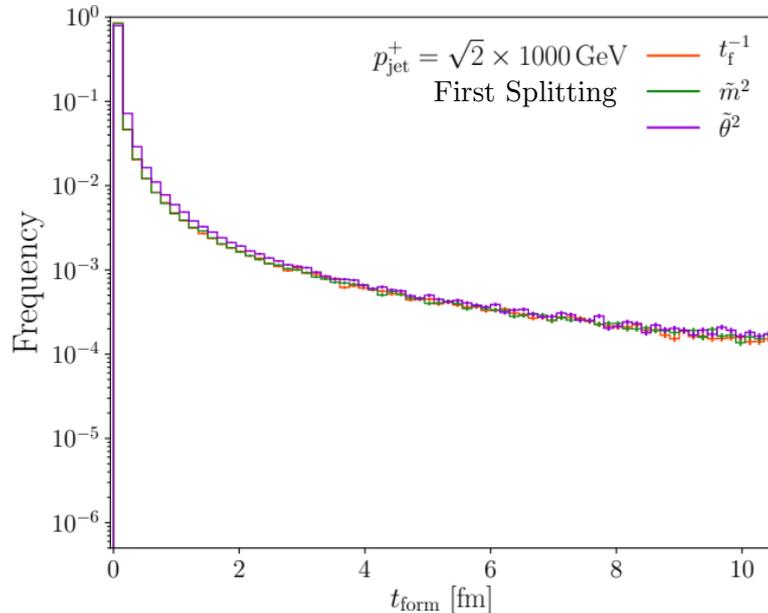
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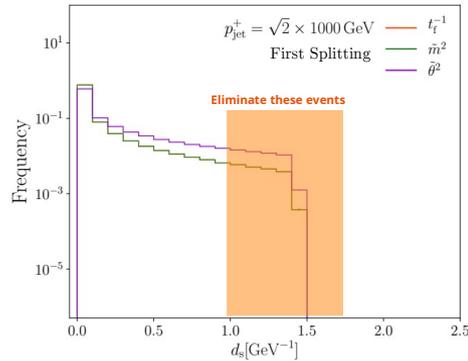
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- **A slightly less simplistic model:**

- Eliminate event if $d_s > d_{\text{coh}} = \frac{1}{\sqrt{\hat{q}(L - t_{\text{form}})}}$ (Finite formation time)
- And if $t_{\text{form}} < L$



Simple (Pseudo-)Quenching Models



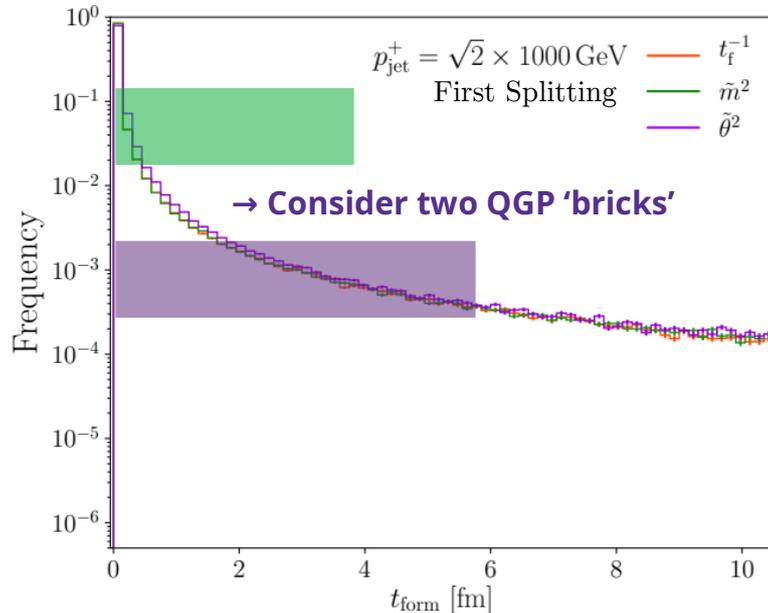
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- **A slightly less simplistic model:**

- Eliminate event if $d_s > d_{\text{coh}} = \frac{1}{\sqrt{\hat{q}(L - t_{\text{form}})}}$ (Finite formation time)
- And if $t_{\text{form}} < L$



Influence of the first splitting on quenching

- Apply this pseudo-quenching model to all orderings
 - Compute the percentage of 'quenched' events

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L [fm]	4	6	
\hat{q} [GeV ² /fm]	2	5	5
t_f^{-1}	1.1 %	3.1 %	5.9 %
\tilde{m}^2	1.1 %	3.1 %	5.9 %
$\tilde{\theta}^2$	4.0 %	9.1 %	15.6 %

Apply quenching condition to the
first splitting

Influence of the first splitting on quenching

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L [fm]	4	6
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Apply quenching condition to the
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L [fm]	4	6
\hat{q} [GeV ² /fm]	2	5
t_f^{-1}	4.6 %	22.0 %
\tilde{m}^2	4.9 %	23.5 %
$\tilde{\theta}^2$	4.6 %	22.0 %

Apply quenching condition to the
entire quark branch

Influence of the first splitting on quenching

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L [fm]	4	6
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Apply quenching condition to the
entire quark branch

Quantifies importance of ordering scale

Summary

- We have created a toy Parton Shower Monte Carlo:
 - To explore differences between ordering variables
 - Aiming at a framework for time-ordered, medium-induced emissions
- Choice of vacuum ordering → Sensitivity to quenching at differential timescales
 - Model does not account for medium dilution, differential energy loss
 - Only implements vacuum emissions [**Medium-induced emissions needed**]
- Is jet quenching sensitive to the ordering of vacuum-like emissions?
 - Suggested by this simple model. [**Work in Progress**]

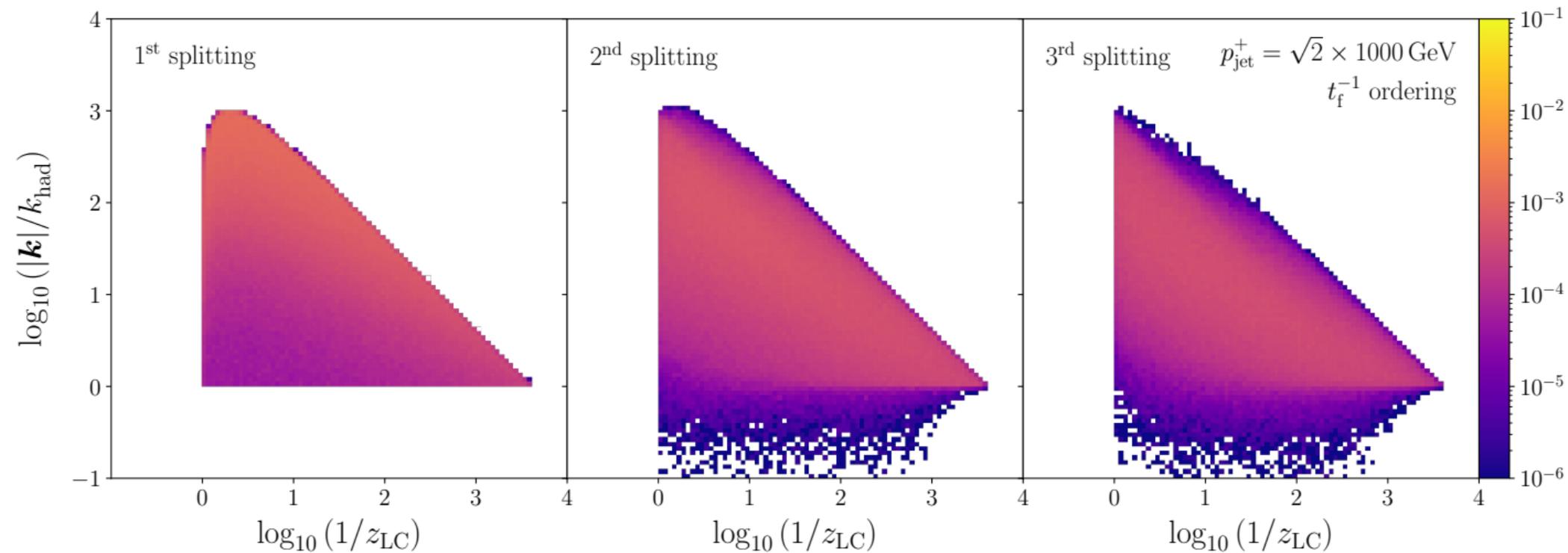
Thank you!

Acknowledgements

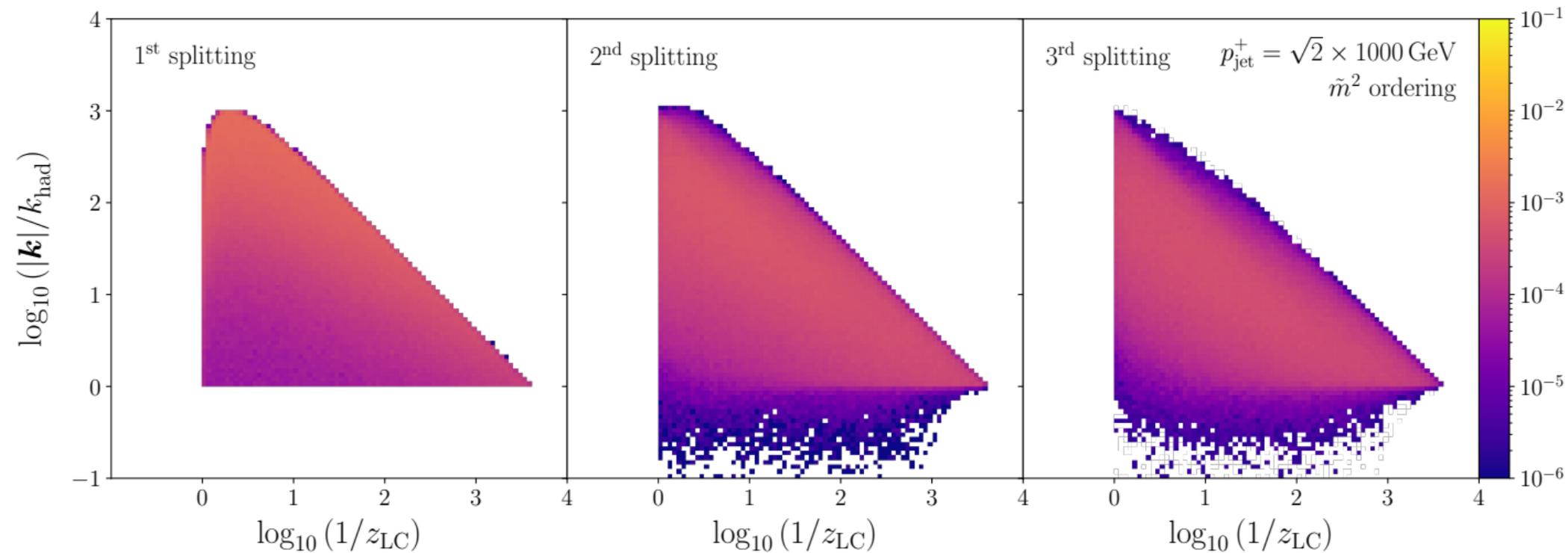


Backup Slides

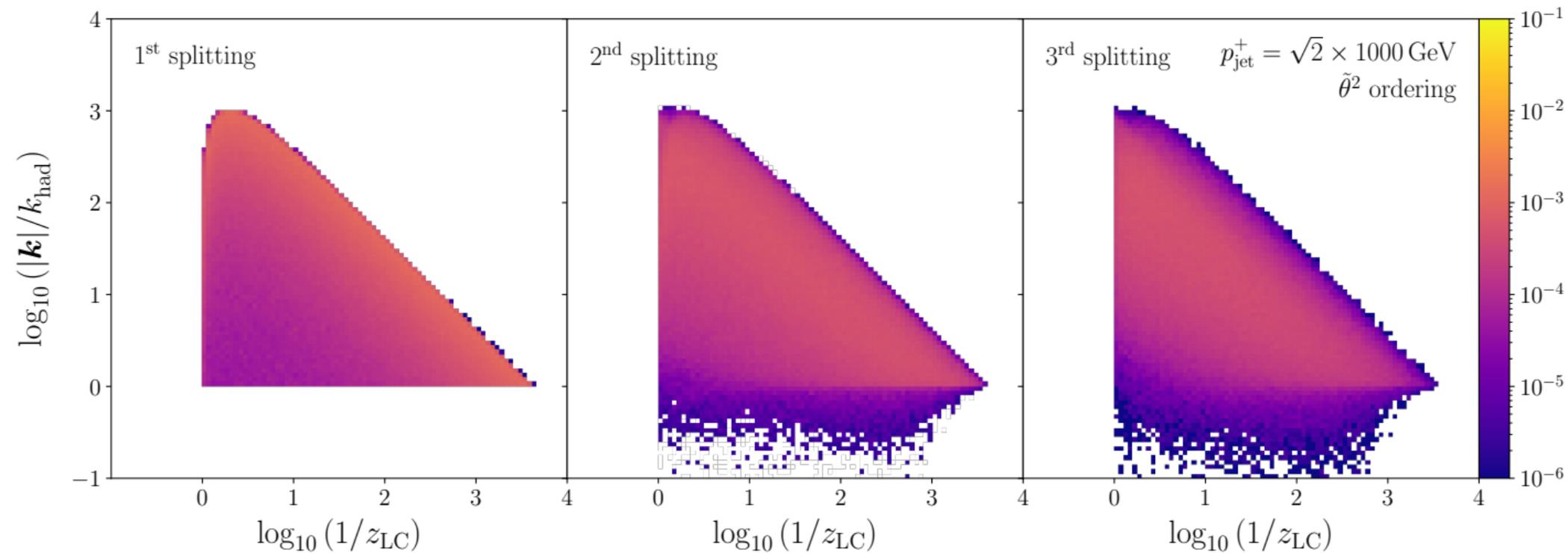
Lund Plane Densities – Time ordering



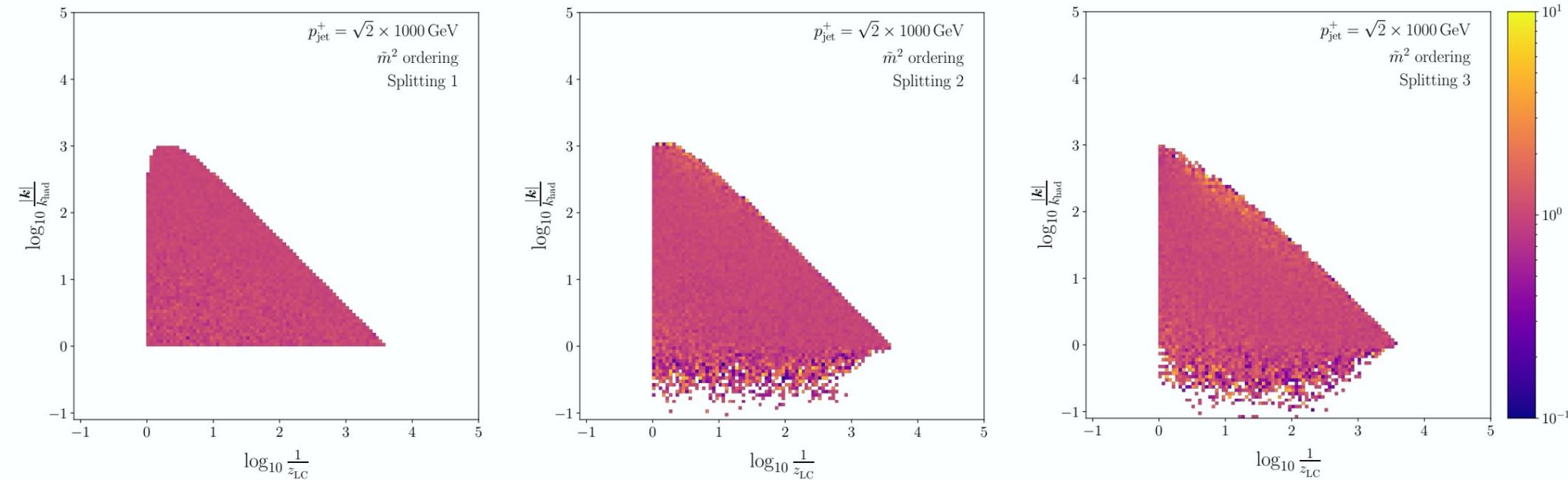
Lund Plane Densities – Virtuality ordering



Lund Plane Densities – Angular ordering

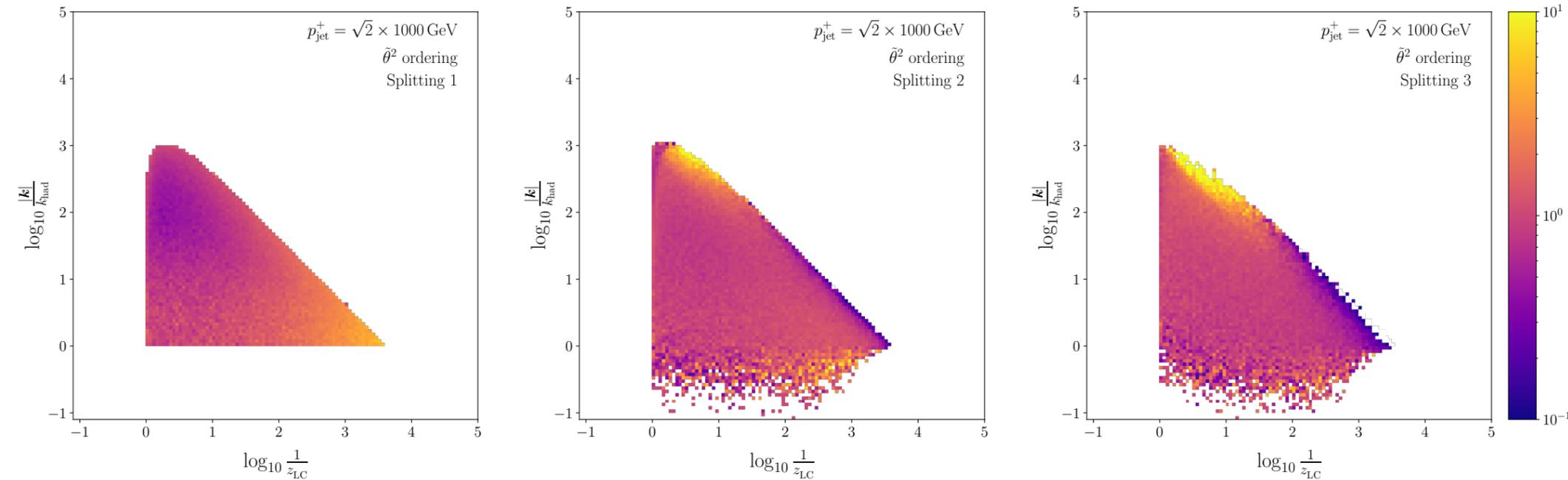


Lund Density Ratio – Mass / Formation Time



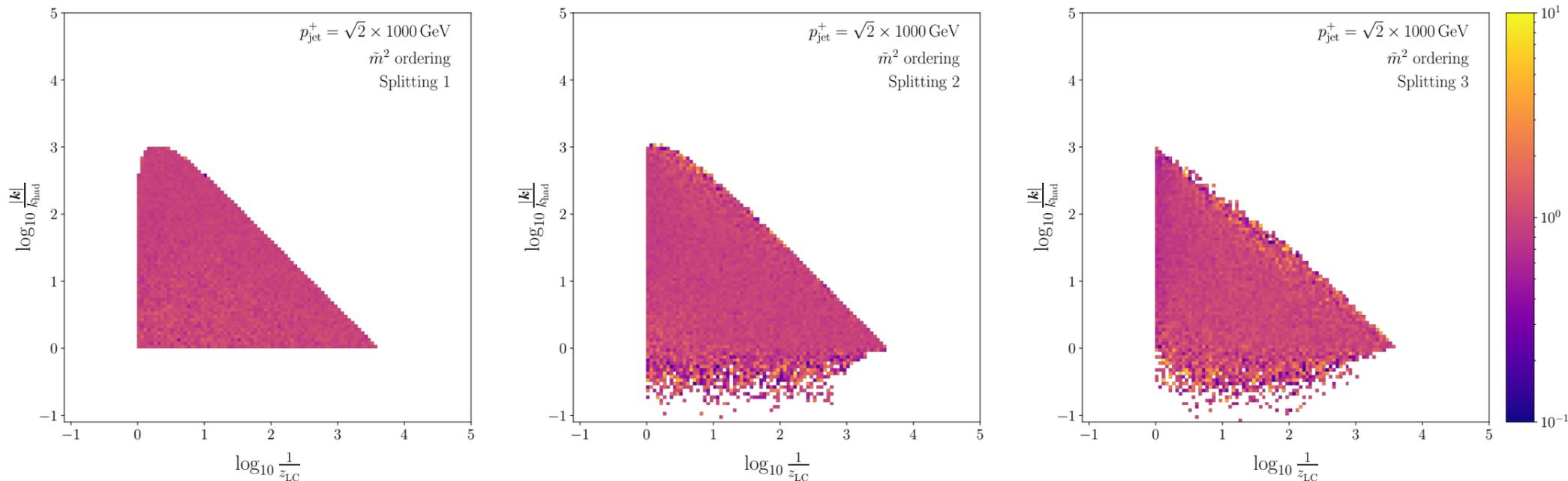
All Events

Lund Density Ratio – Angle / Formation Time



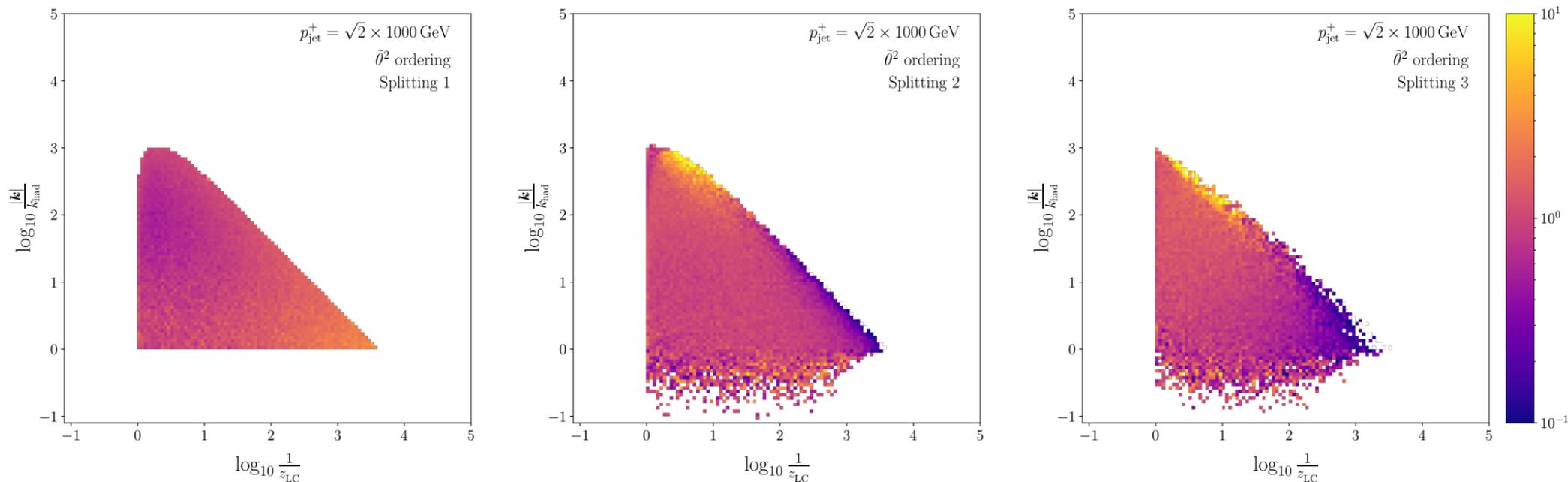
All Events

Lund Density Ratio – Mass / Formation Time



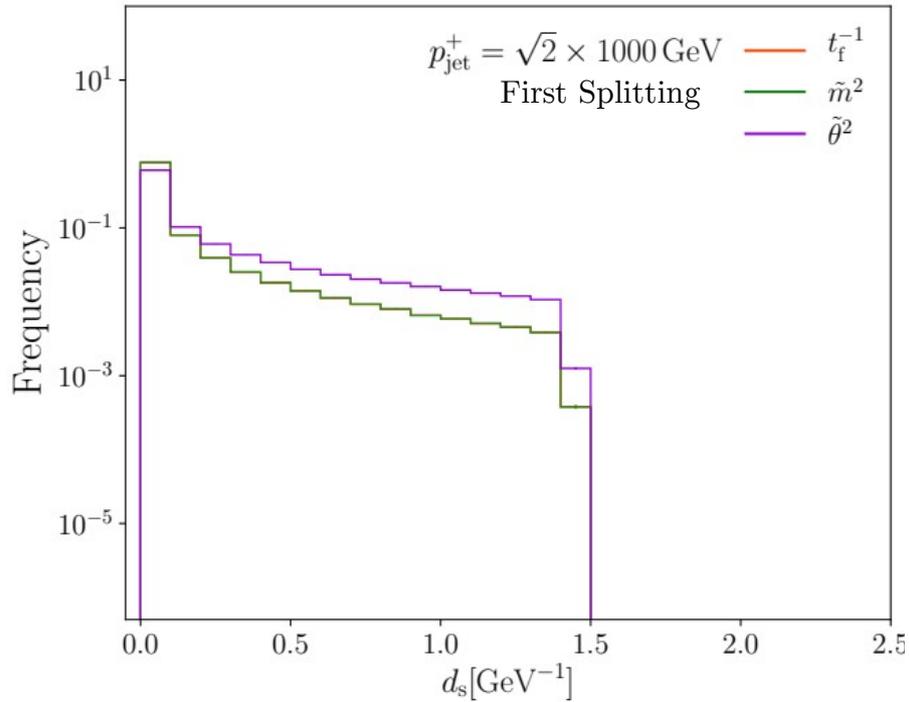
Events with at least 3 quark splittings

Lund Density Ratio – Angle / Formation Time



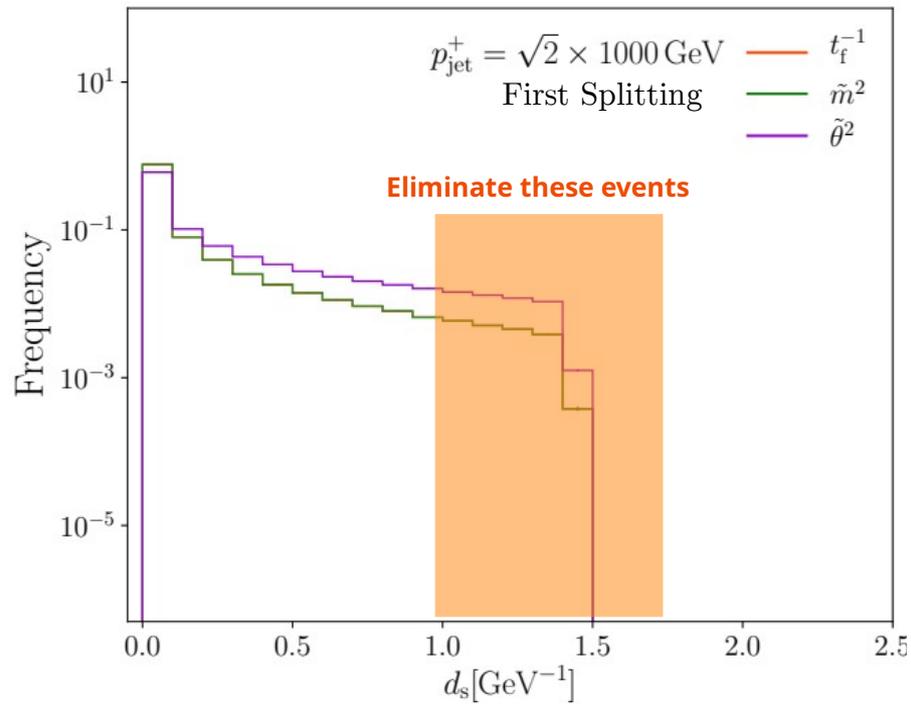
Events with at least 3 quark splittings

Simple (Pseudo-)Quenching Models



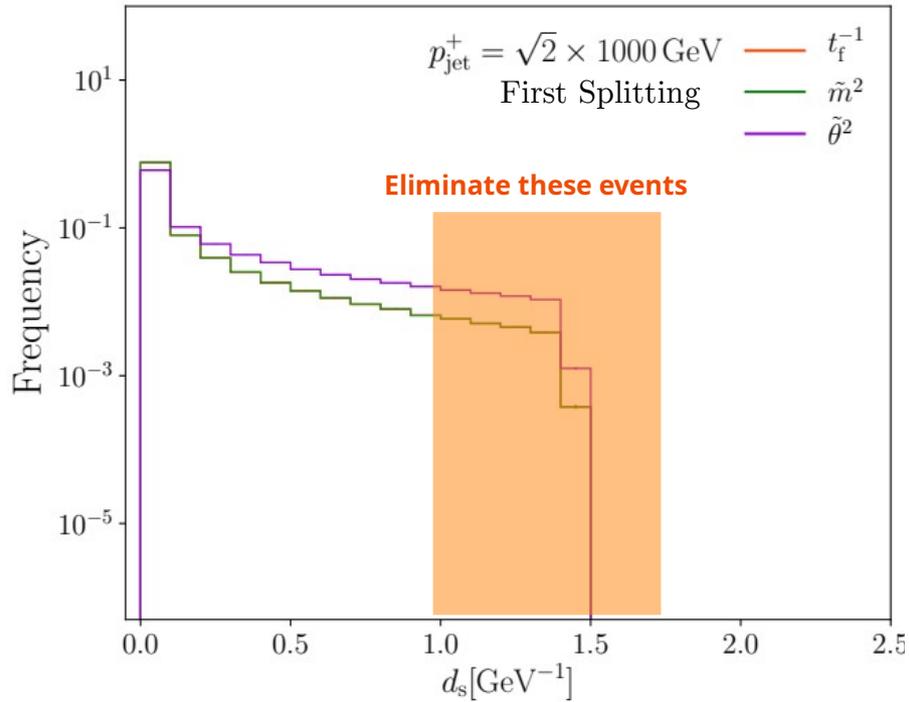
- Consider distance between daughters: $d_s = \sqrt{\frac{t_{\text{form}}}{k^+}}$
- **A simplistic model:**
 - Eliminate event if $d_s > d_{\text{coh}} = \frac{1}{\sqrt{\hat{q}L}}$ (Decoherence)

Simple (Pseudo-)Quenching Models



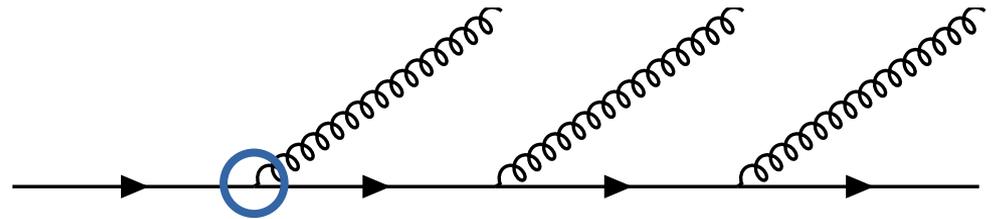
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Simple (Pseudo-)Quenching Models



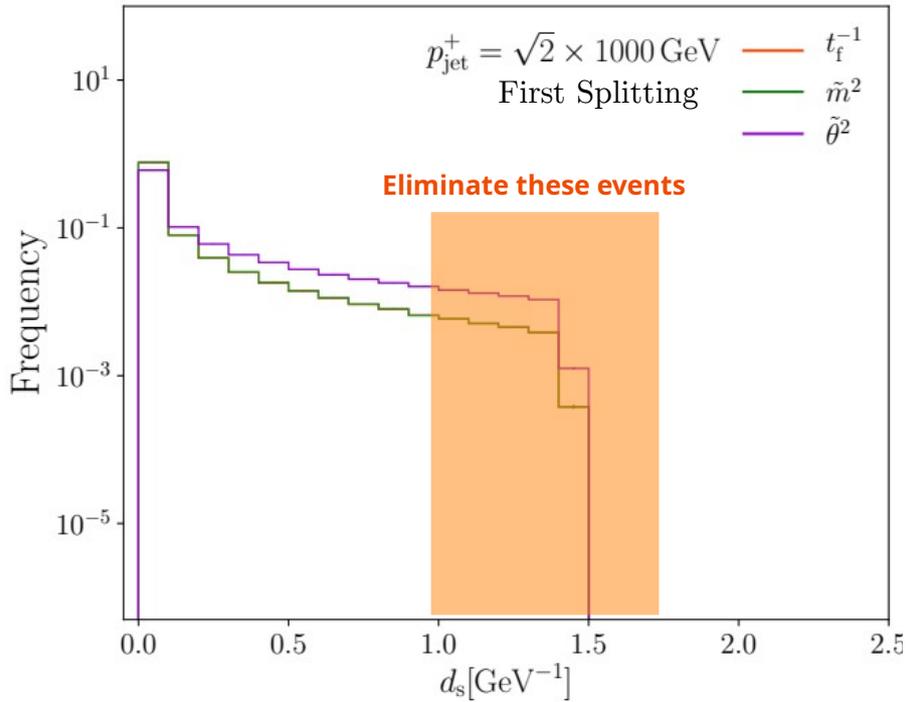
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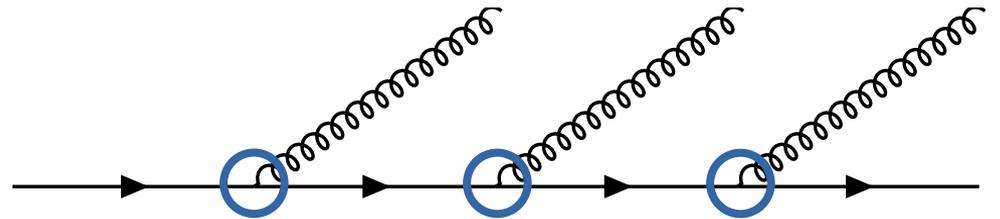


- Option 1: Apply only to first splitting

Simple (Pseudo-)Quenching Models



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- **A simplistic model:**
 - Eliminate event if $d_s > d_{\text{coh}} = \frac{1}{\sqrt{\hat{q}L}}$ (Decoherence)



- Option 1: Apply only to first splitting
- Option 2: Apply to whole quark branch

Quenched events in simple model

- Apply this pseudo-quenching model to all orderings
 - Compute the percentage of ‘quenched’ events

L [fm]	4	5	6
\hat{q} [GeV ² /fm]	2	5	5
t_f^{-1}	2.6 %	4.8 %	7.5 %
\tilde{m}^2	2.6 %	4.8 %	7.5 %
$\tilde{\theta}^2$	8.0 %	12.5 %	18.2 %

Apply quenching condition to the
first splitting

L [fm]	4	5	6
\hat{q} [GeV ² /fm]	2	5	5
t_f^{-1}	11.0 %	18.0 %	28.1 %
\tilde{m}^2	11.8 %	19.3 %	29.9 %
$\tilde{\theta}^2$	10.9 %	18.0 %	28.1 %

Apply quenching condition to the
entire quark branch