### **Analysis of Baryon Transition Electromagnetic Form Factors**

# Teresa Peña in collaboration with Gilberto Ramalho









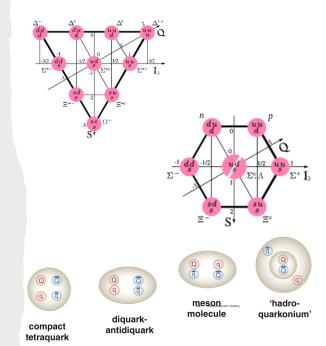


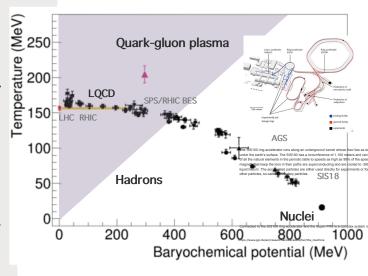
- Hadrons constitute the major part of the visible universe.
- Today's experiments have a new level of scope, precision and accuracy on the still unexplored territory of Hadron structures

(evidence for multiquark and exotic configurations.)

#### Special role of HADES@SIS at GSI and PANDA at FAIR:

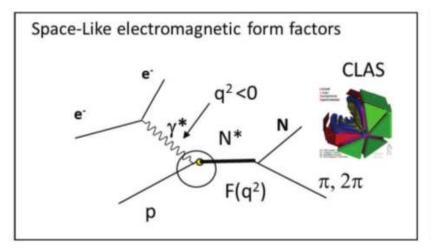
- Exploring QCD phase diagram at high baryonic number and moderate temperatures
- Experiments with pion beam also allow for cold matter studies in the few-GeV region.

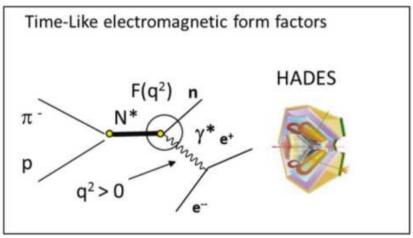




#### Two methods of obtaining information on structure of baryons

Figure: B. Ramstein, AIP Conf. Proc. 1735, 080001 (2016) [HADES]





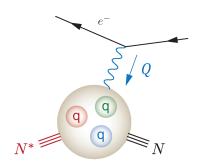
 $q^2 \leq 0$ : CLAS/Jefferson Lab, MAMI,  $q^2 > 0$ : HADES, ELSA, JLab-Hall A, MIT-BATES ...., PANDA  $ep \rightarrow e'N(\cdot\cdot\cdot); \; \gamma^*N \rightarrow N^* \; \pi^-p \rightarrow e^+e^-n$ 

$$q^2 > 0$$
: HADES, ...., PANDA 
$$\pi^- p \to e^+ e^- n; \ N^* \to \gamma^* N \to e^+ e^- N$$

Why use of pion beam:

Separation of in-medium propagation and mechanism, because pions are absorbed at the surface of the nucleus whereas in photon and proton absorption occurs throughout the whole nuclear volume.

### **Transition Electromagnetic form factors**



 $q^2 < 0$ 

#### **Spacelike form factors:**

 Structure information: shape, qqq excitation vs. hybrid, ...

## Baryon resonances transition form factors

CLAS: Aznauryan et al., Phys. Rev. C 80 (2009)

MAID: Drechsel, Kamalov, Tiator, EPJ A 34 (2009)

See Gernot Eichmann and Gilberto Ramalho Phys. Rev. D 98, 093007 (2018)

 $q^2 > 0$ 

#### **Timelike form factors:**

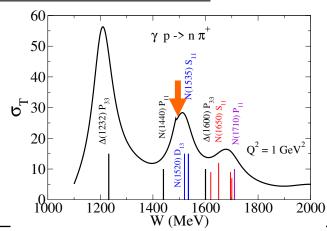
Particle production channels

#### This talk:

Connect Timelike and SpacelikeTransition Form Factors (TFF)
Obtain Baryon-photon coupling evolution with 4 momentum transfer

## Baryon resonances S=0 PDG

I	S	$J^P = \frac{1}{2}^+$	$\frac{3}{2}$ +	$\frac{5}{2}$ +	$\frac{1}{2}$	$\frac{3}{2}$	$rac{5}{2}$
$\frac{1}{2}$	0	N(940) $N(1440)$ $N(1710)$ $N(1880)$	N(1720) $N(1900)$	<b>N</b> (1680) N(1860)	N(1535) $N(1650)$ $N(1895)$	$\frac{\mathbf{N}(1520)}{N(1700)}$ $N(1875)$	N(1675)
$\frac{3}{2}$	0	$oldsymbol{\Delta}(1910)$	$\Delta$ (1232) $\Delta$ (1600) $\Delta$ (1920)	$\Delta(1905)$	$\Delta$ (1620) $\Delta$ (1900)	$\Delta(1700)$ $\Delta(1940)$	$\Delta(1930)$



#### Our approach is phenomenological

"Murray looked at two pieces of paper, looked at me and said 'In our field it is costumary to put theory and experiment on the same piece of paper'.

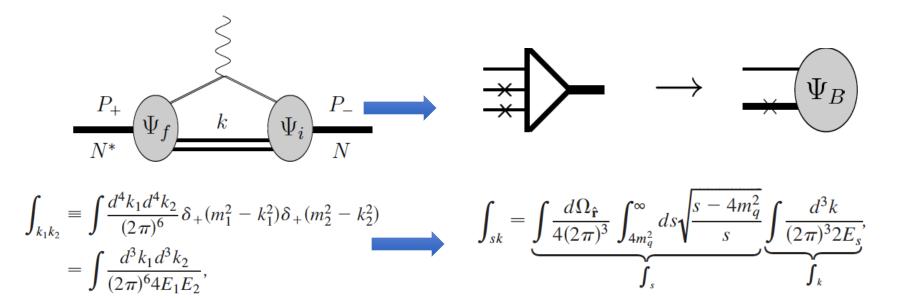
I was mortified but the lesson was valuable"

Memories of Murray and the Quark Model George Zweig, Int.J.Mod.Phys.A25:3863-3877,2010



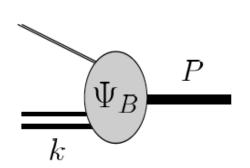
Zweig quark or the constituent quark

#### E.M. matrix element



- Baryon wavefunction integrated over spectator quarks variables.
   (Covariant Spectator Model CST)
- •E.M. matrix element is then written in terms of an effective vertex composed by an off-mass-shell quark, and an on-mass-shell quark pair (diquark) with an average mass.

- ✓ The Diquark is not pointlike.
- Nucleon "wavefunction" (S wave)
   (symmetry based only; not dynamical based)



- A quark + scalar-diquark component
- A quark+ axial vector-diquark component

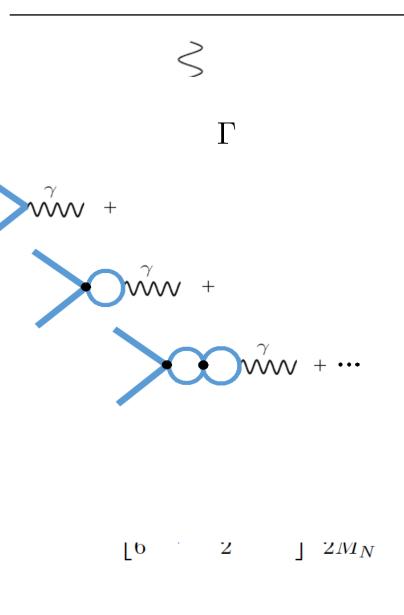
$$\begin{split} \Psi_{N\lambda_n}^S(P,k) &= \frac{1}{\sqrt{2}} \big[ \phi_I^0 u_N(P,\lambda_n) - \phi_I^1 \varepsilon_{\lambda P}^{\alpha*} U_\alpha(P,\lambda_n) \big] \\ &\times \psi_N^S(P,k). \end{split}$$
 Phenomenological function

$$U_{\alpha}(P, \lambda_n) = \frac{1}{\sqrt{3}} \gamma_5 \left( \gamma_{\alpha} - \frac{P_{\alpha}}{m_H} \right) u_N(P, \lambda_n),$$

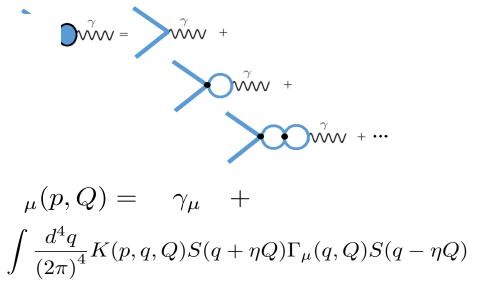
- Delta (1232) "wavefunction" (S wave)
  - Only quark + axial vector-diquark term contributes

$$\Psi^{S}_{\Delta}(P,k) = -\psi^{S}_{\Delta}(P,k) \tilde{\phi}^{1}_{I} \varepsilon^{\beta*}_{\lambda P} w_{\beta}(P,\lambda_{\Delta})$$

#### **Quark E.M. Current**



Quark-photon vertex



To parametrize the current we use Vector Meson Dominance at the quark level, a truncation to the rho and omega poles of the full meson spectrum contribution to the quark-photon coupling.

4 parameters

#### **Transition E.M. Current**

$$\gamma N \rightarrow \Delta$$

$$\Gamma^{\beta\mu}(P,q) = [G_1 q^{\beta} \gamma^{\mu} + G_2 q^{\beta} P^{\mu} + G_3 q^{\beta} q^{\mu} - G_4 g^{\beta\mu}] \gamma_5$$

- Only 3 G<sub>i</sub> are independent:
  - E.M. Current has to be conserved

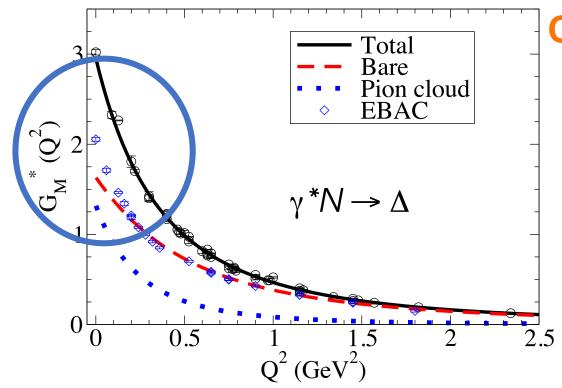
$$q^{\mu}\Gamma_{\beta\mu}=0$$

 $G_M$ ,  $G_E$ ,  $G_C$  Scadron-Jones popular choice.

#### **Model independent feature (Covariant Spectator Theory)**

$$\gamma N \longrightarrow \Delta$$
  $G_M^* = G_M^B + G_M^{\pi}$ 

Separation seems to be supported by experiment. Missing strength of  $G_M$  at the origin.



#### **CST**<sup>©</sup>2009

#### Bare quark core:

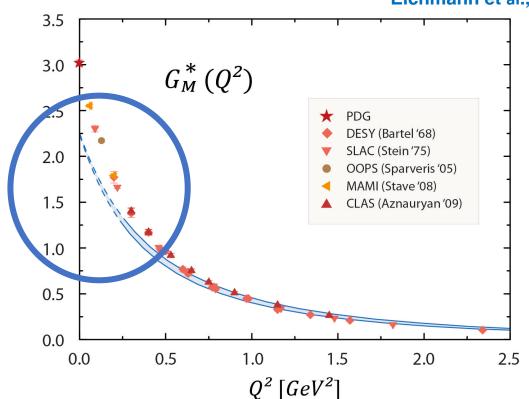
- dominates in the large  $oldsymbol{Q}^2$  region.
- agrees with other calculations ("EBAC") with pion couplings switched off.

#### Model independent feature

$$\gamma N \rightarrow \Delta$$

Missing strength of G<sub>M</sub> at the origin is an universal feature, even in dynamical quark calculations.

Eichmann et al., Prog. Part. Nucl. Phys. 91 (2016)

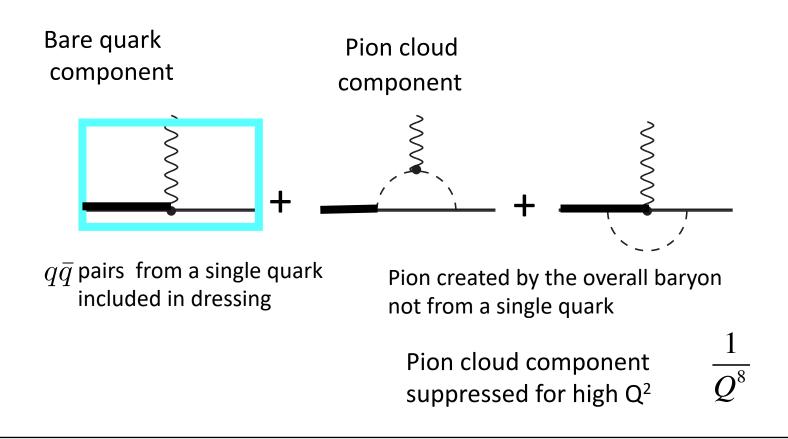


Effect of vicinity of the mass of the Delta to the pion-nucleon threshold.

$$G_M^* = G_M^B + G_M^\pi$$

#### Bare quark (partonic) and pion cloud (hadronic) components

For low  $Q^2$ : add coupling with pion in flight.

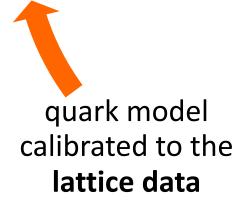


#### VMD as link to LQCD

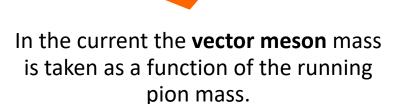
experimental data well described in the large Q<sup>2</sup> region.



Take the limit of the physical pion mass value



**VMD** 



Pion cloud contribution negligible for large pion masses

$$N \rightarrow N*(1520)$$
 TFFs

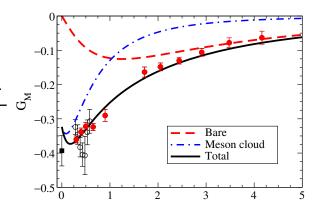
$$J^{P}=3/2^{-}$$
 I=1/2  
60% decay  $\pi$  N  
30% decay to  $\pi\Delta$ 

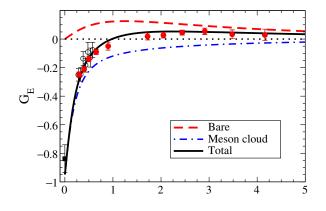
- Bare quark model gives good description in the high momentum transfer region.
- Use CST quark model to infer meson cloud from the data.

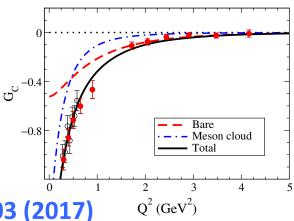
• Important role of meson cloud extracted dominated by the isovector part, due to the  $\pi$ N and  $\pi\Delta$  channels.

Consistent with Aznauryan and Burkert, PRC 85 055202 2012 and PDG

$$A_{3/2}^V \approx 0.13 \; ; A_{3/2}^S \approx 0.01 \, (GeV^{-1/2})$$







G. Ramalho, M. T. P., PHYSICAL REVIEW D 95 014003 (2017)

$$N \to N * (1535)$$
 **TFFs**

JP=1/2 $^{-}$  I=3/2 ~50% decay to  $\pi$ N ~50% decay to  $\eta$ N

$$J^{\mu} = \bar{u}_R \left[ F_1^* \left( \gamma^{\mu} - \frac{\not q q^{\mu}}{q^2} \right) + F_2^* \frac{i \sigma^{\mu\nu} q_{\nu}}{M_N + M_R} \right] \frac{\gamma_5 u_N}{q_N}$$

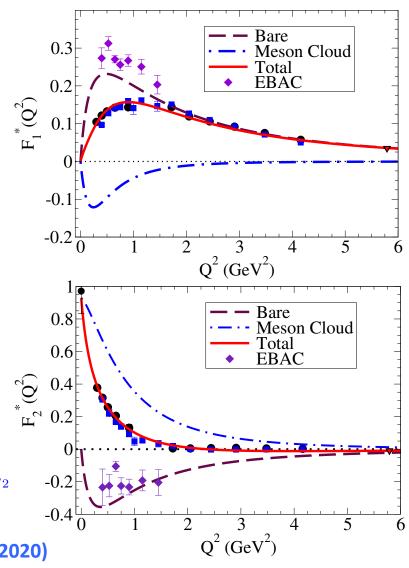
• Use CST quark model to infer meson cloud from the data.

Again good agreement of bare quark core with EBAC analysis.

- Bare quark effects dominate F<sub>1</sub>\* for large
  - 0

• Meson cloud effects dominate  $F_2^*$  with meson cloud extending to high region. (effect from the  $\eta$ N channel?).

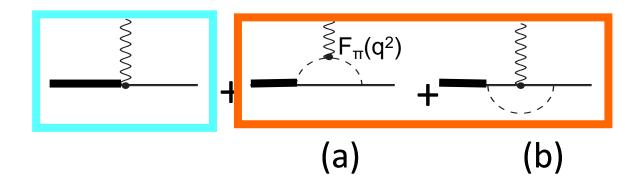
$$A_{1/2}^V(0) = 0.090 \pm 0.013 \,\, \mathrm{GeV}^{-1/2} \quad A_{1/2}^S(0) = 0.015 \pm 0.013 \,\, \mathrm{GeV}^{-1/2}$$



 $Q^{-}(GeV^{-})$ 

G. Ramalho, M. T. P., PHYSICAL REVIEW D 101 114008 (2020)

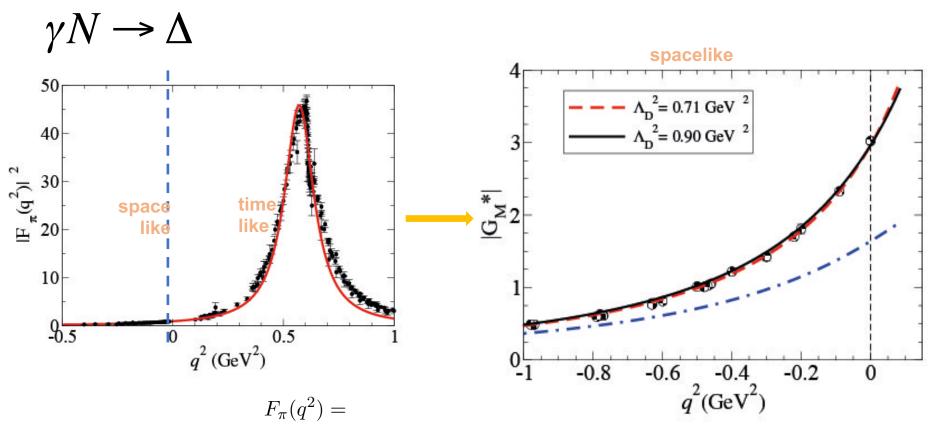
## **Extension to the Timelike region**



The residue of the pion from factor  ${\bf F}_{\pi}({\bf q}^2)$  at the timelike  $\rho$  pole is proportional to the  $ho \to \pi\pi$  decay

Diagram (a) related with pion electromagnetic form factor  $F_{\pi}(q^2)$ 

Ramalho, Pena, Weil, Van Hees, Mosel, Phys.Rev. C93 (2016)



Parametrization of pion Form Factor

$$\frac{\alpha}{\alpha - q^2 - \frac{1}{\pi}\beta q^2 \log \frac{q^2}{m_\pi^2} + i\beta q^2}$$

$$\alpha = 0.696 \text{ GeV}^2$$

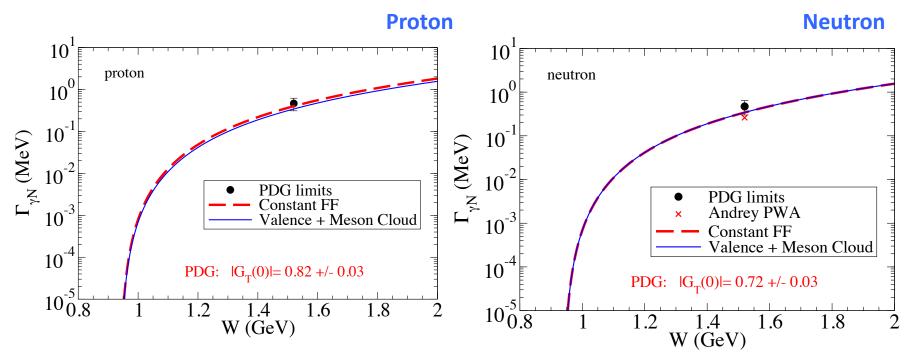
$$\beta = 0.178$$

$$\Gamma_{\gamma^*N}(q;W) = \frac{\alpha}{16} \frac{(W+M)^2}{M^2 W^3} \sqrt{y_+ y_-} y_- |G_T(q^2, W)|^2$$
$$|G_T(q^2; M_\Delta)|^2 = |G_M^*(q^2; W)|^2 + 3|G_E^*(q^2; W)|^2 + \frac{q^2}{2W^2} |G_C^*(q^2; W)|^2$$
$$y_{\pm} = (W \pm M)^2 - q^2$$

$$\Gamma_{\gamma N}(W) \equiv \Gamma_{\gamma^* N}(0; W)$$

$$\Gamma_{e^+e^-N}(W) = \frac{2\alpha}{3\pi} \int_{2m_e}^{W-M} \Gamma_{\gamma^* N}(q; W) \frac{dq}{q}$$

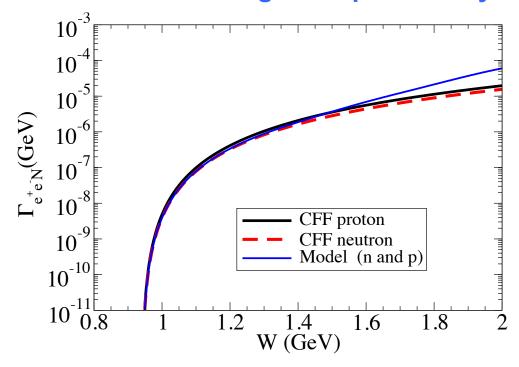
 $N^*(1520) \begin{tabular}{ll} J^P=3/2^- & I=1/2 \\ 60\% & decay $\pi$ N \\ 30\% & decay to $\pi \Delta$ \end{tabular}$ 



G. Ramalho and M.T. P. Phys. Rev. D 95, 014003 (2017)

Devenish (1976) normalization of transition form factors Result Consistent with PDG value for  $\gamma$ N decay width.

#### **Neutron and Proton light dilepton decay width**



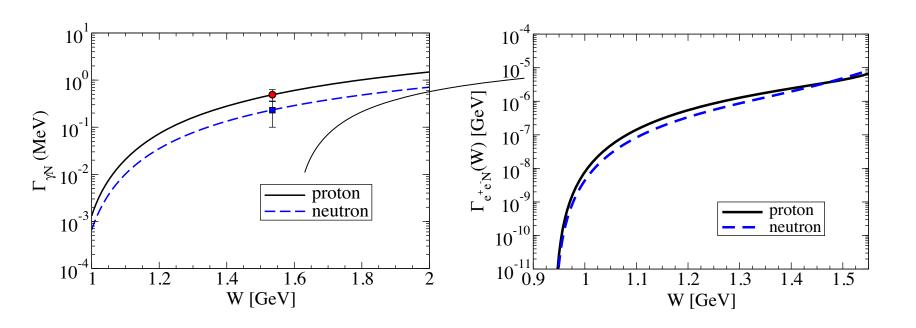
G. Ramalho and M.T. P. Phys. Rev. D 95, 014003 (2017)

Similar Proton and neutron results due to iso-vector dominance of meson cloud.

At higher energies evolution of  $G_T(q^2, W)$  with  $q^2$  becomes important.

## **Decay widths**

 $J^{P}=1/2^{-}I=1/2$ N\*(1535) ~50% decay to  $\pi N$ ~50% decay to  $\eta$ N



G. Ramalho and M.T. P. Phys.Rev.D 101 (2020) 11, 114008, (2020)

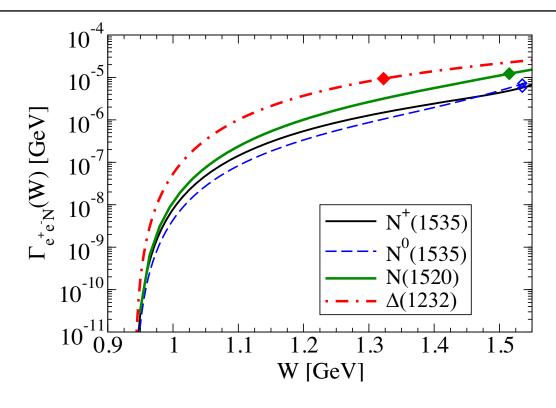
Different results for proton and neutron electromagnetic widths

due to iso-scalar term in the eta meson cloud.

Timelike results give information on the neutron.

_	$A_{1/2}(0)$ [GeV	<i>J</i> -1/2 <sub>1</sub>	$\Gamma_{\gamma N}$ [MeV]			
	$\frac{n_{1/2}(0)            }{\text{Data}}$	Model		PDG limits	Model	
	$0.105 \pm 0.015 \\ -0.075 \pm 0.020$				0.503 0.240	

## Comparison between different resonances



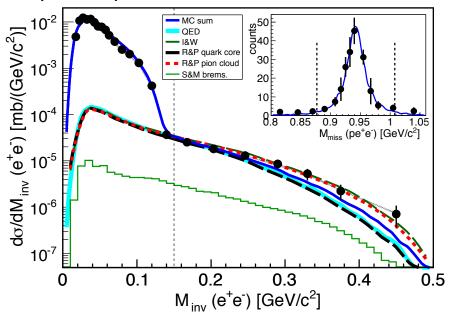
G. Ramalho and M.T. P. Phys.Rev.D 101 (2020) 11, 114008, (2020)

Dominance of the J=3/2 channel

## Dilepton mass spectrum

#### HADES Collaboration, Phys.Rev. C95 0652205 (2017)

proton-proton collisions @1.25 GeV



Signature of form factors q<sup>2</sup> dependence

 $\Delta$  Dalitz decay branching ratio extracted 4.19 x 10<sup>-5</sup>

<sup>1</sup> The systematic uncertainty includes the model dependence.

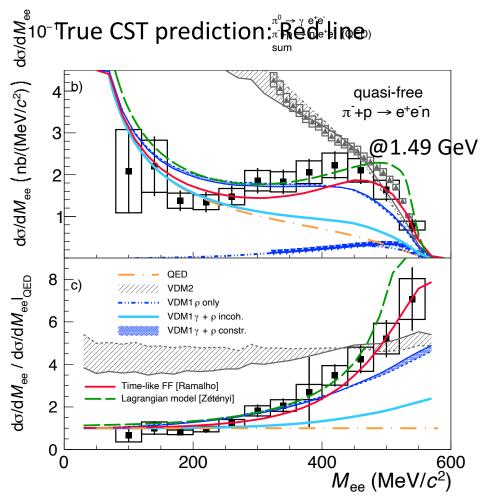
Entry in PDG

The obtained  $\Delta$  Dalitz branching ratio at the pole position is equal to  $4.19 \times 10^{-5}$  when extrapolated with the help of the Ramalho-Peña model [27], which is taken as the reference, since it describes the data better. The branching ratio

 $\Gamma_5/\Gamma$ 

## Disepton mass spectrum

## N\*(1520) + N\*(1535) Dalitz decay



Simulations based on the CST model (red line) for these resonances also give a satisfactory description of the data.

Below 200 MeV/c2, data agrees with a pointlike baryon-photon vertex (QED orange line).

At larger invariant masses, data is more than 5 times larger than the pointlike result, showing a strong effect of the transition form factor.

#### **HADES Collaboration**

"First measurement of massive virtual photon emission from N\* baryon resonances" e-Print: 2205.15914 [nucl-ex]

## **Extension to Strangeness in the timelike region**

CST seems to work well at large Q<sup>2</sup>.

$$e^+e^- \to \gamma^* \to B\bar{B}$$

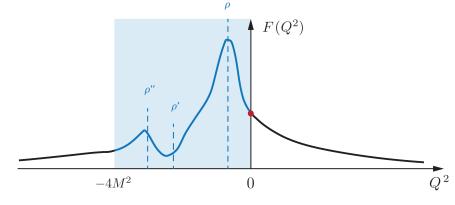
$$|G(q^{2})|^{2} = \left(1 + \frac{1}{2\tau}\right)^{-1} \left[ |G_{M}(q^{2})|^{2} + \frac{1}{2\tau} |G_{E}(q^{2})|^{2} \right]$$

$$= \frac{2\tau |G_{M}(q^{2})|^{2} + |G_{E}(q^{2})|^{2}}{2\tau + 1}. \quad \tau = \frac{q^{2}}{4M_{B}^{2}}$$

Effective Form factor that gives the integrated cross section

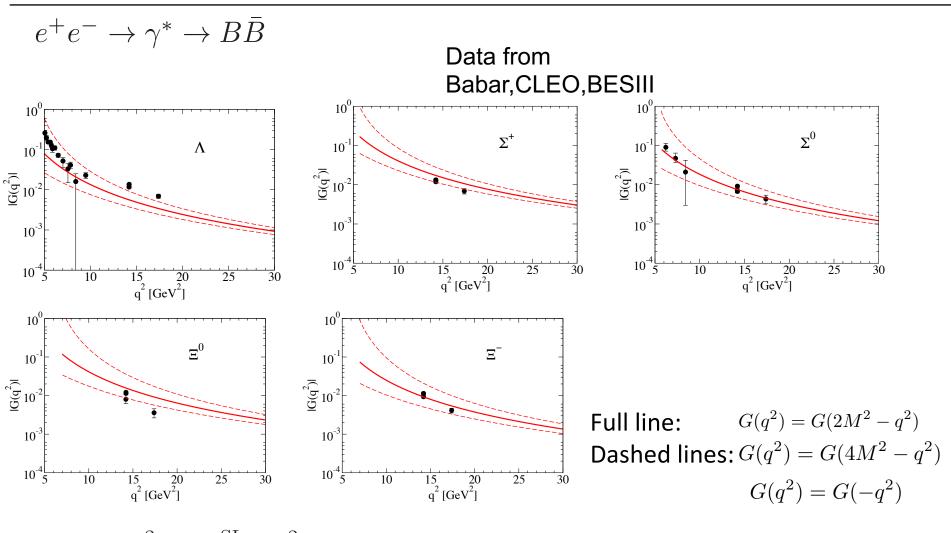
Unitarity and Analiticity demand that for  $q^2 \to \infty$ 

$$G_M(q^2) \simeq G_M^{\rm SL}(-q^2),$$
  
 $G_E(q^2) \simeq G_E^{\rm SL}(-q^2).$ 



S.Pacetti, R. Baldini Ferroli and E. Tomasi-Gustafsson, Phys. Rept. 550-551,1 (2015)

## Extension to Strangeness in the timelike region



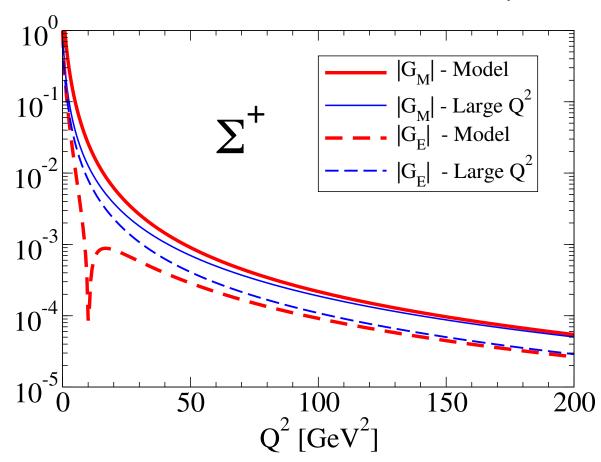
$$G_M(q^2) \simeq G_M^{\rm SL}(-q^2),$$
  
 $G_E(q^2) \simeq G_E^{\rm SL}(-q^2).$ 

G. Ramalho and M.T.P. Phys.Rev.D 101 (2020) 1, 014014, (2020)

## Asymptotic behavior reached at energies higher than reflection property

$$e^+e^- \to \gamma^* \to B\bar{B}$$

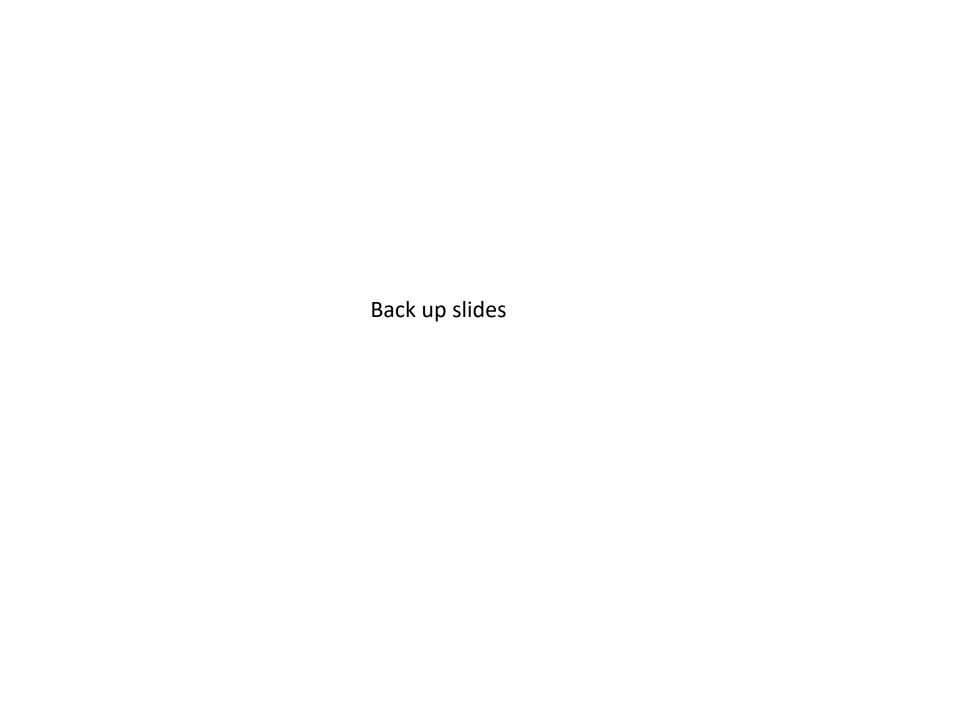
Perturbative QCD limit is way above the region where refletion symmetry starts to be valid (100 GeV<sup>2</sup> versus 10 GeV<sup>2</sup>)



## **Summary**

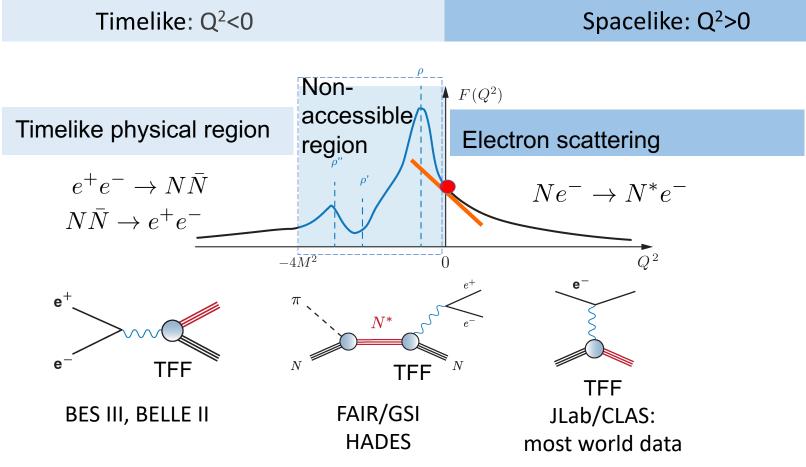
With a CST phenomenological ansatz for the baryon wave functions we described different excited states of the nucleon, with a variety of spin and orbital motion.

- 1 Evidence of separation of partonic and hadronic (pion cloud) effects from the  $\Delta$  (1232)
- **2** Made consistent with LQCD in the large pion mass regime, enabling extraction of "pion cloud" effects indirectly from data.
- 3 Spacelike e.m. transition FFs for: N\*(1440), N\*(1520), N\*(1535), ..., baryon octet, etc.
- **4** Extension to timelike e.m. transition FFs and predictions for dilepton mass spectrum and decay widths.
- 5 Descriptions consistent with experimental data at high Q<sup>2</sup>.



#### **Crossing the Boundaries to explore baryon resonances**

$$Q^2 = -q^2$$



Results have to match at the photon point.

CLAS/JLab electron scattering data constrain interpretation of dilepton production data.

## **CST**<sup>©</sup> Covariant **Spectator Theory**

- Formulation in Minkowski space.
- Motivation is partial cancellation



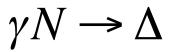
Manifestly covariant, although only three-dimensional loop integrations.

$$\int_{k} = \int \frac{d^3 \mathbf{k}}{2E_D (2\pi)^3}$$

 Provides wave functions from covariant vertex with simple transformation properties under Lorentz boosts, appropriate angular momentum structures and smooth non-relativistic limit.

To parametrize the current use Vector Meson Dominance at the quark level a truncation to the rho and omega poles of the full meson spectrum contribution to the quark-photon coupling.

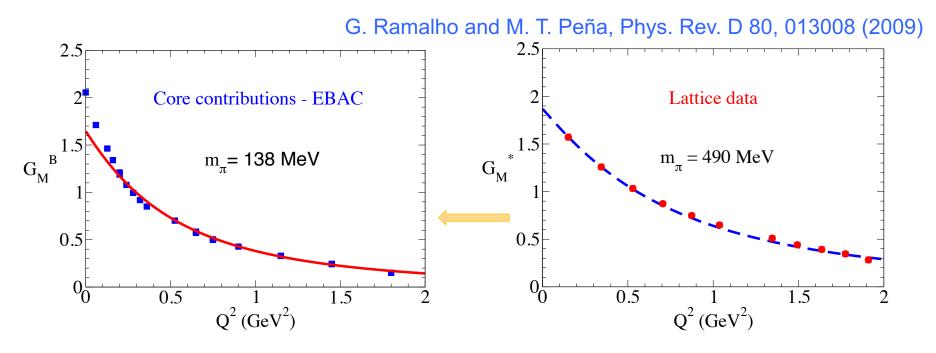
#### 4 parameters



#### **Connection to Lattice QCD**

To control model dependence:

CST model and LQCD data are made compatible.

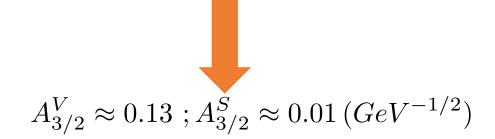


Model (no pion cloud) valid for lattice pion mass regime. No refit of wave function scale parameters for the physical pion mass limit.

$$N \rightarrow N * (1520)$$

PDG data at the photon point:

$A_{1/2}$	$A_{3/2}$	$ A ^2$
$p - 0.025 \pm 0.005$	$0.140 \pm 0.005$	$20.2 \pm 1.4$
$n - 0.050 \pm 0.005$	$-0.120\pm0.005$	$15.7 \pm 1.3$



Dominance of iso-vector channel concurs to our model of the meson cloud: pion only

$$N \rightarrow N*(1535)$$

Iso-vector + iso-scalar channels included into our model of the meson cloud: pion and eta cloud.

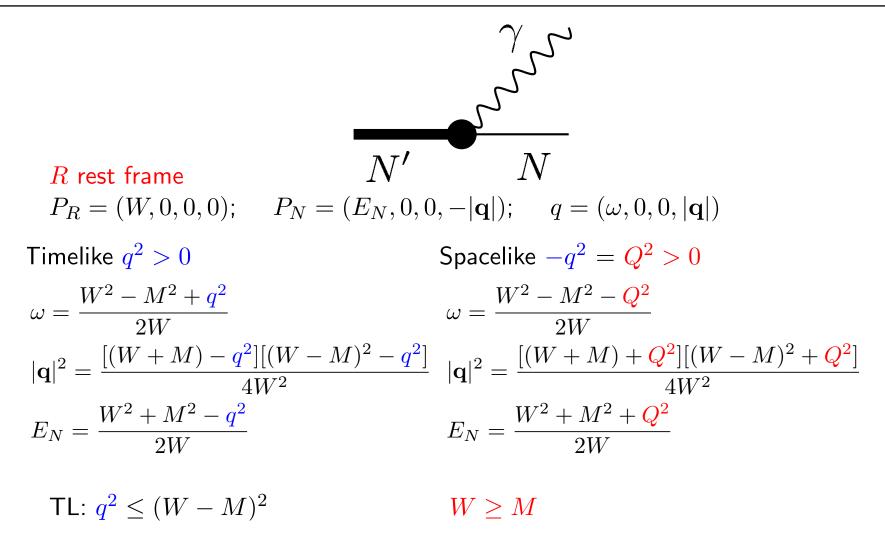
$$F_1^{\text{MC}} = Q^2 \tilde{C}(Q^2) \tau_3$$
  $F_2^{\text{MC}} = A(Q^2) + B(Q^2) \tau_3$ 

PDG data at the photon point:

$$A_{1/2}^V(0) = 0.090 \pm 0.013 \text{ GeV}^{-1/2}$$
  $A_{1/2}^S(0) = 0.015 \pm 0.013 \text{ GeV}^{-1/2}$ 

Isovector dominance to some extent

#### **Extension to Timelike**

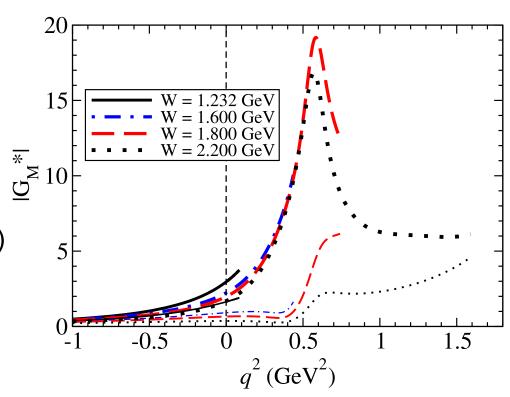


Transition form factors in the timelike region are restricted to a given kinematic region that depends on the varying resonance mass W.

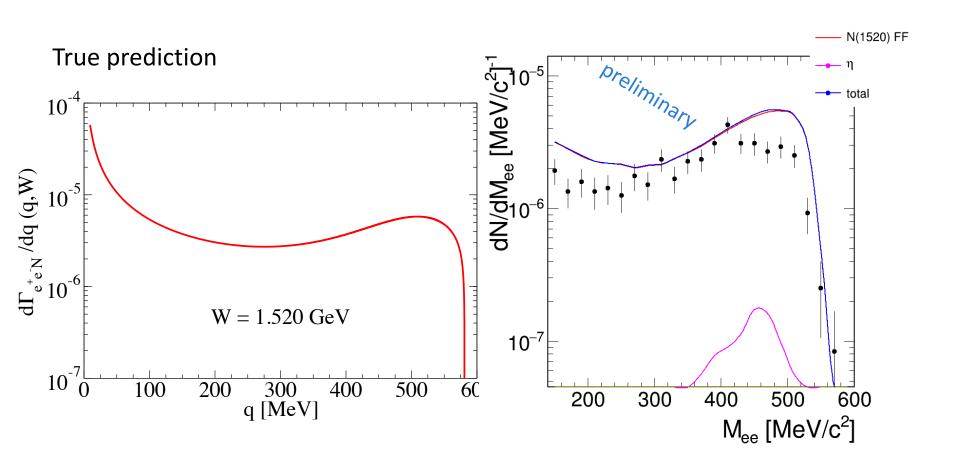
#### **Extension to Timelike**

$$\gamma N \rightarrow \Delta$$

- Extension to higher W shows effect of the rho mass pole
- In that pole region small bare quark contribution (thin lines)

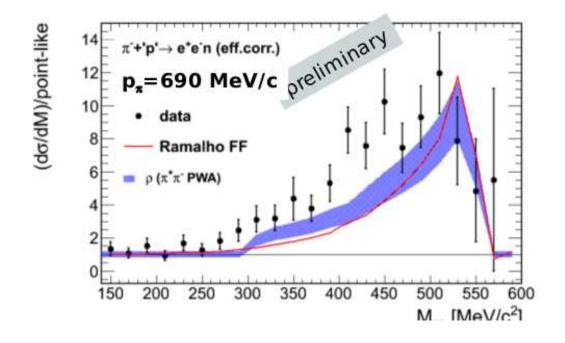


## $N^*(1520)$ Dalitz decay



HADES Collaboration 2018

Effect of dependence of e.m. coupling with W True prediction



B. Ramstein, NSTAR2019

**HADES Collaboration** 

Ratio to pointlike case

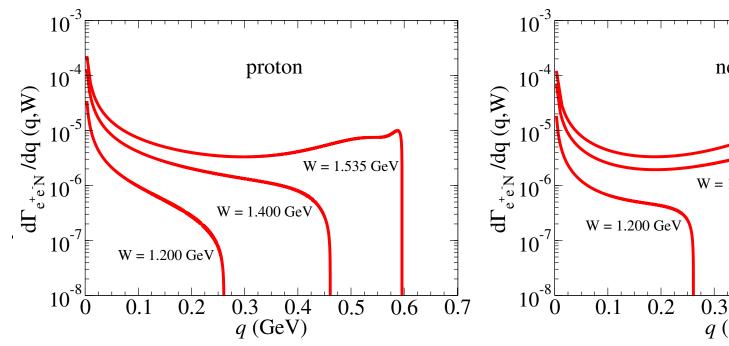
## **Crossing the boundaries**

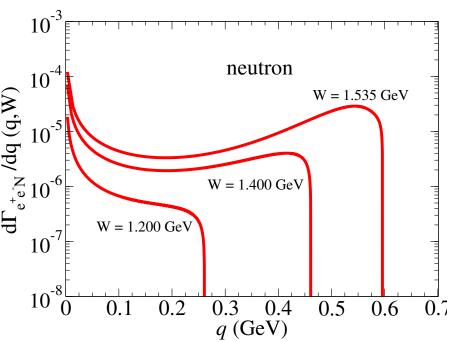
## N\*(1535) Dalitz decay

$$\Gamma_{\gamma^* N}(q, W) = \frac{\alpha}{2W^3} \sqrt{y_+ y_-} y_+ B \|G_T(q^2, W)\|^2,$$

$$|G_T(q^2, W)|^2 = |G_E(q^2, W)|^2 + \frac{q^2}{2W^2} |G_C(q^2, W)|^2$$

$$\frac{d\Gamma_{e^+ e^- N}}{dq} (q, W) = \frac{2\alpha}{3\pi q^3} (2\mu^2 + q^2) \sqrt{1 - \frac{4\mu^2}{q^2}} \Gamma_{\gamma^* N}(q, W),$$





## Extension to Strangeness in the Spacelike region with a global fit to lattice data and physical magnetic moments

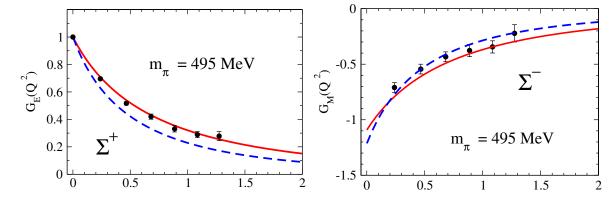
Extend the parametrization of the e.m. current to the valence quark d.o.f of the **whole** baryon octet.

$$j_i = \frac{1}{6} f_{i+} \lambda_0 + \frac{1}{2} f_{i-} \lambda_3 + \frac{1}{6} f_{i0} \lambda_s$$

$$\lambda_0 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad \lambda_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$
$$\lambda_s = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -2 \end{pmatrix}$$

Two examples:

Red line: lattice
Blue line: physical regime



Parameters for valence quark degrees of freedom and the pion cloud dressing determined by a **global fit** to octet baryon lattice data for the e.m. form factors

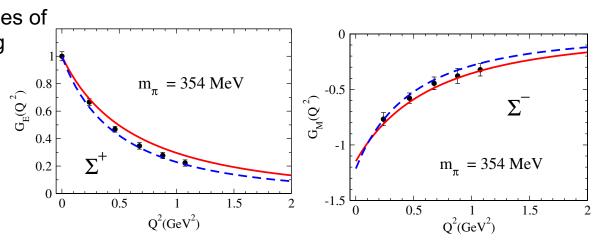
and physical magnetic moments.

Output

Description:

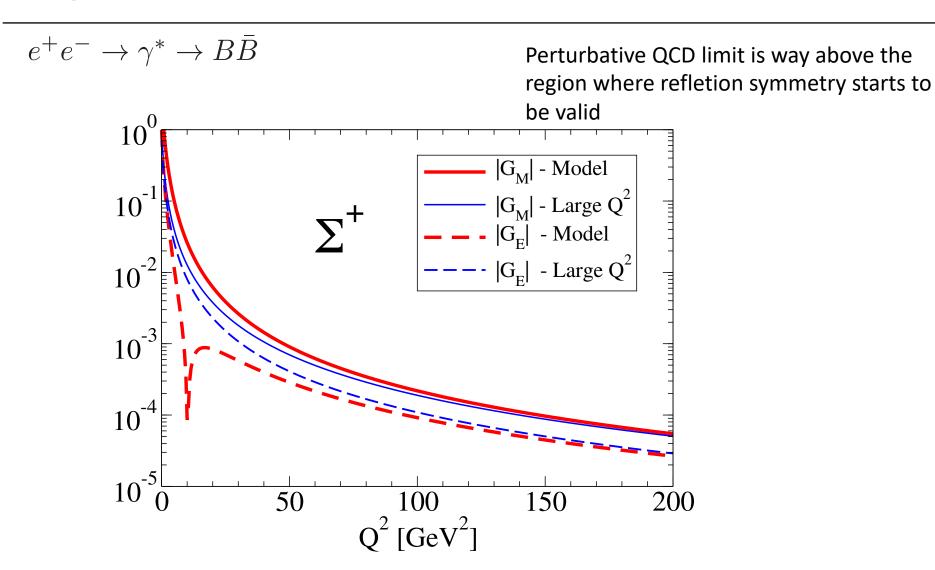
#### **Lattice data:**

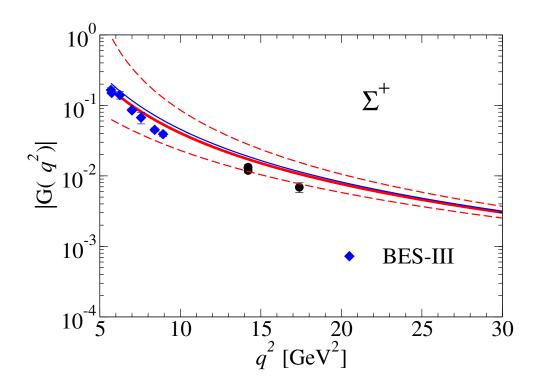
H.W. Lin and K. Orginos, Phys. Rev. D 79, 074507 (2009).



G. Ramalho and K.Tsushima, PRD 84, 054014 (2011)

## **Asymptotic behavior**





## **Predictive power:**

S. Capstick and W. Roberts, are part of a large supermultiplet (I=1/2)D13(J=3/2-) **S11**(J=1/2-) Prog. Part. Nucl. Phys. 45, (SU(6) spin-flavor with O(3) symmetry) S241 (2000); V. D. Burkert et al. Phys. Rev. C 67, 035204 (2003). Input: N(1520), N(1535); Output:  $N(1650), N(1700), \Delta(1620)$ ,  $\Delta(1700)$ D13 D33 80 PDGCLAS-1CLAS-2MAID 20  $A_{3/2} (10^{-3} \text{ GeV}^{-1/2})$  $A_{1/2} (10^{-3} \text{ GeV}^{-1/2})$ PDGCLAS-1  $A_{1/2} (10^{-3} \text{ GeV}^{-1/2})$ -10 ■ PDG • CLAS-1 -20 -30 N(1650) N(1700)N(1700)100 120 PDGCLAS-1CLAS-2MAID PDG
CLAS-1
CLAS-2
MAID PDG CLAS-2 120 80  $A_{1/2} (10^{-3} \text{ GeV}^{-1/2})$  $A_{3/2} (10^{-3} \text{ GeV}^{-1/2})$ MAID NSTAR  $A_{1/2} (10^{-3} \text{ GeV}^{-1/2})$ 100 60  $\Delta(1620)$  $\Delta(1700)$  $\Delta(1700)$ 60 20 -20 0  $Q^2(\text{GeV}^2)$ Bare quark CST description  $Q^2(GeV^2)$ 

G. Ramalho, PRD 90, 033010 (2014)

expected to work well in high Q<sup>2</sup> region!

#### **Summary**

Covariant Spectator quark-diquark model for baryons enables description of different states, with a variety of spin and orbital motion.

Several applications:  $\Delta(1232)$ , N\*(1440), N\*(1535), N\*(1520), DIS, dilepton mass spectrum, hyperons of the baryon octet.

Consistent with experimental data at high Q<sup>2</sup>.

Made consistent with LQCD in the large pion mass regime informing on "pion cloud" effects, and high q<sup>2</sup> behavior of time-like FFs.

VMD and "pion cloud" sustained extension to the timelike region of the TFF of the  $\Delta(1232)$ , N\*(1520), N\*(1535), ...