QCD & Heavy-Ion Physics

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LIP Internship Program



Gauge Bosons ("Force carriers")









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- Example: Quantum Electrodynamics (QED)
 - Electrons, muons,... with electric charge (+/-)
 - Photon: neutral particle









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- Example: Quantum Electrodynamics (QED)
 - Electrons, muons,... with electric charge (+/-)
 - Photon: neutral particle
- Example: Quantum Chromodynamics (QCD)
 - Quarks with 1 color charge (RGB)
 - Gluon: with "~2" color charges (RR, GG, BB)









- Higgs: mass to elementary particles
- QCD: contributes largely to the mass of composite particles (mesons, baryons,...)











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Standard Model of Elementary Particles

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- Higgs: mass to elementary particles
- QCD: contributes largely to the mass of composite particles (mesons, baryons,...)



(more realistic) proton structure



valence + sea (quarks and gluons) 100% mass



Standard Model of Elementary Particles

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Quantum Electrodynamics

Photons do not have electric charge



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• Quantum Chromodynamics

Gluons are colourful







Quantum Electrodynamics

Photons do not have electric charge





Smaller attraction





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• Quantum Chromodynamics

Gluons are colourful





Quantum Electrodynamics

Photons do not have electric charge





Smaller attraction





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• Quantum Chromodynamics

Gluons are colourful

Smaller attraction







Quantum Electrodynamics

Photons do not have electric charge





Smaller attraction





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• Quantum Chromodynamics = Strong Force

Gluons are colourful

Smaller attraction



Larger attraction









Coupling Constant

Interaction strength given by α_{QED} and α_{QCD}





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Coupling Constant











Coupling Constant

Interaction strength given by α_{QED} and α_{QCD}



probing small distance scales (x) \rightarrow







Quantum Chromodynamics

Interaction strength given by α_{QED} and α_{QCD}







 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \overline{g}_{i} \left((\partial^{\mu} D_{\mu} + m_{i}) g_{i} \right) \\ &= \frac{1}{4g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \overline{g}_{i}^{\alpha} + \mathcal{G}_{\mu\nu}^{\alpha} \overline{g}_{i}^{\alpha} \right) \\ &= \frac{1}{4g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \overline{g}_{\mu\nu}^{\alpha} + \mathcal{G}_{\mu\nu}^{\alpha} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\ &= \frac{1}{2g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \right) \\$





Quantum Chromodynamics

Interaction strength given by α_{OED} and α_{OCD}







 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \overline{g}_{i} \left((\partial^{\mu} \mathcal{D}_{\mu} + m_{i}) g_{i} \right) \right. \\ & \text{where } \left(\mathcal{G}_{\mu\nu}^{\alpha} = \partial_{\mu} \mathcal{H}_{\nu}^{\alpha} - \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} + \mathcal{H}_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\beta} \mathcal{H}_{\nu}^{\alpha} \right. \\ & \text{and } \mathcal{D}_{\mu} = \partial_{\mu} + i t^{\alpha} \mathcal{H}_{\mu}^{\alpha} \\ & \mathcal{T} hat's it ! \end{aligned}$





Quantum Chromodynamics

Interaction strength given by α_{QED} and α_{QCD}







 $\begin{aligned} \mathcal{J} &= \frac{1}{m_{q^{\alpha}}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{i} \left((\partial^{\mu} \mathcal{D}_{\mu} + m_{j}) \right) \right) \\ &= \frac{1}{m_{q^{\alpha}}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu} + \frac{1}{2} \overline{g}_{i} \left((\partial^{\mu} \mathcal{D}_{\mu} + m_{j}) \right) \right) \\ &= \frac{1}{m_{q^{\alpha}}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{m_{q^{\alpha}}} \left(\mathcal{D}_{\mu\nu} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{m_{q^{\alpha}}} \left(\mathcal{D}_{\mu\nu} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2} \overline{g}_{\mu\nu}^{\alpha} + \frac$







How do we "work" with QCD?



 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \left((\partial^{\mu} D_{\mu} + m_i) g_i \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \left((\partial^{\mu} D_{\mu} + m_i) g_i \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{$

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Asymptotic Freedom



 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2} \overline{\vartheta}_{i} \left((\vartheta^{\mu} D_{\mu} + m_{i}) \vartheta_{i} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\mu\nu}^{\alpha} + \frac{1}{2} \overline{\vartheta}_{i} \left((\vartheta^{\mu} D_{\mu} + m_{i}) \vartheta_{\mu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} = \partial_{\mu} \mathcal{H}_{\nu}^{\alpha} - \partial_{\nu} \mathcal{H}_{\mu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \partial_{\mu} \mathcal{H}_{\nu}^{\alpha} - \partial_{\nu} \mathcal{H}_{\mu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \\ &= \frac{1}{4g^2} \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} - \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \\ &= \frac{1}{4g^2} \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} - \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \\ &= \frac{1}{4g^2} \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \\ &= \frac{1}{4g^2} \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} + m_{i} \vartheta_{\mu\nu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \mathcal{H}_{\mu}^{\alpha} \\ &= \frac{1}{4g^2} \partial_{\mu} \mathcal{H}_{\mu}^{\alpha} \mathcal{H}_{\mu}$

Example: Taylor Series of f(x)

$$f(a)+rac{f'(a)}{1!}(x-a)+rac{f''(a)}{2!}(x-a)^2+rac{f'''(a)}{3!}(x-a)^3+$$

$$\sin(x) pprox x - rac{x^3}{3!} + rac{x^5}{5!} - rac{x^7}{7!}.$$

Higher order terms can be neglected for x << 1



Asymptotic Freedom



QCD Lagrangian within perturbation theory!

→ perturbative QCD (pQCD)

 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{i} \left((\partial^{\mu} D_{\mu} + m_{i}) g_{i} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{i} \left((\partial^{\mu} D_{\mu} + m_{i}) g_{\mu}^{\alpha} \right) \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} = \frac{1}{2g^2} \overline{g}_{\mu\nu} \mathcal{G}_{\mu\nu}^{\alpha} - \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} \mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{4g^2} \overline{g}_{\mu\nu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} \right) \\ &= \frac{1}{2g^2} \left(\mathcal{G}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_{\mu\nu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}$

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$$\sin(x) pprox x - rac{x^3}{3!} + rac{x^5}{5!} - rac{x^7}{7!}.$$

Higher order terms can be neglected for x << 1



Confinement



 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^{\alpha}} \overline{g}_{i} \left((\partial^{\mu} \mathcal{D}_{\mu} + m_{i}) g \right) \\ &= \frac{1}{4g^{\alpha}} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu} + \frac{1}{2g^{\alpha}} \overline{g}_{i} + \frac{1}{2g^{\alpha}} \overline{g}_{\mu}^{\alpha} + \frac{1}{2g^{\alpha}} \overline{g}_{\mu}^{\alpha} - \frac{1}{2g^{\alpha}} \overline{g}_{\mu}^{\alpha} + \frac{1}{2g^{\alpha}} + \frac{1}{2g^{\alpha}} + \frac{1}{2g^{\alpha}} + \frac{1}{2g^{\alpha}} + \frac{1}{2g^{\alpha$

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Confinement



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Confinement



Perturbation theory not possible...

→ Non-perturbative QCD (non-pQCD)

 $\begin{aligned} \mathcal{J} &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \left((\partial^{\mu} \mathcal{D}_{\mu} + m_i) g \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \left((\partial^{\mu} \mathcal{D}_{\mu} + m_i) g \right) \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \overline{g}_i \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{\mu\nu}^{\alpha} \right) \\ &= \frac{1}{4g^2} \left(\mathcal{G}_{\mu\nu}^{\alpha} + \frac{1}{2g^2} \mathcal{G}_{$



??

10





QCD: Two limits, same theory



Quarks & gluons

Hadrons



What we detect experimentally?



• Process with a large momentum transfer:









Process with a large momentum transfer:









Process with a large momentum transfer:











Process with a large momentum transfer:









Process with a large momentum transfer:









Process with a large momentum transfer:







 α_{QCD} no longer << 1



Process with a large momentum transfer:







 α_{QCD} no longer << 1

Particles @ detector



Process with a large momentum transfer:



Particles @ detector





Jets





Particles @ detector



What we calculate





QCD Parton Shower to Jets

What is a jet?

• Spray of collimated particles that were originated by a high momentum parton (quark or gluon)











QCD Parton Shower to Jets

What is a jet?

• Spray of collimated particles that were originated by a high momentum parton (quark or gluon)










• Need a recipe to define a jet:

- Jet size (radius): maximum "distance" that two particles can be to be considered as part of the same jet
- Jet clustering algorithm: define criteria to decide which particles are going to be clustered in the same jet



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$$R_{ij}^{2} = (y_{i} \ y_{j})^{2} + (\phi_{i} - \phi_{j})^{2}$$

which
$$d_{ij} = \min(p_{T,i}^{2p}, p_{T,j}^{2p}) \frac{\Delta R_{ij}^{2}}{R^{2}} \begin{cases} p = 1 & k_{T} \ algorithmodel{eq:k_T} \\ p = 0 & Cambridge/k_{T} \\ p = -1 & anti - k_{T} \ algorithmodel{eq:k_T} \end{cases}$$

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An example of QCD success

- Jets in pp collisions: excellent phenomenological tool!
 - Theoretical understanding from first principles
 - Accurate theoretical description of jet production in 10 orders of magnitude in cross-section!
 - Well controlled experimentally
 - Used in a multitude of phenomenological studies (top quark physics, Higgs, Electroweak, BSM searches, ...)









Is QCD limited to a collection of small particles?



From dilute QCD to dense QCD

QCD matter has a rich and vast phase diagram:







Phase diagram of QCD matter





From dilute QCD to dense QCD

QCD matter has a rich and vast phase diagram:

QCD theory (1973) SU(3) Color symmetry; confinement; asymptotic freedom, ...

QGP initial idea (1975) "Weakly coupling quark soup"

State of matter where quarks and gluons are asymptotically free





Phase diagram of QCD matter





QGP @ Early Universe



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QGP @ Heavy-lon Collisions

Heavy-Ion Collisions:







Nuclei

QGP @ Heavy-lon Collisions

Heavy-Ion Collisions:













??? $(fm/c = 10^{-24} s)$

How to probe the QGP @ lab?

• Look to the result of the collision (Soft probes)





Try different centrality collisions

Peripheral Collision



(near) Central Collision







- Sensitive to macroscopic properties of the QGP:
 - Local or large scale collective behaviour?



Response of the system to initial spatial anisotropy





Sensitive to macroscopic properties of the QGP:

• Local or large scale collective behaviour?

Superposition of multiple pp collisions





"Gas-like" behaviour?

Uniform distribution of final particles





Response of the system to initial spatial anisotropy





Sensitive to macroscopic properties of the QGP:

Local or large scale collective behaviour?

Superposition of multiple pp collisions





"Gas-like" behaviour?

Uniform distribution of final particles





Response of the system to initial spatial anisotropy

"Liquid-like" behaviour?



Initial anisotropies also present in the distribution of final particles









- Sensitive to macroscopic properties of the QGP:
 - Local or large scale collective behaviour?





Collective bulk behaviour



$t = 0.0 \, \text{fm/c}$



- Sensitive to macroscopic properties of the QGP:
 - Local or large scale collective behaviour?





Collective bulk behaviour



$t = 0.0 \, \text{fm/c}$



Measuring the imperfection factor (viscosity)....



QGP: an almost perfect liquid



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QGP: an almost perfect liquid



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Most perfect liquid: η/s ~0.8

nature hysics

AND THE WOLLS NO.4



Stranger and stranger says ALICE

ELECTRON GASES Spin and charge part wave

DUANTUM SINUCATION Familiation stations

TOPOLOGICAL PHOTONICS Optical Weyl points and Fermiance





Most perfect liquid: η/s ~0.8

> Hottest liquid: 10¹²K

(100,000 x temperature of the Sun core)

nature

ANTICANCER BLOCKBUSTER? RISE AND FALL OF THE SLIDE RULE

AMERICAN Quark Soup

Bringing **DNA** Computers to Life

HAT 2006 WWW.SCIAH.COM



PHYSICISTS RE-CREATE THE LIQUID STUFF OF THE EARLIEST UNIVERSE

ELECTRO Spina se BURNT Familie TOPOLOI Opena W

Birth of the Amazon

Stopping

Future

Giant Telesco





Most perfect liquid: η/s ~0.8

> Hottest liquid: **10**¹²K

(100,000 x temperature of the Sun core)

Smallest liquid: ~yoctosegundos (10-23)



ANTICANCER BLOCKBUSTER?

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nature

The geometry of a quark-gluon plasma



BLACK HOLES Analogue horizons

MARCH 2019 VOL 15 NO 3

TOPOLOGICAL INSULATORS A local marker

AMORPHOUS SUPERCONDUCTIVITY Energy of preformed pairs

ELECTHO Spinals o BURNTU Familius

TOPOLOG Optica W





Most perfect liquid: η/s ~0.8

> Hottest liquid: 10¹²K

(100,000 x temperature of the Sun core)

Smallest liquid: ~yoctosegundos (10-23)

> Most vortical liquid: $\omega \sim 10^{22}/s$

(Atmosphere: $\omega \sim 10^{-4}/s$ Tornado: $\omega \sim 10^{-1}/s$)

nature ANTICANCER BLOCKBUSTER? . RISE AND FALL OF THE SLIDE RULE

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quark-gl

nature

Bringing **DNA** Computers to Life

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probing small distance scales (x) \rightarrow



large momentum transfer (Q^2) \rightarrow







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probing small distance scales (x) \rightarrow



probes

non-pQCD







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probing small distance scales (x) \rightarrow









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probing small distance scales (x) \rightarrow









probing small distance scales (x) \rightarrow



Caveat: need to rely on selfgenerated probes





Using internal probes that can be self-calibrated:






How to probe the QGP @ lab (v2)

Using internal probes that can be self-calibrated:







How to probe the QGP @ lab (v2)

Using internal probes that can be self-calibrated:



Jets in PbPb





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"Shoot" a calibrated probe and see the final modifications with respect to a reference (usually pp)



Example: jets in pp

(well known and theoretically understood)





Example: jets in PbPb

(modifications related to the QGP microscopic properties)



"Shoot" a calibrated probe and see the final modifications with respect to a reference (usually pp)



CMS Experiment at LHC, CERN Data recorded: Sun Nov 14 19:31:39 2010 CEST Run/Event: 151076 / 1328520 Lumi section: 249

Striking signature of QGP presence!

Jet 1, pt: 70.0 GeV







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- QGP:
 - High momentum coloured objects:
 - Single particle measurements (B-meson, quarkonia,...)
 - Jets (Inclusive jets, b-initiated jets, ...)





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And more on Hard Probes

- Huge area! Not enough time to cover everything...
 - Lots of new opportunities to test frontiers of QCD and unveil QGP characteristics



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Summary

- Quantum Chromodynamics (QCD):
 - Building blocks: quarks and gluons
 - Gluon also carry "colour charge"
 - Two limits: perturbative vs non-perturbative

 $\alpha_{\rm eff}(\mathbf{Q}^2)$



probing small distance scales (x) \rightarrow



More on Friday! [T. Peña]



Summary

- Quantum Chromodynamics (QCD):
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 - More on Friday! [T. Peña]

 $\alpha_{_{\text{eff}}}(\mathbf{Q}^2)$

- Heavy-Ions:
 - Unique opportunity to study the Quark-Gluon Plasma
 - New state of QCD matter
 - Test theoretical description of the interaction from QCD first principles;



probing small distance scales (x) \rightarrow







Summary

- Quantum Chromodynamics (QCD):
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Questions?

 $\alpha_{_{\text{eff}}}(\mathbf{Q}^2)$



probing small distance scales (x) \rightarrow





